

First Pass, remove combo rules

Pgm = kwdprog Vargroup Fcndefs Main

Main = kwdmain BBlock

BBlock = brace1 Vargroup Stmts brace2

Pgm = kwdprog Vargroup Fcndefs kwdmain brace1 Vargroup Stmts brace2

Vargroup = kwdvars PPvarlist

Vargroup = eps

PPvarlist = parens1 Varlist parens2

Varlist = Varitem semi Varlist

Varlist = eps

Varitem = Vardecl

Varitem = Vardecl equal Varinit

Varitem = Classdecl

Varitem = Classdef

Vardecl = Simplekind Varspec

Simplekind = Basekind

Simplekind = Classid

Basekind = int

Basekind = float

Basekind = string

Classid = id

Varspec = Varid

Varspec = Arrspec

Varspec = Deref\_id

Varid = id

Arrspec = Varid KKint

KKint = bracket1 int bracket2

Deref\_id = Deref id

Deref = aster

Varinit = Expr

Varinit = BBexprs

BBexprs = brace1 Exprlist brace2

BBexprs = brace1 brace2

Exprlist = Expr Moreexprs

Moreexprs = comma Exprlist

Moreexprs = eps

Classdecl = kwddclass Classid

Classdef = Classheader BBclassitems

BBclassitems = brace1 Classitems brace2

Classheader = Classdecl Classmom Interfaces

Classmom = colon Classid

Classmom = eps

Classitems = Classgroup Classitems

Classitems = eps

Classgroup = Class\_ctrl

Classgroup = Varlist

Classgroup = Mddecls

Class\_ctrl = colon id // in {public, protected, private}

Interfaces = colon Classid Interfaces

Interfaces = eps

Mddecls = Mdheader Mddecls

Mddecls = eps

Mdheader = kwdfcn Md\_id PParmlist Retkind

Md\_id = Classid colon Fcnid

Fcndefs = Fcndef Fcndefs

Fcndefs = eps

Fcndef = Fcnheader BBlock

Fcnheader = kwdfcn Fcnid PParmlist Retkind

Fcnid = id

Retkind = Kind

PParmlist = parens1 Varspecs parens2

PParmlist = PPOnly

Varspecs = Varspec More\_varspecs

More\_varspecs = comma Varspecs

More\_varspecs = eps

PPOnly = parens1 parens2

Stmts = Stmt semi Stmts

Stmts = eps

Stmt = Stasgn

Stmt = Fcall  
Stmt = Stif  
Stmt = Stwhile  
Stmt = Stprint  
Stmt = Strtn

Stasgn = Lval equal Expr  
Lval = Varid  
Lval = Aref  
Lval = Deref\_id  
Aref = Varid KKexpr  
KKexpr = bracket1 Expr bracket2

Fcall = Fcnid PPexprs  
PPexprs = parens1 Exprlist parens2  
PPexprs = PPonly

Stif = kwdif PPexpr BBlock Elsepart  
Elsepart = kwdelseif PPexpr BBlock Elsepart  
Elsepart = kwdelse BBlock  
Elsepart = eps

Stwhile = kwdwhile PPexpr BBlock  
Stprint = kprint PPexprs

Strtn = kwdreturn Expr  
Strtn = kwdreturn

PPexpr = parens1 Expr parens2  
Expr = Expr Oprel Rterm  
Expr = Rterm  
Rterm = Rterm Opadd Term  
Rterm = Term  
Term = Term Opmul Fact  
Term = Fact  
Fact = Basekind  
Fact = Lval  
Fact = Addrrof\_id  
Fact = Fcall

Fact = PPexpr  
Addrof\_id = ampersand id  
Oprel = opeq  
Oprel = opne  
Oprel = Lthan  
Oprel = ople  
Oprel = opge  
Oprel = Gthan  
Lthan = angle1  
Gthan = angle2  
Opadd = plus  
Opadd = minus  
Opmul = aster  
Opmul = slash  
Opmul = caret

Second Pass, LRE

Pgm = kwdprog Vargroup Fcndefs Main  
Main = kwdmain BBlock  
BBlock = brace1 Vargroup Stmts brace2

Vargroup = kwdvars PPvarlist  
Vargroup = eps  
PPvarlist = parens1 Varlist parens2  
Varlist = Varitem semi Varlist  
Varlist = eps  
Varitem = Vardecl  
Varitem = Vardecl equal Varinit  
Varitem = Classdecl  
Varitem = Classdef  
Vardecl = Simplekind Varspec  
Simplekind = Basekind  
Simplekind = Classid  
Basekind = int  
Basekind = float  
Basekind = string  
Classid = id

