

IF GOINGToCrash(): DONT()
RISC-V ARCHITECTURE FOR MOTION PLANNING
ALGORITHMS IN AUTONOMOUS UAVs

A senior design project submitted in partial fulfillment of the requirements for the degree of
Bachelor of Science at Harvard University

Anthony J.W. Kenny
S.B. Candidate in Electrical Engineering

Faculty Advisor: Vijay Janapa Reddi

Harvard University School of Engineering and Applied Sciences
Cambridge, MA

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Abstract

This thesis describes a process for accelerating motion planning in autonomous robots through the design of specialised microarchitecture and instruction set architecture. First, it shows the analysis of computational performance of Rapidly-exploring Random Tree (RRT), a sampling-based motion planning algorithm commonly used in autonomous drones. Having identified collision detection as the biggest area of opportunity for improved performance, it describes the process of designing specialized hardware, taking advantage of parallelization, that quickly detects collisions. Finally, it presents how this specialized functional unit can be implemented in a processor, and a RISC-V Instruction Set Architecture (ISA) extension designed to massively reduce the execution time of collision detection.

Rewrite Abstract

Contents

Preface	i
Abstract	i
Table of Contents	ii
List of Acronyms	iv
List of Algorithms	vi
List of Figures	vii
List of Tables	viii
1 Introduction	1
1.1 Problem Summary	1
1.1.1 Background	1
1.1.2 Problem Definition	4
1.2 Prior Work	4
1.2.1 Hardware Acceleration	4
1.2.2 RISC-V	6
1.3 Project Overview	8
1.3.1 Proposed Solution	8
1.3.2 Project Specifications	9
1.3.3 Project Structure	9
2 Motion Planning in Software	11
2.1 Background	11
2.1.1 Key Concepts	12
2.2 Rapidly-Exploring Random Tree	13
2.2.1 Algorithm	13
2.2.2 Implementation	16
2.3 Performance Analysis	19
2.3.1 Methodology	19
2.3.2 Results	20

3	Motion Planning in Hardware	25
3.1	Defining the Collision Detection Unit	25
3.1.1	Edge Collision Function	25
3.1.2	Technical Specifications	25
3.1.3	Performance Specifications	26
3.2	HoneyBee	27
3.2.1	Design	27
3.2.2	Build	28
3.2.3	Measurement and Analysis	29
4	RISC-V Processor	32
4.1	Introduction to the Reduced Instruction Set Computer	32
4.1.1	Instruction Set Architecture	32
4.1.2	RISC Processor Design	32
4.2	RISC-V ISA	32
4.2.1	RV32I	32
4.2.2	Motion Planning Extension	34
4.3	PhilosophyV	34
4.3.1	Baseline Implementation	34
4.3.2	Implementing HoneyBee	34
4.4	Performance Analysis	36
5	Conclusion	37
5.1	Discussion of Results	37
5.2	Evaluation of Success	37
5.3	Future Work	37
	Bibliography	38
	Glossary	40
	Appendices	43
A	Project Repository	44
B	Budget	45
C	RRT Supporting Documentation	46
C.1	Justification of K:DIM Ratio	46

List of Acronyms

2D 2-Dimensional

3D 3-Dimensional

API Application Programming Interface

ARM Advanced RISC Machine

CISC Complex Instruction Set Computer

CPI Cycles Per Instruction

CPU Central Processing Unit

DOF Degree-of-Freedom

FPGA Field Programmable Gate Array

GPU Graphics Processing Unit

GUI Graphical User Interface

HB-A HoneyBee-A

HDL Hardware Description Language

HLS High Level Synthesis

ISA Instruction Set Architecture

OGM Occupancy Grid Map

PRM Probabalistic Road Map

RISC Reduced Instruction Set Computer

RRT Rapidly-exploring Random Tree

RRT* Rapidly-exploring Random Tree Star

RTOS Real-Time Operating Systems

RV32I RISC-V 32-Bit Integer

SoC System on Chip

UAV Unmanned Aerial Vehicle

List of Algorithms

2.1	Rapidly-Exploring Random Tree in Free configuration Space	13
2.2	Rapidly-Exploring Random Tree with Collision Detection	15

List of Figures

1.1	The use of Autonomous Robots over time [TODO]	2
1.2	Simple Visualization of Computer Implementation Hierarchy	5
1.3	Typical Process of Adding Non-Standard Extension to RISC-V ISA	7
1.4	System Diagram of Overall Project	8
2.1	Example of 2 Robot Configurations in 3D Space for Motion Planning Purposes	12
2.2	Step by step demonstration of RRT Algorithm for 2D robot in 2D space	14
2.3	2D RRT Implementation shown by Graphical User Interface (GUI)	17
2.4	3D RRT Implementation shown by GUI	18
2.5	VTune Amplifier TopDown Analysis Example	19
2.6	RRT Functions as a % of Total CPU Execution Time	21
2.6	RRT Functions as a % of Total CPU Execution Time (cont.)	22
2.7	RRT Functions Execution Time, with Bucket Optimization	24
3.1	Pipelining to Improve Latency	27
3.2	Interface Summary of HoneyBee-A Synthesis in Vivado HLS	29
3.3	RRT Simulated Execution Time with HB-A (microseconds)	31
4.1	5-Stage Reduced Instruction Set Computer (RISC) Datapath	32
4.2	Philosophy V Processor	35

List of Tables

1.1	List of System Components and their Descriptions	9
2.1	Technical Specifications for RRT Implementation	16
2.2	Comparison of Timing Methods	20
3.1	Technical Specifications for Edge Collision Detection Unit	26
3.2	Simulated performance of HB-A in microseconds	30
3.3	RRT Simulated Execution Times with HB-A (seconds)	30
4.1	Register State for RV32I Base Instruction Set	33
4.2	RV32I Base Instruction Formats	34

Chapter 1

Introduction

Define goal: Somewhere here I need to define very clearly the following

1. Overall Goal:~ Deliver an example of how RISC-V can be leveraged to design a custom processor for motion planning
2. 4 Objectives:
 - Profile a standard motion planning algorithm to determine the bottleneck function
 - Design a functional hardware unit that eliminates that bottleneck
 - Define a non standard extension
 - Implement Processor and verify all above

1.1 Problem Summary

1.1.1 Background

The Unmanned Aerial Vehicle (UAV) has been utilised in military applications extensively throughout the late 20th and early 21st century. However, over the last decade, their use in non-military applications, such as commercial, scientific, agricultural, and recreational, has increased such that the number of civilian drones vastly outnumber military UAVs. Particularly in the commercial sector, such rapid growth in the number and range of applications means that autonomy is key for the profitable adoption of UAVs. Such autonomy relies on efficient computation of motion planning algorithms. However, the implementation of these algorithms can be quite computationally expensive, and thus slow and/or detrimentally power consuming. As such, this thesis aims to design specialized hardware to more efficiently compute motion plans for autonomous drones.

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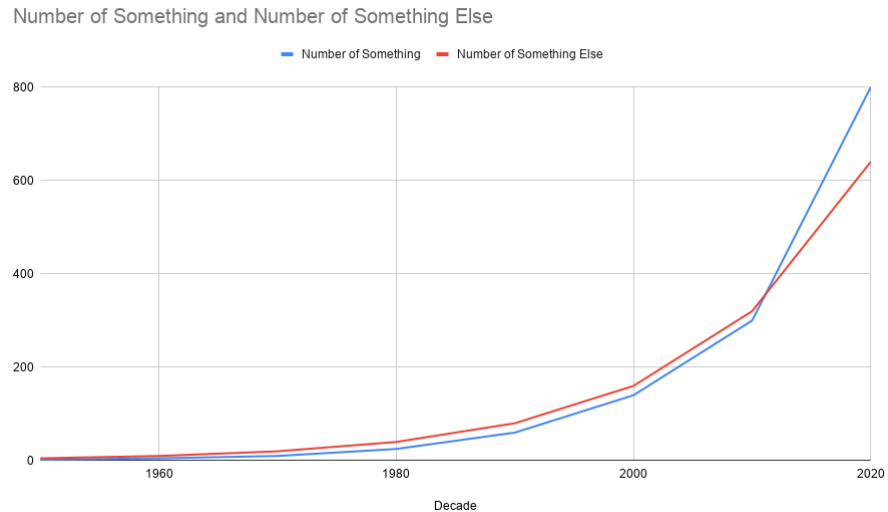


Figure 1.1: The use of Autonomous Robots over time [TODO]

Robotics

For well over 2000 years, the concept of robotics, albeit not always with such a term, has fascinated humans. As early as the first century A.D., the Greek mathematician and engineer, Heron of Alexandria, described more than 100 different machines and automata in *Pneumatica* and *Automata* [1]. In 1898, Nikola Tesla demonstrated the first radio-controlled vessel. Since then, the world has seen widespread application of robotics in manufacturing, mining, transport, exploration, and weaponry. For the last few decades, robots have operated in controlled, largely unchanging environments (e.g. an assembly line) where their environment and movements are largely known *a priori*.

However, in recent years a new generation of autonomous robots has been developed for a wide range of real-world, complex applications. The increasing trend the use of autonomous robots is shown in Figure 1.1. These new robots, unlike those traditional ones described above, are required to adapt to the changing environment in which they operate. As such, they must perform motion planning in real-time.

Motion Planning

More of an introduction to motion planning.

Motion Planning refers to the problem of determining how a robot moves through a space to achieve a goal. Chapter 2 provides a detailed explanation of motion planning and

of Rapidly-exploring Random Tree (RRT), a commonly used motion planning algorithm. On the algorithmic level, motion planning has been extensively studied and many solutions exist. However, current algorithms running on regular Central Processing Unit (CPU)s are too slow to execute in real-time for robots operating in complex environments. Simply solving this problem with more raw computing power, using energy hungry Graphics Processing Unit (GPU)s may have merit in tethered robots. On the other hand, untethered applications, such as autonomous drones, where limiting power consumption is a primary concern, this strategy is infeasible.

Subsubsection for Problem Overview: Add a subsubsection here about the current issue of slowness to transition into problem statement

1.1.2 Problem Definition

Problem Statement

Motion planning algorithms implemented in software that runs on general purpose CPUs cannot execute quickly enough for fully autonomous UAVs to operate in high-complexity environments. The state-of-the-art strategy of using power-hungry GPUs to accelerate the execution of these algorithms requires too much power to be cost-effective or feasible for UAVs to sustain flight for useful periods of time.

Improve Problem Statement: Existing research into accelerating robotic motion planning is <reason for RISC-V, inaccessible?> and mainly focussed on tethered arm moving robots.

End User

This thesis aims to provide developers of autonomous drones with specialized hardware for motion planning. Such developers have a need for computing hardware that executes motion planning algorithms faster and more power efficiently than existing methods. This thesis will provide a processor design that is synthesizable on an Field Programmable Gate Array (FPGA), giving developers a processor for which a Real-Time Operating Systems (RTOS), or bare metal code, can be deployed.

Revise End User

1.2 Prior Work

1.2.1 Hardware Acceleration

Hardware acceleration refers to the strategy of using computer hardware specifically designed to execute a function more efficiently than can be achieved by software running on a general purpose CPU. Specialized hardware designed to perform specific functions can yield significantly higher performance than software running on general purpose processors, and lower power consumption than GPUs.

