

f) What are the terms  $a_0, a_1, a_2$ , and  $a_3$  of the sequence  $\{a_n\}$  where  $a_n$  equals:

a)  $(-2)^n$ :  $-2^0 = 1, -2^1 = -2, -2^2 = 4, -2^3 = -8$

b) 3:  $a_0 = 3, a_1 = 3, a_2 = 3, a_3 = 3$

c)  $7 + 4^n$ :  $7 + 4^0 = 8, 7 + 4^1 = 11, 7 + 4^2 = 23, 7 + 4^3 = 71$

d)  $2^n + (-2)^n$ :  $2^0 + (-2)^0 = 2, 2^1 + (-2)^1 = 0, 2^2 + (-2)^2 = 8, 2^3 + (-2)^3 = 0$

29) What are the values of these sums?

a)  $\sum_{k=1}^5 (-2)^k (k+1) = \sum_{k=1}^5 k + \sum_{k=1}^5 1 = 15 + 5 = 20$

c)  $\sum_{i=1}^{10} 3 = 30$  ( $10 \cdot 3$ )

b)  $\sum_{j=0}^4 (-2)^j = (-2^0) + (-2^1) + (-2^2) + (-2^3) + (-2^4) = 1 + (-2) + 4 + (-8) + 16 = 11$

\*d)  $\sum_{j=0}^8 (2^{j+1} - 2^j) = \sum_{j=0}^8 2^j = \frac{2^{8+1} - 2^0}{2 - 1} = 511$

31) What is the val of each of these sums of terms of a geo progression?

a)  $\sum_{j=0}^8 3 \cdot 2^j = 3 \sum_{j=0}^8 2^j = 3 \left( \frac{2^{8+1} - 1}{2 - 1} \right) = 1533$

b)  $\sum_{j=1}^8 2^j = \sum_{j=1}^8 2^j - \sum_{j=0}^0 2^j = \frac{2^{8+1} - 2^0}{2 - 1} - \frac{2^1 - 2^0}{2 - 1} = 511 - 1 = 510$

c)  $\sum_{j=2}^9 (-3)^j = \frac{-3^{8+1} - (-3^2)}{-3 - 1} = \frac{-3^9 + 9}{-4} = 4923$

d)  $\sum_{j=0}^8 2 \cdot (-3)^j = 2 \sum_{j=0}^8 (-3)^j = 2 \left( \frac{-3^{8+1} - 1}{-3 - 1} \right) = \frac{-3^9 - 1}{-4} = 4921 \times 2 = 9842$

32) Find the val of each of these sums

a)  $\sum_{j=0}^8 (1 + (-1)^j)$

b)  $\sum_{j=0}^8 (3^j - 2^j) = \sum_{j=0}^8 3^j - \sum_{j=0}^8 2^j = \frac{3^{8+1} - 1}{3 - 1} - \frac{2^{8+1} - 1}{2 - 1} = \frac{3^9 - 1}{2} - 511 = 9841 - 511 = 9330$

c)  $\sum_{j=0}^8 (2 \cdot 3^j + 3 \cdot 2^j) = 2 \sum_{j=0}^8 3^j + 3 \sum_{j=0}^8 2^j = 2 \left( \frac{3^9 - 1}{3 - 1} \right) + 3 \left( \frac{2^9 - 1}{2 - 1} \right) = 21215$