Varspec = Varid  
Varspec = Arrspec  
Varspec = Deref\_id  
Varid = id  
Arrspec = Varid KKint  
KKint = bracket1 int bracket2  
Deref\_id = Deref id  
Deref = aster

Varinit = Expr  
Varinit = BBexprs  
BBexprs = brace1 Exprlist brace2  
BBexprs = brace1 brace2  
Exprlist = Expr Moreexprs  
Moreexprs = comma Exprlist  
Moreexprs = eps

Classdecl = kwdclass Classid  
Classdef = Classheader BBclassitems  
BBClassitems = brace1 Classitems brace2  
Classheader = Classdecl Classmom Interfaces  
Classmom = colon Classid  
Classmom = eps  
Classitems = Classgroup Classitems  
Classitems = eps  
Classgroup = Class\_ctrl  
Classgroup = Varlist  
Classgroup = Mddecls  
Class\_ctrl = colon id // in {public, protected, private}  
Interfaces = colon Classid Interfaces  
Interfaces = eps

Mddecls = Mdheader Mddecls  
Mddecls = eps  
Mdheader = kwdfcn Md\_id PParmlist Retkind  
Md\_id = Classid colon Fcnid

Fcndefs = Fcndef Fcndefs  
Fcndefs = eps

Fcndef = Fcnheader BBlock

Fcnheader = kwdfcn Fcnid PParmlist Retkind

Fcnid = id

Retkind = Kind

PParmlist = parens1 Varspecs parens2

PParmlist = PPOnly

Varspecs = Varspec More\_varspecs

More\_varspecs = comma Varspecs

More\_varspecs = eps

PPOnly = parens1 parens2

Stmts = Stmt semi Stmts

Stmts = eps

Stmt = Stasgn

Stmt = Fcall

Stmt = Stif

Stmt = Stwhile

Stmt = Stprint

Stmt = Strtn

Stasgn = Lval equal Expr

Lval = Varid

Lval = Aref

Lval = Deref\_id

Aref = Varid KKexpr

KKexpr = bracket1 Expr bracket2

Fcall = Fcnid PPexprs

PPexprs = parens1 Exprlist parens2

PPExprs = PPOnly

Stif = kwdif PPexpr BBlock Elsepart

Elsepart = kwelseif PPexpr BBlock Elsepart

Elsepart = kwelse BBlock

Elsepart = eps

Stwhile = kwdwhile PPexpr BBlock

Stprint = kprint PPexprs

Strtn = kwdreturn Expr

Strtn = kwdreturn

Q = eps

PPexpr = parens1 Expr parens2

Expr = Expr Oprel Rterm

Expr = Expr Oprel Rterm Q

Q = Oprel Rterm Q

Expr = Rterm

Rterm = Rterm Opadd Term

Rterm = Rterm Opadd Term Q

Q = Opadd Term Q

Rterm = Term

Term = Term Opmul Fact

Term = Term Opmul Fact Q

Q = Opmul Fact Q

Term = Fact

Fact = Basekind

Fact = Lval

Fact = Addr<sub>of</sub>\_id

Fact = Fcall

Fact = PPexpr

Addr<sub>of</sub>\_id = ampersand id

Oprel = opeq

Oprel = opne

Oprel = Lthan

Oprel = ople

Oprel = opge

Oprel = Gthan

Lthan = angle1

Gthan = angle2

Opadd = plus

Opadd = minus

Opmul = aster

Opmul = slash

Opmul = caret

Added LRE Rules:

$Q = \text{eps}$

$Q = \text{Oprel Rterm } Q$

$Q = \text{Opadd Term } Q$

$Q = \text{Opmul Fact } Q$

Third Pass, identify disappearing Non-Terminals

Disappearing Non-Terminals:

Direct:

Vargroup

Varlist

Moreexprs

Classmom

Classitems

Interfaces

Mddecls

Fndefs

More\_varspecs

Stmts

Elsepart

Indirect:

Rule 44:  $\text{Classgroup} \rightarrow \text{Varlist} \rightarrow \text{eps}$

Rule 45:  $\text{Classgroup} \rightarrow \text{Mddecls} \rightarrow \text{eps}$

1.  $\text{Pgm} = \text{kwdprog Vargroup Fndefs Main}$
2.  $\text{Main} = \text{kwdmain BBlock}$
3.  $\text{BBlock} = \text{brace1 Vargroup Stmts brace2}$
4.  $\text{Vargroup} = \text{kwdvars PPvarlist}$
5.  $\text{Vargroup} = \text{eps}$
6.  $\text{PPvarlist} = \text{parens1 Varlist parens2}$
7.  $\text{Varlist} = \text{Varitem semi Varlist}$
8.  $\text{Varlist} = \text{eps}$
9.  $\text{Varitem} = \text{Vardecl}$
10.  $\text{Varitem} = \text{Vardecl equal Varinit}$