Computer Implementation Hierarchy

To briefly frame the space in which this thesis operates, consider the typical computer implementation hierarchy, demonstrated in Figure 1.2. **User level applications**, such as Google Chrome, Microsoft Word, and Apple's iTunes, sit at the top of the abstraction hierarchy. These applications are implemented in **High-Mid Level Languages**, such as C/C++, Python, Java, etc. These programming languages have their own hierarchy, but for the purpose of this thesis, it is sufficient to understand that these programming languages are then compiled into **Assembly Language**. Assembly language closely follows the execution of instructions on the **processor**, and is defined by an **ISA**. An ISA can be

thought of as the contract between software programmers and processor engineers, agreeing what instructions the processor is able to implement. This assembly code is finally loaded into the processor's instruction memory and executed.

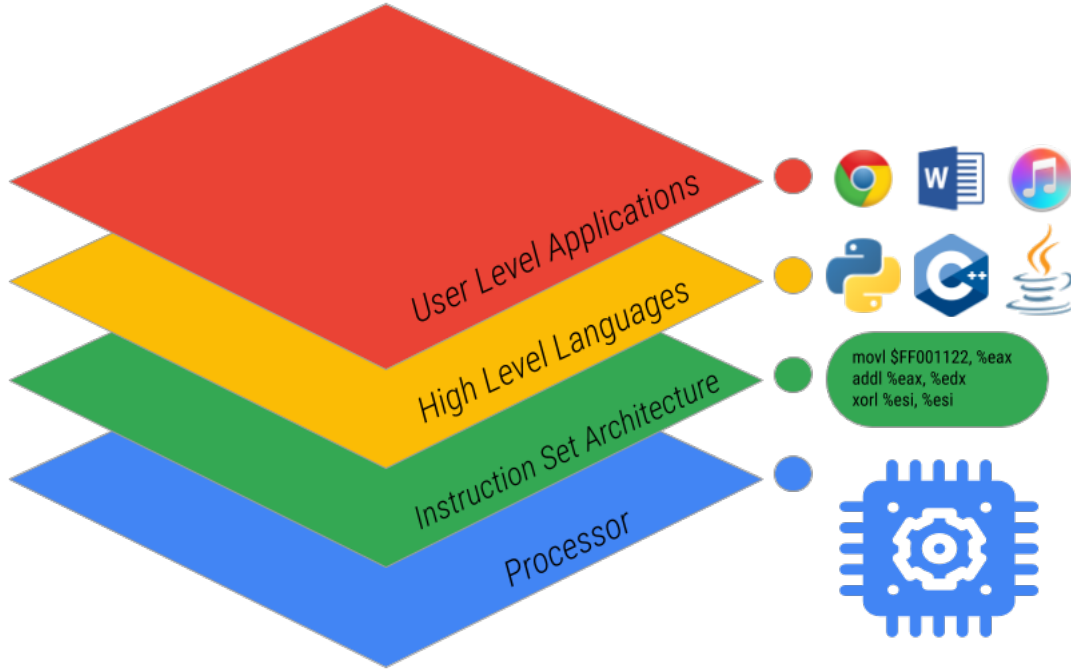


Figure 1.2: Simple Visualization of Computer Implementation Hierarchy

As will be outlined in Section 1.3, this thesis operates extensively on the lower two levels of this hierarchy, extending an existing ISA and building hardware at the processor level that supports these extensions.

Acceleration of Motion Planning

Accelerating motion planning with hardware is a fairly well studied problem.

A Motion Planning Processor on Reconfigurable Hardware [2] studied the performance benefits of using FPGA-based motion planning hardware as either a motion planning processor, co-processor, or collision detection chip. It targeted the feasibility checks of motion planning (largely collision detection) and found their solution could build a roadmap using the Probabalistic Road Map (PRM) algorithm up to 25 times faster than a Pentium-4 3Ghz CPU could.

In *A Programmable Architecture for Robot Motion Planning Acceleration* [3], Murray et

al. built on the work of the aforementioned paper, to accelerate several aspects of motion planning in an efficient manner.

FPGA based Combinatorial Architecture for Parallelizing RRT [4] studies the possibility of building architecture to allow multiple RRTs to work simultaneously to uniformly explore a map. Taking advantage of hardware parallelism allows systems such as this to compute more information per clock cycle.

Finally, in the paper *Robot Motion Planning on a Chip* [5], Murray et al. describe a method for constructing robot-specific hardware for motion planning, based on the method of constructing collision detection circuits for PRM that are completely parallelised, such that edge collision computation performance is independent of the number of edges in the graph. With this method, they could compute motion plans for a 6-degree-of-freedom robot more than 3 orders of magnitude faster than previous methods.

1.2.2 RISC-V

RISC-V (pronounced “risk-five”) is an ISA developed by the University of California, Berkeley. It is established on the principles of a RISC, a class of instruction sets that allow a processor to have fewer Cycles Per Instruction (CPI) than a Complex Instruction Set Computer (CISC) (x86, the ISA on which macOS and linux operating systems run, is an example of a CISC instruction set). What makes RISC-V unique is its open-source nature. What makes CPU design so expensive is that it requires expertise across many disciplines (compilers, digital logic, operating systems, etc). RISC-V was started with the philosophy of creating a practical, open-source ISA that was usable in any hardware or software without royalties. The first report describing the RISC-V Instruction Set was published in 2011 by Andrew Waterman, Yunsup Lee, David A. Patterson, and Krste Asanović [6].

Extending RISC-V

RISC-V is designed cleverly in a modular way, with a set of base instruction sets and a set of standard extensions. As a result, processors can be designed to only implement the instruction groups it requires, saving time, space and power on instructions that won’t be used. In addition, another goal of RISC-V is to provide a basis for more specialized instruction-set extensions or more customized accelerators. This is described in the most recent *RISC-V Instruction Set Manual* [7]. This is a powerful feature, as it does not break any software compatibility, but allows for designers to easily follow the steps outlined in Figure 1.3. From a hardware acceleration point of view, this is particularly useful as it allows the designer to directly invoke whatever functional unit or accelerator they implement from assembly code.

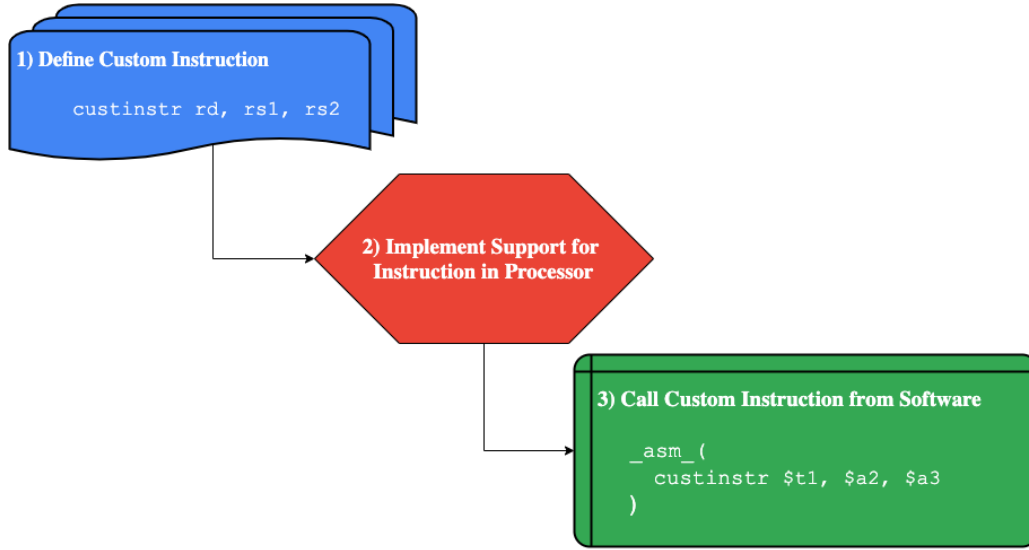


Figure 1.3: Typical Process of Adding Non-Standard Extension to RISC-V ISA

Accelerating RISC-V Processors

Having only been released in 2011, RISC-V is still a relatively unexplored opportunity for non-education applications. However, it shows promise in the commercial space, with Alibaba recently developing the Xuantie, a 16-core, 2.5GHz processor, currently the fastest RISC-V processor. Recently there has been promising research into accelerating computationally complex applications, particularly in edge-computing, with RISC-V architecture. *Towards Deep Learning using TensorFlow Lite on RISC-V*, a paper co-written by the faculty advisor of this thesis, V.J. Reddi, presented the software infrastructure for optimizing the execution of neural network calculations by extending the RISC-V ISA and adding processor support for such extensions. A small number of instruction extensions achieved coverage over a wide variety of speech and vision application deep neural networks. Reddi et al. were able to achieve an 8 times speedup over a baseline implementation when using the extended instruction set. *GAP-8: A RISC-V SoC for AI at the Edge of the IoT* proposed a programmable RISC-V computing engine with 8-core and convolutional neural network accelerator for power efficient, battery operated, IoT edge-device computing with order-of-magnitude performance improvements with greater energy efficiency.

1.3 Project Overview

1.3.1 Proposed Solution

This thesis proposes a non-standard RISC-V Instruction Set Extension, supported by a functional unit embedded in a FPGA synthesizable processor design that more rapidly computes motion planning for autonomous UAVs. It will use the RRT algorithm as a benchmark for performance analysis. Profiling of RRT described in chapter 2 found that edge collision detection was the most performance limiting function of RRT. As such, this thesis aims to design a RISC-V extension and specific circuitry that support the faster execution of edge collision detection.

System Overview

Figure 1.4 shows a high level overview of the system this thesis proposes.

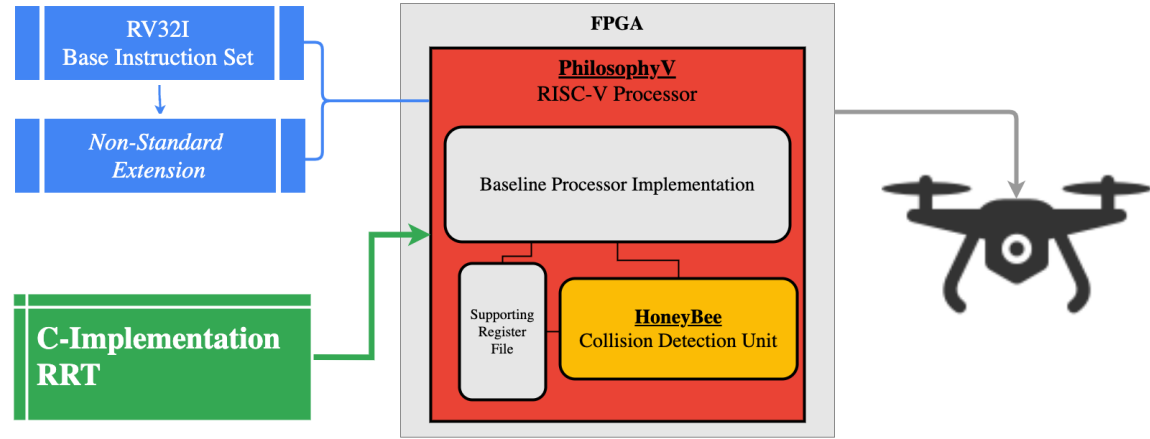


Figure 1.4: System Diagram of Overall Project

The **Extended RISC-V ISA** is made up of the RISC-V 32-Bit Integer (RV32I) Base Instruction Set and a non-standard extension that this thesis will define. The **PhilosophyV Processor** is a RISC-V chip built in Hardware Description Language (HDL) for this thesis. It implements both the RV32I instruction set and the non-standard extension. The PhilosophyV Core includes, along with a baseline 5-stage processor implementation, the **HoneyBee** collision detection unit. A **C Implementation of RRT** is loaded into the instruction memory of the PhilosophyV processor. This processor, synthesized on an **FPGA**, is used as the main processor, co-processor, or accelerator on an **Autonomous UAV**. Table 1.1 outlines the components of this system and their descriptions.

