wannier90: User Guide

Version 1.0.3

 $31\mathrm{st}~\mathrm{July}~2007$

Chapter 1

Introduction

1.1 Methodology

wannier90 computes maximally-localised Wannier functions (MLWF) following the method of Marzari and Vanderbilt (MV) [1]. For entangled energy bands, the method of Souza, Marzari and Vanderbilt (SMV) [2] is used. We introduce briefly the methods and key definitions here, but full details can be found in the original papers and in Ref. [4].

First-principles codes typically solve the electronic structure of periodic materials in terms of Bloch states, $\psi_{n\mathbf{k}}$. These extended states are characterised by a band index n and crystal momentum \mathbf{k} . An alternative representation can be given in terms of spatially localised functions known as Wannier functions (WF). The WF centred on a lattice site \mathbf{R} , $w_{n\mathbf{R}}(\mathbf{r})$, is written in terms of the set of Bloch states as

$$w_{n\mathbf{R}}(\mathbf{r}) = \frac{V}{(2\pi)^3} \int_{BZ} \left[\sum_{m} U_{mn}^{(\mathbf{k})} \psi_{m\mathbf{k}}(\mathbf{r}) \right] e^{-i\mathbf{k}\cdot\mathbf{R}} d\mathbf{k} , \qquad (1.1)$$

where V is the unit cell volume, the integral is over the Brillouin zone (BZ), and $\mathbf{U^{(k)}}$ is a unitary matrix that mixes the Bloch states at each \mathbf{k} . $\mathbf{U^{(k)}}$ is not uniquely defined and different choices will lead to WF with varying spatial localisations. We define the spread Ω of the WF as

$$\Omega = \sum_{n} \left[\langle w_{n\mathbf{0}}(\mathbf{r}) | r^2 | w_{n\mathbf{0}}(\mathbf{r}) \rangle - |\langle w_{n\mathbf{0}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2 \right]. \tag{1.2}$$

The total spread can be decomposed into a gauge invariant term $\Omega_{\rm I}$ plus a term $\tilde{\Omega}$ that is dependant on the gauge choice $\mathbf{U}^{(\mathbf{k})}$. $\tilde{\Omega}$ can be further divided into terms diagonal and off-diagonal in the WF basis, $\Omega_{\rm D}$ and $\Omega_{\rm OD}$,

$$\Omega = \Omega_{\rm I} + \tilde{\Omega} = \Omega_{\rm I} + \Omega_{\rm D} + \Omega_{\rm OD} \tag{1.3}$$

where

$$\Omega_{\rm I} = \sum_{n} \left[\langle w_{n\mathbf{0}}(\mathbf{r}) | r^2 | w_{n\mathbf{0}}(\mathbf{r}) \rangle - \sum_{\mathbf{R}m} |\langle w_{n\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2 \right]$$
(1.4)

$$\Omega_{\rm D} = \sum_{n} \sum_{\mathbf{R} \neq \mathbf{0}} |\langle w_{n\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2$$
(1.5)

$$\Omega_{\rm OD} = \sum_{m \neq n} \sum_{\mathbf{R}} |\langle w_{m\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2$$
(1.6)

The MV method minimises the gauge dependent spread $\tilde{\Omega}$ with respect the set of $\mathbf{U^{(k)}}$ to obtain MLWF.

wannier90 requires two ingredients from an initial electronic structure calculation.

1. The overlaps between the cell periodic part of the Bloch states $|u_{n\mathbf{k}}\rangle$

$$M_{mn}^{(\mathbf{k},\mathbf{b})} = \langle u_{m\mathbf{k}} | u_{n\mathbf{k}+\mathbf{b}} \rangle, \tag{1.7}$$

where the vectors **b**, which connect a given k-point with its neighbours, are determined by wannier90 according to the prescription outlined in Ref. [1].

2. As a starting guess the projection of the Bloch states $|\psi_{n\mathbf{k}}\rangle$ onto trial localised orbitals $|g_n\rangle$

$$A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}} | g_n \rangle, \tag{1.8}$$

Note that $\mathbf{M}^{(\mathbf{k},\mathbf{b})}$, $\mathbf{A}^{(\mathbf{k})}$ and $\mathbf{U}^{(\mathbf{k})}$ are all small, $N \times N$ matrices¹ that are independent of the basis set used to obtain the original Bloch states.

To date wannier90 has been used in combination with electronic codes based on plane-waves and pseudopotentials (norm-conserving and ultrasoft [5]) as well as mixed basis set techniques such as FLAPW [6].

1.1.1 Entangled Energy Bands

The above description is sufficient to obtain MLWF for an isolated set of bands, such as the valence states in an insulator. In order to obtain MLWF for entangled energy bands we use the "disentanglement" procedure introduced in Ref. [2].

We define an energy window (the "outer window"). At a given k-point \mathbf{k} , $N_{\text{win}}^{(\mathbf{k})}$ states lie within this energy window. We obtain a set of N Bloch states by performing a unitary transformation amongst the Bloch states which fall within the energy window at each k-point:

$$|u_{n\mathbf{k}}^{\text{opt}}\rangle = \sum_{m \in N_{\text{win}}^{(\mathbf{k})}} U_{mn}^{\text{dis}(\mathbf{k})} |u_{m\mathbf{k}}\rangle$$
 (1.9)

where $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ is a rectangular $N \times N_{\mathrm{win}}^{(\mathbf{k})}$ matrix². The set of $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ are obtained by minimising the gauge invariant spread Ω_{I} within the outer energy window. The MV procedure can then be used to minimise $\tilde{\Omega}$ and hence obtain MLWF for this optimal subspace.

It should be noted that the energy bands of this optimal subspace may not correspond to any of the original energy bands (due to mixing between states). In order to preserve exactly the properties of a system in a given energy range (e.g., around the Fermi level) we introduce a second energy window. States lying within this inner, or "frozen", energy window are included unchanged in the optimal subspace.

¹Technically, this is true for the case of an isolated group of N bands from which we obtain N MLWF. When using the disentanglement procedure of Ref. [2], $\mathbf{A}^{(\mathbf{k})}$, for example, is a rectangular matrix. See Section 1.1.1.
²As $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ is a rectangular matrix this is a unitary operation in the sense that $(\mathbf{U}^{\mathrm{dis}(\mathbf{k})})^{\dagger}\mathbf{U}^{\mathrm{dis}(\mathbf{k})} = \mathbf{1}$.

1.1.2 Getting Help

The latest version of wannier90 and documentation can always be found at

```
http://www.wannier.org
```

There is a wannier90 mailing list for discussing issues in the development, theory, coding and algorithms pertinent to MLWF. You can register for this mailing list by following the links at

http://www.wannier.org/forum.html

1.1.3 Citation

We ask that you acknowledge the use of wannier90 in any publications arising from the use of this code through the following reference

```
[ref] A. A. Mostofi, J. R. Yates, Y.-S. Lee, I. Souza, D. Vanderbilt and N. Marzari http://www.wannier.org/
```

It would also be appropriate to cite the original articles:

Maximally localized generalized Wannier functions for composite energy bands N. Marzari and D. Vanderbilt, Phys. Rev. B 56, 12847 (1997)

Maximally localized Wannier functions for entangled energy bands I. Souza, N. Marzari and D. Vanderbilt, Phys. Rev. B 65, 035109 (2001)

1.1.4 Credits

The present release of wannier90 was written by Arash A. Mostofi (Imperial College London, UK), Jonathan R. Yates (University of Cambridge, UK), and Young-Su Lee (KIST, S. Korea). wannier90 is based on routines written in 1996-7 for occupied bands by Nicola Marzari and David Vanderbilt, and for entangled bands by Ivo Souza, Nicola Marzari, and David Vanderbilt in 2000-1.

Acknowledgements: Stefano de Gironcoli (SISSA, Trieste, Italy) for the PWSCF interface; Michel Posternak (EPFL, Switzerland) for the original plotting routines.

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1.1.5 Licence

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Chapter 2

Parameters

2.1 Usage

```
wannier90.x [-pp] [seedname]
```

- seedname If a seedname string is given the code will read its input from a file seedname.win.

 The default value is wannier.
- -pp This optional flag tells the code to generate a list of the required overlaps and then exit. This information is written to the file seedname.nnkp.

2.2 seedname.win File

The wannier90 input file seedname.win has a flexible free-form structure.

