

$$2x = 6 \tag{1}$$

$$(2x - 6) = 0 (2)$$

$$x = ? (3)$$

$$2x = 6 \tag{4}$$

$$(2x - 6) = 0 (5)$$

$$x = ? (6)$$

$$x = 6/2 = 3$$
 (7)

$$2(3) - 6 = 0 \tag{8}$$

$$2a + b + c = 4 \tag{9}$$

$$a + 3b + 2c = 5 (10)$$

$$a = 6 \tag{11}$$

$$\begin{bmatrix} 2 & 1 & 1 \\ 1 & 3 & 2 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$$
 (12)

$$A = \begin{bmatrix} 2 & 1 & 1 \\ 1 & 3 & 2 \\ 1 & 0 & 0 \end{bmatrix}, x = \begin{bmatrix} a \\ b \\ c \end{bmatrix}, b = \begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$$
 (13)



$$\begin{bmatrix} 2 & 1 & 1 \\ 1 & 3 & 2 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$$
 (14)

$$Ax = b \tag{15}$$

$$(Ax - b) = ? (16)$$

$$\begin{bmatrix} 2 & 1 & 1 \\ 1 & 3 & 2 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$$
 (17)

$$Ax = b \tag{18}$$

$$(Ax - b) = 0 ag{19}$$

$$x = \begin{bmatrix} a \\ b \\ c \end{bmatrix} = ? \tag{20}$$



What is Regression

Regression?



What is Regression

$$x + y = z$$

Solving Ax=b

$$\begin{bmatrix} 2 & 1 & 1 \\ 1 & 3 & 2 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$$
 (21)

$$X W = Y \tag{22}$$

$$(X W - Y) = 0 \tag{23}$$

$$W = \begin{bmatrix} a \\ b \\ c \end{bmatrix} = ? \tag{24}$$

$$X^{\dagger} X W = X^{\dagger} Y \tag{25}$$

$$I W = X^{\dagger} Y \tag{26}$$

$$W = X^{\dagger} Y \tag{27}$$



Decimal Value Prediction

ID	digit1	digit2	digit3	value
1	0	0	0	0
2	0	0	1	1
3	0	1	0	2
4	0	1	1	3
5	1	0	0	4
6	1	0	1	5
7	1	1	0	6
8	1	1	1	7

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} w1 & w2 & w3 \end{bmatrix}^{T} = \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{bmatrix}$$
(28)

$$\mathbf{X} \ \mathbf{w}^T = \mathbf{y} \tag{29}$$

$$\mathbf{X}^{\dagger} \ X \ \mathbf{w}^{T} = X^{\dagger} \ \mathbf{y} \tag{30}$$

$$\mathbf{w}^T = X^{\dagger} \mathbf{y} \tag{31}$$

$$\mathbf{w}^{T} = \mathbf{X}^{\dagger} \mathbf{y} = \mathbf{X}^{\dagger} \begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{vmatrix} = \begin{bmatrix} 4 & 2 & 1 \end{bmatrix}^{T} = \begin{bmatrix} w1 & w2 & w3 \end{bmatrix}^{T}$$
 (32)

$$\mathbf{X} \ \mathbf{w}^T = \mathbf{y} \tag{33}$$

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 4 & 2 & 1 \end{bmatrix}^{T} = \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{bmatrix}$$

$$(34)$$

$$\mathbf{X} \ \mathbf{w}^T = \mathbf{y}^{pre} \tag{35}$$

$$cost \ function = \frac{1}{m} \sum_{i}^{m} (\mathbf{y}_{i} - \mathbf{y}_{i}^{pre})^{2}$$
 (36)

training error =
$$sum(abs(y - y^{pre}))$$
 (37)

$$\mathbf{y} - \mathbf{y}^{pre} = \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{bmatrix} - \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{bmatrix} = sum \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} = 0$$
 (38)



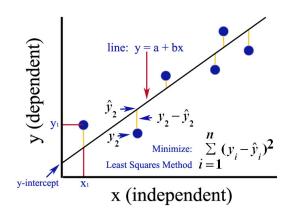
$$\begin{bmatrix} digit1 & digit2 & digit3 \end{bmatrix} \begin{bmatrix} w1 & w2 & w3 \end{bmatrix}^T = \begin{bmatrix} value \end{bmatrix}$$
 (39)

$$digit1 * w1 + digit2 * w2 + digit3 * w3 = value$$
 (40)

$$\begin{bmatrix} digit1 & digit2 & digit1 \end{bmatrix} \begin{bmatrix} 4 & 2 & 1 \end{bmatrix}^T = \begin{bmatrix} value \end{bmatrix}$$
 (41)

$$digit1 * 4 + digit2 * 2 + digit3 * 1 = value$$
 (42)

