wannier90: User Guide

Version 1.0.3

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Chapter 1

Introduction

1.1 Methodology

wannier90 computes maximally-localised Wannier functions (MLWF) following the method of Marzari and Vanderbilt (MV) [1]. For entangled energy bands, the method of Souza, Marzari and Vanderbilt (SMV) [2] is used. We introduce briefly the methods and key definitions here, but full details can be found in the original papers and in Ref. [4].

First-principles codes typically solve the electronic structure of periodic materials in terms of Bloch states, $\psi_{n\mathbf{k}}$. These extended states are characterised by a band index n and crystal momentum \mathbf{k} . An alternative representation can be given in terms of spatially localised functions known as Wannier functions (WF). The WF centred on a lattice site \mathbf{R} , $w_{n\mathbf{R}}(\mathbf{r})$, is written in terms of the set of Bloch states as

$$w_{n\mathbf{R}}(\mathbf{r}) = \frac{V}{(2\pi)^3} \int_{BZ} \left[\sum_{m} U_{mn}^{(\mathbf{k})} \psi_{m\mathbf{k}}(\mathbf{r}) \right] e^{-i\mathbf{k}\cdot\mathbf{R}} d\mathbf{k} , \qquad (1.1)$$

where V is the unit cell volume, the integral is over the Brillouin zone (BZ), and $\mathbf{U^{(k)}}$ is a unitary matrix that mixes the Bloch states at each \mathbf{k} . $\mathbf{U^{(k)}}$ is not uniquely defined and different choices will lead to WF with varying spatial localisations. We define the spread Ω of the WF as

$$\Omega = \sum_{n} \left[\langle w_{n\mathbf{0}}(\mathbf{r}) | r^2 | w_{n\mathbf{0}}(\mathbf{r}) \rangle - |\langle w_{n\mathbf{0}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2 \right]. \tag{1.2}$$

The total spread can be decomposed into a gauge invariant term $\Omega_{\rm I}$ plus a term $\tilde{\Omega}$ that is dependant on the gauge choice $\mathbf{U}^{(\mathbf{k})}$. $\tilde{\Omega}$ can be further divided into terms diagonal and off-diagonal in the WF basis, $\Omega_{\rm D}$ and $\Omega_{\rm OD}$,

$$\Omega = \Omega_{\rm I} + \tilde{\Omega} = \Omega_{\rm I} + \Omega_{\rm D} + \Omega_{\rm OD} \tag{1.3}$$

where

$$\Omega_{\rm I} = \sum_{n} \left[\langle w_{n\mathbf{0}}(\mathbf{r}) | r^2 | w_{n\mathbf{0}}(\mathbf{r}) \rangle - \sum_{\mathbf{R}m} |\langle w_{n\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2 \right]$$
(1.4)

$$\Omega_{\rm D} = \sum_{n} \sum_{\mathbf{R} \neq \mathbf{0}} |\langle w_{n\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2$$
(1.5)

$$\Omega_{\rm OD} = \sum_{m \neq n} \sum_{\mathbf{R}} |\langle w_{m\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2$$
(1.6)

The MV method minimises the gauge dependent spread $\tilde{\Omega}$ with respect the set of $\mathbf{U^{(k)}}$ to obtain MLWF.

wannier90 requires two ingredients from an initial electronic structure calculation.

1. The overlaps between the cell periodic part of the Bloch states $|u_{n\mathbf{k}}\rangle$

$$M_{mn}^{(\mathbf{k},\mathbf{b})} = \langle u_{m\mathbf{k}} | u_{n\mathbf{k}+\mathbf{b}} \rangle, \tag{1.7}$$

where the vectors **b**, which connect a given k-point with its neighbours, are determined by wannier90 according to the prescription outlined in Ref. [1].

2. As a starting guess the projection of the Bloch states $|\psi_{n\mathbf{k}}\rangle$ onto trial localised orbitals $|g_n\rangle$

$$A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}} | g_n \rangle, \tag{1.8}$$

Note that $\mathbf{M}^{(\mathbf{k},\mathbf{b})}$, $\mathbf{A}^{(\mathbf{k})}$ and $\mathbf{U}^{(\mathbf{k})}$ are all small, $N \times N$ matrices¹ that are independent of the basis set used to obtain the original Bloch states.

To date, wannier90 has been used in combination with electronic codes based on plane-waves and pseudopotentials (norm-conserving and ultrasoft [5]) as well as mixed basis set techniques such as FLAPW [6].

1.1.1 Entangled Energy Bands

The above description is sufficient to obtain MLWF for an isolated set of bands, such as the valence states in an insulator. In order to obtain MLWF for entangled energy bands we use the "disentanglement" procedure introduced in Ref. [2].

We define an energy window (the "outer window"). At a given k-point \mathbf{k} , $N_{\text{win}}^{(\mathbf{k})}$ states lie within this energy window. We obtain a set of N Bloch states by performing a unitary transformation amongst the Bloch states which fall within the energy window at each k-point:

$$|u_{n\mathbf{k}}^{\text{opt}}\rangle = \sum_{m \in N_{\text{min}}^{(\mathbf{k})}} U_{mn}^{\text{dis}(\mathbf{k})} |u_{m\mathbf{k}}\rangle$$
(1.9)

where $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ is a rectangular $N \times N_{\mathrm{win}}^{(\mathbf{k})}$ matrix². The set of $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ are obtained by minimising the gauge invariant spread Ω_{I} within the outer energy window. The MV procedure can then be used to minimise $\tilde{\Omega}$ and hence obtain MLWF for this optimal subspace.

It should be noted that the energy bands of this optimal subspace may not correspond to any of the original energy bands (due to mixing between states). In order to preserve exactly the properties of a system in a given energy range (e.g., around the Fermi level) we introduce a second energy window. States lying within this inner, or "frozen", energy window are included unchanged in the optimal subspace.

