

## Credits

Team #: 1 | Authors: Cooper White & Gian-Mateo Tifone | Date: 11/28/2023

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### Step 1/2 - initialization

---

```
clear;

cie = loadCIEdata;
XYZ_D50 = ref2XYZ(cie.PRD, cie.cmf2deg, cie.illD50);
XYZ_D65 = ref2XYZ(cie.PRD, cie.cmf2deg, cie.illD65);
```

### Step 3

---

```
load_ramps_data;
```

### Step 4 - Forward Matrix

---

```
Red_max.X = max(ramp_R_XYZs(1, :)); %X_r,max
Red_max.Y = max(ramp_R_XYZs(2, :)); %Y_r,max
Red_max.Z = max(ramp_R_XYZs(3, :)); %Z_r,max

Green_max.X = max(ramp_G_XYZs(1, :)); %X_g,max
Green_max.Y = max(ramp_G_XYZs(2, :)); %Y_g,max
Green_max.Z = max(ramp_G_XYZs(3, :)); %Z_g,max

Blue_max.X = max(ramp_B_XYZs(1, :)); %X_g,max
Blue_max.Y = max(ramp_B_XYZs(2, :)); %Y_g,max
Blue_max.Z = max(ramp_B_XYZs(3, :)); %Z_g,max

% Create matrix of max
m_fwd = [Red_max.X, Green_max.X, Blue_max.X ;
         Red_max.Y, Green_max.Y, Blue_max.Y ;
         Red_max.Z, Green_max.Z, Blue_max.Z];

% Subtract the XYZ of display (XYZk)
m_fwd = m_fwd-XYZk;

% Add XYZk (black) collumn
m_fwd = cat(2, m_fwd, XYZk);

% Divide the XYZw value (Y)
m_fwd = m_fwd / XYZw(2, 1);
```

```
% Display Matrix
```

```
m_fwd
```

```
m_fwd =
```

```
    0.3736    0.3652    0.2095    0.0008  
    0.2248    0.6260    0.1452    0.0008  
    0.0518    0.1140    1.0149    0.0014
```

## Step 5 - Derive the LUTs

```
% Step a/b
```

```
RedRamp = ramp_R_XYZs - XYZk; % XYZ of Red minus black
```

```
GreenRamp = ramp_G_XYZs - XYZk; % XYZ of Green minus black
```

```
BlueRamp = ramp_B_XYZs - XYZk; % XYZ of Blue minus black
```

```
% Step c
```

```
RedRamp = RedRamp / XYZw(2, 1); % Divide XYZ by (Y) of white
```

```
GreenRamp = GreenRamp / XYZw(2, 1); % Divide XYZ by (Y) of white
```

```
BlueRamp = BlueRamp / XYZw(2, 1); % Divide XYZ by (Y) of white
```

```
% Clip out of bounds numbers
```

```
RedRamp(RedRamp<0) = 0; % Less than 0 becomes 0
```

```
RedRamp(RedRamp>1) = 1; % Greater than 1 becomes 1
```

```
GreenRamp(GreenRamp<0) = 0;
```

```
GreenRamp(GreenRamp>1) = 1;
```

```
BlueRamp(BlueRamp<0) = 0;
```

```
BlueRamp(BlueRamp>1) = 1;
```

```
% Step d
```

```
% Estimate Radiometric Scalars
```

```
m_fwd_inv = pinv(m_fwd(1:3,1:3)); % Calculate inverse matrix of 3x3 forward matrix
```

```
% The RS means they're converted into RGB, meaning R;G;B [3x11] for 11
```

```
% patches
```

```
RedRampRS = m_fwd_inv * RedRamp; % Multiply XYZ by inverse forward matrix
```

```
GreenRampRS = m_fwd_inv * GreenRamp; %
```

```
BlueRampRS = m_fwd_inv * BlueRamp; %
```

```
% Step e
```

```
% Extract the Red/Green/Blue channels from the RSs of each ramp
```

```
% I.e. Extract Red RS from RedRamp
```

```
% Extract Green RS from GreenRamp
```

```
% Extract Blue RS from BlueRamp
```

```
RedRampRS_R = RedRampRS(1,:); % Red channel of red
```

```
%RedRampRS_G = RedRampRS(2,:);
```

```
%RedRampRS_B = RedRampRS(3,:);
```

```
%GreenRampRS_R = GreenRampRS(1,:);
```

```
GreenRampRS_G = GreenRampRS(2,:); % Green channel of green
```

```
%GreenRampRS_B = GreenRampRS(3,:);
```

```
%BlueRampRS_R = BlueRampRS(1,:);
```

```
%BlueRampRS_G = BlueRampRS(2,:);
```

```
BlueRampRS_B = BlueRampRS(3,:); % Blue channel of blue
```

```
% Step f
```

```
% Interpolate channels from 0-255 using 'pchip'
```

```
ramp_DCs = round(linspace(0,255,11));
```

```
% Create LUT for Red/Green/Blue
```