Linear Regression



source: solutions4statistics.com



Decimal Value Prediction

ID	digit1	digit2	digit3	value	decision
1	0	0	0	0	0
2	0	0	1	1	0
3	0	1	0	2	0
4	0	1	1	3	0
5	1	0	0	4	1
6	1	0	1	5	1
7	1	1	0	6	1
8	1	1	1	7	1

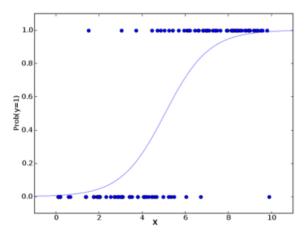


$$\begin{bmatrix} digit1 & digit2 & digit3 \end{bmatrix} \begin{bmatrix} w1 & w2 & w3 \end{bmatrix}^T = \begin{bmatrix} value \end{bmatrix}$$
 (43)

$$digit1 * w1 + digit2 * w2 + digit3 * w3 = value$$
 (44)

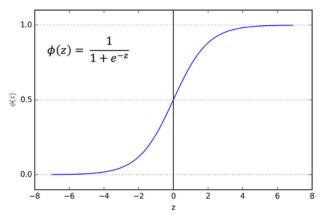
$$Prediction = \begin{cases} 1 & \text{if } 4 \geqslant value \\ 0 & \text{else} \end{cases} \tag{45}$$

Logistic Regression



source: solutions4statistics.com

Logistic - Sigmoid Function



https://sebastianraschka.com/images/faq/logisticregr-neuralnet/sigmoid.png



<u> Logistic - Sigmoid</u>

$$\Phi(z) = \frac{1}{1 + \exp^{-z}} \tag{46}$$

$$\Phi(-6) = \frac{1}{1 + \exp^{-(-6)}} = \frac{1}{1 + 403.42} = 0.0024 \tag{47}$$

$$\Phi(0) = \frac{1}{1 + exp^0} = \frac{1}{1+1} = 0.5 \tag{48}$$

$$\Phi(6) = \frac{1}{1 + \exp^{-(6)}} = \frac{1}{1 + 0.0024} = 0.997 \tag{49}$$

Logistic Regression

$$\Phi(z) = \frac{1}{1 + exp^{-z}} \tag{50}$$

$$\mathbf{y} = \Phi(\mathbf{X} \ \mathbf{w}^T) = \frac{1}{1 + exp^{-(\mathbf{X} \ \mathbf{w}^T)}}$$
 (51)

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} w1 & w2 & w3 \end{bmatrix}^{T} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$
(52)

$$\mathbf{X} \ \mathbf{w}^T = \mathbf{y} \tag{53}$$

$$\mathbf{X}^{\dagger} \mathbf{X} \mathbf{w}^{T} = \mathbf{X}^{\dagger} \mathbf{y}$$
 (54)

$$\mathbf{w}^T = \mathbf{X}^\dagger \ \mathbf{y} \tag{55}$$

$$\mathbf{w}^{T} = \mathbf{X}^{\dagger} \mathbf{y} = \mathbf{X}^{\dagger} \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1.24 & -0.11 & -0.11 \end{bmatrix}^{T} = \begin{bmatrix} w1 & w2 & w3 \end{bmatrix}^{T}$$

$$(56)$$



$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 1.24 & -0.11 & -0.11 \end{bmatrix}^T = sigmoid \begin{pmatrix} \begin{bmatrix} 0.0 \\ -0.11 \\ -0.22 \\ 1.24 \\ 1.12 \\ 1.01 \end{bmatrix} \end{pmatrix}$$

$$\mathbf{X} \ \mathbf{w}^T = sigmoid(\mathbf{y}^{pre})$$

$$sigmoid \begin{pmatrix} \begin{bmatrix} 0.0 \\ -0.11269202 \\ -0.11269202 \\ -0.22538404 \\ 1.24054754 \\ 1.12785552 \\ 1.12785552 \\ 1.0151635 \end{bmatrix} = \begin{bmatrix} 0.5 \\ 0.47185 \\ 0.47185 \\ 0.44389 \\ 0.77565 \\ 0.75544 \\ 0.75544 \\ 0.73402 \end{bmatrix}$$
 (57)

$$X \mathbf{w} = sigmoid(\mathbf{y}^{pre}) \tag{58}$$

$$cost \ function = \frac{1}{m} \sum_{i}^{m} (\mathbf{y}_{i} - sigmoid(\mathbf{y}_{i}^{pre}))^{2}$$
 (59)

training error =
$$sum(abs(\mathbf{y} - sigmoid(\mathbf{y}^{pre}))$$
 (60)