¹Technically, this is true for the case of an isolated group of N bands from which we obtain N MLWF. When using the disentanglement procedure of Ref. [2], $\mathbf{A}^{(\mathbf{k})}$, for example, is a rectangular matrix. See Section 1.1.1.
²As $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ is a rectangular matrix this is a unitary operation in the sense that $(\mathbf{U}^{\mathrm{dis}(\mathbf{k})})^{\dagger}\mathbf{U}^{\mathrm{dis}(\mathbf{k})} = \mathbf{1}$.

1.1.2 Getting Help

The latest version of wannier90 and documentation can always be found at

```
http://www.wannier.org
```

There is a wannier90 mailing list for discussing issues in the development, theory, coding and algorithms pertinent to MLWF. You can register for this mailing list by following the links at

```
http://www.wannier.org/forum.html
```

Finally, many frequently asked questions are answered in Chapter 8.

1.1.3 Citation

We ask that you acknowledge the use of wannier90 in any publications arising from the use of this code through the following reference

```
[ref] A. A. Mostofi, J. R. Yates, Y.-S. Lee, I. Souza, D. Vanderbilt and N. Marzari, wannier90: A Tool for Obtaining Maximally-Localised Wannier Functions, Comput. Phys. Commun., submitted (2007); http://arxiv.org/abs/0708.0650
```

It would also be appropriate to cite the original articles:

Maximally localized generalized Wannier functions for composite energy bands, N. Marzari and D. Vanderbilt, *Phys. Rev. B* **56**, 12847 (1997)

Maximally localized Wannier functions for entangled energy bands, I. Souza, N. Marzari and D. Vanderbilt, *Phys. Rev. B* **65**, 035109 (2001)

1.1.4 Credits

The present release of wannier90 was written by Arash A. Mostofi (Imperial College London, UK), Jonathan R. Yates (University of Cambridge, UK), and Young-Su Lee (KIST, S. Korea). wannier90 is based on routines written in 1996-7 for isolated bands by Nicola Marzari and David Vanderbilt, and for entangled bands by Ivo Souza, Nicola Marzari, and David Vanderbilt in 2000-1.

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1.1.5 Licence

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Chapter 2

Parameters

2.1 Usage

```
wannier90.x [-pp] [seedname]
```

- seedname: If a seedname string is given the code will read its input from a file seedname.win. The default value is wannier.
- -pp: This optional flag tells the code to generate a list of the required overlaps and then exit. This information is written to the file seedname.nnkp.

2.2 seedname.win File

The wannier90 input file seedname.win has a flexible free-form structure.

The ordering of the keywords is not significant. Case is ignored (so num_bands is the same as Num_Bands). Characters after !, or # are treated as comments. Most keywords have a default value that is used unless the keyword is given in seedname.win. Keywords can be set in any of the following ways

```
num_wann 4
num_wann = 4
num_wann : 4
```

A logical keyword can be set to .true. using any of the following strings: T, true, .true..

For further examples see Section 9.1 and the wannier90 Tutorial.

2.3 Keyword List

Keyword	Type	Description
	Syste	em Parameters
NUM_WANN	I	Number of WF
NUM_BANDS	I	Number of bands passed to the code
UNIT_CELL_CART	P	Unit cell vectors in Cartesian coor-
		dinates
ATOMS_CART *	P	Positions of atoms in Cartesian co-
		ordinates
ATOMS_FRAC *	R	Positions of atoms in fractional co-
		ordinates with respect to the lattice
		vectors
MP_GRID	I	Dimensions of the Monkhorst-Pack
		grid of k-points
KPOINTS	R	List of k-points in the Monkhorst-
		Pack grid
GAMMA_ONLY	L	Wavefunctions from underlying ab
		initio calculation are manifestly real
NUM_SHELLS	I	Number of shells in finite difference
		formula
SHELL_LIST	I	Which shells to use in finite differ-
		ence formula
SEARCH_SHELLS	I	The number of shells to search
		when determining finite difference
		formula

Table 2.1: seedname.win file keywords defining the system. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

^{*} ATOMS_CART and ATOMS_FRAC may not both be defined in the same input file.

Keyword	Type	Description
	Job	Control
POSTPROC_SETUP	L	To output the seedname.nnkp file
EXCLUDE_BANDS	I	List of bands to exclude from the
		calculation
RESTART	С	Restart from checkpoint file
IPRINT	I	Output verbosity level
LENGTH_UNIT	S	System of units to output lengths
WVFN_FORMATTED	L	Read the wavefunctions from a
		(un)formatted file
SPIN	S	Which spin channel to read
DEVEL_FLAG	S	Flag for development use
TIMING_LEVEL	I	Determines amount of timing infor-
		mation written to output
TRANSLATE_HOME_CELL	L	To translate final Wannier centres to
		home unit cell when writing xyz file
WRITE_XYZ	L	To write final centres in xyz file for-
		mat

Table 2.2: seedname.win file keywords defining the system. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string. TRANSLATE_HOME_CELL only relevant if WRITE_XYZ is .true.

Keyword	Type	Description
Dis	sentangl	ement Parameters
DIS_WIN_MIN	Р	Bottom of the outer energy window
DIS_WIN_MAX	P	Top of the outer energy window
DIS_FROZ_MIN	P	Bottom of the inner (frozen) energy
		window
DIS_FROZ_MAX	P	Top of the inner (frozen) energy
		window
DIS_NUM_ITER	I	Number of iterations for the minimi-
		sation of $\Omega_{\rm I}$
DIS_MIX_RATIO	R	Mixing ratio during the minimisa-
		tion of Ω_{I}
DIS_CONV_TOL	R	The convergence tolerance for find-
		$\log\Omega_{ m I}$
DIS_CONV_WINDOW	I	The number of iterations over which
		convergence of $\Omega_{\rm I}$ is assessed.

