

CH 6.5: 6, 8, 12, 14

6) How many ways are there to select five unordered elements from a set with three elements when repetition is allowed?

$5 + 2 \text{ bars} = 7$

5 elements

$$C(7, 5) = 7!/5!2! = \mathbf{21}$$

8) How many different ways are there to choose a dozen donuts from the 21 varieties at a donut shop

$$C(21 + 12 - 1, 12) = C(32, 12) = \mathbf{225,792,840}$$

12) How many different combinations of pennies, nickels, dimes, quarters, and half dollars can a piggy bank contain if it has 20 coins in it?

$$C(5+20-1, 20) = C(24, 20) = C(24, 4) = \mathbf{10,626}$$

14) How many solutions are there to the equation $x_1 + x_2 + x_3 + x_4 = 17$, where x_1, x_2, x_3 , and x_4 are nonnegative integers?

$$C(4 + 17 - 1, 17) = C(20, 17) = C(20, 3) = \mathbf{1,140}$$