The ordering of the keywords is not significant. Case is ignored (so num_bands is the same as Num_Bands). Characters after !, or # are treated as comments. Most keywords have a default value which is used unless the keyword is given in the win file. Keywords can be set in any of the following ways

```
num_wann 4
num_wann = 4
num_wann : 4
```

A logical keyword can be set to .true. using any of the following strings: T, true, .true..

For futher examples see Chapter 8.1 and the wannier90 Tutorial.

2.3 Keyword List

Keyword	Type	Description
	Syste	em Parameters
NUM_WANN	I	Number of Wannier Functions
NUM_BANDS	I	Number of bands passed to the code
UNIT_CELL_CART	Р	Unit cell vectors
ATOMS_CART *	P	Positions of atoms in Cartesian co-
		ordinates
ATOMS_FRAC *	R	Positions of atoms in lattice vectors
MP_GRID	I	Dimensions of the Monkhorst-Pack
		grid
KPOINTS	R	List of k-points in the Monkhorst-
		Pack grid
GAMMA_ONLY	L	Wavefunctions from underlying ab
		initio calculation are manifestly real
NUM_SHELLS	I	Number of shells in finite difference
		formula
SHELL_LIST	I	Which shells to use in finite differ-
		ence formula

Table 2.1: seedname.win file keywords defining the system. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

^{*} ATOMS_CART $\,$ and ATOMS_FRAC $\,$ may not both be defined in the same input file.

Keyword	Type	Description
	Job	Control
POSTPROC_SETUP	L	To output the nnkp file
EXCLUDE_BANDS	I	List of bands to exclude from the
		calculation
RESTART	С	Restart from checkpoint file
IPRINT	I	Output verbosity level
LENGTH_UNIT	S	System of units to output lengths
WVFN_FORMATTED	L	Read the wavefunctions from a
		(un)formatted file
SPIN	S	Which spin channel to read
DEVEL_FLAG	S	Flag for development use
TIMING_LEVEL	I	Determines amount of timing infor-
		mation written to output
TRANSLATE_HOME_CELL	L	To translate final Wannier centres to
		home unit cell
WRITE_XYZ *	L	To write final centres in xyz file for-
		mat

Table 2.2: seedname.win file keywords defining the system. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string. * write_xyz is only effective if translate_home_cell is true

Keyword	Type	Description
Dis	sentangl	ement Parameters
DIS_WIN_MIN	Р	Bottom of the outer energy window
DIS_WIN_MAX	P	Top of the outer energy window
DIS_FROZ_MIN	P	Bottom of the inner (frozen) energy
		window
DIS_FROZ_MAX	P	Top of the inner (frozen) energy
		window
DIS_NUM_ITER	I	Number of iterations for the minimi-
		sation of Ω_I
DIS_MIX_RATIO	R	Mixing ratio during the minimisa-
		tion of Ω_I
DIS_CONV_TOL	R	The convergence tolerance for find-
		$\log\Omega_I$
DIS_CONV_WINDOW	I	The number of iterations over which
		convergence of Ω_I is assessed.

Table 2.3: seedname.win file keywords controlling the disentanglement. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description
	<u> </u>	D
V		se Parameters
NUM_ITER	I	Number of iterations for the minimi-
		sation of Ω
NUM_CG_STEPS	I	During the minimisation of Ω the
		number of Conjugate Gradient steps
		before resetting to Steepest De-
		scents
CONV_TOL	P	The convergence tolerance for find-
		$\log \Omega$
CONV_WINDOW	I	The number of iterations over which
		convergence of Ω is assessed
NUM_DUMP_CYCLES	I	Control frequency of check-pointing
NUM_PRINT_CYCLES	I	Control frequency of printing
WRITE_R2MN	L	Write matrix elements of r^2 between
		Wannier functions to file
GUIDING_CENTRES	L	Use guiding centres
NUM_GUIDE_CYCLES	I	Frequency of guiding centres
NUM_NO_GUIDE_ITER	I	The number of iterations after
		which guiding centres are used
TRIAL_STEP *	R	The trial step length for the
		parabolic line search during the
		minimisation of Ω
FIXED_STEP *	R	The fixed step length to take dur-
		ing the minimisation of Ω , instead
		of doing a parabolic line search
USE_BLOCH_PHASES **	L	To use phases for initial projections

Table 2.4: seedname.win file keywords controlling the wannierisation. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string. * FIXED_STEP and TRIAL_STEP may not both be defined in the same input file. **Cannot be used in conjunction with disentanglement.

Keyword	Type	Description	
Ple	Plot Parameters		
WANNIER_PLOT	L	Plot the Wannier Functions	
WANNIER_PLOT_LIST	I	List of Wannier Functions to plot	
WANNIER_PLOT_SUPERCELL	I	Size of the supercell for plotting the	
		Wannier Functions	
WANNIER_PLOT_FORMAT	S	File format in which to plot the	
		Wannier Functions	
WANNIER_PLOT_MODE	S	Mode in which to plot the Wannier	
		Functions, molecule or crystal	
BANDS_PLOT	L	Plot and interpolated band struc-	
		ture	
KPOINT_PATH	P	K-point path for the interpolated	
		band structure	
BANDS_NUM_POINTS	I	Number of points along the first sec-	
		tion of the k-point path	
BANDS_PLOT_FORMAT	S	File format in which to plot the in-	
		terpolated bands	
FERMI_SURFACE_PLOT	L	Plot the Fermi surface	
FERMI_SURFACE_NUM_POINTS	I	Number of points in the Fermi sur-	
		face plot	
FERMI_ENERGY	P	The Fermi energy	
FERMI_SURFACE_PLOT_FORMAT	S	File format for the Fermi surface	
		plot	

Table 2.5: seedname.win file keywords controlling the plotting. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

2.4 System

2.4.1 integer :: num_wann

Number of Wannier functions to be found.

No default.

2.4.2 integer :: num_bands

Total number of bands passed to the code in the seedname.mmn file.

Default num_bands=num_wann

2.4.3 Cell Lattice Vectors

The cell lattice vectors should be specified in Cartesian coordinates.

begin unit_cell_cart
[units]

$$R_{1x}$$
 R_{1y} R_{1z}
 R_{2x} R_{2y} R_{2z}
 R_{3x} R_{3y} R_{3z}

end unit_cell_cart

Here R_{1x} is the x-component of the first lattice vector, R_{2y} is the y-component of the second lattice vector etc.

[units] specifies the units in which the lattice vectors are defined: either Bohr or Ang.

The default value is Ang.

2.4.4 Ionic Positions

The ionic positions may be specified in fractional coordinates relative to the lattice vectors of the unit cell, or in absolute cartesian coordinates. Only one of atoms_cart and atoms_frac may be given in the input file.

Cartesian coordinates

begin atoms_cart
[units]

$$\begin{array}{cccc} X & R_{1i} & R_{1j} & R_{1k} \\ Y & R_{2i} & R_{2j} & R_{2k} \\ & \cdot & \end{array}$$

end atoms_cart

The first entry on a line is the atomic symbol. The next three entries are the atom's position in Cartesian coordinates in units specified by length_unit.

[units] specifies the units in which the lattice vectors are defined either bohr or ang. If not present, the default is Å.

Fractional coordinates

begin atoms_frac

$$\begin{array}{ccccc} X & R_{1i} & R_{1j} & R_{1k} \\ Y & R_{2i} & R_{2j} & R_{2k} \\ \vdots & & & \end{array}$$

end atoms_frac

The first entry on a line is the atomic symbol. The next three entries are the atom's position in fractional coordinates.

2.4.5 integer, dimension :: mp_grid(3)

Dimensions of the regular (Monkhorst-Pack) k-point mesh. For example, for a $2 \times 2 \times 2$ grid:

No default.

2.4.6 logical :: gamma_only

If gamma_only=TRUE, then wannier90 uses a branch of algorithms for disentanglement and localisation that exploit the fact that the Bloch eigenstates obtained from the underlying ab initio calculation are manifestly real. This can be the case when only the Γ -point is used to sample the Brillouin zone. The localisation procedure that is used in the Γ -only branch is based on the method of Ref. [3].

2.4.7 K-points

Each line gives the coordinate of a k-point in relative units, i.e. in units of the reciprocal lattice vectors. The position of each k-point in this list assigns its numbering; the first k-point is k-point 1, the second is k-point 2, and so on.

begin kpoints

$$\begin{array}{ccc} R_{1i} & R_{1j} & R_{1k} \\ R_{2i} & R_{2j} & R_{2k} \\ \vdots & & \end{array}$$

end kpoints

There is no default.