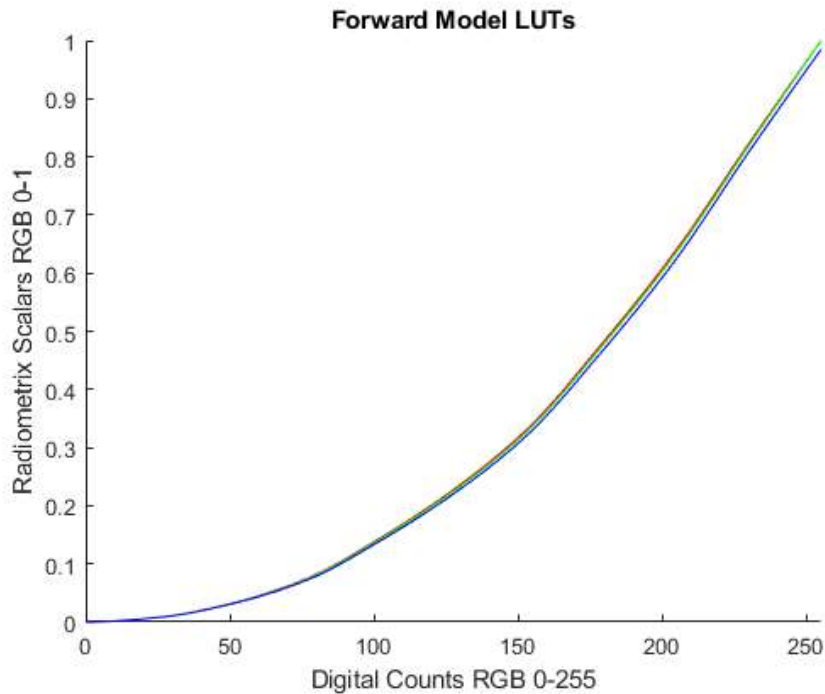
```
RedLUT_fwd = interp1(ramp_DCs, RedRampRS_R, 0:1:255, 'pchip'); % Red LUT forward
```

```
GreenLUT_fwd = interp1(ramp_DCs, GreenRampRS_G, 0:1:255, 'pchip'); % Green LUT forward
```

```
BlueLUT_fwd = interp1(ramp_DCs, BlueRampRS_B, 0:1:255, 'pchip'); % Blue LUT forward
```

```
% Plot LUT
figure
hold on
plot(0:255, RedLUT_fwd, 'Color', [1, 0, 0])
plot(0:255, GreenLUT_fwd, 'Color', [0, 1, 0])
plot(0:255, BlueLUT_fwd, 'Color', [0, 0, 1])

xlabel("Digital Counts RGB 0-255")
ylabel("Radiometric Scalars RGB 0-1")
title("Forward Model LUTs")
ylim([0 1])
xlim([0 255])
```



## Step 6 - Reverse Model

```
m_rev = m_fwd_inv
```

```
m_rev =
```

```
    4.1476   -2.3243   -0.5238
   -1.4787    2.4687   -0.0479
   -0.0455   -0.1586    1.0174
```

