4141 HW 2

Duncan Wilkie

4 February 2022

1

The probability amplitude is

$$P = \int_{\mathbb{R}} \psi \psi^* = \int_{\mathbb{R}} |\psi^2| = C^2 \int_{-\infty}^{\infty} \frac{1}{(a^2 + x^2)^2} dx$$

Using the substitution $x = a \tan u$, $dx = a \sec^2 u du$ this is

$$= C^{2} \int \frac{a \sec^{2} u}{a^{2} + a^{2} \tan^{2} u} du = C^{2} \int \frac{a \sec^{2} u}{a^{2} (\sec^{2} u)} du$$

$$=\frac{C^2}{a}\int du = \frac{C^2}{a}u = \frac{C^2}{a}\tan^{-1}\left(\frac{x}{a}\right)\Big|_{-\infty}^{\infty} = \frac{\pi C^2}{a}$$