Component	Source	Description
RISC-V Instruction Set		
RV32I	Berkeley	40 Instructions defined such that RV32I is sufficient to form a compiler target and suport modern operating systems [7].
Extension	<i>New</i>	This is the custom extension defined by this thesis targeting motion planning instructions. It is outlined in Chapter 4.
C-Implementation of RRT		
RRT	<i>New</i>	Due to lack of available implementations of RRT suitable for the purposes of this thesis, RRT was implemented from the ground up in C. This is detailed in Chapter 2
FPGA Synthesized Chip		
Zynq-7000	Xilinx	The Zynq-7000 family of System on Chip (SoC)s are a low cost FPGA and Advanced RISC Machine (ARM) combined unit.
PhilosophyV	<i>New</i>	The processor built for this thesis to demonstrate how the RISC-V extension and hardware unit work together. This is detailed in Chapter 4
HoneyBee	<i>New</i>	The functional unit designed specifically for faster execution of edge collision detection computations. Outlined in Chapter 3

Table 1.1: List of System Components and their Descriptions

1.3.2 Project Specifications

Project Specifications: These need significant revision from the last checkpoint

1.3.3 Project Structure

This report is structured to follow the timeline of this project, and is outlined below:

1. A benchmark motion planning algorithm, RRT, was selected and implemented in software. Once implemented, a variety of performance analysis methods were used to profile the computational hotspots of the algorithm. It was found that edge collision detection was the critical function limiting execution time. This process is detailed in Chapter 2.

2. With edge collision detection having been identified as the critical function, the process of designing specialised hardware to execute this function began. The technical specifications, performance specifications, designs, build phases, measurement and analysis of this hardware unit is presented in Chapter 3.
3. With the aforementioned functional unit's performance verified in simulation, the next step was to implement this in a processor. First, a baseline processor was designed and built for this project to implement a base RISC-V instruction set. The performance of RRT is again profiled on this baseline processor (as up until this point, it was profiled on x86 architecture). A non-standard extension to the RISC-V ISA was then defined and support for this was implemented in the processor. Comparative performance analysis was then conducted. This process is described in detail in Chapter 4.
4. Chapter 5 is a discussion of results and future work.

Summary of Results: Do I need a summary of results section in the introduction?

Chapter 2

Motion Planning in Software

The first objective of this thesis is to identify a typical motion planning algorithm, profile its execution, and determine computational bottlenecks.

Chapter 2 provides an introduction to motion planning and details the process of implementing and analysing Rapidly-exploring Random Tree (RRT), a commonly used motion planning algorithm, to identify computational hot-spots and thus identify the biggest opportunities for hardware optimization of the algorithm.

Update
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properly
defined
goals and
objectives

2.1 Background

A funny paradox in computer science is the fact that it is relatively easy to teach a computer to perform tasks that humans find very complicated, but extremely difficult to program one to execute functions that humans master during infancy. Consider, it was as early as 1949 that Claude Shannon presented his paper *Programming a Computer for Playing Chess*[8], and by 1997 the *Deep Blue* computer defeated Garry Kasparov, reigning world champion, in a six game chess match.[9] Compare that with some of the most advanced autonomous humanoid robots to date displaying dexterity comparable with a toddler. The task of finding a collision free path, performed constantly without thought by a human, is an example of this paradigm. For a robot to compute a collision free path, it relies on a set of Motion Planning Algorithms.

Motion Planning Algorithms refer to the set of algorithms that find possible sequences of valid configurations for a robot in a space. In plain English, they are algorithms that determine the movements a robot can make in a map, with the intent of eventually finding a path from one point to another.

2.1.1 Key Concepts

Workspace

The workspace, also known as the map, is the space which the robot and obstacles occupy.

Configuration & Configuration Space

A configuration describes the position, orientation, and pose of the robot. The complexity of a robot's configuration is therefore dependant on the dimension of the workspace, the complexity of the robot itself, and in what level of detail the robot must be represented. For example:

- Most simply, a robot can be represented as a point by the Cartesian coordinates (x, y, z) in 2-Dimensional (2D) space and (x, y, z) in 3-Dimensional (3D) space.
- More realistically, a robot such as a drone may be represented in 3D by an origin point (x, y, z) and 3 Euler angles (α, β, γ) describing its orientation.
- In a more complex form, a fixed base robot with N Degree-of-Freedom (DOF) would require an N -dimensional configuration.

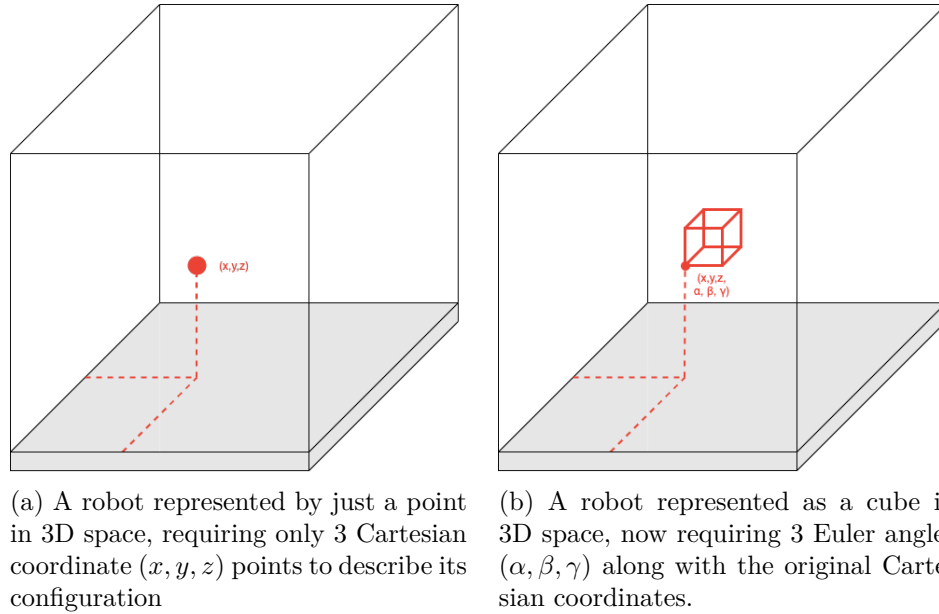


Figure 2.1: Example of 2 Robot Configurations in 3D Space for Motion Planning Purposes

2.2 Rapidly-Exploring Random Tree

RRT is an algorithm designed to efficiently search, and thus plan a path through, a high-complexity environment by randomly sampling points and building a tree. The algorithm randomly samples points, draws an edge from the nearest currently existing node in the tree, to grow the tree in the space. It is inherently biased to grow towards large unsearched areas of the problem. RRT was developed by S. LaVelle[10] and J. Kuffner[11]. It is used in autonomous robotic motion planning problems such as autonomous drones, the focus of this thesis.

2.2.1 Algorithm

Building the Tree

Put simply, RRT builds a tree (referred to as a graph) of possible configurations, connected by edges, for a robot of some physical description. It does so by randomly sampling the configuration space and adding configurations to the graph. From this graph, a path from the initial configuration to some goal configuration can be found, given a high enough number of iterations. As such, RRT can be considered probabilistically complete. The pseudo-code for RRT can be seen in Algorithm 2.1

Algorithm 2.1: Rapidly-Exploring Random Tree in Free configuration Space

Inputs: Initial configuration q_{init} ,
Number of nodes in graph K ,
Incremental Distance Δq

Output: RRT Graph G with K configurations $[q]$ & edges $[e]$

$G.init();$
for $k = 1$ to K **do**
 $q_{rand} \leftarrow \text{randomConfiguration}();$
 $q_{near} \leftarrow \text{nearestVertex}(q_{rand}, G);$
 $q_{new} \leftarrow \text{newVertex}(q_{near}, q_{rand}, \Delta q);$
 $G.addVertex(q_{new});$
 $G.addEdge(q_{near}, q_{new});$
end

Algorithm 2.1 can be visually represented in Figure 2.2. Consider a 2D robot operating in a 2D workspace. A Graph G is initialized containing an initial configuration, q_{init} , with constraints on the number of nodes that the graph can hold, K , and the maximum distance between two nodes, Δq . This is shown in Sub-figure 2.2a. A random configuration for the robot, q_{rand} is generated (2.2b). The nearest existing configuration in G , q_{near} , is found. (In the first iteration, $q_{near} = q_{init}$, shown in Sub-figure 2.2c). The distance between q_{near}

and q_{rand} is calculated. If this distance is less than Δq , $q_{new} = q_{rand}$. If not, q_{new} is selected, typically by moving by Δq from q_{near} towards q_{rand} (2.2c). q_{new} is then added to G . This is repeated for K configurations.

