

CH 6.3: 6, 10, 12, 24, 26

6) Find the value of each of these quantities.

a)  $C(5, 1) = 5!/4!1! = 5/1 = \mathbf{5}$

b)  $C(5, 3) = 5!/2!3! = 5 \times 2 = \mathbf{10}$

c)  $C(8, 4) = 8!/4!4! = 2 \times 7 \times 2 \times 5/2 = \mathbf{70}$

d)  $C(8, 8) = 8!/8!0! = \mathbf{1}$

e)  $C(8, 0) = 8!/0!8! = \mathbf{1}$

f)  $C(12, 6) = 12!/6!6! = 2 \times 11 \times 2 \times 3 \times 7 = \mathbf{924}$

10) There are six different candidates for governor of a state. In how many different orders can the names of the candidates be printed on a ballot?

$P(6, 6) = 6 \times 5 \times 4 \times 3 \times 2 \times 1 = \mathbf{720}$

12) How many bit strings of length 12 contain

a) exactly three 1s?

$C(12, 3) = 12!/3!9! = 4 \times 11 \times 5 = \mathbf{220}$

b) at most three 1s?

$C(12, 0)C(12, 1)C(12, 2)C(12, 3)$

$1$

$12!/1!11! = 12$

$12!/2!10! = 66$

$12!/3!9! = 220$

$1 + 12 + 66 + 220 = \mathbf{299}$

c) at least three 1s?

$2^{12} = 4096$  (all poss.)

$C(12, 0)C(12, 1)C(12, 2) = 79$

$4096 - 79 = \mathbf{4017}$

d) an equal number of 0s and 1s?

$C(12, 6) = \mathbf{924}$  (per 6F)

24) How many ways are there for 10 women and six men to stand in a line so that no two men stand next to each other? [Hint: First position the women and then consider possible positions for the men.]

M W M W M W M W M W M W M W M W M W M W M

$C(10, 10)C(11, 6) = 10! \times 11!/5! = \mathbf{1, 207, 084, 032, 000}$

26) Thirteen people on a softball team show up for a game.

a) How many ways are there to choose 10 players to take the field?

$C(13, 10) = 13!/10!3! = 13 \times 4 \times 11 / 2 = \mathbf{286}$

b) How many ways are there to assign the 10 positions by selecting players from the 13 people who show up?

$13 \times 12 \times 11 \times 10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 / 3 \times 2 \times 1 = \mathbf{1,037,836,800}$

c) Of the 13 people who show up, three are women. How many ways are there to choose 10 players to take the field if at least one of these players must be a woman?

$C(13, 10) - 1 = 286 - 1 = \mathbf{285}$