2.4.8 Shells

The MV scheme requires a finite difference expression for $\nabla_{\mathbf{k}}$ defined on a uniform Monkhorst-Pack mesh of k-points. The vectors $\{\mathbf{b}\}$ connect each mesh-point \mathbf{k} to its nearest neighbours. $N_{\rm sh}$ shells of neighbours are included in the finite-difference formula, with M_s vectors in the $s^{\rm th}$ shell. For $\nabla_{\mathbf{k}}$ to be correct to linear order, we require that the following equation is satisfied (Eq. B1 of Ref. [1]):

$$\sum_{s}^{N_{\rm sh}} w_s \sum_{i}^{M_s} b_{\alpha}^{i,s} b_{\beta}^{i,s} = \delta_{\alpha\beta} , \qquad (2.1)$$

where $\mathbf{b}^{i,s}$, $i \in [1, M_s]$, is the i^{th} vector belonging to the s^{th} shell with associated weight w_s , and α and β run over the three Cartesian indices.

2.4.9 integer :: num_shells

If num_shells> 0, then the number of shells to include in the finite difference expression. If num_shells= 0, then the code will choose the shells automatically.

The default value is 0.

2.4.10 integer :: shell_list(num_shells)

If num_shells> 0, then shell_list is vector listing the shells to include in the finite difference expression.

2.5 Projection

The projections block defines a set of localised functions used to generate an initial guess for the unitary transformations. This data will be written in the seedname.nnkp file to be used by a first-principles code.

begin projections

end projections

If guiding_centres=TRUE, then the projection centres are used as the guiding centres in the Wannierisation routine.

For details see section 3.1.

2.6 Job Control

2.6.1 logical :: postproc_setup

If postproc_setup=TRUE, then the wannier code will write seedname.nnkp file and exit. If wannier90 is called with the option -pp, then postproc_setup is set to TRUE, over-riding its value in the seedname.win file.

The default value is FALSE.

2.6.2 integer :: iprint

This indicates the level of verbosity of the output from 0, the bare minimum, to 3, which corresponds to full debugging output.

The default value is 1.

2.6.3 character(len=20) :: length_unit

The length unit to be used for output.

The valid options for this parameter are:

```
- Ang (default)
```

- Bohr

2.6.4 character(len=50) :: devel_flag

Not a regular keyword. Its purpose is to allow a developer to pass a string into the code to be used inside a new routine as it is developed.

No default.

2.6.5 integer :: exclude_bands(:)

A k-point independent list of states to excluded from the calculation of the overlap matrices; for example to select only valence states, or ignore semi-core states. This keyword is passed to the first-principles code via the seedname.nnkp file. For example, to exclude bands 2, 6, 7, 8 and 12:

```
exclude_bands : 2, 6-8, 12
```

2.6.6 character(len=20) :: restart

If restart is present the code will attempt to restart the calculation from the seedname.chk file. The value of the parameter determines the position of the restart

The valid options for this parameter are:

- default. Restart from the point at which the check file seedname.chk was written
- wannierise. Restart from the beginning of the wannierise routine
- plot. Go directly to the plotting phase

2.6.7 character(len=20) :: wvfn_formatted

If wvfn_formatted=TRUE, then the wavefunctions will be read from disk as formatted (ie ASCII) files; otherwise they will be read as unformatted files. Unformatted is generally preferable as the files will take less disk space and I/O is significantly faster. However such files will not be transferable between all machine architectures and formatted files should be used if transferability is required (i.e., for test cases).

The default value of this parameter is FALSE.

2.6.8 character(len=20) :: spin

For bands from a spin polarised calculation spin determines which set of bands to read in, either up or down.

The default value of this parameter is up.

2.6.9 integer :: timing_level

Determines the amount of timing information regarding the calculation that will be written to the output file. A value of 1 produces the least information.

The default value is 1.

2.6.10 logical :: translate_home_cell

Determines whether to translate the final Wannier centres to the home unit cell at the end of the calculation. Useful for molecular systems in which the molecule resides entirely within the home unit cell.

The default value is false.

2.6.11 logical :: write_xyz

Determines whether to write the final Wannier centres to an xyz formatted file, seedname_centres.xyz, for subsequent visualisation. Only effective when TRANSLATE_HOME_CELL is true.

The default value is false.

2.7 Disentanglement

These keywords control the disentanglement routine of Ref. [2]. This routine will be activated if num_wann<num_bands.

2.7.1 real(kind=dp) :: dis_win_min

The lower bound of the outer energy window for the disentanglement procedure.

The default is the lowest eigenvalue in the system.

2.7.2 real(kind=dp) :: dis_win_max

The upper bound of the outer energy window for the disentanglement procedure.

The default is the highest eigenvalue in the given states (ie all states are included in the disentanglement procedure).

2.7.3 real(kind=dp) :: dis_froz_min

The lower bound of the inner energy window for the disentanglement procedure.

If dis_froz_max is given, then the default for dis_froz_min is dis_win_min.

2.7.4 real(kind=dp) :: dis_froz_max

The upper bound of the inner energy window for the disentanglement procedure. If dis_froz_max is not specified, then there are no frozen states.

No default.

2.7.5 integer :: dis_num_iter

In the disentanglement procedure, the number of iterations used to extract the most connected subspace.

The default value is 200.

2.7.6 real(kind=dp) :: dis_mix_ratio

In the disentanglement procedure, the mixing parameter to use for convergence (see pages 4-5 of Ref. [2]). A value of 0.5 is a 'safe' choice. Using 1.0 (ie no mixing) often gives faster convergence, but may cause the minimisation to be unstable in some cases.

Restriction: $0.0 < \texttt{dis_mix_ratio} \ge 1.0$. The default value is 0.5

2.7.7 real(kind=dp) :: dis_conv_tol

In the disentanglement procedure, the minimisation is said to to converged if the fractional change in the spread between successive iterations is less than dis_conv_tol for dis_conv_window iterations.

The default value is 1.0E-10

2.7.8 integer :: dis_conv_window

In the disentanglement procedure, the minimisation is said to to converged if the fractional change in the spread between successive iterations is less than dis_conv_tol for dis_conv_window iterations.

The default value of this parameter is 3.

2.8 Wannierise

Minimise the non-invariant part of the spread functional.

2.8.1 integer :: num_iter

Total number of iterations in the minimisation procedure.

The default value is 100.

2.8.2 integer :: num_cg_steps

Number of conjugate gradient steps to take before resetting to steepest descents.

The default value is 5.

2.8.3 integer :: num_dump_cycles

Write sufficient information to do a restart every num_dump_cycles iterations.

The default is 100

2.8.4 integer :: num_print_cycles

Write data to the seedname.wout file every num_print_cycles iterations.

The default is 1.

2.8.5 logical :: write_r2mn

If write_r2mn = true, then the matrix elements $\langle m|r^2|n\rangle$ (where m and n refer to Wannier functions) are written to file seedname.r2mn at the end of the Wannierisation procedure.

The default value of this parameter is FALSE.

2.8.6 logical :: guiding_centres

Use guiding centres during the minimisation, in order to avoid local minima.

The default value is FALSE.

2.8.7 integer :: num_guide_cycles

If guiding_centres is set to true, then the guiding centres are used only every num_guide_cycles.

The default value is 1.

2.8.8 integer :: num_no_guide_iter

If guiding_centres is set to true, then the guiding centres are used only after num_no_guide_iter minimisation iterations have been completed.

The default value is 0.

2.8.9 real(kind=dp) :: trial_step

The value of the trial step for the parabolic fit in the line search minimisation used in the minimisation of the spread function. Cannot be used in conjunction with fixed_step (see below). If the minimisation procedure doesn't converge, try decreasing the value of trial_step to give a more accurate line search.

The default value is 2.0

2.8.10 real(kind=dp) :: fixed_step

If this is given a value in the input file, then a fixed step of length fixed_step (instead of a parabolic line search) is used at each iteration of the spread function minimisation. Cannot

be used in conjunction with trial_step. This can be useful in cases in which minimisation with a line search fails to converge.

There is no default value.

2.8.11 logical :: use_bloch_phases

Determines whether to use the Bloch functions as the initial guess for the projections. Can only be used if disentanglement = false.

Th default value is false.

2.9 Post-Processing

Capabilities:

- Plot the Wannier functions
- Plot the interpolated band structure
- Plot the Fermi surface

2.9.1 logical :: wannier_plot

If wannier_plot = TRUE, then the code will write out the wannier functions in a super-cell wannier_plot_supercell times the original unit cell in a format specified by wannier_plot_format

The default value of this parameter is FALSE.