## Step 7 - Reverse LUT

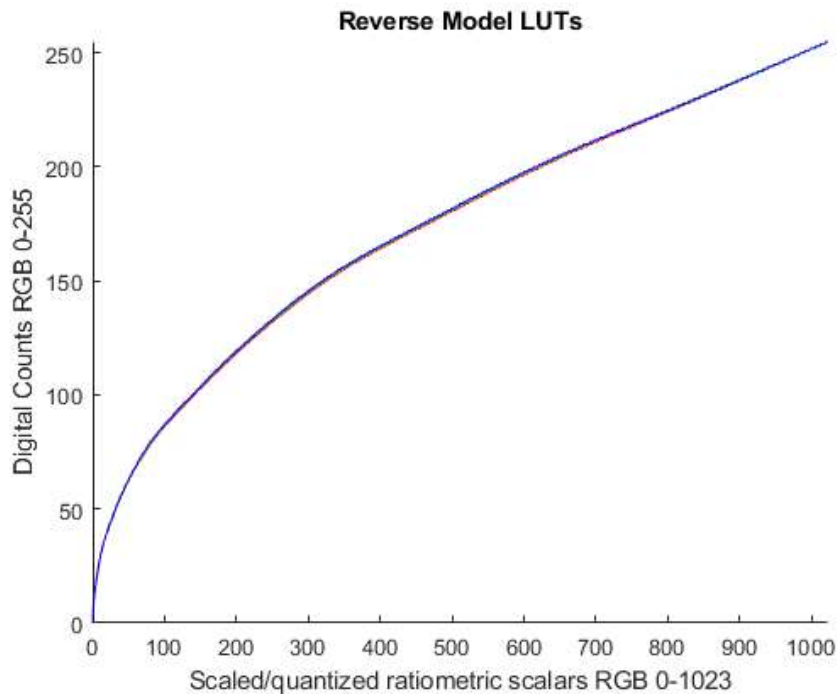
```
RedLUT_rev = uint8(round(interp1(RedLUT_fwd, 0:255, linspace(0, max(RedLUT_fwd), 1024), 'pchip', 0))); % Red LUT reverse
GreenLUT_rev = uint8(round(interp1(GreenLUT_fwd, 0:255, linspace(0, max(GreenLUT_fwd), 1024), 'pchip', 0))); % Green LUT reverse
BlueLUT_rev = uint8(round(interp1(BlueLUT_fwd, 0:255, linspace(0, max(BlueLUT_fwd), 1024), 'pchip', 0))); % Blue LUT reverse

% Plot
figure
hold on
plot(0:1023, RedLUT_rev, 'Color', [1, 0, 0])
plot(0:1023, GreenLUT_rev, 'Color', [0, 1, 0])
plot(0:1023, BlueLUT_rev, 'Color', [0, 0, 1])
```

```

ylabel("Digital Counts RGB 0-255")
xlabel("Scaled/quantized ratiometric scalars RGB 0-1023")
title("Reverse Model LUTs")
ylim([0 255])
xlim([0 1023])

```



## Step 8 - Final Display Model

```

XYZw_display = XYZw; % White of display
XYZk_display = XYZk; % Black of display
M_Display = m_rev; % Reverse matrix of display
RLUT_display = RedLUT_rev; % Red LUT reverse model
GLUT_display = GreenLUT_rev; % Green LUT reverse model
BLUT_display = BlueLUT_rev; % Blue LUT reverse model

% Saves the B&W, and Reverse matrix of the display. Saves the R,G,B LUTs of
% the reverse model
save ('display_model.mat', 'XYZw_display', 'XYZk_display', 'M_Display', ...
      'RLUT_display', 'GLUT_display', 'BLUT_display');