Table 2.3: seedname.win file keywords controlling the disentanglement. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description		
Wannierise Parameters				
NUM_ITER	I	Number of iterations for the minimi-		
		sation of Ω		
NUM_CG_STEPS	I	During the minimisation of Ω the		
		number of Conjugate Gradient steps		
		before resetting to Steepest De-		
	_	scents		
CONV_WINDOW	I	The number of iterations over which		
		convergence of Ω is assessed		
CONV_TOL	P	The convergence tolerance for find-		
G0377 34049 4349	D	$\log \Omega$		
CONV_NOISE_AMP	R	The amplitude of random noise ap-		
		plied towards end of minimisation		
CONV_NOISE_NUM	Ī	procedure The number of times random noise		
CONV_NOISE_NOM	1	is applied		
NUM_DUMP_CYCLES	I	Control frequency of check-pointing		
NUM PRINT CYCLES	Ī	Control frequency of printing		
WRITE_R2MN	L	Write matrix elements of r^2 between		
VV 101112_1021/11V		WF to file		
GUIDING_CENTRES	$_{ m L}$	Use guiding centres		
NUM_GUIDE_CYCLES	I	Frequency of guiding centres		
NUM_NO_GUIDE_ITER	I	The number of iterations after		
		which guiding centres are used		
TRIAL_STEP *	R	The trial step length for the		
		parabolic line search during the		
		minimisation of Ω		
FIXED_STEP *	R	The fixed step length to take dur-		
		ing the minimisation of Ω , instead		
		of doing a parabolic line search		
USE_BLOCH_PHASES **	L	To use phases for initial projections		

Table 2.4: seedname.win file keywords controlling the wannierisation. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string. *fixed_step and trial_step may not both be defined in the same input file. **Cannot be used in conjunction with disentanglement.

Keyword	Type	Description		
Plot Parameters				
WANNIER_PLOT	L	Plot the WF		
WANNIER_PLOT_LIST	I	List of WF to plot		
WANNIER_PLOT_SUPERCELL	I	Size of the supercell for plotting the		
William I and I and I all the East I		WF		
WANNIER_PLOT_FORMAT	S	File format in which to plot the WF		
WANNIER_PLOT_MODE	S	Mode in which to plot the WF,		
		molecule or crystal		
WANNIER_PLOT_RADIUS	R	Cut-off radius of WF*		
BANDS_PLOT	L	Plot interpolated band structure		
KPOINT_PATH	P	K-point path for the interpolated		
		band structure		
BANDS_NUM_POINTS	I	Number of points along the first sec-		
		tion of the k-point path		
BANDS_PLOT_FORMAT	S	File format in which to plot the in-		
		terpolated bands		
BANDS_PLOT_MODE	S	Slater-Koster type interpolation or		
		Hamiltonian cut-off		
BANDS_PLOT_DIM	I	Dimension of the system		
FERMI_SURFACE_PLOT	L	Plot the Fermi surface		
FERMI_SURFACE_NUM_POINTS	I	Number of points in the Fermi sur-		
		face plot		
FERMI_ENERGY	P	The Fermi energy		
FERMI_SURFACE_PLOT_FORMAT	S	File format for the Fermi surface		
		plot		
HR_PLOT	L	Write the Hamiltonian in the WF		
		basis		
HR_CUTOFF	P	Cut-off for the absolute value of the		
	_	Hamiltonian		
DIST_CUTOFF	P	Cut-off for the distance between WF		
DIST_CUTOFF_MODE	S	Dimension in which the distance be-		
		tween WF is calculated		
ONE_DIM_AXIS	S	Extended direction for a one-		
		dimensional system		
TRANSLATION_CENTRE_FRAC	R	Centre of the unit cell to which final		
		WF are translated		

Table 2.5: seedname.win file keywords controlling the plotting. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string. * Only applies when WANNIER_PLOT_FORMAT is cube.

Keyword	Type	Description		
Transport Parameters				
TRANSPORT	L	Calculate quantum conductance		
TIMMOI OILI		and density of states		
TRANSPORT_MODE	S	Bulk or left-lead_conductor_right-		
TRANSFORT_MODE		lead calculation		
TRAN_WIN_MIN	P	Bottom of the energy window for		
I KAN_WIN_WIN	1	transport calculation		
TRAN_WIN_MAX	P	Top of the energy window for trans-		
TRAN_WIN_MAX	1	port calculation		
TD AN ENEDGY CTED	R	Sampling interval of the energy val-		
TRAN_ENERGY_STEP	11	ues		
EEDMI ENEDGY	R	The Fermi energy		
FERMI_ENERGY TRAN_NUM_BB	I	Size of a bulk Hamiltonian		
TRAN_NUM_LL	I	Size of a left-lead Hamiltonian		
TRAN_NUM_RR	I	Size of a right-lead Hamiltonian		
TRAN_NUM_CC	I	Size of a right-lead Hamiltonian		
TRAN_NUM_LC	I	Number of columns in a left-		
TRANSNOWSEC	1	lead_conductor Hamiltonian		
TRAN_NUM_CR	I	Number of rows in a conduc-		
TRANINOMICK	1	tor_right-lead Hamiltonian		
TRAN_NUM_BANDC	I	Half-bandwidth+1 of a band-		
TITAN IN OWLDANDO	1	diagonal conductor Hamiltonian		
TRAN_WRITE_HT	L	Write the Hamiltonian for transport		
TITAN_WITTE_III		calculation		
TRAN_READ_HT	$_{ m L}$	Read the Hamiltonian for transport		
		calculation		
TRAN_USE_SAME_LEAD	L	Left and right leads are the same		
HR_CUTOFF	P	Cut-off for the absolute value of the		
	_	Hamiltonian		
DIST_CUTOFF	P	Cut-off for the distance between WF		
DIST_CUTOFF_MODE	S	Dimension in which the distance be-		
		tween WF is calculated		
ONE_DIM_AXIS	S	Extended direction for a one-		
		dimensional system		
TRANSLATION_CENTRE_FRAC	R	Centre of the unit cell to which final		
		WF are translated		

Table 2.6: seedname.win file keywords controlling transport. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

2.4 System

2.4.1 integer :: num_wann

Number of WF to be found.

No default.

2.4.2 integer :: num_bands

Total number of bands passed to the code in the seedname.mmn file.