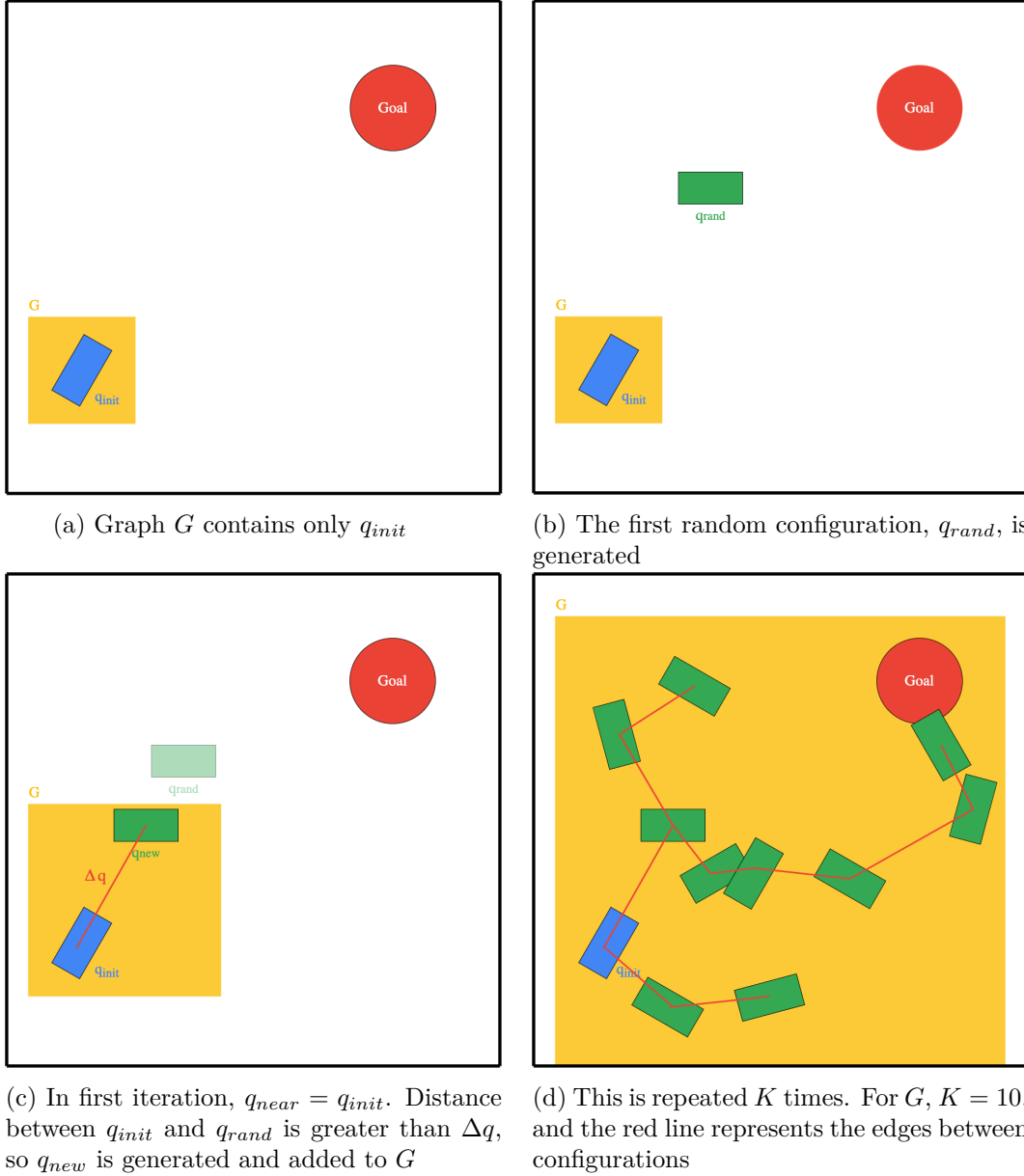


Figure 2.2: Step by step demonstration of RRT Algorithm for 2D robot in 2D space

Collision Detection

Algorithm 2.1 shows how RRT builds a graph of possible configurations connected by edges in a free configuration space. However, in real-world applications, a robot's configuration space often contains obstacles. As such, collision detection must be included in the algorithm. The two types of collisions the algorithm must check for are *configuration collisions* (those where the robot would collide with an obstacle in a given configuration) and *edge collisions* (where the robot would collide when moving between two collision free configurations).

The RRT with configuration and edge collision detection can be seen in Algorithm 2.2. The method of implementing RRT with collision detection to model a drone in 3D space is detailed in Section 2.2.2.

Algorithm 2.2: Rapidly-Exploring Random Tree with Collision Detection

Inputs: Initial configuration q_{init} ,
Number of nodes in graph K ,
Incremental Distance Δq ,
Space S containing obstacles

Output: RRT Graph G with K configurations $[q]$ & edges $[e]$

```

G.init();
for  $k = 1$  to  $K$  do
    while !pointCollision( $q_{new}$ ) do
         $q_{rand} \leftarrow \text{randomConfiguration}()$ ;
         $q_{near} \leftarrow \text{nearestVertex}(q_{rand}, G)$ ;
         $q_{new} \leftarrow \text{newVertex}(q_{near}, q_{rand}, \Delta q)$ ;
    end
     $e_{new} \leftarrow \text{newEdge}(q_{near}, q_{new})$ 
    if !edgeCollision( $e_{new}$ ) then
        G.addVertex( $q_{new}$ );
        G.addEdge( $q_{near}, q_{new}$ );
    else
         $k = k - 1$ ;
    end
end

```

2.2.2 Implementation

With RRT selected as the benchmark algorithm against which to test specialised hardware, this project required an implementation of the algorithm that satisfied the following criteria.

Requirement	Description and Justification
C/C++ Implementation	As outlined in Section 1.3.3, the critical step in determining the design of specialized hardware to accelerate RRT is CPU performance analysis of the algorithm to determine computational hot-spots. Implementations in C allow for the use of certain CPU profiling tools, described in Section 2.3.1, unlike higher-level languages such as Python.
Models Drone as Point	In reality, implementing RRT for a drone would model the robot as a 3D object defined by coordinates $\{x, y, z\}$ and Euler angles $\{\alpha, \beta, \gamma\}$. However, for simplicity's sake, modelling the drone as a point defined by coordinates $\{x, y, z\}$ will suffice. Time permitting, this could be revisited. Change this based on whether time does permit
Mirrors Algorithm	In order for the results of CPU performance analysis to be easy to understand, software implementation of RRT should call functions that mirror the functions described in Algorithms 2.1 and 2.2.

Better
RRT Im-
plementa-
tion intro-
ductory
sentence

Table 2.1: Technical Specifications for RRT Implementation

Improve this table

The original intention was to find an existing implementation of RRT that could fulfill these requirements. Most open source implementations found online were in Python, and all those implemented in C were unsuitable[12][13][14][15], as they had extraneous GUIs, reliance on external Application Programming Interface (API)s, and other features that would distort analysis of algorithmic hot-spots.

As a result, it was necessary to build a C implementation of RRT from the ground up that satisfied the requirements in Table 2.1. It can be found in this project's GitHub repository. It follows Algorithm 2.1 closely. For monitoring correctness, I build in an optional GUI that shows the tree, starting node, and obstacles.

Modelling a UAV for RRT

Implementation in 2D

The first step was to implement RRT with a 2-Dimensional workspace.

