

Section 2.1: 8, 10, 14, 18, 20, 32

8)

a). $\{x \in \mathbb{R} \mid x \text{ is an integer greater than } 1\}$

No.

b). $\{x \in \mathbb{R} \mid x \text{ is the square of an integer}\}$

No.

c). $\{2, \{2\}\}$

Yes.

d). $\{\{2\}, \{\{2\}\}\}$

Yes.

e). $\{\{2\}, \{2, \{2\}\}\}$

Yes.

f). $\{\{\{\{2\}\}\}\}$

No.

10)

a). $\emptyset \in \{\emptyset\}$

True.

b). $\emptyset \in \{\emptyset, \{\emptyset\}\}$

True.

c). $\{\emptyset\} \in \{\emptyset\}$

False.

d). $\{\emptyset\} \in \{\{\emptyset\}\}$

True.

e). $\{\emptyset\} \subset \{\emptyset, \{\emptyset\}\}$

True.

f). $\{\{\emptyset\}\} \subset \{\emptyset, \{\emptyset\}\}$

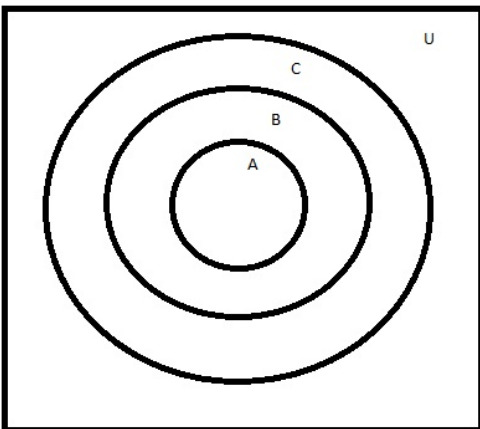
True.

sets are not equal.)

g). $\{\{\emptyset\}\} \subset \{\{\emptyset\}, \{\emptyset\}\}$

False. These are equal.

14)



18) Find two sets A and B such that $A \in B$ and $A \subseteq B$.

$A = \{1\}$

$B = \{2, \{1\}\}$

20)

a). $|\emptyset|$

0 this is not a set

b) $|\{\emptyset\}|$

1

c) $|\{\emptyset, \{\emptyset\}\}|$

2

d) $|\{\emptyset, \{\emptyset\}, \{\emptyset, \{\emptyset\}\}\}|$

3

32) Let $A = \{a, b, c\}$, $B = \{x, y\}$. and $C = \{0, 1\}$

a) $A \times B \times C$

$\{(a, x, 0), (a, x, 1), (a, y, 0), (a, y, 1), (b, x, 0), (b, x, 1), (b, y, 0), (b, y, 1), (c, x, 0), (c, x, 1), (c, y, 0), (c, y, 1)\}$

b) $C \times B \times A$

$\{(0, x, a), (0, x, b), (0, x, c), (1, x, a), (1, x, b), (1, x, c), (0, y, a), (0, y, b), (0, y, c), (1, y, a), (1, y, b), (1, y, c)\}$

c) $C \times A \times B$

$\{(0, a, x), (0, a, y), (0, b, x), (0, b, y), (0, c, x), (0, c, y), (1, a, x), (1, a, y), (1, b, x), (1, b, y), (1, c, x), (1, c, y)\}$

d) $B \times B \times B$

$\{(x, x, x), (x, x, y), (x, y, x), (x, y, y), (y, x, x), (y, x, y), (y, y, x), (y, y, y)\}$