```

## Step 9 - Render RGB image from XYZ

```

% Step a
XYZ_D50;

% Step b - Load in Munki XYZ + Lab
load("loadMunkiData.mat")

% Step c - Adapt XYZ under D50 -> XYZ under Display's whitepoint
catXYZ = catBradford(Munki.XYZ, XYZ_D50, XYZw_display);

% Step d - Subtract the black level
catXYZ = catXYZ - XYZk_display;

% Step e - Multiply XYZ by the Display to produce RS
%           [3x3]   [3x24]
munki_CC_RS = M_Display * catXYZ;

% Step f
munki_CC_RS = munki_CC_RS/100;

```

```

% Step g
munki_CC_RS(munki_CC_RS<0) = 0;
munki_CC_RS(1<munki_CC_RS) = 1;

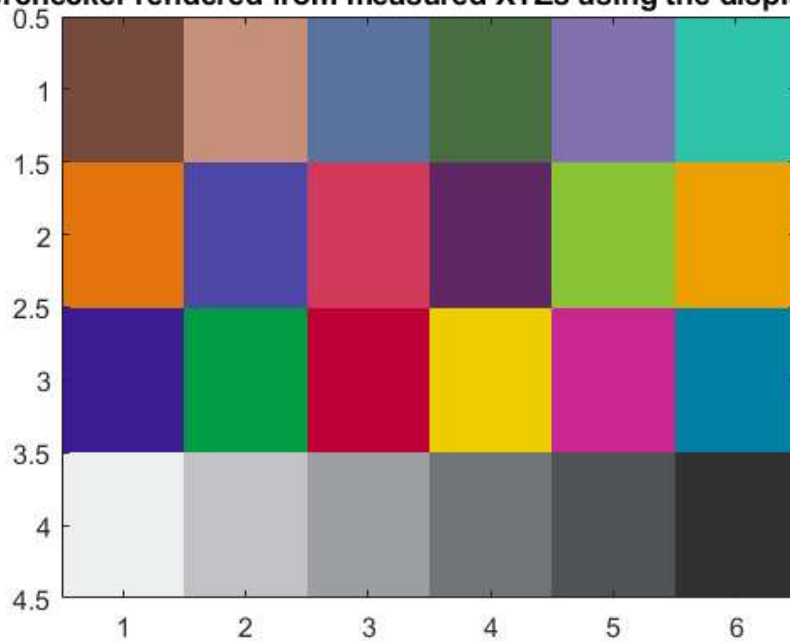
% Step h
munki_CC_RS = round(munki_CC_RS*1023 + 1);

% Step i
munki_CC_DC(1,:) = RedLUT_rev(munki_CC_RS(1,:));
munki_CC_DC(2,:) = GreenLUT_rev(munki_CC_RS(2,:));
munki_CC_DC(3,:) = BlueLUT_rev(munki_CC_RS(3,:));

% Step j - Visualize Chart Patches
pix = uint8(reshape(munki_CC_DC', [6 4 3]));
pix = fliplr(imrotate(pix, -90));
figure
image(pix);
set(gca, 'FontSize', 12);
title("colorchecker rendered from measured XYZs using the display model")

```

**colorchecker rendered from measured XYZs using the display model**



## Step 10 - Evaluate Color Accuracy of Display Model

```

% Step a - Double cast and rescale to [0-100] range
munki_CC_DC = uint8( double(munki_CC_DC) * (100/255) );%Normalize to 1, then x100.

% Step b - Matrix table4ti1
table4ti1 = ones(30, 4);
table4ti1(:, 1) = 1:30;
table4ti1(1:24, 2:4) = munki_CC_DC';
table4ti1(25:27, 2:4) = 0;
table4ti1(28:30, 2:4) = 100;

% Step c - Write .ti1 file
write_ti1_file(table4ti1, 'disp_model_test.ti1');

% Step d - Use da Munki
% disp_model_test.ti3 made

% Step e - Load in XYZ values
disp_XYZs = importdata('disp_model_test.ti3',' ',20);