More detail

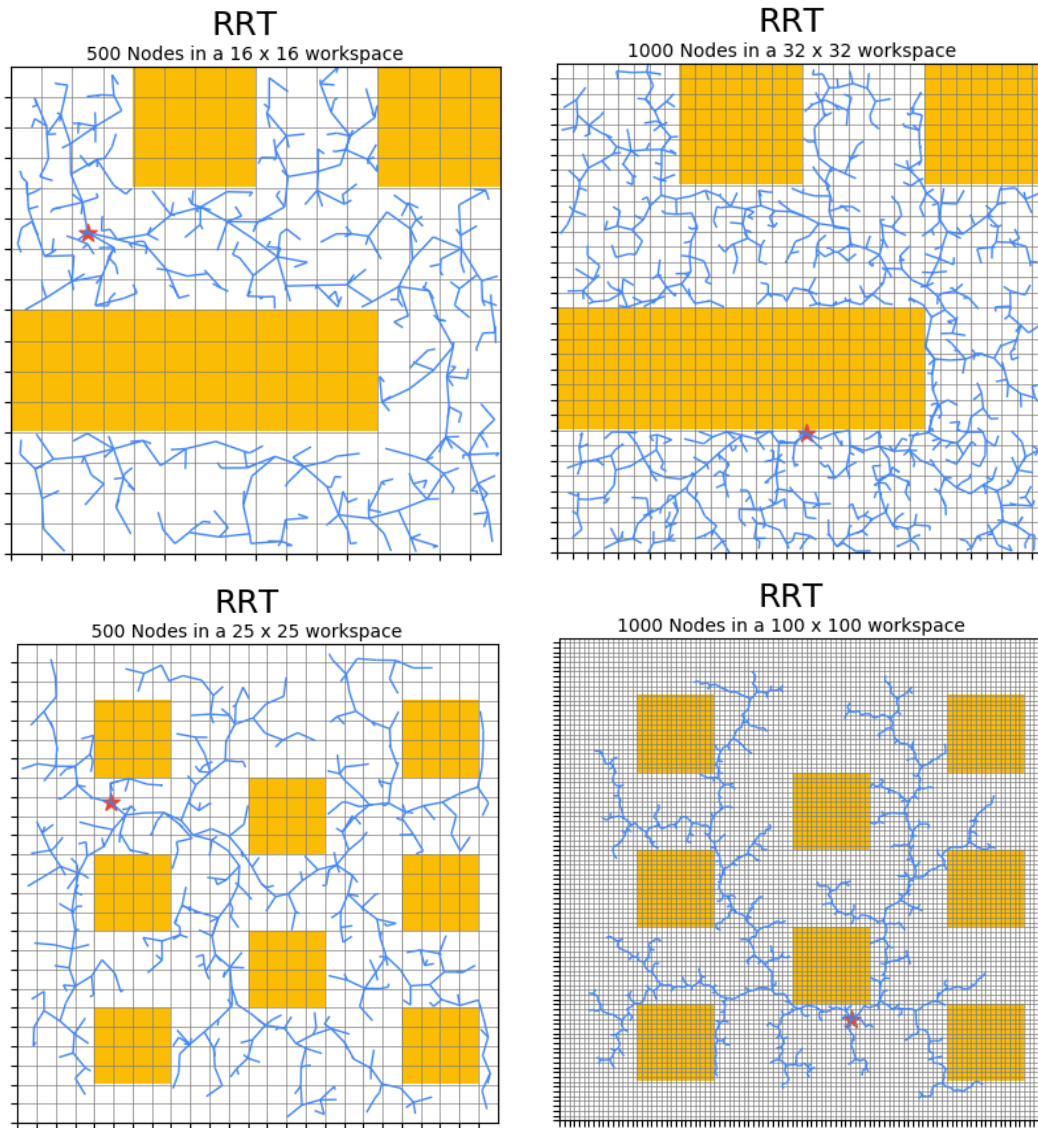


Figure 2.3: 2D RRT Implementation shown by GUI

Implementation in 3D

Describe implementation in 3D

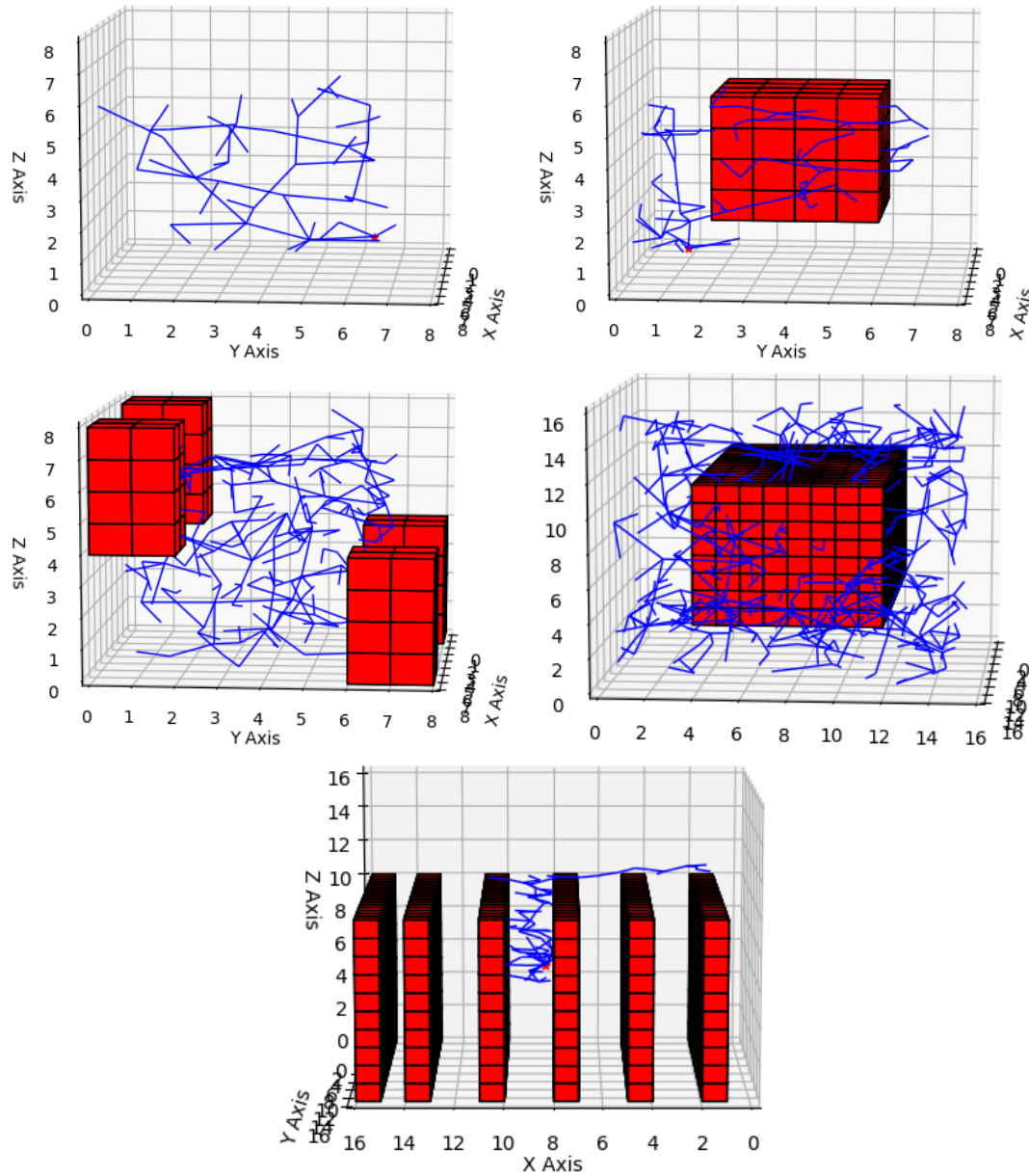


Figure 2.4: 3D RRT Implementation shown by GUI

2.3 Performance Analysis

Brief introduction outlining purpose of performance analysis

2.3.1 Methodology

To restate, the aim of this thesis is to design a computer processor with reduced execution time of motion planning algorithms, such as RRT. As such, it is important to understand the elements of the algorithm that have the highest percentage of CPU execution time. To determine this, it was necessary to implement my own, naive but typical, RRT in C. This program could then be compiled and analysed using a software performance profiling tool. With this, I could design experiments to determine the critical RRT functions (those occupying a majority of CPU time) and see how this varies given different parameters.

Outline of method of analysis. Something better than the above

VTune Profiler

VTune Profiler performance profiler is an application for software performance analysis. It provides functionality to examine hot-spots for CPU execution time through a top down analysis, shown below in Figure 2.5. As can be seen from the figure, the top down analysis tool shows the percentage of CPU time taken up by each function. I used this tool to profile the algorithm's performance as I changed certain parameters.

Rewrite the above

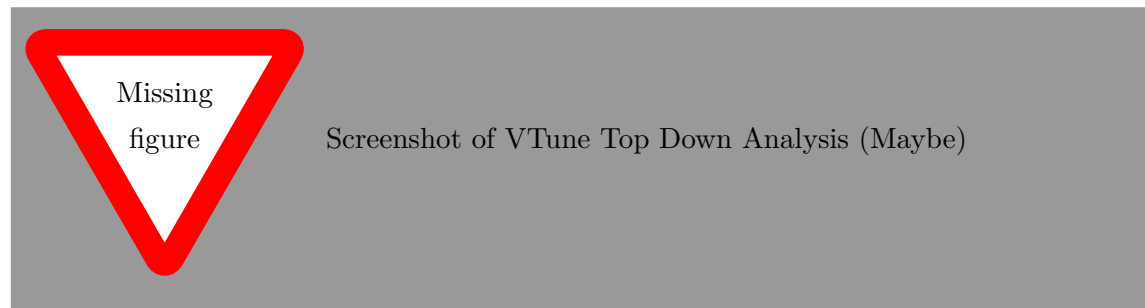


Figure 2.5: VTune Amplifier TopDown Analysis Example

Internal Timing

The limitation of VTune Profiler is that it can only profile software running on Intel processors, which implement the x86 ISA. As such, when the time comes to analyse performance

of the software running on a RISC-V processor, another method will be required. A simple and effective way of measuring execution performance is to insert timing functionality into the software itself.

Provide or link to appendix of explanation of internal timing

Comparison

Before proceeding to use either of these methods to profile the software implementation of RRT, it was important to verify that the two methods yielded similar results for the same program. Table 2.2 summarizes the results of analysis of a simple C executable. The program calls 5 functions, $\{A, B, C, D, E\}$, each a simple iteration in which a integer is incremented. Since the Internal Timing method returned similar results to the (trusted) VTune Profiler, it was considered to be a reliable method. While it was encouraging to see both methods returned similar results for absolute execution time, the more important metric was the similarity in percentage of total execution time.

function	Vtune Profiler		Internal Timing	
	time (s)	time (% total)	time (s)	time (% total)
A	0.488	57.4%	0.497	57.6%
B	0.2	23.5%	0.198	23.1%
C	0.102	12.0%	0.099	11.5%
D	0.048	5.7%	0.049	5.6%
E	0.012	1.4%	0.019	2.2%

Table 2.2: Comparison of Timing Methods

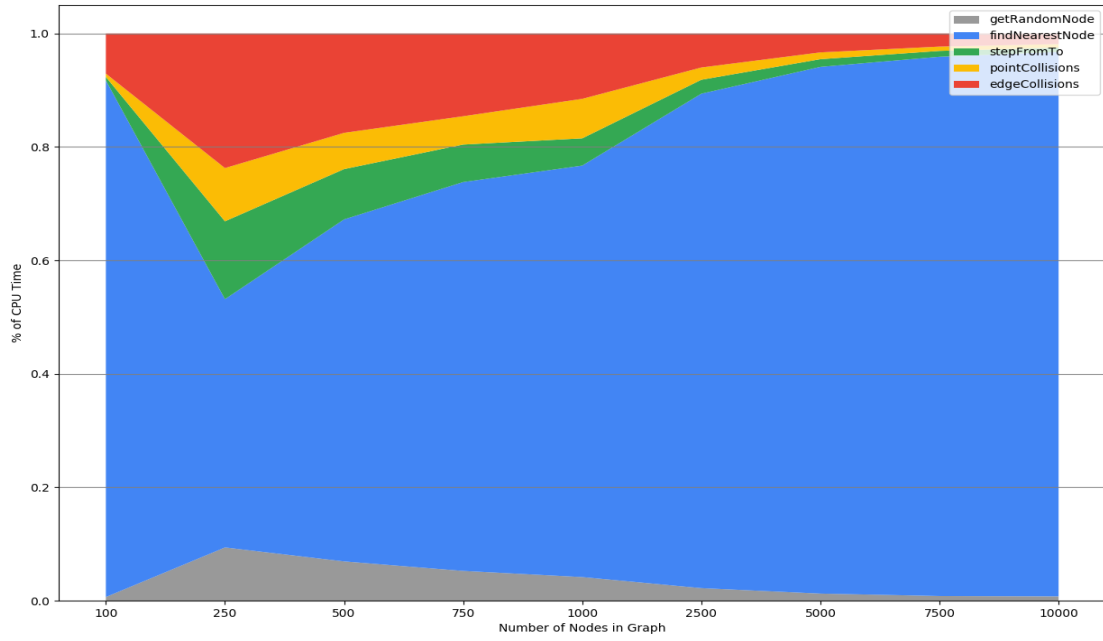
Experimental Design

In profiling RRT in software, the goal was to find the critical task across different values of K and sizes of configuration space. Multiple tests were run, varying these two constraints, to find this critical function. The results of this analysis can be found in Section 2.3.2.

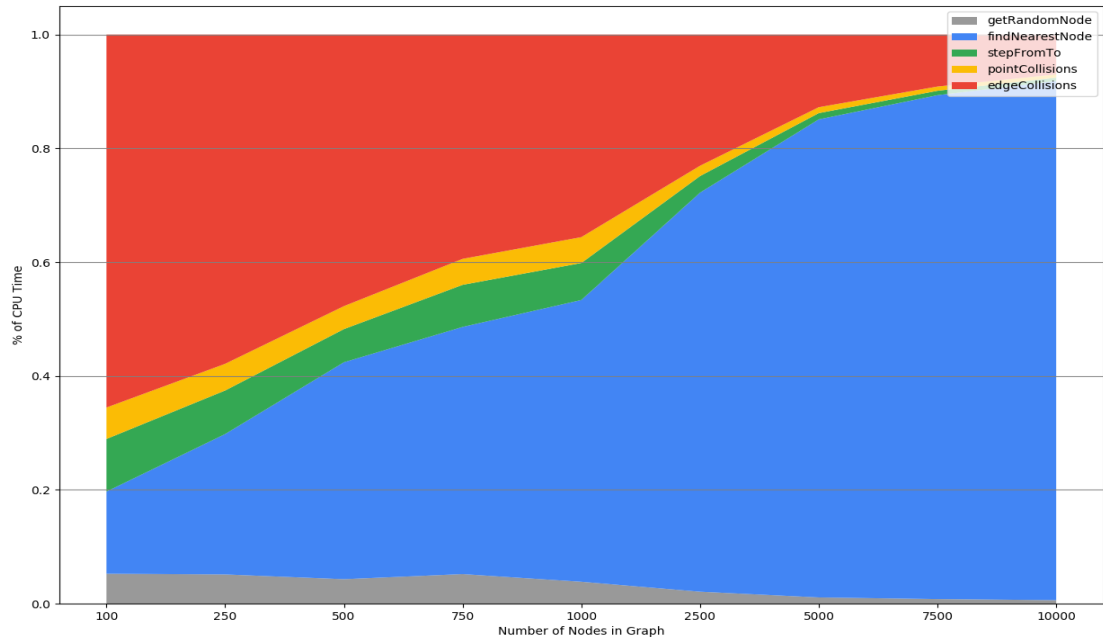
2.3.2 Results

Figure 2.6 shows the profile of functions within RRT, for $100 \leq K \leq 10000$, and cubic configuration spaces with dimensions $\{4, 8, 16, 32\}$. Each subfigure shows a similar profile, with the % of CPU Execution Time taken by `findNearestNode` increasing with K . This is to be expected. However, it is also seen that `edgeCollisions` increases with larger configuration spaces, taking up the overwhelming majority of execution time for a $32 \times 32 \times 32$ configuration space.