11. Varitem = Classdecl  
12. Varitem = Classdef  
13. Vardecl = Simplekind Varspec  
14. Simplekind = Basekind  
15. Simplekind = Classid  
16. Basekind = int  
17. Basekind = float  
18. Basekind = string  
19. Classid = id  
20. Varspec = Varid  
21. Varspec = Arrspec  
22. Varspec = Deref\_id  
23. Varid = id  
24. Arrspec = Varid KKind  
25. KKind = bracket1 int bracket2  
26. Deref\_id = Deref id  
27. Deref = aster  
  
28. Varinit = Expr  
29. Varinit = BBexprs  
30. BBexprs = brace1 Exprlist brace2  
31. BBexprs = brace1 brace2  
32. Exprlist = Expr Moreexprs  
33. Moreexprs = comma Exprlist  
34. Moreexprs = eps  
  
35. Classdecl = kwdclass Classid  
36. Classdef = Classheader BBclassitems  
37. BBClassitems = brace1 Classitems brace2  
38. Classheader = Classdecl Classmom Interfaces  
39. Classmom = colon Classid  
40. Classmom = eps  
41. Classitems = Classgroup Classitems  
42. Classitems = eps  
43. Classgroup = Class\_ctrl  
44. Classgroup = Varlist  
45. Classgroup = Mddecls  
46. Class\_ctrl = colon id // in {public, protected, private}  
47. Interfaces = colon Classid Interfaces

48. Interfaces = eps

49. Mddecls = Mdheader Mddecls

50. Mddecls = eps

51. Mdheader = kwdfcn Md\_id PParmlist Retkind

52. Md\_id = Classid colon Fcnid

53. Fcndefs = Fcndef Fcndefs

54. Fcndefs = eps

55. Fcndef = Fcnheader BBlock

56. Fcnheader = kwdfcn Fcnid PParmlist Retkind

57. Fcnid = id

58. Retkind = Simplekind       //Asked professor during lab and said he needed to correct  
it from Retkind = Kind

59. PParmlist = parens1 Varspecs parens2

60. PParmlist = POnly

61. Varspecs = Varspec More\_varspecs

62. More\_varspecs = comma Varspecs

63. More\_varspecs = eps

64. POnly = parens1 parens2

65. Stmts = Stmt semi Stmts

66. Stmts = eps

67. Stmt = Stasgn

68. Stmt = Fcall

69. Stmt = Stif

70. Stmt = Stwhile

71. Stmt = Stprint

72. Stmt = Strtn

73. Stasgn = Lval equal Expr

74. Lval = Varid

75. Lval = Aref

76. Lval = Deref\_id

77. Aref = Varid KKexpr

78. KKexpr = bracket1 Expr bracket2

79. Fcall = Fcnid PPexprs

80. PPexprs = parens1 Exprlist parens2  
81. PPExprs = PPonly

82. Stif = kwdif PPexpr BBlock Elsepart  
83. Elsepart = kwdelseif PPexpr BBlock Elsepart  
84. Elsepart = kwdelse BBlock  
85. Elsepart = eps

86. Stwhile = kwdwhile PPexpr BBlock  
87. Stprint = kprint PPexprs

88. Strtn = kwdreturn Expr  
89. Strtn = kwdreturn

90. PPexpr = parens1 Expr parens2  
91. Expr = Rterm  
92. Rterm = Term  
93. Term = Fact  
94. Fact = Basekind  
95. Fact = Lval  
96. Fact = Addrrof\_id  
97. Fact = Fcall  
98. Fact = PPexpr  
99. Addrrof\_id = ampersand id

100. Oprel = opeq  
101. Oprel = opne  
102. Oprel = Lthan  
103. Oprel = ople  
104. Oprel = opge  
105. Oprel = Gthan  
106. Lthan = angle1  
107. Gthan = angle2  
108. Opadd = plus  
109. Opadd = minus  
110. Opmul = aster  
111. Opmul = slash  
112. Opmul = caret

Added LRE Rules:

- 113.  $Q = \text{eps}$
- 114.  $Q = \text{Oprel Rterm } Q$
- 115.  $Q = \text{Opadd Term } Q$
- 116.  $Q = \text{Opmul Fact } Q$