```

```

% Step f - Extra XYZs and average
CC_XYZ = disp_XYZs.data(1:24, 5:7);           % Extract XYZ Color
display_black = disp_XYZs.data(25:27, 5:7); % Extract XYZ display black
display_white = disp_XYZs.data(28:30, 5:7); % Extract XYZ display white
XYZw = mean(display_white); % XYZ white is average of three measurements
XYZk = mean(display_black); % XYZ black is average of three measurements
CC_XYZ = CC_XYZ';
XYZw = XYZw';

% Step g - Calculate Lab from CC patches
Display_Lab = XYZ2Lab(CC_XYZ, XYZw);

% Step h - Calculate dEab
dEab = deltaEab(Display_Lab, Munki.Lab);

% Step i
print_display_model_error(Munki.Lab, Display_Lab, dEab);

```

Display model color error  
XYZ\_real->display\_model->RGB\_disp->display

patch #	Real			displayed			dEab
	L	a	b	L	a	b	
1	37.1865	14.9985	15.2592	36.8865	14.2261	15.5284	0.8713
2	65.8188	16.8695	18.0267	65.6802	14.8212	18.1930	2.0596
3	49.9949	-3.1841	-23.5159	51.0788	-0.7536	-21.3123	3.4552
4	42.6411	-15.3251	20.0423	42.7415	-17.8604	21.8983	3.1437
5	54.6852	9.6978	-26.7126	55.2683	12.8836	-26.1391	3.2891
6	71.2441	-33.1391	-0.5010	71.3126	-32.6945	1.0255	1.5914
7	62.2558	34.1094	57.7774	61.6009	30.0253	57.6497	4.1383
8	39.5890	9.9980	-43.6388	40.5232	17.0778	-42.7419	7.1972
9	51.8424	48.1403	16.0636	51.4238	46.1820	14.6605	2.4451
10	29.4495	22.4255	-21.7661	30.0405	23.9639	-21.6209	1.6543
11	71.6264	-24.3441	57.6850	71.4577	-30.1075	58.1888	5.7878
12	72.2288	20.6039	69.0149	71.7194	15.9079	67.0791	5.1048
13	28.6402	18.5907	-51.4092	29.8424	25.7203	-48.6971	7.7221
14	54.6309	-39.5493	32.8341	55.0122	-41.1915	34.6212	2.4567
15	42.5988	54.6049	25.7315	42.8231	50.4198	25.3424	4.2092
16	82.4265	3.8689	78.8570	82.3103	-2.5619	76.1660	6.9721
17	51.5476	49.5154	-14.3758	51.2270	50.0912	-14.4897	0.6688
18	49.3892	-26.5473	-28.6645	51.9430	-13.5950	-24.4903	13.8459
19	95.4458	-0.4414	0.0244	96.0094	-0.9179	0.3093	0.7911
20	80.0339	0.1309	-0.9345	80.3975	-0.0666	0.2644	1.2683
21	66.0107	-0.0004	-1.1463	66.4131	0.1474	-0.4507	0.8171
22	50.5546	-0.6207	-0.9616	51.0370	-0.4016	-0.8122	0.5504
23	35.1532	-0.0632	-0.9708	35.8202	0.2682	-0.7166	0.7870
24	20.3224	-0.2858	-0.5603	19.9919	0.0087	0.2874	0.9564
min							0.5504
max							13.8459
mean							3.4076