Explanation of time complexity

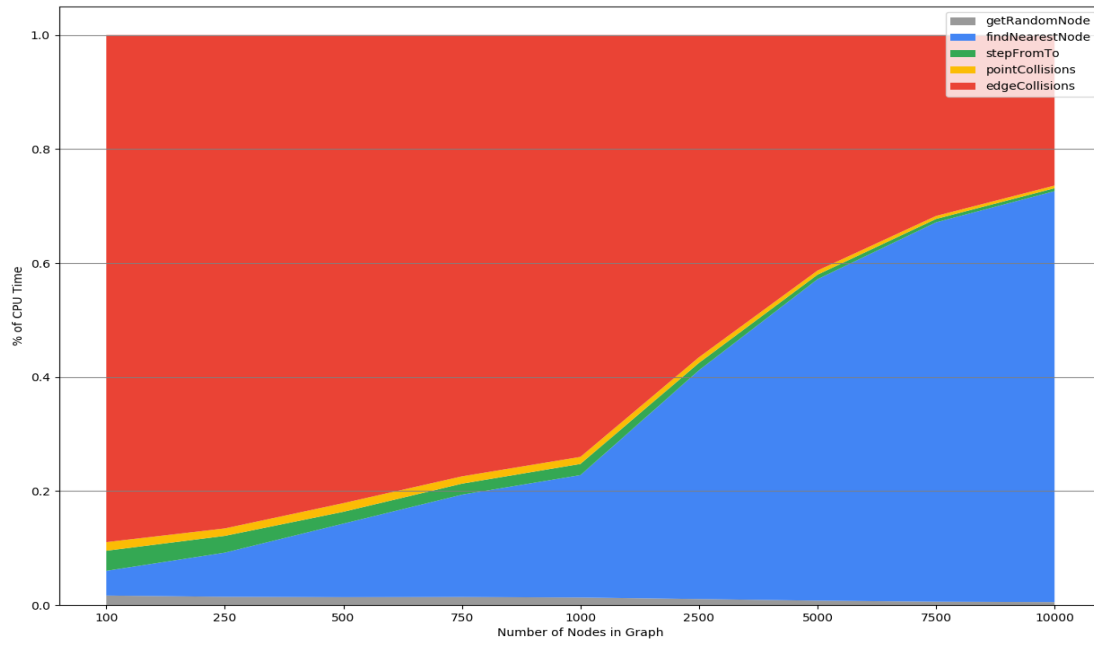


(a) 4x4x4 configuration Space

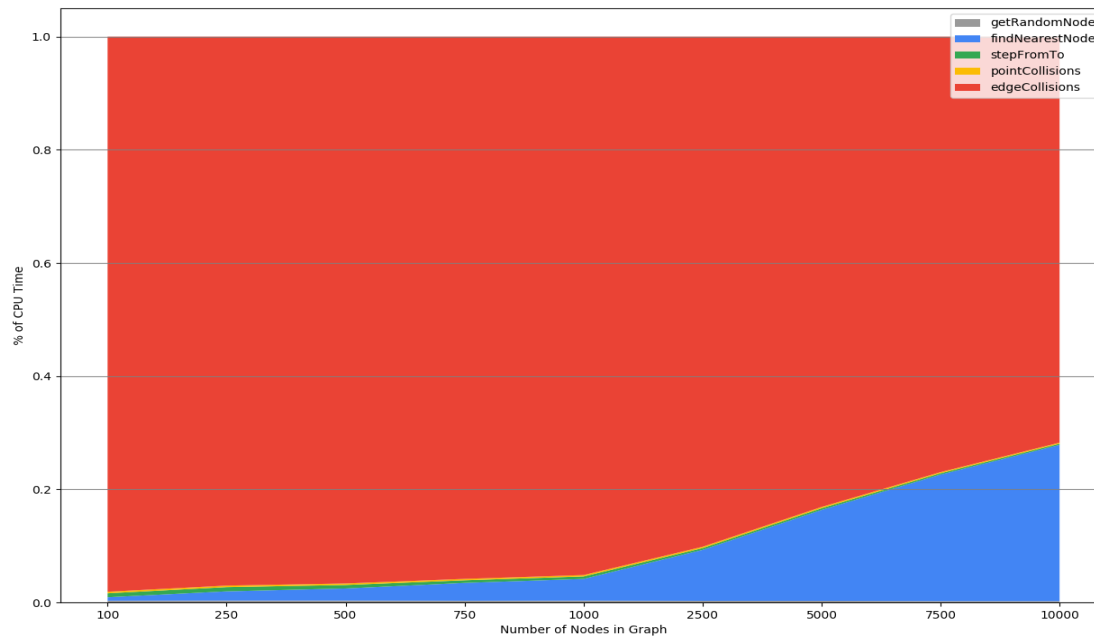


(b) 8x8x8 configuration Space

Figure 2.6: RRT Functions as a % of Total CPU Execution Time



(c) 16x16x16 configuration Space



(d) 32x32x32 configuration Space

Figure 2.6: RRT Functions as a % of Total CPU Execution Time (cont.)

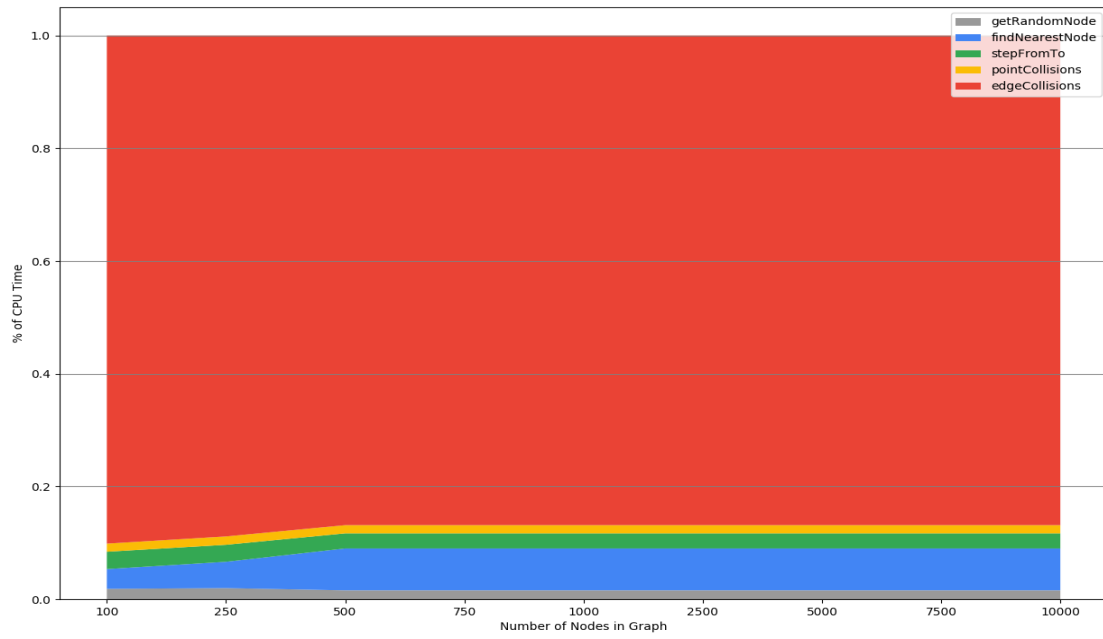
Change Y axis to % and increase text size

Furthermore, the computational load of `findNearestNode` can be reduced through a variety of software optimizations. A simple one used here to demonstrate that fact is storing nodes in separate “buckets,” sorted by their x value. By using only two buckets, the execution time of `findNearestNode` fell drastically. Figure 2.7b shows edge collision detection accounting for over 95% of execution time for $100 \leq K \leq 10000$. This is consistent with the profiling results of RRT in prior work[16].

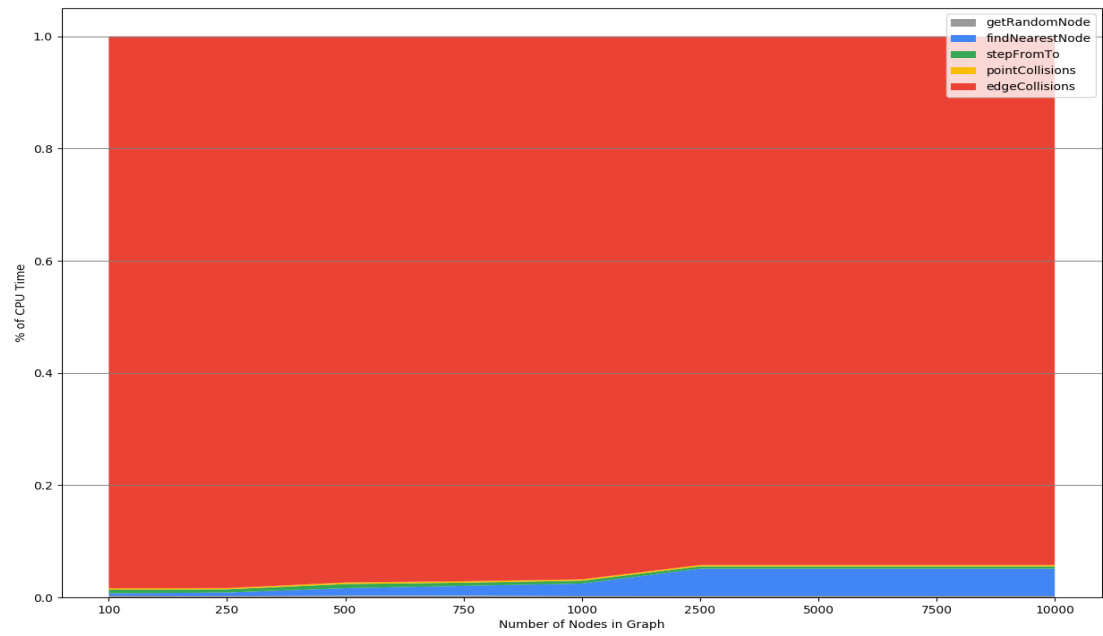
Conclusion

From the above data, it was identified that, as prior work suggested, edge collision detection shows the greatest promise for potential speedup through specialized hardware. The next chapter details the process of designing and building this hardware.

Add simulations to determine correct K



(a) 16x16x16 configuration Space



(b) 32x32x32 configuration Space

Figure 2.7: RRT Functions Execution Time, with Bucket Optimization

Chapter 3

Motion Planning in Hardware

3.1 Defining the Collision Detection Unit

It was demonstrated in Section 2.3.2 that the critical function of RRT was edge collision detection. As such, the thesis proposes designing a functional unit that takes advantage of pipelining and parallelization to speed up the detection of edge collisions. Section 3.1.2 outlines the technical specifications for the functional unit. Section 3.1.3 outlines the performance specifications.

3.1.1 Edge Collision Function

Edge Collision Function Description: Edge collision function and algorithm, perhaps both for normal and parallelized?

3.1.2 Technical Specifications

Put simply, the functional unit that implements the edge collision detection function in hardware should have the same rough technical specifications as when the function is defined in software (Section 3.1.1). That is, it should take an edge e and an Occupancy Grid Map (OGM) and return a boolean value: True, if the edge collides with an obstacle, otherwise False. Table 3.1 outlines the required technical specifications for the functional unit.

Element	Description/Justification
Constraints	
Dimension N	N defines the dimension of the cubic configuration space for which the functional unit should take an identically sized OGM
Inputs	
Edge e	An Edge e defined for a 3D configuration space by two points $\{p1, p2\}$, each defined by a set of 3D coordinates $\{x, y, z\}$.
Space S	In an abstract sense, the edge collision detection function takes Space S as an input. In a more practical sense, the functional unit will take an $N \times N \times N$ Occupancy Grid Map
Control Inputs	The functional unit must also have ports for control signals such as clock, reset, start, etc. These are required for adding the unit to a processor.
Outputs	
Return Value	1 bit return value: 1 if collision, 0 otherwise.
Control Outputs	Output ports for control signals such as idle, done, ready, etc. These are required for adding the unit to a processor.

Table 3.1: Technical Specifications for Edge Collision Detection Unit

Improve Technical Specifications: More detail on control units.

3.1.3 Performance Specifications

Performance Specifications Functional Unit

3.2 HoneyBee

The Honey Bee has long been renowned for its tireless work ethic. But people rarely give the Honey Bee credit for its remarkable navigation and collision avoidance strategies during flight. As such, it is quite appropriate that this functional unit, designed to work tirelessly, rapidly and efficiently to execute collision detection computations, is named HoneyBee.

More Iterations of HoneyBee Design: Note: Currently this report only shows the design/build/measurement of the first pass at designing the functional unit (Designated HoneyBee-A, or HB-A). Final report will detail further iterations.

3.2.1 Design

HoneyBee-A Design

The first design iteration, designated HoneyBee-A (HB-A), was designed to take advantage of the performance improvements associated with pipelining. Figure 3.1 demonstrates how pipelining in hardware improves latency. By default, instructions are executed in order, one at a time. Pipelining takes advantage of operations that are independent of each other to reduce the number of clock cycles required to complete a set of instructions.

