

4271 HW 5

Duncan Wilkie

27 March 2023

Problem 1. Which of the following reactions are allowed and which are forbidden by the conservation laws appropriate for weak interactions?

- $\nu_\mu + p \rightarrow \mu^+ + n$
- $\nu_e + p \rightarrow n + e^- + \pi^+$
- $K^+ \rightarrow \pi^0 + \mu^+ + \nu_\mu$
- $\nu_e + p \rightarrow e^- + \pi^+ + p$
- $\tau^+ \rightarrow \mu^+ + \bar{\nu}_\mu + \nu_\tau$

Solution. If a conserved quantity is not mentioned, that is because it is zero on both sides of the equation in question. The first is allowed, because baryon number and muon lepton number are conserved. The second is allowed, because baryon number and electron lepton number are all conserved. The third is disallowed, because strangeness goes from 1 to zero. The fourth is allowed, because baryon number and electron lepton number all conserved. The fifth is allowed, because tau lepton number and muon lepton number are conserved. \square

Problem 2. In the decay of ^{47}Ca to ^{47}Sc , what kinetic energy is given to the neutrino when the electron has kinetic energy 0.8 MeV.

Solution. Looking at the JAEA nuclear data tables, the difference in atomic masses of these two nucleides is, in energy terms, 1.992 MeV. Accordingly, the kinetic energy of the neutrino is, taking a relativistic approximation so that the mass of both ejectates is negligible,

$$K_\nu = BE - K_e = 1.992 \text{ MeV} - 0.8 \text{ MeV} = 1.19 \text{ MeV}$$

\square

Problem 3. Classify the following decays by degree of forbiddenness:

1. $^{81}\text{Ge}\left(\frac{5}{2}^-\right) \rightarrow ^{81}\text{Ge}\left(\frac{9}{2}^+\right)$
2. $^{93}\text{Kr}\left(\frac{1}{2}^+\right) \rightarrow ^{93}\text{Rb}\left(\frac{5}{2}^+\right)$
3. $^{93}\text{Kr}\left(\frac{1}{2}^+\right) \rightarrow ^{93}\text{Rb}\left(\frac{3}{2}^+\right)$

4. $^{178}\text{Lu}(1^+) \rightarrow ^{178}\text{Hf}(3^+)$

Solution. Looking at the table in the slides,

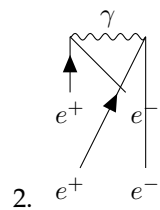
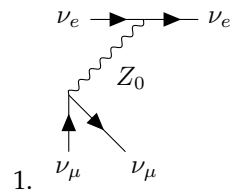
1. $\Delta J = 2$, parity changes \Rightarrow first-forbidden
2. $\Delta J = 2$, parity the same \Rightarrow second-forbidden
3. $\Delta J = 1$, parity the same \Rightarrow allowed
4. $\Delta J = 2$, parity the same \Rightarrow second-forbidden

□

Problem 4. Draw the lowest-order Feynman diagrams for:

1. $\nu_e - \nu_\mu$ elastic scattering,
2. $e^+ + e^- \rightarrow e^+ + e^-$,
3. (Bonus) a fourth-order diagram for $\gamma + \gamma \rightarrow e^- + e^+$

Solution. There's a TikZ library for everything.



□