Default num_bands=num_wann

2.4.3 Cell Lattice Vectors

The cell lattice vectors should be specified in Cartesian coordinates.

begin unit_cell_cart
[units]

$$\begin{array}{cccc} A_{1x} & A_{1y} & A_{1z} \\ A_{2x} & A_{2y} & A_{2z} \\ A_{3x} & A_{3y} & A_{3z} \end{array}$$

end unit_cell_cart

Here A_{1x} is the x-component of the first lattice vector \mathbf{A}_1 , A_{2y} is the y-component of the second lattice vector \mathbf{A}_2 , etc.

[units] specifies the units in which the lattice vectors are defined: either Bohr or Ang.

The default value is Ang.

2.4.4 Ionic Positions

The ionic positions may be specified in fractional coordinates relative to the lattice vectors of the unit cell, or in absolute cartesian coordinates. Only one of atoms_cart and atoms_frac may be given in the input file.

Cartesian coordinates

begin atoms_cart
[units]

$$\begin{array}{cccc} P & R_x^P & R_y^P & R_z^P \\ Q & R_x^Q & R_y^Q & R_z^Q \\ \vdots & & & \end{array}$$

end atoms_cart

The first entry on a line is the atomic symbol. The next three entries are the atom's position $\mathbf{R} = (R_x, R_y, R_z)$ in Cartesian coordinates. The first line of the block, [units], specifies the units in which the coordinates are given and can be either bohr or ang. If not present, the default is ang.

Fractional coordinates

begin atoms_frac

$$\begin{array}{ccccc} P & F_{1}^{P} & F_{2}^{P} & F_{3}^{P} \\ Q & F_{1}^{Q} & F_{2}^{Q} & F_{3}^{Q} \\ \vdots & & & & \end{array}$$

end atoms_frac

The first entry on a line is the atomic symbol. The next three entries are the atom's position in fractional coordinates $\mathbf{F} = F_1 \mathbf{A}_1 + F_2 \mathbf{A}_2 + F_3 \mathbf{A}_3$ relative to the cell lattice vectors \mathbf{A}_i , $i \in [1,3]$.

2.4.5 integer, dimension :: mp_grid(3)

Dimensions of the regular (Monkhorst-Pack) k-point mesh. For example, for a $2 \times 2 \times 2$ grid:

mp_grid : 2 2 2

No default.

2.4.6 K-points

Each line gives the coordinate $\mathbf{K} = K_1\mathbf{B}_1 + K_2\mathbf{B}_2 + K_3\mathbf{B}_3$ of a k-point in relative (crystallographic) units, i.e., in fractional units with respect to the primitive reciprocal lattice vectors \mathbf{B}_i , $i \in [1, 3]$. The position of each k-point in this list assigns its numbering; the first k-point is k-point 1, the second is k-point 2, and so on.

begin kpoints

$$\begin{array}{cccc} K_1^1 & K_2^1 & K_3^1 \\ K_1^2 & K_2^2 & K_3^2 \\ \vdots & & & \end{array}$$

end kpoints

There is no default.

2.4.7 logical :: gamma_only

If gamma_only=TRUE, then wannier90 uses a branch of algorithms for disentanglement and localisation that exploit the fact that the Bloch eigenstates obtained from the underlying ab initio calculation are manifestly real. This can be the case when only the Γ -point is used to sample the Brillouin zone. The localisation procedure that is used in the Γ -only branch is based on the method of Ref. [3].

The default value is FALSE.

2.4.8 Shells

The MV scheme requires a finite difference expression for $\nabla_{\mathbf{k}}$ defined on a uniform Monkhorst-Pack mesh of k-points. The vectors $\{\mathbf{b}\}$ connect each mesh-point \mathbf{k} to its nearest neighbours. $N_{\rm sh}$ shells of neighbours are included in the finite-difference formula, with M_s vectors in the $s^{\rm th}$ shell. For $\nabla_{\mathbf{k}}$ to be correct to linear order, we require that the following equation is satisfied (Eq. B1 of Ref. [1]):

$$\sum_{s}^{N_{\rm sh}} w_s \sum_{i}^{M_s} b_{\alpha}^{i,s} b_{\beta}^{i,s} = \delta_{\alpha\beta} , \qquad (2.1)$$

where $\mathbf{b}^{i,s}$, $i \in [1, M_s]$, is the i^{th} vector belonging to the s^{th} shell with associated weight w_s , and α and β run over the three Cartesian indices.

2.4.9 integer :: num_shells

If num_shells> 0, then the number of shells to include in the finite difference expression. If num_shells= 0, then the code will choose the shells automatically.

The default value is 0.

2.4.10 integer :: shell_list(num_shells)

If num_shells> 0, then shell_list is vector listing the shells to include in the finite difference expression.

2.4.11 integer :: search_shells

Specifies the number of shells of neighbours over which to search in attempting to determine an automatic solution to the B1 condition Eq. 2.1.

The default value is 12.

2.5 Projection

The projections block defines a set of localised functions used to generate an initial guess for the unitary transformations. This data will be written in the seedname.nnkp file to be used by a first-principles code.

```
begin projections
.
.
end projections
```

If guiding_centres=TRUE, then the projection centres are used as the guiding centres in the Wannierisation routine.

For details see Section 3.1.

2.6 Job Control

2.6.1 logical :: postproc_setup

If postproc_setup=TRUE, then the wannier code will write seedname.nnkp file and exit. If wannier90 is called with the option -pp, then postproc_setup is set to TRUE, over-riding its value in the seedname.win file.

The default value is FALSE.

2.6.2 integer :: iprint

This indicates the level of verbosity of the output from 0, the bare minimum, to 3, which corresponds to full debugging output.

The default value is 1.

2.6.3 character(len=20) :: length_unit

The length unit to be used for writing quantities in the output file seedname.wout.

The valid options for this parameter are:

```
- Ang (default)
```

- Bohr

2.6.4 character(len=50) :: devel_flag

Not a regular keyword. Its purpose is to allow a developer to pass a string into the code to be used inside a new routine as it is developed.

No default.

