7210 HW 7

Duncan Wilkie

25 October 2022

Problem 1 (D&F 7.1.30). Let $A = \mathbb{Z} \times \mathbb{Z} \times \cdots$ be the direct product of copies of \mathbb{Z} indexed by the positive integers (so A is a ring under componentwise addition and multiplication) and let R be the ring of all group homomorphisms from A to itself with addition pointwise and multiplication defined as function composition. Let ϕ be the element of R defined by $\phi(a_1, a_1, a_3, \ldots)$

1.

Problem 2 (D&F 7.3.29). Problem 3 (D&F 7.3.33). Problem 4 (D&F 7.4.15).

Problem 5 (D&F 7.4.27).

Problem 6 (D&F 7.4.30).

Problem 7 (D&F 7.4.37).