2.9.2 integer :: wannier_plot_supercell

Dimension of the 'super-unit-cell' in which the Wannier functions are plotted. The super-unit-cell is wannier_plot_supercell times the unit cell along all three linear dimensions (the 'home' unit cell is kept approximately in the middle)

The default value is 2.

2.9.3 character(len=20) :: wannier_plot_format

The valid options for this parameter are:

- xcrysden (default)

2.9.4 integer :: wannier_plot_list(:)

A list of Wannier functions to plot. The Wannier functions numbered as per the **seedname.wout** file after the minimisation of the spread.

The default behaviour is to plot all Wannier functions. For example, to plot Wannier functions 4, 5, 6 and 10:

```
wannier_plot_list: 4-6, 10
```

2.9.5 character(len=20) :: wannier_plot_mode

Choose the mode in which to plot the Wannier functions, either as a molecule or as a crystal.

The valid options for this parameter are:

```
- crystal (default)
```

- molecule

2.9.6 logical :: bands_plot

If bands_plot = TRUE, then the code will calculate the band structure, through Wannier interpolation, along the path in k-space defined by bands_kpath using bands_num_points along the first section of the path and write out an output file in a format specified by bands_plot_format.

The default value is FALSE.

2.9.7 kpoint_path

Defines the path in kspace along which to calculate the bandstructure. Each line gives the start and end point (with labels) for a section of the path.

begin kpoint_path

end kpoint_path

There is no default

2.9.8 integer :: bands_num_points

If bands_plot = TRUE, then the number of points along the first section of the bandstructure plot given by kpoint_path. Other sections will have the same density of k-points.

The default value for bands_num_points is 100.

2.9.9 character(len=20) :: bands_plot_format

Format in which to plot the interpolated band structure The valid options for this parameter are:

- gnuplot (default)
- xmgrace

2.9.10 logical :: fermi_surface_plot

If fermi_surface_plot = TRUE, then the code will calculate, through Wannier interpolation, the eigenvalues on a regular grid with fermi_surface_num_points in each direction. The code will write a file in bxsf format which can be read by XCrySDen in order to plot the Fermi surface.

The default value is FALSE.

2.9.11 integer :: fermi_surface_num_points

If fermi_surface_plot = TRUE, then the number of divisions in the regular k-point grid used to calculate the Fermi surface.

The default value for fermi_surface_num_points is 50.

2.9.12 real(kind=dp) :: fermi_energy

The Fermi energy in eV. Whilst this is not directly used by the wannier90, it is a useful parameter to set as it will be written driectly into the bxsf file.

The default value is $0.0 \,\mathrm{eV}$.

2.9.13 character(len=20) :: fermi_surface_plot_format

Format in which to plot the Fermi surface. The valid options for this parameter are:

```
- xcrysden (default)
```

Chapter 3

Projections

3.1 Specification of projections in seedname.win

Here we describe the projection functions used to construct the initial guess $A_{mn}^{(\mathbf{k})}$ for the unitary transformations.

Each projection is associated with a site and an angular momentum state defining the projection function. Optionally, one may define, for each projection, the spatial orientation, the radial part, the diffusivity, and the volume over which real-space overlaps A_{mn} are calculated.

The code is able to

- 1. project onto s,p,d and f angular momentum states, plus the hybrids sp, sp 2 , sp 3 , sp 3 d, sp 3 d 2 .
- 2. control the radial part of the projection functions to allow higher angular momentum states, e.g., both 3s and 4s in silicon.

The atomic orbitals of the hydrogen atom provide a good basis to use for constructing the projection functions: analytical mathematical forms exist in terms of the good quantum numbers n, l and m; hybrid orbitals (sp, sp², sp³, sp³d etc.) can be constructed by simple linear combination $|\phi\rangle = \sum_{nlm} C_{nlm} |nlm\rangle$ for some coefficients C_{nlm} .

The angular functions that use as a basis for the projections are not the canonical spherical harmonics Y_{lm} of the hydrogenic Schrödinger equation but rather the real (in the sense of non-imaginary) states Θ_{lm_r} , obtained by a unitary transformation. For example, the canonical eigenstates associated with l=1, $m=\{-1,0,1\}$ are not the real p_x , p_y and p_z that we want. See Section 3.3 for our mathematical conventions regarding projection orbitals for different n, l and m_r .

We use the following format to specify projections in <seedname>.win:

Begin Projections

units

site:ang_mtm:zaxis:xaxis:radial:zona:box-size

:

End Projections

Notes:

24

units:

Optional. Either Ang or Bohr to specify whether the projection centres specified in this block (if given in Cartesian co-ordinates) are in units of Angstrom or Bohr, respectively. The default value is Ang.

site:

C, Al, etc. applies to all atoms of that type

f=0,0.50,0 - centre on (0.0,0.5,0.0) in fractional coordinates (crystallographic units) relative to the direct lattice vectors

c=0.0,0.805,0.0 – centre on (0.0,0.805,0.0) in Cartesian coordinates in units specified by the optional string units in the first line of the projections block (see above).

ang_mtm:

Angular momentum states may be specified by 1 and mr, or by the appropriate character string. See Tables 3.1 and 3.2. Examples:

```
1=2,mr=1 or dz2 - a single projection with l=2, m_{\Gamma}=1 (i.e., d_{z^2})
```

1=2,mr=1,4 or dz2,dx2-y2 - two functions: d_{z^2} and d_{xz}

1=-3 or $sp3 - four sp^3$ hybrids

Specific hybrid orbitals may be specified as follows:

1=-3, mr=1,3 or sp3-1, sp3-3 - two specific sp³ hybrids

Multiple states may be specified by separating with ';', e.g.,

sp3;1=0 or 1=-3;1=0 - four sp^3 hybrids and one s orbital

zaxis (optional):

z=1,1,1- set the z-axis to be in the (1,1,1) direction. Default is z=0,0,1

xaxis (optional):

x=1,1,1- set the x-axis to be in the (1,1,1) direction. Default is x=1,0,0

radial (optional):

r=2 – use a radial function with one node (ie second highest pseudostate with that angular momentum). Default is r=1. Radial functions associated with different values of r should be orthogonal to each other.

```
zona (optional):
```

zona=2.0 – the value of $\frac{Z}{a}$ for the radial part of the atomic orbital (controls the diffusivity of the radial function). Units always in reciprocal Angstrom. Default is zona=1.0.

box-size (optional):

b=2.0 – the linear dimension of the real-space box (or sphere) for calculating the overlap $\langle \psi_{m\mathbf{k}} | \phi_n \rangle$ of a wavefunction with the localised projection function. Units are always in Angstrom. Default is b=1.0. This feature is not currently used.

Examples

1. CuO, s,p and d on all Cu; sp³ hybrids on O:

Cu:1=0;1=1;1=2

0:1=-3 or 0:sp3

2. A single projection onto a p_z orbital orientated in the (1,1,1) direction:

3. Project onto s, p and d (with no radial nodes), and s and p (with one radial node) in silicon:

Si:1=0;1=1;1=2

Si:1=0;1=1:r=2

3.2 Short-Cuts

3.2.1 Random projections

It is possible to specify the projections as follows:

Begin Projections

random

End Projections

in which case the code chooses the appropriate number of randomly-centred s-type gaussian functions for the initial projection.

3.2.2 Bloch phases

Setting use_bloch_phases = true in the input file absolves the user of the need to specify explicit projections. In this case, the Bloch wave-functions are used as the projection orbitals, namely $A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}} | \psi_{n\mathbf{k}} \rangle = \delta_{mn}$.

3.3 Orbital Definitions

The angular functions $\Theta_{lm_r}(\theta,\varphi)$ associated with particular values of l and m_r are given in Tables 3.1 and 3.2.