2.6.5 integer :: exclude_bands(:)

A k-point independent list of states to excluded from the calculation of the overlap matrices; for example to select only valence states, or ignore semi-core states. This keyword is passed to the first-principles code via the seedname.nnkp file. For example, to exclude bands 2, 6, 7, 8 and 12:

exclude_bands : 2, 6-8, 12

2.6.6 character(len=20) :: restart

If restart is present the code will attempt to restart the calculation from the seedname.chk file. The value of the parameter determines the position of the restart

The valid options for this parameter are:

- default. Restart from the point at which the check file seedname.chk was written
- wannierise. Restart from the beginning of the wannierise routine
- plot. Go directly to the plotting phase

2.6.7 character(len=20) :: wvfn_formatted

If wvfn_formatted=TRUE, then the wavefunctions will be read from disk as formatted (ie ASCII) files; otherwise they will be read as unformatted files. Unformatted is generally preferable as the files will take less disk space and I/O is significantly faster. However such files will not be transferable between all machine architectures and formatted files should be used if transferability is required (i.e., for test cases).

The default value of this parameter is FALSE.

2.6.8 character(len=20) :: spin

For bands from a spin polarised calculation spin determines which set of bands to read in, either up or down.

The default value of this parameter is up.

2.6.9 integer :: timing_level

Determines the amount of timing information regarding the calculation that will be written to the output file. A value of 1 produces the least information.

The default value is 1.

2.6.10 logical :: translate_home_cell

Determines whether to translate the final Wannier centres to the home unit cell at the end of the calculation. Mainly useful for molecular systems in which the molecule resides entirely within the home unit cell and user wants to write an xyz file (write_xyz=.TRUE.) for the WF centres to compare with the structure.

The default value is false.

2.6.11 logical :: write_xyz

Determines whether to write the final Wannier centres to an xyz file, seedname_centres.xyz, for subsequent visualisation.

The default value is false.

2.7 Disentanglement

These keywords control the disentanglement routine of Ref. [2], i.e., the iterative minimisation of $\Omega_{\rm I}$. This routine will be activated if num_wann < num_bands.

2.7.1 real(kind=dp) :: dis_win_min

The lower bound of the outer energy window for the disentanglement procedure. Units are eV.

The default is the lowest eigenvalue in the system.

2.7.2 real(kind=dp) :: dis_win_max

The upper bound of the outer energy window for the disentanglement procedure. Units are eV.

The default is the highest eigenvalue in the given states (i.e., all states are included in the disentanglement procedure).

2.7.3 real(kind=dp) :: dis_froz_min

The lower bound of the inner energy window for the disentanglement procedure. Units are eV.

If dis_froz_max is given, then the default for dis_froz_min is dis_win_min.

2.7.4 real(kind=dp) :: dis_froz_max

The upper bound of the inner (frozen) energy window for the disentanglement procedure. If dis_froz_max is not specified, then there are no frozen states. Units are eV.

No default.

2.7.5 integer :: dis_num_iter

In the disentanglement procedure, the number of iterations used to extract the most connected subspace.

The default value is 200.

2.7.6 real(kind=dp) :: dis_mix_ratio

In the disentanglement procedure, the mixing parameter to use for convergence (see pages 4-5 of Ref. [2]). A value of 0.5 is a 'safe' choice. Using 1.0 (i.e., no mixing) often gives faster convergence, but may cause the minimisation of $\Omega_{\rm I}$ to be unstable in some cases.

Restriction: $0.0 < dis_mix_ratio \le 1.0$

The default value is 0.5

2.7.7 real(kind=dp) :: dis_conv_tol

In the disentanglement procedure, the minimisation of Ω_I is said to be converged if the fractional change in the gauge-invariant spread between successive iterations is less than dis_conv_tol for dis_conv_window iterations. Units are Å².

The default value is 1.0E-10

2.7.8 integer :: dis_conv_window

In the disentanglement procedure, the minimisation is said to be converged if the fractional change in the spread between successive iterations is less than dis_conv_tol for dis_conv_window iterations.

The default value of this parameter is 3.

2.8 Wannierise

Iterative minimisation of $\widetilde{\Omega}$, the non-gauge-invariant part of the spread functional.

2.8.1 integer :: num_iter

Total number of iterations in the minimisation procedure.

The default value is 100

2.8.2 integer :: num_cg_steps

Number of conjugate gradient steps to take before resetting to steepest descents.

The default value is 5

2.8.3 integer :: conv_window

If $conv_window > 1$, then the minimisation is said to be converged if the change in Ω over $conv_window$ successive iterations is less than $conv_tol$. Otherwise, the minimisation proceeds for num_iter iterations (default).

The default value is -1

2.8.4 real(kind=dp) :: conv_tol

If conv_window > 1, then this is the convergence tolerance on Ω , otherwise not used. Units are \mathring{A}^2 .

The default value is 1.0E-10

2.8.5 real(kind=dp) :: conv_noise_amp

If conv_noise_amp > 0, once convergence (as defined above) is achieved, some random noise f is added to the search direction, and the minimisation is continued until convergence is achieved once more. If the same value of Ω as before is arrived at, then the calculation is considered to be converged. If not, then random noise is added again and the procedure repeated up to a maximum of conv_noise_num times. conv_noise_amp is the amplitude of the random noise f that is added to the search direction: $0 < |f| < \text{conv_noise_amp}$. This functionality requires conv_window > 1. If conv_window is not specified, it is set to the value 5 by default.

If $conv_noise_amp \le 0$, then no noise is added (default).

The default value is -1.0

2.8.6 integer :: conv_noise_num

If conv_noise_amp > 0, then this is the number of times in the minimisation that random noise is added.

The default value is 3

2.8.7 integer :: num_dump_cycles

Write sufficient information to do a restart every num_dump_cycles iterations.

The default is 100

2.8.8 integer :: num_print_cycles

Write data to the master output file seedname.wout every num_print_cycles iterations.