Left Factoring Rules:

To resolve: 9,10 in one cell

9.  $\text{Varitem} = \text{Vardecl } A$

117.  $A = \text{eps}$

118.  $A = \text{equal Varinit}$

To resolve 11,12 in one cell

11.  $\text{Varitem} = \text{ClassDecl VaritemTail}$

119.  $\text{VaritemTail} = \text{ClassDefTail}$

120.  $\text{VaritemTail} = \text{eps}$

121.  $\text{ClassDefTail} = \text{Classmom Interfaces BBclassitems}$

To resolve 20, 21 in one cell

20.  $\text{Varspec} = \text{id VarspecTail}$

122.  $\text{VarspecTail} = \text{eps}$

123.  $\text{VarspecTail} = \text{KKint}$

To resolve 30,31 in one cell

30.  $\text{BBexprs} = \text{brace1 BBexprsTail}$

124.  $\text{BBexprsTail} = \text{Exprlist brace2}$

125.  $\text{BBexprsTail} = \text{brace2}$

39, 40

41,42

41.  $\text{Classitems} = \text{ClassitemsTail}$

126.  $\text{ClassitemsTail} = \text{eps}$

127.  $\text{ClassitemsTail} = \text{ClassgroupTail Classitems}$

128.  $\text{ClassgroupTail} = \text{Class\_ctrl}$

129.  $\text{ClassgroupTail} = \text{VarlistTail}$

130.  $\text{ClassgroupTail} = \text{Mdheader Mddecls}$

131.  $\text{VarlistTail} = \text{Varitem semi Varlist}$

59,60

59.PParmlist = parens1 PParmlistTail

132.PParmlistTail = Varspecs parens2

133.PParmTail = parens2

67,68

67.Stmt = id StmtTail

134.StmtTail = PPEXPRS

135.StmtTail = equal Expr

74,75

74.Lval = id LvalTail

136.LvalTail = eps

137..LvalTail = KKExpr

80,81

80.PPEXPR = parens1 PPEXPRTail

138.PPEXPRTail = Exprlist parens2

139.PPEXPRTail = parens2

88,89

88.Strtn = kwdreturn StrtnTail

140.StrtnTail = Expr

141.StrtnTail = eps

95,97

95.Fact = id FactTail

142.FactTail = eps

143.FactTail = KKExpr

145.FactTail = PPEXPR

Fourth Pass, remove redundant left factored rules

Disappearing Non-Terminals:

Direct:

Vargroup

Varlist  
Moreexprs  
Classmom  
Classitems  
Interfaces  
Mddecls  
Fcndefs  
More\_varspecs  
Stmts  
Elsepart

Indirect:

Rule 44: Classgroup  $\rightarrow$  Varlist  $\rightarrow$  eps

Rule 45: Classgroup  $\rightarrow$  Mddecls  $\rightarrow$  eps

1. Pgm = kwdprog Vargroup Fcndefs Main
2. Main = kwdmain BBlock
3. BBlock = brace1 Vargroup Stmts brace2
4. Vargroup = kwdvars PPvarlist
5. Vargroup = eps
6. PPvarlist = parens1 Varlist parens2
7. Varlist = Varitem semi Varlist
8. Varlist = eps
9. Varitem = Vardecl A
- ~~10. Varitem = Vardecl equal Varinit~~
11. Varitem = kwdclass Varitemtail
- ~~12. Varitem = Classdef~~
13. Vardecl = Simplekind Varspec
14. Simplekind = Basekind
15. Simplekind = Classid
16. Basekind = int
17. Basekind = float
18. Basekind = string
19. Classid = id
20. Varspec = id VarspecTail
- ~~21. Varspec = Arrspec~~
22. Varspec = Deref\_id

23. Varid = id  
 24. Arrspec = Varid KKind  
 25. KKind = bracket1 int bracket2  
 26. Deref\_id = Deref id  
 27. Deref = aster  
  
 28. Varinit = Expr  
 29. Varinit = BBexprs  
 30. BBexprs = brace1 BBexprsTail  
~~31. BBexprs = brace1 brace2~~  
 32. Exprlist = Expr Moreexprs  
 33. Moreexprs = comma Exprlist  
 34. Moreexprs = eps  
  