The radial functions $R_r(r)$ associated with different values of r should be orthogonal. One choice would be to take the set of solutions to the radial part of the hydrogenic Schrödinger equation for l = 0, i.e., the radial parts of the 1s, 2s, 3s... orbitals, which are given in Table 3.3.

l	$m_{ m r}$	Name	$\Theta_{lm_{ m r}}(heta,arphi)$
0	1	s	$\frac{1}{\sqrt{4\pi}}$
1	1	pz	$\sqrt{rac{3}{4\pi}}\cos heta$
1	2	px	$\sqrt{\frac{3}{4\pi}}\sin\theta\cos\varphi$
1	3	ру	$\sqrt{rac{3}{4\pi}}\sin heta\sinarphi$
2	1	dz2	$\sqrt{\frac{5}{16\pi}}(3\cos^2\theta - 1)$
2	2	dxz	$\sqrt{\frac{15}{4\pi}}\sin\theta\cos\theta\cos\varphi$
2	3	dyz	$\sqrt{\frac{15}{4\pi}}\sin\theta\cos\theta\sin\varphi$
2	4	dx2-y2	$\sqrt{\frac{15}{16\pi}}\sin^2\theta\cos2\varphi$
2	5	dxy	$\sqrt{\frac{15}{16\pi}}\sin^2\theta\sin2\varphi$
3	1	fz3	$\frac{\sqrt{7}}{4\sqrt{\pi}}(5\cos^3\theta - 3\cos\theta)$
3	2	fxz2	$\frac{\sqrt{21}}{4\sqrt{2\pi}}(5\cos^2\theta - 1)\sin\theta\cos\varphi$
3	3	fyz2	$\frac{\sqrt{21}}{4\sqrt{2\pi}} (5\cos^2\theta - 1)\sin\theta\sin\varphi$
3	4	fz(x2-y2)	$\frac{\sqrt{105}}{4\sqrt{\pi}}\sin^2\theta\cos\theta\cos2\varphi$
3	5	fxyz	$\frac{\sqrt{105}}{4\sqrt{\pi}}\sin^2\theta\cos\theta\sin2\varphi$
3	6	fx(x2-3y2)	$\frac{\sqrt{35}}{4\sqrt{2\pi}}\sin^3\theta(\cos^2\varphi - 3\sin^2\varphi)\cos\varphi$
3	7	fy(3x2-y2)	$\frac{\sqrt{35}}{4\sqrt{2\pi}}\sin^3\theta(3\cos^2\varphi-\sin^2\varphi)\sin\varphi$

Table 3.1: Angular functions $\Theta_{lm_r}(\theta,\varphi)$ associated with particular values of l and m_r for $l \geq 0$.

l	$m_{ m r}$	Name	$\Theta_{lm_{ m r}}(heta,arphi)$
-1	1	sp-1	$\frac{1}{\sqrt{2}}$ s $+\frac{1}{\sqrt{2}}$ px
-1	2	sp-2	$\frac{1}{\sqrt{2}}$ s $-\frac{1}{\sqrt{2}}$ px
-2	1	sp2-1	$\frac{1}{\sqrt{3}}s - \frac{1}{\sqrt{6}}px + \frac{1}{\sqrt{2}}py$
-2	2	sp2-2	$\frac{1}{\sqrt{3}}$ s $-\frac{1}{\sqrt{6}}$ px $-\frac{1}{\sqrt{2}}$ py
-2	3	sp2-3	$\frac{1}{\sqrt{3}}$ s $+\frac{2}{\sqrt{6}}$ px
-3	1	sp3-1	$\tfrac{1}{2}(\mathtt{s}+\mathtt{p}\mathtt{x}+\mathtt{p}\mathtt{y}+\mathtt{p}\mathtt{z})$
-3	2	sp3-2	$\frac{1}{2}(\mathtt{s}+\mathtt{px}-\mathtt{py}-\mathtt{pz})$
-3	3	sp3-3	$\frac{1}{2}(\mathtt{s}-\mathtt{px}+\mathtt{py}-\mathtt{pz})$
-3	4	sp3-4	$\frac{1}{2}(\mathtt{s}-\mathtt{px}-\mathtt{py}+\mathtt{pz})$
-4	1	sp3d-1	$\frac{1}{\sqrt{3}}s - \frac{1}{\sqrt{6}}px + \frac{1}{\sqrt{2}}py$
-4	2	sp3d-2	$\frac{1}{\sqrt{3}}$ s $-\frac{1}{\sqrt{6}}$ px $-\frac{1}{\sqrt{2}}$ py
-4	3	sp3d-3	$\frac{1}{\sqrt{3}}$ s $+\frac{2}{\sqrt{6}}$ px
-4	4	sp3d-4	$\frac{1}{\sqrt{2}}$ pz $+\frac{1}{\sqrt{2}}$ dz2
-4	5	sp3d-5	$-rac{1}{\sqrt{2}}$ pz $+rac{1}{\sqrt{2}}$ dz2
-5	1	sp3d2-1	$\frac{1}{\sqrt{6}}s - \frac{1}{\sqrt{2}}px - \frac{1}{\sqrt{12}}dz^2 + \frac{1}{2}dx^2y^2$
-5	2	sp3d2-2	$\frac{1}{\sqrt{6}}s + \frac{1}{\sqrt{2}}px - \frac{1}{\sqrt{12}}dz2 + \frac{1}{2}dx2$ -y2
-5	3	sp3d2-3	$\frac{1}{\sqrt{6}}$ s $-\frac{1}{\sqrt{2}}$ py $-\frac{1}{\sqrt{12}}$ dz2 $-\frac{1}{2}$ dx2-y2
-5	4	sp3d2-4	$\frac{1}{\sqrt{6}}s + \frac{1}{\sqrt{2}}py - \frac{1}{\sqrt{12}}dz2 - \frac{1}{2}dx2$ -y2
-5	5	sp3d2-5	$rac{1}{\sqrt{6}}$ s $-rac{1}{\sqrt{2}}$ pz $+rac{1}{\sqrt{3}}$ dz2
-5	6	sp3d2-6	$\frac{1}{\sqrt{6}}s + \frac{1}{\sqrt{2}}pz + \frac{1}{\sqrt{3}}dz2$

Table 3.2: Angular functions $\Theta_{lm_r}(\theta,\varphi)$ associated with particular values of l and m_r for l < 0, in terms of the orbitals defined in Table 3.1.

r	$R_{ m r}(r)$
1	$2\alpha^{3/2}\exp(-\alpha r)$
2	$\frac{1}{2\sqrt{2}}\alpha^{3/2}(2-\alpha r)\exp(-\alpha r/2)$
3	$\sqrt{\frac{4}{27}}\alpha^{3/2}(1 - 2\alpha r/3 + 2\alpha^2 r^2/27)\exp(-\alpha r/3)$

Table 3.3: One possible choice for the radial functions $R_r(r)$ associated with different values of r: the set of solutions to the radial part of the hydrogenic Schrödinger equation for l=0, i.e., the radial parts of the 1s, 2s, 3s... orbitals, where $\alpha=Z/a=$ zona.

Chapter 4

Code Overview

wannier90 can operate in two modes:

- 1. Post-processing mode: read in the overlaps and projections from file as computed inside a first-principles code. We expect this to be the most common route to using wannier90, and is described in Ch. 5;
- 2. Library mode: as a set of library routines to be called from within a first-principles code that passes the overlaps and projections to the wannier90 library routines and in return gets the unitary transformation corresponding to MLWF. This route should be used if the MLWF are needed within the first-principles code, for example in post-LDA methods such as LDA+U or SIC, and is described in Ch. 6.

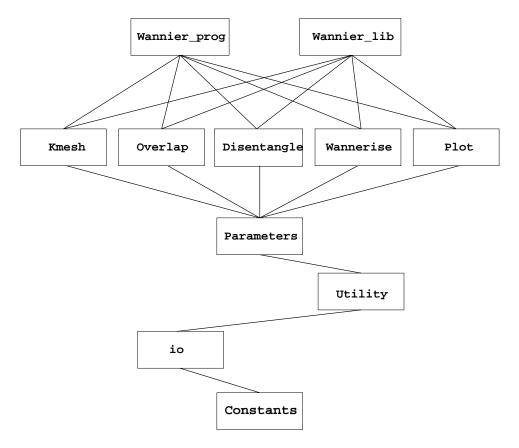


Figure 4.1: Schematic overview of the module structure of wannier90. Modules may only use data and subroutines from lower modules.

Chapter 5

wannier90 as a post-processing tool

This is a description of how to use wannier90 as a post-processing tool.

The code must be run twice. On the first pass either the logical keyword postproc_setup must be set to .true. in the input file seedname.win or the code must be run with the command line option -pp. Running the code then generates the file seedname.nnkp which provides the information required to construct the $M_{mn}^{(\mathbf{k},\mathbf{b})}$ overlaps (Ref. [1], Eq. (25)) and $A_{mn}^{(\mathbf{k})}$ (Ref. [1], Eq. (62); Ref. [2], Eq. (22)).

Once the overlaps and projection have been computed and written to files seedname.mmn and seedname.amn, respectively, set postproc_setup to .false. and run the code. Output is written to the file seedname.wout.