The default is 1

2.8.9 logical :: write_r2mn

If write_r2mn = true, then the matrix elements $\langle m|r^2|n\rangle$ (where m and n refer to WF) are written to file seedname.r2mn at the end of the Wannierisation procedure.

The default value of this parameter is FALSE.

2.8.10 logical :: guiding_centres

Use guiding centres during the minimisation, in order to avoid local minima.

The default value is FALSE.

2.8.11 integer :: num_guide_cycles

If guiding_centres is set to true, then the guiding centres are used only every num_guide_cycles.

The default value is 1.

2.8.12 integer :: num_no_guide_iter

If guiding_centres is set to true, then the guiding centres are used only after num_no_guide_iter minimisation iterations have been completed.

The default value is 0.

2.8.13 real(kind=dp) :: trial_step

The value of the trial step for the parabolic fit in the line search minimisation used in the minimisation of the spread function. Cannot be used in conjunction with fixed_step (see below). If the minimisation procedure doesn't converge, try decreasing the value of trial_step to give a more accurate line search.

The default value is 2.0

2.8.14 real(kind=dp) :: fixed_step

If this is given a value in the input file, then a fixed step of length fixed_step (instead of a parabolic line search) is used at each iteration of the spread function minimisation. Cannot be used in conjunction with trial_step. This can be useful in cases in which minimisation with a line search fails to converge.

There is no default value.

2.8.15 logical :: use_bloch_phases

Determines whether to use the Bloch functions as the initial guess for the projections. Can only be used if disentanglement = false.

Th default value is false.

2.9 Post-Processing

Capabilities:

- Plot the WF
- Plot the interpolated band structure
- Plot the Fermi surface
- Output the Hamiltonian in the WF basis
- Transport calculation (quantum conductance and density of states)

2.9.1 logical :: wannier_plot

If wannier_plot = TRUE, then the code will write out the wannier functions in a super-cell wannier_plot_supercell times the original unit cell in a format specified by wannier_plot_format

The default value of this parameter is FALSE.

2.9.2 integer :: wannier_plot_supercell

Dimension of the 'super-unit-cell' in which the WF are plotted. The super-unit-cell is wannier_plot_supercell times the unit cell along all three linear dimensions (the 'home' unit cell is kept approximately in the middle).

The default value is 2.

2.9.3 character(len=20) :: wannier_plot_format

WF can be plotted in either XCrySDen (xsf) format or Gaussian cube format. The valid options for this parameter are:

```
- xcrysden (default)
```

cube

If wannier_plot_format=cube: Most visualisation programs (including XCrySDen) are only able to handle cube files for systems with orthogonal lattice vectors. wannier90 checks this on reading the seedname.win and reports an error if cube format has been selected and the lattice vectors are not mutually orthogonal.

2.9.4 integer :: wannier_plot_list(:)

A list of WF to plot. The WF numbered as per the **seedname.wout** file after the minimisation of the spread.

The default behaviour is to plot all WF. For example, to plot WF 4, 5, 6 and 10:

```
wannier_plot_list : 4-6, 10
```

2.9.5 character(len=20) :: wannier_plot_mode

Choose the mode in which to plot the WF, either as a molecule or as a crystal. Only relevant if wannier_plot_format=xcrysden.

The valid options for this parameter are:

```
- crystal (default)
```

- molecule

¹It's worth noting that the visualisation program VMD (http://www.ks.uiuc.edu/Research/vmd), for example, is able to deal with certain special cases of non-orthogonal lattice vectors. See http://www.ks.uiuc.edu/Research/vmd/plugins/molfile/cubeplugin.html. At present wannier90 only supports orthogonal lattice vectors for cube output.

2.9.6 real(kind=dp) :: wannier_plot_radius

If wannier_plot_format is cube, then wannier_plot_radius determines the cut-off radius of the WF for the purpose of plotting. wannier_plot_radius must be greater than 0. Units are Å.

The default value is 3.5.

2.9.7 logical :: bands_plot

If bands_plot = TRUE, then the code will calculate the band structure, through Wannier interpolation, along the path in k-space defined by bands_kpath using bands_num_points along the first section of the path and write out an output file in a format specified by bands_plot_format.

The default value is FALSE.

2.9.8 kpoint_path

Defines the path in k-space along which to calculate the bandstructure. Each line gives the start and end point (with labels) for a section of the path. Values are in fractional coordinates with respect to the primitive reciprocal lattice vectors.

begin kpoint_path

end kpoint_path

There is no default

2.9.9 integer :: bands_num_points

If bands_plot = TRUE, then the number of points along the first section of the bandstructure plot given by kpoint_path. Other sections will have the same density of k-points.

The default value for bands_num_points is 100.

2.9.10 character(len=20) :: bands_plot_format

Format in which to plot the interpolated band structure. The valid options for this parameter are:

```
- gnuplot (default)
```

xmgrace

2.9.11 character(len=20) :: bands_plot_mode

To interpolate the band structure along the k-point path, either use the Slater-Koster interpolation scheme or truncate the Hamiltonian matrix in the WF basis. Truncation criteria are provided by hr_cutoff and dist_cutoff.

The valid options for this parameter are:

```
- s-k (default)
```

- cut

2.9.12 integer :: bands_plot_dim

Dimension of the system. If bands_plot_dim <3 and bands_plot_mode = cut, lattice vector $\mathbf{R} = N_1 \mathbf{A}_1 + N_2 \mathbf{A}_2 + N_3 \mathbf{A}_3$, where $N_i = 0$ if \mathbf{A}_i is parallel to any of the confined directions specified by one_dim_axis, are exclusively used in the band structure interpolation.

The valid options for this parameter are:

```
- 3 (default)
```

-2

- 1

2.9.13 logical :: fermi_surface_plot

If fermi_surface_plot = TRUE, then the code will calculate, through Wannier interpolation, the eigenvalues on a regular grid with fermi_surface_num_points in each direction. The code will write a file in bxsf format which can be read by XCrySDen in order to plot the Fermi surface.

The default value is FALSE.