 35. Classdecl = kwdclass Classid  
 36. Classdef = Classheader BBclassitems  
 37. BBClassitems = brace1 Classitems brace2  
 38. Classheader = Classdecl Classmom Interfaces  
 39. Classmom = colon Classid  
 40. Classmom = eps  
 41. Classitems = ClassitemsTail  
~~42. Classitems = eps~~  
 43. Classgroup = Class\_ctrl  
 44. Classgroup = Varlist  
 45. Classgroup = Mddecls  
 46. Class\_ctrl = colon id // in {public, protected, private}  
 47. Interfaces = colon Classid Interfaces  
 48. Interfaces = eps  
  
 49. Mddecls = Mdheader Mddecls  
 50. Mddecls = eps  
 51. Mdheader = kwdfcn Md\_id PParmlist Retkind  
 52. Md\_id = Classid colon Fcnid  
  
 53. Fcndefs = Fcndef Fcndefs  
 54. Fcndefs = eps  
 55. Fcndef = Fcnheader BBlock  
  
 56. Fcnheader = kwdfcn Fcnid PParmlist Retkind

57. Fcnid = id  
 58. Retkind = Simplekind       //Asked professor during lab and said he needed to correct  
     it from Retkind = Kind  
 59. PParmlist = parens1 PParmlistTail  
 60. ~~PParmlist = PParmlist~~  
 61. Varspecs = Varspec More\_varspecs  
 62. More\_varspecs = comma Varspecs  
 63. More\_varspecs = eps  
 64. PParmlist = parens1 parens2  
  
 65. Stmts = Stmt semi Stmts  
 66. Stmts = eps  
 67. Stmt = id StmtTail  
 68. ~~Stmt = Feall~~  
 69. Stmt = Stif  
 70. Stmt = Stwhile  
 71. Stmt = Stprint  
 72. Stmt = Strtn  
  
 73. Stasgn = Lval equal Expr  
 74. Lval = id LvalTail  
 75. ~~Lval = Aref~~  
 76. Lval = Deref\_id  
 77. Aref = Varid KKExpr  
 78. KKExpr = bracket1 Expr bracket2  
  
 79. Fcall = Fcnid PPEXPRS  
 80. PPEXPRS = parens1 PPEXPRS  
 81. ~~PPEXPRS = PPEXPRS~~  
  
 82. Stif = kwdif PPEXPRS BBlock Elsepart  
 83. Elsepart = kwdelseif PPEXPRS BBlock Elsepart  
 84. Elsepart = kwdelse BBlock  
 85. Elsepart = eps  
  
 86. Stwhile = kwdwhile PPEXPRS BBlock  
 87. Stprint = kprint PPEXPRS  
  
 88. Strtn = kwdreturn StrtnTail



~~89. Strtn = kwdreturn~~

90. PPexpr = parens1 Expr parens2

91. Expr = Rterm

92. Rterm = Term

93. Term = Fact

94. Fact = Basekind

95. Fact = id FactTail

96. Fact = Addrof\_id

~~97. Fact = Feall~~

98. Fact = PPexpr

99. Addrof\_id = ampersand id

100. Oprel = opeq

101. Oprel = opne

102. Oprel = Lthan

103. Oprel = ople

104. Oprel = opge

105. Oprel = Gthan

106. Lthan = angle1

107. Gthan = angle2

108. Opadd = plus

109. Opadd = minus

110. Opmul = aster

111. Opmul = slash

112. Opmul = caret

#### Added Rules

113. Q = eps

114. Q = Oprel Rterm Q

115. Q = Opadd Term Q

116. Q = Opmul Fact Q

117. A = eps

118. A = equal Varinit

119. VaritemTail = ClassDefTail

120. VaritemTail = eps

121. ClassDefTail = Classmom Interfaces BBclassitems

- 122. VarspecTail = eps
- 123. VarspecTail = KKint
  
- 124. BBexprsTail = Exprlist brace2
- 125. BBexprsTail = brace2
  
- 126. ClassitemsTail = eps
- 127. ClassitemsTail = ClassgroupTail Classitems
- 128. ClassgroupTail = Class\_ctrl
- 129. ClassgroupTail = VarlistTail
- 130. ClassgroupTail = Mdheader Mddecls
- 131. VarlistTail = Varitem semi Varlist
  
- 132. PParmlistTail = Varspecs parens2
- 133. PParmTail = parens2
  
- 134. StmtTail = PPexprs
- 135. StmtTail = equal Expr
  
- 136. LvalTail = eps
- 137. LvalTail = KKexpr
  
- 138. PPEexprTail = Exprlist parens2
- 139. PPEexprTail = parens2
  
- 140. StrtnTail = Expr
- 141. StrtnTail = eps
  
- 142. FactTail = eps
- 143. FactTail = KKExpr
- 144. FactTail = PPEexpr