5.1 nnkp file

OUTPUT, if postproc_setup = .true.

The file seedname.nnkp provides the information needed to determine the required overlap elements $M_{mn}^{(\mathbf{k},\mathbf{b})}$ and projections $A_{mn}^{(\mathbf{k})}$. It is written automatically when the code is invoked with the -pp command-line option (or when postproc_setup=.true. in seedname.win. There should be no need for the user to edit this file.

Much of the information in seedname.nnkp is arranged in blocks delimited by the strings begin block_name...end block_name, as described below.

5.1.1 Keywords

The first line of the file is a user comment, e.g., the date and time:

File written on 12Feb2006 at 15:13:12

The only logical keyword is calc_only_A, eg,

calc_only_A : F

5.1.2 Real_lattice block

```
begin real_lattice
2.250000 0.000000 0.000000
0.000000 2.250000 0.000000
0.000000 0.000000 2.250000
end real_lattice
```

The real lattice vectors in units of Angstrom.

5.1.3 Recip_lattice block

```
begin recip_lattice
2.792527 0.000000 0.000000
0.000000 2.792527 0.000000
0.000000 0.000000 2.792527
end recip_lattice
```

The reciprocal lattice vectors in units of inverse Angstrom.

5.1.4 Kpoints block

```
begin kpoints
8
0.00000 0.00000 0.00000
0.00000 0.50000 0.00000
.
.
.
0.50000 0.50000 0.50000
end kpoints
```

The first line in the block is the total number of k-points num_kpts. The subsequent num_kpts lines specify the k-points in crystallographic co-ordinates relative to the reciprocal lattice vectors.

5.1.5 Projections block

```
begin projections
  n_proj
  centre l mr r
   z-axis x-axis zona box-size
  centre l mr r
```

```
z-axis x-axis zona box-size
.
.
end projections
```

Notes:

n_proj: integer; the number of projection centres, equal to the number of MLWF num_wann.

centre: three real numbers; projection function centre in crystallographic co-ordinates relative to the direct lattice vectors.

1 mr r: three integers; l and m_r specify the angular part $\Theta_{lm_r}(\theta,\varphi)$, and r specifies the radial part $R_r(r)$ of the projection function (see Tables 3.1, 3.2 and 3.3).

z-axis: three real numbers; default is 0.0 0.0 1.0; defines the axis from which the polar angle θ in spherical polar coordinates is measured.

x-axis: three real numbers; must be orthogonal to z-axis; default is 1.0 0.0 0.0 or a vector perpendicular to z-axis if z-axis is given; defines the axis from with the azimuthal angle φ in spherical polar coordinates is measured.

zona: real number; the value of $\frac{Z}{a}$ associated with the radial part of the atomic orbital. Units are in reciprocal Angstrom.

box-size: real number; the linear dimension of the real-space box (or sphere) for calculating the overlap $\langle \psi_{m\mathbf{k}} | \phi_n \rangle$ of a wavefunction with the localised projection function. Units are in Angstrom. This feature is not currently used.

5.1.6 nnkpts block

```
begin nnkpts
    10
    1    2    0    0    0
    .
    .
end nnkpts
```

First line: nntot, the number of nearest neighbours belonging to each k-point of the Monkhorst-Pack mesh

Subsequent lines: nntot×num_kpts lines, ie, nntot lines of data for each k-point of the mesh.

Each line of consists of 5 integers. The first is the k-point number nkp. The second to the fifth specify it's nearest neighbours k+b: the second integer points to the k-point that is the periodic image of the k+b that we want; the last three integers give the G-vector, in reciprocal lattice units, that brings the k-point specified by the second integer (which is in the first BZ) to the actual k+b that we need.

5.1.7 exclude_bands block

```
begin exclude_bands
```

8

1 2

•

end exclude_bands

To exclude bands (independent of k-point) from the calculation of the overlap and projection matricies, for example to ignore shallow-core states. The first line is the number of states to exclude, the following lines give the states for be excluded.

5.1.8 An example of projections

As a concrete example: one wishes to have a set of four sp^3 projection orbitals on, say , a carbon atom at (0.5,0.5,0.5) in fractional co-ordinates relative to the direct lattice vectors. In this case $\mathrm{seedname.win}$ will contain the following lines:

```
begin projections
C:1=-1
end projections
```

and seedname.nnkp, generated on the first pass of wannier90 (with postproc_setup=T), will contain:

```
begin projections
```

```
4
  0.50000
              0.50000
                         0.50000
     0.000
                            1.000
                                   0.000
                                         0.000
                                                  2.00
                                                        2.00
            0.000 1.000
  0.50000
              0.50000
                         0.50000
                                     -1
                                         2
                                            1
     0.000
            0.000 1.000
                            1.000
                                   0.000 0.000
                                                        2.00
                                                  2.00
  0.50000
              0.50000
                         0.50000
                                     -1
                                         3
                                            1
     0.000
           0.000
                  1.000
                           1.000
                                   0.000
                                          0.000
                                                  2.00
                                                        2.00
  0.50000
              0.50000
                         0.50000
                                     -1
                                         4
                                         0.000
     0.000 0.000
                   1.000
                           1.000
                                  0.000
                                                  2.00
                                                        2.00
end projections
```

where the first line tells us that in total four projections are specified, and the subsquent lines provide the projection centre, the angular and radial parts of the orbital (see Section 3.3 for definitions), the z and x axes, and the diffusivity and cut-off radius for the projection orbital.

PWSCF, or any other *ab initio* electronic structure code, then reads **seedname.nnkp** file, calculates the projections and writes them to **seedname.amn**.

5.2 mmn file

INPUT.

The file seedname.mmn contains the overlaps $M_{mn}^{(\mathbf{k},\mathbf{b})}$.

First line: a user comment, e.g., the date and time

Second line: 3 integers: num_bands, num_kpts, nntot

Then: num_kpts × nntot blocks of data:

First line of each block: 5 integers. The first specifies the \mathbf{k} (i.e., gives the ordinal corresponding to its position in the list of k-points in seedname.win). The 2nd to 5th integers specify $\mathbf{k} + \mathbf{b}$. The 2nd integer, in particular, points to the k-point on the list that is a periodic image of $\mathbf{k} + \mathbf{b}$, and in particular is the image that is actually mentioned in the list. The last three integers specify the \mathbf{G} vector, in reciprocal lattice units, that brings the k-point specified by the fourth integer, and that thus lives inside the first BZ zone, to the actual $\mathbf{k} + \mathbf{b}$ that we need.

Subsequent num_bands × num_bands lines of each block: two real numbers per line. These are the real and imaginary parts, respectively, of the actual scalar product $M_{mn}^{(\mathbf{k},\mathbf{b})}$ for $m,n\in[1,\text{num_bands}]$. The order of these elements is such that the first index m is fastest.

5.3 amn file

INPUT.

The file seedname.amn contains the projection $A_{mn}^{(\mathbf{k})}$.

First line: a user comment, e.g., the date and time

Second line: 3 integers: num_bands, num_kpts, num_wann

Subsequently num_bands × num_wann × num_kpts lines: 3 integers and 2 real numbers on each line. The first two integers are the band indices m and n. The third integer specifies the k by giving the ordinal corresponding to its position in the list of k-points in seedname.win. The real numbers are the real and imaginary parts, respectively, of the actual $A_{mn}^{(k)}$.

5.4 eig file

INPUT.

Required if any of disentanglement, plot_bands, plot_fermi_surface or plot_dos are .true.

The file seedname.eig contains the Kohn-Sham eigenvalues $\varepsilon_{n\mathbf{k}}$ (in eV) at each point in the Monkhorst-Pack mesh.

Each line consist of two integers and a real number. The first integer is the band index, the second integer gives the ordinal corresponding to the k-point in the list of k-points in seedname.win, and the real number is the eigenvalue.

E.g.,

1	1	-6.43858831271328
2	1	19.3977795287297
3	1	19.3977795287297
4	1	19.3977795287298

5.5 Interface with PWSCF

- 1. Run 'scf'/'nscf' calculation(s) with pw
- 2. Run wannier90 with postproc_setup = .true. to generate seedname.nnkp
- 3. Run pw2wannier90. First it reads pw2wannier90.in, which defines prefix and outdir for the underlying 'scf' calculation, as well as the name of the file seedname.nnkp, and does a consistency check between the direct and reciprocal lattice vectors read from seedname.nnkp and those defined in the files specified by prefix. pw2wannier90 generates seedname.mmn, seedname.amn and seedname.eig
- 4. Run wannier90 with postproc_setup = .false. to disentangle bands (if required) and localise MLWF.