2.9.14 integer :: fermi_surface_num_points

If fermi_surface_plot = TRUE, then the number of divisions in the regular k-point grid used to calculate the Fermi surface.

The default value for fermi_surface_num_points is 50.

2.9.15 real(kind=dp) :: fermi_energy

The Fermi energy in eV. This parameter is written into the bxsf file.

The default value is 0.0

2.9.16 character(len=20) :: fermi_surface_plot_format

Format in which to plot the Fermi surface. The valid options for this parameter are:

```
- xcrysden (default)
```

2.9.17 logical :: hr_plot

If hr_plot = TRUE, then the Hamiltonian matrix in the WF basis will be written to a file seedname_hr.dat.

The default value is FALSE.

2.9.18 logical :: transport

If transport = TRUE, then the code will calculate quantum conductance and density of states.

The default value of this parameter is FALSE.

2.9.19 character(len=20) :: transport_mode

If transport_mode = bulk, quantum conductance and density of states are calculated for a perfectly-periodic one-dimensional system. In this case, the transport part can either use the Hamiltonian matrix in the WF basis generated by wannier90 or read a Hamiltonian matrix from an external file seedname_htB.dat.

If transport_mode = lcr, quantum conductance and density of states are calculated for a system where semi-infinite, left and right leads are connected through a central conductor region. In this case, the transport part will work independently from the wannierise procedure, and Hamiltonian matrices must be provided by the five external files: seedname_htL.dat, seedname_htL.dat, seedname_htC.dat, seedname_htC.dat,

The valid options for this parameter are:

```
- bulk (default)
```

- lcr

2.9.20 real(kind=dp) :: tran_win_min

The lower bound of the energy window for the transport calculation. Units are eV. The default value is -3.0.

2.9.21 real(kind=dp) :: tran_win_max

The upper bound of the energy window for the transport calculation. Units are eV.

The default value is 3.0.

2.9.22 real(kind=dp) :: tran_energy_step

Sampling interval of the energy values from tran_win_min to tran_win_max. Units are eV. The default value is 0.01.

2.9.23 real(kind=dp) :: fermi_energy

The Fermi energy in eV. The energy axis of the quantum conductance and density of states data are shifted rigidly by this amount.

The default value is 0.0

2.9.24 integer :: tran_num_bb

Size of a bulk Hamiltonian matrix.

The default value is 0.

2.9.25 integer :: tran_num_ll

Size of a left-lead Hamiltonian matrix.

The default value is 0.

2.9.26 integer :: tran_num_rr

Size of a right-lead Hamiltonian matrix.

The default value is 0.

2.9.27 integer :: tran_num_cc

Size of a conductor Hamiltonian matrix.

The default value is 0.

2.9.28 integer :: tran_num_lc

Number of columns in a left-lead_conductor Hamiltonian matrix. Number of rows is equal to tran_num_11.

The default value is 0.

2.9.29 integer :: tran_num_cr

Number of rows in a conductor_rigt-lead Hamiltonian matrix. Number of columns is equal to tran_num_rr.

The default value is 0.

2.9.30 integer :: tran_num_bandc

Half-bandwidth+1 of a band-diagonal conductor Hamiltonian matrix.

The default value is 0.

2.9.31 logical :: tran_write_ht

If tran_write_ht = TRUE, then the Hamiltonian matrix formatted for the transport calculation will be written to a file seedname_htB.dat.

The default value is FALSE.

2.9.32 logical :: tran_read_ht

If tran_write_ht = TRUE, then the Hamiltonian matrix formatted for the transport calculation will be read from a set of files described in the parameter transport_mode.

The default value is FALSE.

2.9.33 logical :: tran_use_same_lead

If tran_use_same_lead = TRUE, then the left and the right leads are the same. In this case, seedname_htR.dat is not required.

The default value is TRUE.

2.9.34 real(kind=dp) :: translation_centre_frac(3)

Centre of the unit cell to which the final Wannier centers are translated. Numbers are in fractional coordinates with respect to the lattice vectors.

The default value is (0.0,0.0,0.0).

2.9.35 real(kind=dp) :: hr_cutoff

The absolute value of the smallest matrix element of the Hamiltonian in the WF basis. If $h_{mn}(\mathbf{R}) > \text{hr_cutoff}$, then the matrix element $h_{mn}(\mathbf{R})$ is retained and used in the band structure interpolation (when bands_plot_mode = cut) or in the transport calculation. Otherwise it is deemed to be insignificant and is discarded. Units are eV.

The default value is 0.0.

2.9.36 real(kind=dp) :: dist_cutoff

The largest distance between WF for which the Hamiltonian matrix element is retained and used in the band interpolation (when bands_plot_mode = cut) or in the transport calculation. Units are Å.

The default value is 1000.0.

2.9.37 character(len=20) :: dist_cutoff_mode

Dimension in which the distance between WF is calculated. The vector connecting two WF may be projected to a line (one_dim) or a plane (two_dim). The size of the projected vector is calculated, and dist_cutoff is applied. When one_dim or two_dim is used, one_dim_axis must be given to specify extended or confined direction.

The valid options for this parameter are:

```
- three_dim (default)
```

— two_dim

- one_dim

2.9.38 character(len=20) :: one_dim_axis

Extended direction for a one-dimensional system. This direction must be parallel to one of the Cartesian axes. Confined direction in a two-dimensional system can be specified through this parameter.

The valid options for this parameter are:

— x

— у

- z

No default.

Chapter 3

Projections

3.1 Specification of projections in seedname.win

Here we describe the projection functions used to construct the initial guess $A_{mn}^{(\mathbf{k})}$ for the unitary transformations.

Each projection is associated with a site and an angular momentum state defining the projection function. Optionally, one may define, for each projection, the spatial orientation, the radial part, the diffusivity, and the volume over which real-space overlaps A_{mn} are calculated.

The code is able to

- 1. project onto s,p,d and f angular momentum states, plus the hybrids sp, sp 2 , sp 3 , sp 3 d, sp 3 d 2 .
- 2. control the radial part of the projection functions to allow higher angular momentum states, e.g., both 3s and 4s in silicon.