$$abs(\mathbf{y} - sigmoid(\mathbf{y}^{pre})) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & - & 0 \\ 1 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 \end{bmatrix}$$
(61)

training error
$$= 0$$
 (62)

$$\begin{bmatrix}
0.5 \\
0.47185 \\
0.47185 \\
0.44389 \\
0.77565 \\
0.75544 \\
0.75544 \\
0.73402
\end{bmatrix}
=
\begin{bmatrix}
0 \\
0 \\
1 \\
1 \\
0.73402
\end{bmatrix}$$
(63)

$$Prediction = \begin{cases} 1 & \text{if } sigmoid(\mathbf{y}^{pre}) \geqslant 0.5 \\ 0 & \text{else} \end{cases}$$
 (64)

$$\begin{bmatrix} digit1 & digit2 & digit3 \end{bmatrix} \begin{bmatrix} 1.24 & -0.11 & -0.11 \end{bmatrix}^2 = \begin{bmatrix} value \end{bmatrix}$$
 (65)

$$digit1 * w1 + digit2 * w2 + digit3 * w3 = value$$
 (66)

$$sigmoid(\mathbf{y}^{pre}) = \frac{1}{1 + \exp^{-(\operatorname{digit1} * w1 + \operatorname{digit2} * w2 + \operatorname{digit3} * w3)}}$$
 (67)

$$Prediction = \begin{cases} 1 & \text{if } sigmoid(\mathbf{y}^{pre}) \geqslant 0.5 \\ 0 & \text{else} \end{cases}$$
 (68)



Evaluating the model

Accuracy

$$Accuracy = \frac{\# \ correctly \ classified \ instances}{total\# \ instances}$$
 (69)

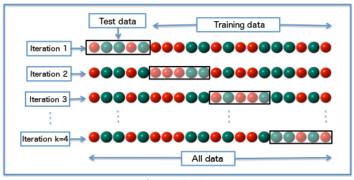


Evaluating the model

Accuracy =
$$6 / 8 * 100 = 75 \%$$

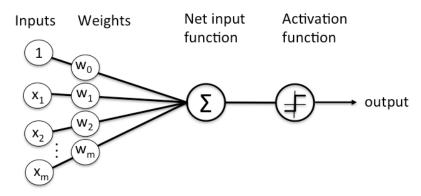
Improving the performance

10 - fold 10-cross validation



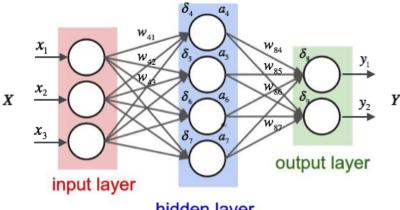
Source: wikipedia

Logistic Regression as a Neuron



www.techmaru.com/technology/artificial-neural-networks/neural-network-elements

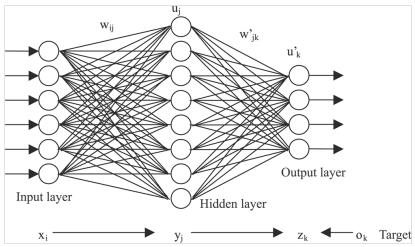
Neuron to Neurons



hidden layer

medium.com/@curiousily/tensorflow-for-hackers-part-iv-neural-network-from-scratch-1a4f504dfa8

Single Layer Network

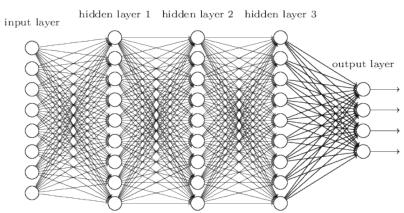


www.extremetech.com/extreme/

215170-artificial-neural-networks-are-changing-the-world-what-are-they

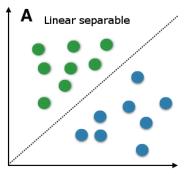


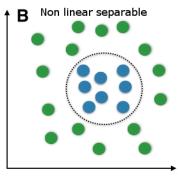
Multi Layer Network



in.mathworks.com/matlabcentral/fileexchange/64247-simple-neural-network

Why Deep Learning?



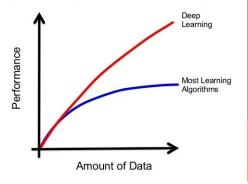


Source: https:

//leonardoaraujosantos.gitbooks.io/artificial-inteligence/content/linear_classification.html

Why Deep Learning?

BIG DATA & DEEP LEARNING



Source: https://qph.ec.quoracdn.net/main-qimg-bf69c291005e68620a1bef39ae8f029e-c

Why now Deep Learning?