5.5.1 pw2wannier90.in

```
A number of keywords may be specified in the pw2wannier90 input file:
```

```
outdir - Location to write output files. Default is './'

prefix - Prefix for the PWSCF calculation. Default is ','

seedname - Seedname for the wannier90 calculation. Default is 'wannier'

spin_component - Spin component. Takes values 'up',

'down' or 'none' (default).

write_unk - Set to true to write the periodic part of the Bloch functions for plotting in wannier90. Default is .false.
```

wvfn_formatted - Set to .true. to write formatted wavefunctions. Default is .false. (only relevant if write_unk=.true.)

```
write_amn - Set to .false. if A_{mn}^{(\mathbf{k})} not required. Default is .true. write_mmn - Set to .false. if M_{mn}^{(\mathbf{k},\mathbf{b})} not required. Default is .true.
```

Chapter 6

wannier90 as a library

This is a description of the interface between any external program and the wannier code. There are two subroutines: wannier_setup and wannier_run. Calling wannier_setup will return information required to construct the $M_{mn}^{(\mathbf{k},\mathbf{b})}$ overlaps (Ref. [1], Eq. (25)) and $A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}} | g_n \rangle$ projections (Ref. [1], Eq. (62); Ref. [2], Eq. (22)). Once the overlaps and projection have been computed, calling wannier_run activates the minimisation and plotting routines in wannier90.

6.1 Subroutines

6.1.1 wannier_setup

- character(len=*), intent(in) :: seed_name
 The seedname of the current calculation.
- integer, dimension(3), intent(in) :: mp_grid The dimensions of the Monkhorst-Pack k-point grid.
- integer, intent(in) :: num_kpts

 The number of k-points on the Monkhorst-Pack grid.
- real(kind=dp), dimension(3,3), intent(in) :: real_lattice The lattice vectors in Cartesian co-ordinates in units of Angstrom.
- real(kind=dp), dimension(3,3), intent(in) :: recip_lattice

 The reciprocal lattice vectors in Cartesian co-ordinates in units of reciprocal Angstrom.

- real(kind=dp), dimension(3,num_kpts), intent(in) :: kpt_latt

 The positions of the k-points in fractional co-ordinates relative to the reciprocal lattice vectors.
- integer, intent(in) :: num_bands_tot

 The total number of bands in the first-principles calculation (note: including semi-core states).
- integer, intent(in) :: num_atoms

 The total number of atoms in the system.
- character(len=20), dimension(num_atoms), intent(in) :: atom_symbols The elemental symbols of the atoms.
- real(kind=dp), dimension(3,num_atoms), intent(in) :: atoms_cart The positions of the atoms in Cartesian co-ordinates in Angstrom.
- integer, intent(out) :: nntot
 The total number of nearest neighbours for each k-point.
- integer, dimension(num_kpts,num_nnmax), intent(out) :: nnlist The list of nearest neighbours for each k-point.
- integer, dimension (3, num_kpts, num_nnmax), intent (out) :: nncell The vector, in fractional reciprocal lattice co-ordinates, that brings the nn^{th} nearest neighbour of k-point nkp to its periodic image that is needed for computing the overlap $M_{mn}^{(\mathbf{k},\mathbf{b})}$.
- integer, intent(out) :: num_bands

 The number of bands in the first-principles calculation used to form the overlap matricies
 (note: excluding eg. semi-core states).
- integer, intent(out) :: num_wann
 The number of MLWF to be extracted.
- real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_site Projection function centre in crystallographic co-ordinates relative to the direct lattice vectors.
- integer, dimension(num_bands_tot), intent(out) :: proj_1 l specifies the angular part $\Theta_{lm_r}(\theta,\varphi)$ of the projection function (see Tables 3.1, 3.2 and 3.3).
- integer, dimension(num_bands_tot), intent(out) :: proj_m $m_{\rm r}$ specifies the angular part $\Theta_{lm_{\rm r}}(\theta,\varphi)$, of the projection function (see Tables 3.1, 3.2 and 3.3).
- integer, dimension(num_bands_tot), intent(out) :: proj_radial r specifies the radial part $R_r(r)$ of the projection function (see Tables 3.1, 3.2 and 3.3).

- real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_z Defines the axis from which the polar angle θ in spherical polar coordinates is measured. Default is 0.0 0.0 1.0.
- real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_x Must be orthogonal to z-axis; default is 1.0 0.0 0.0 or a vector perpendicular to proj_z if proj_z is given; defines the axis from with the azimuthal angle φ in spherical polar coordinates is measured.
- real(kind=dp), dimension(num_bands_tot), intent(out) :: proj_zona The value of $\frac{Z}{a}$ associated with the radial part of the atomic orbital. Units are in reciprocal Angstrom.
- integer, dimension(num_bands_tot), intent(out) :: exclude_bands Kpoints independant list of bands to exclude from the calculation of the MLWF (e.g., semi-core states).

Conditions:

```
\star \  \, \texttt{num\_kpts} = \texttt{mp\_grid(1)} \times \texttt{mp\_grid(2)} \times \texttt{mp\_grid(3)}.
```

 \star num_nnmax = 12

This subroutine returns the information required to determine the required overlap elements $M_{mn}^{(\mathbf{k},\mathbf{b})}$ and projections $A_{mn}^{(\mathbf{k})}$, i.e., M_matrix and A_matrix, described in Section 6.1.2.

For the avoidance of doubt, real_lattice(1,2) is the y-component of the first lattice vector \mathbf{A}_1 , etc.

The list of nearest neighbours of a particular k-point nkp is given by nnlist(nkp,1:nntot).

Additionally, the parameters num_shells and shell_list may be specified in the wannier90 input file.

6.1.2 wannier_run

- character(len=*), intent(in) :: seed_name
 The seedname of the current calculation.
- integer, dimension(3), intent(in) :: mp_grid The dimensions of the Monkhorst-Pack k-point grid.
- integer, intent(in) :: num_kpts

 The number of k-points on the Monkhorst-Pack grid.

- real(kind=dp), dimension(3,3), intent(in) :: real_lattice The lattice vectors in Cartesian co-ordinates in units of Angstrom.
- real(kind=dp), dimension(3,3), intent(in) :: recip_lattice

 The reciprical lattice vectors in Cartesian co-ordinates in units of inverse Angstrom.
- real(kind=dp), dimension(3,num_kpts), intent(in) :: kpt_latt

 The positions of the k-points in fractional co-ordinates relative to the reciprocal lattice vectors.
- integer, intent(in) :: num_bands

 The total number of bands to be processed.
- integer, intent(in) :: num_wann
 The number of MLWF to be extracted.
- integer, intent(in) :: nntot

 The number of nearest neighbours for each k-point.
- integer, intent(in) :: num_atoms
 The total number of atoms in the system.
- character(len=20), dimension(num_atoms), intent(in) :: atom_symbols The elemental symbols of the atoms.
- real(kind=dp), dimension(3,num_atoms), intent(in) :: atoms_cart The positions of the atoms in Cartesian co-ordinates in Angstrom.
- complex(kind=dp), dimension(num_bands,num_bands,nntot,num_kpts), intent(in) :: M_matrix

 The matrices of overlaps between neighbouring periodic parts of the Bloch eigenstates at each k-point, $M_{mn}^{(\mathbf{k},\mathbf{b})}$ (Ref. [1], Eq. (25)).
- real(kind=dp), dimension(num_bands,num_kpts), intent(in) :: eigenvalues The eigenvalues $\varepsilon_{n\mathbf{k}}$ corresponding to the eigenstates, in eV.

- logical, dimension(num_bands,num_kpts), intent(out) :: lwindow
 The element lwindow(nband,nkpt) is .true. if the band nband lies within the outer
 energy window at kpoint nkpt.
- real(kind=dp), dimension(3,num_wann), intent(out) :: wann_centres The centres of the MLWF in Cartesian co-ordinates in Angstrom.
- real(kind=dp), dimension(num_wann), intent(out) :: wann_spreads The spread of each MLWF in \mathring{A}^2 .
- real(kind=dp), dimension(3), intent(out) :: spread The values of Ω , $\Omega_{\rm I}$ and $\tilde{\Omega}$ (Ref. [1], Eq. (13)).