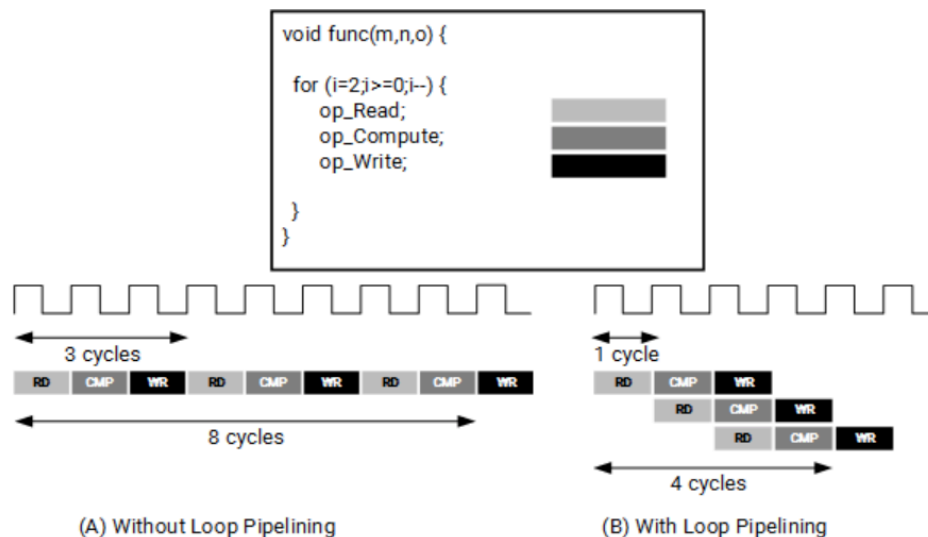


Figure 3.1: Pipelining to Improve Latency

Make my own version of this figure

3.2.2 Build

Hardware Description Languages

Introduction to Hardware Description Languages

High Level Synthesis

High Level Synthesis (HLS) is an automated hardware design process that takes design files (written in high-level languages, such as C, C++ or SystemC) specifying the algorithmic function of a piece of hardware, interprets those files and creates digital hardware designs that execute this function. It effectively translates programming languages into hardware description languages. Key advantages of using HLS is speed and verification. It is much faster and easier to define functionality in C than it is in a HDL such as Verilog, and thus design iterations are faster. It is also much simpler to verify one's design, as the functional units can be put through test benches written in C. This project used Vivado HLS to build the HoneyBee Unit.

HoneyBee-A Synthesis

Figure 3.2 shows the interface summary of successful synthesis of HoneyBee-A. Notice that the edge input has been split into 6 32 bit input ports.

RTL Ports	Dir	Bits	Protocol	Source Object	C Type
ap_clk	in	1	ap_ctrl_hs	honeybee	return value
ap_rst	in	1	ap_ctrl_hs	honeybee	return value
ap_start	in	1	ap_ctrl_hs	honeybee	return value
ap_done	out	1	ap_ctrl_hs	honeybee	return value
ap_idle	out	1	ap_ctrl_hs	honeybee	return value
ap_ready	out	1	ap_ctrl_hs	honeybee	return value
ap_return	out	32	ap_ctrl_hs	honeybee	return value
edge_p1_x	in	32	ap_none	edge_p1_x	scalar
edge_p1_y	in	32	ap_none	edge_p1_y	scalar
edge_p1_z	in	32	ap_none	edge_p1_z	scalar
edge_p2_x	in	32	ap_none	edge_p2_x	scalar
edge_p2_y	in	32	ap_none	edge_p2_y	scalar
edge_p2_z	in	32	ap_none	edge_p2_z	scalar

Figure 3.2: Interface Summary of HoneyBee-A Synthesis in Vivado HLS

Turn this into a table or get image from vivado

3.2.3 Measurement and Analysis

HoneyBee-A

The synthesis results of HoneyBee-A are shown in Table 3.2. It compares the execution time in microseconds for one edge to undergo collision detection if software and then in different synthesis “solutions”. MacOS and Ubuntu executing the function defined in honeybee.c have fairly similar results. Solution 1, which is the synthesized version of honeybee.c without any pipelining, was significantly slower. This is to be expected, as both MacOS and Ubuntu, operating on intel processors, would likely have some degree of pipelining and optimization of executing the compiled C code. However, significant improvements are observed once pipelining is implemented. Solutions 2-4 are increasing amounts of pipelining. Across the board, solutions 3 and 4 are roughly equal, but significantly faster than both solution 1 and the MacOS/Ubuntu execution times. Solution 4 shows a speedup of over 10x MacOS and Ubuntu.

Dimensions	Mac OS	Ubuntu	1	2	3	4
4x4x4	2	2	21.6	1.5	0.44	0.47
8x8x8	23	19	151	5.53	2.2	1.79
16x16x16	166	180	1133	41.37	13.08	12.11
32x32x32	1317	1424	8783	328	103	104

Table 3.2: Simulated performance of HB-A in microseconds

When HoneyBee-A is simulated in full RRT execution, we see similarly promising results. Table 3.3 shows the results of simulated RRT execution with HoneyBee-A. This is also shown in Figure 3.3.

Executions	K	Software	Sol. 1	Sol. 2	Sol. 3	Sol. 4
1221	100	0.420	100.724	0.400	0.125	0.126
2986	250	1.251	26.226	0.979	0.307	0.310
5719	500	1.997	50.229	1.875	0.589	0.594
8299	750	2.907	72.890	2.722	0.854	0.863
11148	1000	4.798	97.912	3.656	1.148	1.159
27203	2500	9.172	238.923	8.922	2.801	2.829
54499	5000	18.509	478.664	17.875	5.613	5.667
80952	7500	27.833	711.001	26.552	8.338	8.419
107487	10000	36.311	944.058	35.255	11.071	11.178

Table 3.3: RRT Simulated Execution Times with HB-A (seconds)

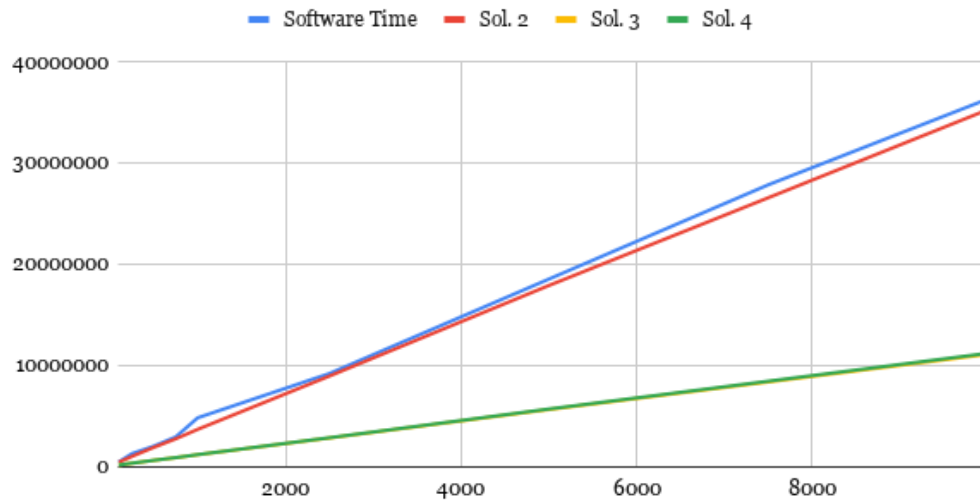


Figure 3.3: RRT Simulated Execution Time with HB-A (microseconds)

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Expand Discussion of HoneyBee-A Results

Chapter 4

RISC-V Processor

4.1 Introduction to the Reduced Instruction Set Computer

4.1.1 Instruction Set Architecture

An Instruction Set Architecture can be thought of as an abstract model of a computer. On a broad level, it defines the data types, memory model, and registers of a computer, along with the instructions that it can execute.

It can also be thought as a “contract” between hardware and software developers. It is the promise made that the hardware will be able to execute all instructions defined in the ISA, and the limitation that software must be compiled into that set of instructions.

4.1.2 RISC Processor Design

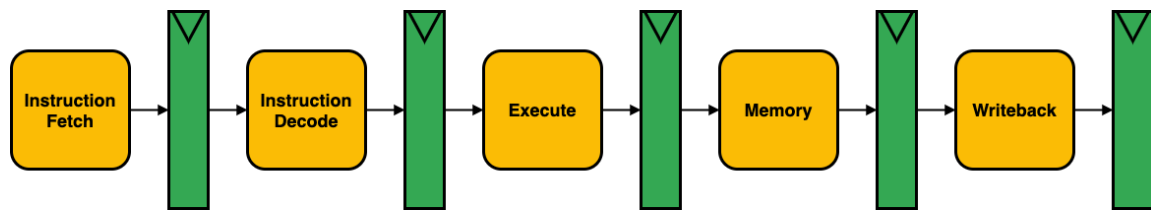


Figure 4.1: 5-Stage RISC Datapath

4.2 RISC-V ISA

4.2.1 RV32I

The following is an excerpt from the RISC-V Specification, outlining the RV32I base integer instruction set [7]

RV32I was designed to be sufficient to form a compiler target and to support modern operating system environments. The ISA was also designed to reduce the hardware required in a minimal implementation. RV32I contains 40 unique instructions, though a simple implementation might ...[reduce] base instruction count to 38 total. RV32I can emulate almost any other ISA extension ...

Subsets of the base integer ISA might be useful for pedagogical purposes, but the base has been defined such that there should be little incentive to subset a real hardware implementation ...

Registers

RV32I defines 32 unprivileged registers, each 32 bits wide. They are designated **x0-x31**, where **x0** is a hard-wired value of 0, and registers **x1-x31** hold values that various instructions use. RISC-V uses the load-store method, meaning that all operations perform on two registers or a register and an immediate, rather than performing operations directly on memory addresses. In addition, the 33rd unprivileged register is the program counter **pc**. Table 4.1 shows the register state for the RV32I Base Integer Instruction Set.

Register	ABI Name	Description
x0	zero	Hard-wired zero
x1	ra	Return address
x2	sp	Stack pointer
x3	gp	Global pointer
x4	tp	Thread pointer
x5-7	t0-2	Temporaries
x8	s0/fp	Saved register/Frame pointer
x9	s1	Saved register
x10-11	a0-1	Function arguments/return values
x12-17	a2-7	Function arguments
x18-27	s2-11	Saved registers
x28-31	t3-6	Temporaries
pc	pc	Program counter

Table 4.1: Register State for RV32I Base Instruction Set

Instruction Formats

Table 4.2 demonstrates the format of each different instruction type.

31	30	25	24	21	20	19	15	14	12	11	8	7	6	0	
funct7				rs2			rs1	funct3		rd			opcode		R-type
imm[11:0]						rs1	funct3		rd			opcode		I-type	
imm[11:5]				rs2			rs1	funct3		imm[4:0]			opcode		S-type
imm[12]	imm[10:5]			rs2			rs1	funct3		imm[4:1]	imm[11]	opcode		B-type	
imm[31:12]										rd			opcode		U-type
imm[20]	imm[10:1]				imm[11]		imm[19:12]			rd			opcode		J-type

Table 4.2: RV32I Base Instruction Formats

4.2.2 Motion Planning Extension

Motion Planning Extension: Full description of design of Non standard extension for motion planning. Should follow define, design, build, measure, analyse etc format.