## Step 11 - Create Display RGB Function

```

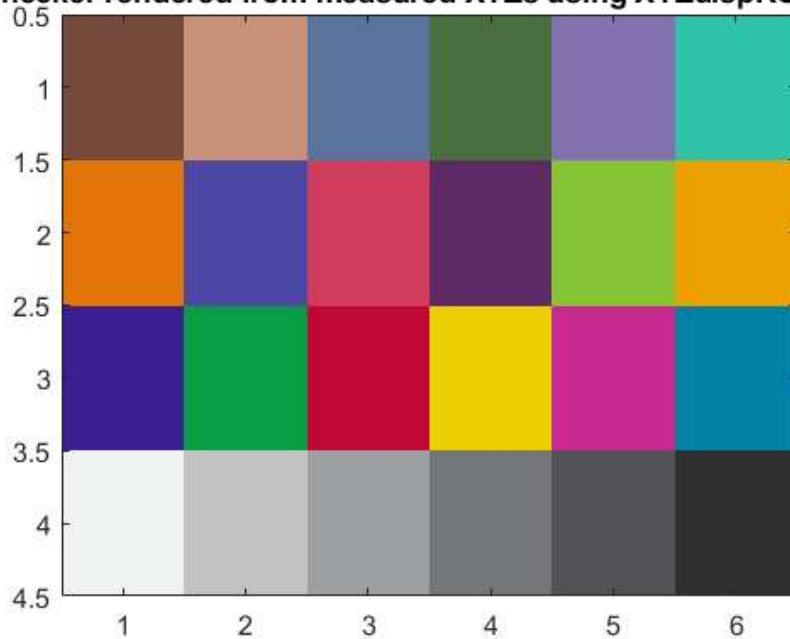
Display_RGB = XYZ2dispRGB("display_model.mat", CC_XYZ, XYZw) ;

% Reusing Ye' Holy Jim Code
pix = reshape(Display_RGB', [6 4 3]);
pix = fliplr(imrotate(pix, -90));
figure;
image(pix);
set(gca, 'FontSize', 12);
title("colorchecker rendered from measured XYZs using XYZdispRGB function");

```

---

## olorchecker rendered from measured XYZs using XYZdispRGB func



### Display XYZ2RGB function

```
function munki_CC_DC = XYZ2dispRGB(display_model, XYZ, XYZn)
% display_model = display_model.mat file
% XYZ [3xn]      = XYZ values of CC patches
% XYZn [3x1]     = Whitepoint / Reference white

load("display_model");

% Step c - Adapt XYZ under D50 -> XYZ under Display's whitepoint
catXYZ = catBradford(XYZ, XYZn, XYZw_display);

% Step d - Subtract the black level
catXYZ = catXYZ - XYZk_display;

% Step e - Multiply XYZ by the Display to produce RS
%           [3x3]      [3x24]
munki_CC_RS = M_Display * catXYZ;

% Step f
munki_CC_RS = munki_CC_RS/100;

% Step g
munki_CC_RS(munki_CC_RS<0) = 0;
munki_CC_RS(1<munki_CC_RS) = 1;

% Step h
munki_CC_RS = round(munki_CC_RS*1023 + 1);

% Step i
munki_CC_DC(1,:) = RLUT_display(munki_CC_RS(1,:));
munki_CC_DC(2,:) = GLUT_display(munki_CC_RS(2,:));
munki_CC_DC(3,:) = BLUT_display(munki_CC_RS(3,:));

% Convert to uint8
uint8(munki_CC_DC);
end
```

### Flex write\_ti1\_file.m

---

```

function filename = write_til_file (table4ti1, filename)

% Open/Create document
fid = fopen(filename, 'w+');

% Create Document
fprintf(fid, '%s\n\n', "CTI1");

fprintf(fid, '%s\n\n', 'COLOR_REP "RGB"');

fprintf(fid, '%s\n', "NUMBER_OF_FIELDS 4");
fprintf(fid, '%s\n', "BEGIN_DATA_FORMAT");
fprintf(fid, '%s\n', "SAMPLE_ID RGB_R RGB_G RGB_B");
fprintf(fid, '%s\n\n', "END_DATA_FORMAT");

fprintf(fid, '%s\n', "NUMBER_OF_SETS 30");
fprintf(fid, '%s\n', "BEGIN_DATA");

for i = 1:size(table4ti1(:, 1))
    fprintf(fid, '%i %i %i %i\n' ,table4ti1(i, 1),table4ti1(i, 2),table4ti1(i, 3),table4ti1(i, 4));
end

fprintf(fid, '%s', "END_DATA");

fclose(fid);
end % End function

```

## Step 12 - Feedback

---

i) Gian-Mateo failed to realize that uint8 did not in-fact mean "round", but all was resolved in the end. ii) Cooper and Gian-Mateo did the functions, code, and revision/cleanup. iii) Using the ones function to build a matrix iv) Explanation of what Step 9.j is doing.