Conditions:

```
★ num_wann ≤ num_bands
```

```
* num_kpts = mp_grid(1) \times mp_grid(2) \times mp_grid(3).
```

If num_bands = num_wann then U_matrix_opt is the identity matrix and lwindow=.true.

For the avoidance of doubt, real_lattice(1,2) is the y-component of the first lattice vector \mathbf{A}_1 , etc.

```
\begin{array}{lcl} \texttt{M\_matrix(m,n,nkp,nn)} &=& \langle u_{m\mathbf{k}} | u_{n\mathbf{k}+\mathbf{b}} \rangle \\ \\ \texttt{A\_matrix(m,n,nkp)} &=& \langle \psi_{m\mathbf{k}} | g_n \rangle \\ \\ \texttt{eigenvalues(n,nkp)} &=& \varepsilon_{n\mathbf{k}} \end{array}
```

where

```
\mathbf{k} = \text{kpt\_latt(1:3,nkp)}

\mathbf{k} + \mathbf{b} = \text{kpt\_latt(1:3,nnlist(nkp,nn))} + \text{nncell(1:3,nkp,nn)}
```

and $\{|g_n\rangle\}$ are a set of initial trial orbitals. These are typically atom or bond-centred Gaussians that are modulated by appropriate spherical harmonics.

Additional parameters should be specified in the wannier90 input file.

Chapter 7

Files

7.1 seedname.win

INPUT. The master input file; contains the specification of the system and any parameters for the run.

7.1.1 Units

The following are the dimensional quantities that are specified in the master input file:

- Direct lattice vectors
- Positions (of atomic or projection) centres in real space
- Energy windows
- Positions of k-points in reciprocal space
- zona and box-size (see Section 3.1)

Notes:

- The units (either ang (default) or bohr) in which the lattice vectors, atomic positions or projection centres are given can be set in the first line of the blocks unit_cell_cart, atoms_cart and projections, respectively, in seedname.win.
- Energy is always in eV.
- Positions of k-points are always in crystallographic coordinates relative to the reciprocal lattice vectors.
- box-size and zona always in Angstrom and reciprocal Angstrom, respectively

• The keyword length_unit may be set to ang (default) or bohr, in order to set the units in which the quantities in the output file are written.

The reciprocal lattice vectors $\{\mathbf{B}_1,\mathbf{B}_2,\mathbf{B}_3\}$ are defined in terms of the direct lattice vectors $\{\mathbf{A}_1,\mathbf{A}_2,\mathbf{A}_3\}$ by the equation

$$\mathbf{B}_1 = \frac{2\pi}{\Omega} \mathbf{A}_2 \times \mathbf{A}_3 \quad \text{etc.}, \tag{7.1}$$

where the cell volume is $V = \mathbf{A}_1 \cdot (\mathbf{A}_2 \times \mathbf{A}_3)$.

7.2 seedname.mmn

INPUT. See Chapter 5.

7.3 seedname.amn

INPUT. See Chapter 5.

7.4 seedname.eig

INPUT. See Chapter 5.

7.5 seedname.nnkp

OUTPUT. See Chapter 5.

7.6 seedname.wout

OUTPUT. The master output file.

7.7 seedname.chk

INPUT/OUTPUT. Information required to restart the calculation or enter the plotting phase. If we have used disentanglement this file also contains the rectangular matrices $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$.

7.8 seedname_um.dat

INPUT/OUTPUT. Contains $\mathbf{U^{(k)}}$ and $\mathbf{M^{(k,b)}}$ (in the basis of the rotated Bloch states). Required to restart the calculation or enter the plotting phase.

7.9 seedname.r2mn

OUTPUT. Written if write_r2mn = true. The matrix elements $\langle m|r^2|n\rangle$ (where m and n refer to MLWF)

7.10 seedname_band.dat

OUTPUT. Written if bands_plot=TRUE. The interpolated band structure.

7.11 seedname_band.gnu

OUTPUT. Written if bands_plot=TRUE. A gnuplot script to plot the interpolated band structure.

7.12 seedname_band.dat

OUTPUT. Written if bands_plot=TRUE. The kpoints used for the interpolated band structure, in units of the reciprical lattice vectors. This file can be used to generate a comparison band structure from a first-principles code.

7.13 seedname.bxsf

OUTPUT. Written if fermi_surface_plot=TRUE. A Fermi surface plot file suitable for plotting with XCrySDen.

7.14 seedname_w.xsf

OUTPUT. Written if wannier_plot=TRUE. The wth in real space in a format suitable for plotting with XCrySDen.

7.15 UNKp.s

INPUT. Read if wannier_plot=TRUE and used to plot the MLWF.

The periodic part of the Bloch states represented on a regular real space grid, indexed by k-point p (from 1 to num_kpts) and spin s ('1' for 'up', '2' for 'down').

The name of the wavefunction file is assumed to have the form:

```
write(wfnname,200) p,spin
200 format ('UNK',i5.5,'.',i1)
```

The first line of each file should contain 5 integers: the number of grid points in each direction (ngx, ngy and ngz), the k-point number ik and the total number of bands num_band in the file. The full file will be read by wannier90 as:

```
read(file_unit) ngx,ngy,ngz,ik,nbnd
do loop_b=1,num_bands
  read(file_unit) (r_wvfn(nx,loop_b),nx=1,ngx*ngy*ngz)
end do
```

The file can be in formatted or unformatted style, this is controlled by the logical keyword wvfn_formatted.

Chapter 8

Sample files

8.1 Input file

8.1.1 seedname.win

```
num_wann
                 : 4 4 4
mp_grid
num_iter
                 : 100
postproc_setup : true
begin unit_cell_cart
-1.61 0.00 1.61
0.00 1.61 1.61
-1.61 1.61 0.00
end unit_cell_cart
begin atoms_frac
   -0.125 -0.125 -0.125
     0.125
           0.125
                   0.125
end atoms_frac
bands_plot
             : true
bands_num_points : 100
bands_plot_format : gnuplot
begin kpoint_path
L 0.50000 0.50000 0.50000 G 0.00000 0.00000 0.00000
G 0.00000 0.00000 0.00000 X 0.50000 0.00000 0.50000
X 0.50000 0.00000 0.50000 K 0.62500 0.25000 0.62500
end kpoint_path
```

```
begin projections
C:1=0,1=1
end projections
begin kpoints
0.00 0.00 0.00
0.00 0.00 0.25
0.00 0.50 0.50
0.75 0.75 0.50
0.75 0.75 0.75
end kpoints
8.1.2
       seedname.nnkp
Running wannier90 on the above input file would generate the following nnkp file:
File written on 9Feb2006 at 15:13: 9
calc_only_A
begin real_lattice
  -1.612340
              0.000000
                        1.612340
  0.000000
              1.612340
                         1.612340
  -1.612340
             1.612340
                        0.000000
end real_lattice
begin recip_lattice
  -1.951300 -1.951300
                        1.951300
   1.951300
            1.951300
                        1.951300
  -1.951300
             1.951300 -1.951300
end recip_lattice
begin kpoints
     64
  0.00000
           0.00000 0.00000
  0.00000
           0.25000 0.00000
  0.00000
            0.50000
                     0.00000
  0.00000
            0.75000
                     0.00000
  0.25000
           0.00000
                    0.00000
```

.

```
0.50000
            0.75000
                       0.75000
 0.75000
            0.00000
                       0.75000
 0.75000
            0.25000
                       0.75000
 0.75000
            0.50000
                       0.75000
 0.75000
            0.75000
                       0.75000
end kpoints
```

begin projections

-0.12500 -0.12500 -0.12500 0 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 2.00 -0.12500 -0.12500 -0.12500 1 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 2.00 -0.12500 -0.12500 -0.12500 1 2 0.000 0.000 1.000 1.000 0.000 0.000 2.00 2.00 -0.12500 -0.12500 -0.12500 1 3 1 0.000 1.000 0.000 1.000 0.000 0.000 2.00 2.00 0.12500 0.12500 0.12500 0 1 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 2.00 0.12500 0.12500 0.12500 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 2.00 0.12500 0.12500 0.12500 1 2 0.000 0.000 1.000 1.000 0.000 0.000 2.00 2.00 0.12500 0.12500 0.12500 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 2.00 end projections

begin nnkpts

.

•				
64	1	1	1	1
64	16	0	0	1
64	43	0	0	0
64	48	0	0	0
64	52	1	0	0
64	60	0	0	0
64	61	0	1	0
64	63	0	0	0
end	nnkpts			

begin exclude_bands

end exclude_bands

Bibliography

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