4.3 PhilosophyV

Philosophy IV, written in 1903 by Mr. Owen Wister of the Class of 1882, recounts the antics of two Harvard students and their last minute attempts to study (or avoid studying) for an exam for which they are hopelessly unprepared. Similarly, this section details the process of my attempt to build a RISC-V processor, by far the most complex part of this Thesis, and a task for which I am unsure of my preparedness. As such, this processor is named Philosophy V; both in reference to the RISC-V ISA for which it is designed, and to the fact that my current situation seems much like a sequel to Mr. Wister's novel.

4.3.1 Baseline Implementation

Description of Baseline Philosophy V core

Figure 4.2 provides a schematic of the PhilosophyV processor.

Display bigger version of processor.

4.3.2 Implementing HoneyBee

Process of implementing honeybee into PhilV.

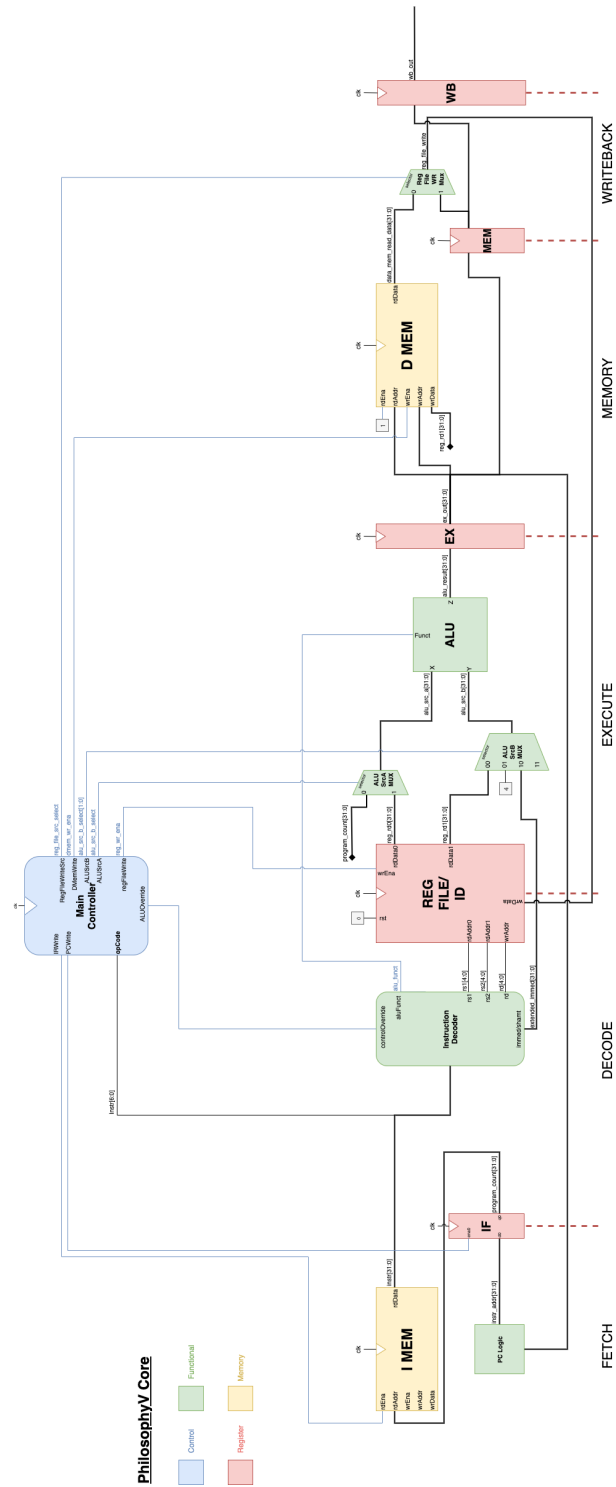


Figure 4.2: Philosophy V Processor

4.4 Performance Analysis

Comparative Performance Analysis of baseline and extended PhilV Core

Chapter 5

Conclusion

5.1 Discussion of Results

Discussion of Results

5.2 Evaluation of Success

Evaluation of Success

5.3 Future Work

Future Work

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Glossary

A priori: relating to or denoting reasoning or knowledge which proceeds from theoretical deduction rather than from observation or experience..

Automata: moving mechanical devices made in imitation of human beings.

Configuration: A specification of a robots location, position, and setting in a space. For example, when a robot is represented by a single point in 3D space, its configuration is merely x, y, and z coordinates. But if a robot is represented as a 3D humanoid with a head, body, arms and legs, then its configuration would be its position in 3D space, its orientation in 3D, and the position of all its joints and limbs such that the space being taken up by the robot can be exactly determined. It is obvious then that as the physical complexity of a robot increases, so too does the complexity of representing it algorithmically..

Hardware acceleration: The process of speeding up the execution of a function by implementing part or whole of that function specifically in hardware..

Probabilistically complete: Describes an algorithm with a likelihood of finding a solution that approaches one as its runtime approaches infinity..

Real-time: Describes a system in which input data is processed in such a time period such that it is available almost immediately. Systems such as missile guidance or collision avoidance in cars are an example of real-time systems.

Tethered robot: Refers to robots that are limited by a cable connection for power, data transfer, communication, or control..

Application Programming Interface (API): A particular set of rules and specifications that a software program can follow to access and make use of the services and resources provided by another particular software program that implements that API.

Advanced RISC Machine (ARM): A family of Reduced Instruction Set Computing architectures for computer processors, configured for various environments..

Complex Instruction Set Computer (CISC): A computer in which single instructions can execute several low-level operations (such as a load from memory, an arithmetic operation, and a memory store) or are capable of multi-step operations or addressing modes within single instructions..

Central Processing Unit (CPU): The component within a computer that executes instructions, by interpreting them and controlling their flow through arithmetic and logic units. It can be thought of as the brain of a computer..

Degree-of-Freedom (DOF): Refers to the number of independent factors that describe the configurations in which a robot can exist and motion can occur..

Field Programmable Gate Array (FPGA): An integrated circuit designed to be configured by a designer after manufacturing – hence the term ‘field-programmable’. Its behaviour is specified in software, using a HDL.

Graphics Processing Unit (GPU): Similar to a CPU, a high-powered circuit designed for highly parallelized computation of images for a display device. Their highly parallel nature mean they can be utilised for other, non-graphics related, computations..

Hardware Description Language (HDL): A computer language used for designing computer hardware. It is used to define the behaviour of modules, simulate their performance, and synthesize them on an FPGA.

High Level Synthesis (HLS): An automated hardware design process that takes software written in high-level languages (often C, C++) that algorithmically defines a function, and converts that into HDL that implements that function..

Instruction Set Architecture (ISA): An abstract model of a computer, that defines the instructions, registers, memory behaviour, and other attributes of a computer architecture. It can be thought of as the contract between software and hardware developers, as the ISA lists the instructions that software may be implemented in, and the instructions that a processor must support..

Occupancy Grid Map (OGM): A method of representing a 2D or 3D space by dividing it into discrete grids and marking each whole grid as ‘occupied’, even if only part of it is..

Probabilistic Road Map (PRM): A motion planning algorithm that randomly samples free space, and then connects sampled configurations with nearby configurations to build a map..

Reduced Instruction Set Computer (RISC): A computer architecture based on a small number of instructions executed in a small number of cycles..

Rapidly-exploring Random Tree (RRT): an algorithm designed to efficiently search, and thus plan a path through, a high-complexity environment by randomly sampling points and building a tree. The algorithm randomly samples points, draws an edge from the nearest currently existing node in the tree, to grow the tree in the space..

Real-Time Operating Systems (RTOS): A type of operating system designed to operate on inputs as they come in, without buffer delays..

RISC-V 32-Bit Integer (RV32I): One of the four base ISAs within RISC-V. While it implements integer values only in 32-bit representations, it contains the minimal number of instructions for a fully working computer processor..

System on Chip (SoC): A chip that includes all required components of a working computer, including one or more CPUs, memory, I/O ports, etc..

Unmanned Aerial Vehicle (UAV): An aircraft without a human pilot on board. It may be piloted remotely completely by a human pilot, autonomously pilot itself, or a mixture of the two..

Appendices

Appendix A

Project Repository

This project's repository can be found at github.com/AnthonyKenny98/Thesis and contains multiple subrepositories. It has the following structure.

Research

This folder holds the academic papers that constitute the background research of this Thesis.

Writeups

This folder holds the writeups required for this Thesis, including checkpoints in fulfillment of Harvard's ES100hf class and this Final Report

RRT

github.com/AnthonyKenny98/RRT

This subrepository holds both the 2D and 3D implementations of RRT used for this thesis, along with the tools required for both VTune Profiler and internal timing analysis.

HoneyBee

github.com/AnthonyKenny98/HoneyBee

This subrepository holds the HoneyBee functional unit, a hardware implementation of collision detection.

PhilosophyV

github.com/AnthonyKenny98/PhilosophyV

This subrepository holds the PhilosophyV RISCv chip

Appendix B

Budget

Budget

Appendix C

RRT Supporting Documentation

C.1 Justification of K:DIM Ratio

Todo list

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<input type="checkbox"/>	Define goal	1
<input type="checkbox"/>	cite	1
<input type="checkbox"/>	More of an introduction to motion planning.	2
<input type="checkbox"/>	Subsubsection for Problem Overview	3
<input type="checkbox"/>	Improve Problem Statement	4
<input type="checkbox"/>	Revise End User	4
<input type="checkbox"/>	Project Specifications	9
<input type="checkbox"/>	Summary of Results	10
<input type="checkbox"/>	Update once I have properly defined goals and objectives	11
<input type="checkbox"/>	Better RRT Implementation introductory sentence	16
<input type="checkbox"/>	Change this based on whether time does permit	16
<input type="checkbox"/>	Improve this table	16
<input type="checkbox"/>	More detail	17
<input type="checkbox"/>	Describe implementation in 3D	18
<input type="checkbox"/>	Brief introduction outlining purpose of performance analysis	19
<input type="checkbox"/>	Outline of method of analysis. Something better than the above	19
<input type="checkbox"/>	Rewrite the above	19
	Figure: Screenshot of VTune Top Down Analysis (Maybe)	19
<input type="checkbox"/>	Provide or link to appendix of explanation of internal timing	20
<input type="checkbox"/>	Explanation of time complexity	20
<input type="checkbox"/>	Change Y axis to % and increase text size	23
<input type="checkbox"/>	Add simulations to determine correct K	23
<input type="checkbox"/>	Edge Collision Function Description	25
<input type="checkbox"/>	Improve Technical Specifications	26
<input type="checkbox"/>	Performance Specifications Functional Unit	26
<input type="checkbox"/>	More Iterations of HoneyBee Design	27
<input type="checkbox"/>	Make my own version of this figure	27
<input type="checkbox"/>	Introduction to Hardware Description Languages	28
<input type="checkbox"/>	Turn this into a table or get image from vivado	29
<input type="checkbox"/>	Make version of this chart in matplotlib for consistency and update axis	31

<input type="checkbox"/>	Expand Discussion of HoneyBee-A Results	31
<input type="checkbox"/>	Motion Planning Extension	34
<input type="checkbox"/>	Description of Baseline Philosophy V core	34
<input type="checkbox"/>	Display bigger version of processor.	34
<input type="checkbox"/>	Process of implementing honeybee into PhilV.	34
<input type="checkbox"/>	Comparative Performance Analysis of baseline and extended PhilV Core	36
<input type="checkbox"/>	Discussion of Results	37
<input type="checkbox"/>	Evaluation of Success	37
<input type="checkbox"/>	Future Work	37
<input type="checkbox"/>	Budget	45