The atomic orbitals of the hydrogen atom provide a good basis to use for constructing the projection functions: analytical mathematical forms exist in terms of the good quantum numbers n, l and m; hybrid orbitals (sp, sp², sp³, sp³d etc.) can be constructed by simple linear combination $|\phi\rangle = \sum_{nlm} C_{nlm} |nlm\rangle$ for some coefficients C_{nlm} .

The angular functions that use as a basis for the projections are not the canonical spherical harmonics Y_{lm} of the hydrogenic Schrödinger equation but rather the real (in the sense of non-imaginary) states Θ_{lm_r} , obtained by a unitary transformation. For example, the canonical eigenstates associated with l=1, $m=\{-1,0,1\}$ are not the real p_x , p_y and p_z that we want. See Section 3.3 for our mathematical conventions regarding projection orbitals for different n, l and m_r .

We use the following format to specify projections in <seedname>.win:

Begin Projections
[units]

site:ang_mtm:zaxis:xaxis:radial:zona

End Projections

Notes:

units:

Optional. Either Ang or Bohr to specify whether the projection centres specified in this block (if given in Cartesian co-ordinates) are in units of Angstrom or Bohr, respectively. The default value is Ang.

site:

C, Al, etc. applies to all atoms of that type

f=0,0.50,0 – centre on (0.0,0.5,0.0) in fractional coordinates (crystallographic units) relative to the direct lattice vectors

c=0.0,0.805,0.0 – centre on (0.0,0.805,0.0) in Cartesian coordinates in units specified by the optional string units in the first line of the projections block (see above).

ang_mtm:

Angular momentum states may be specified by 1 and mr, or by the appropriate character string. See Tables 3.1 and 3.2. Examples:

```
1=2,mr=1 or dz2 - a single projection with l=2, m_{\Gamma}=1 (i.e., d_{z^2})
```

1=2,mr=1,4 or dz2,dx2-y2 - two functions: d_{z^2} and d_{xz}

1=-3 or $sp3 - four sp^3$ hybrids

Specific hybrid orbitals may be specified as follows:

1=-3, mr=1,3 or $sp3-1, sp3-3 - two specific <math>sp^3$ hybrids

Multiple states may be specified by separating with ';', e.g.,

sp3;1=0 or 1=-3;1=0 - four sp^3 hybrids and one s orbital

zaxis (optional):

z=1,1,1- set the z-axis to be in the (1,1,1) direction. Default is z=0,0,1

xaxis (optional):

x=1,1,1- set the x-axis to be in the (1,1,1) direction. Default is x=1,0,0

radial (optional):

r=2 – use a radial function with one node (ie second highest pseudostate with that angular momentum). Default is r=1. Radial functions associated with different values of r should be orthogonal to each other.

```
zona (optional):
```

zona=2.0 – the value of $\frac{Z}{a}$ for the radial part of the atomic orbital (controls the diffusivity of the radial function). Units always in reciprocal Angstrom. Default is zona=1.0.

Examples

1. CuO, s,p and d on all Cu; sp³ hybrids on O:

```
Cu:1=0;1=1;1=2
```

2. A single projection onto a p_z orbital orientated in the (1,1,1) direction:

```
c=0,0,0:l=1,mr=1:z=1,1,1 or c=0,0,0:pz:z=1,1,1
```

3. Project onto s, p and d (with no radial nodes), and s and p (with one radial node) in silicon:

```
Si:1=0;1=1;1=2
Si:1=0;1=1:r=2
```

3.2 Short-Cuts

3.2.1 Random projections

It is possible to specify the projections, for example, as follows:

Begin Projections random C:sp3
End Projections

in which case wannier90 uses four sp³ orbitals centred on each C atom and then chooses the appropriate number of randomly-centred s-type Gaussian functions for the remaining projection functions. If the block only consists of the string random and no specific projection centres are given, then all of the projection centres are chosen randomly.

3.2.2 Bloch phases

Setting use_bloch_phases = true in the input file absolves the user of the need to specify explicit projections. In this case, the Bloch wave-functions are used as the projection orbitals, namely $A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}} | \psi_{n\mathbf{k}} \rangle = \delta_{mn}$.

3.3 Orbital Definitions

The angular functions $\Theta_{lm_r}(\theta,\varphi)$ associated with particular values of l and m_r are given in Tables 3.1 and 3.2.

The radial functions $R_r(r)$ associated with different values of r should be orthogonal. One choice would be to take the set of solutions to the radial part of the hydrogenic Schrödinger equation for l=0, i.e., the radial parts of the 1s, 2s, 3s... orbitals, which are given in Table 3.3.

l	$m_{ m r}$	Name	$\Theta_{lm_{ m r}}(heta,arphi)$
0	1	s	$\frac{1}{\sqrt{4\pi}}$
1	1	pz	$\sqrt{\frac{3}{4\pi}}\cos\theta$
1	2	px	$\sqrt{\frac{3}{4\pi}}\sin\theta\cos\varphi$
1	3	ру	$\sqrt{rac{3}{4\pi}}\sin\theta\sin\varphi$
2	1	dz2	$\sqrt{\frac{5}{16\pi}}(3\cos^2\theta - 1)$
2	2	dxz	$\sqrt{\frac{15}{4\pi}}\sin\theta\cos\theta\cos\varphi$
2	3	dyz	$\sqrt{\frac{15}{4\pi}}\sin\theta\cos\theta\sin\varphi$
2	4	dx2-y2	$\sqrt{\frac{15}{16\pi}}\sin^2\theta\cos2\varphi$
2	5	dxy	$\sqrt{\frac{15}{16\pi}}\sin^2\theta\sin2\varphi$
3	1	fz3	$\frac{\sqrt{7}}{4\sqrt{\pi}}(5\cos^3\theta - 3\cos\theta)$
3	2	fxz2	$\frac{\sqrt{21}}{4\sqrt{2\pi}} (5\cos^2\theta - 1)\sin\theta\cos\varphi$
3	3	fyz2	$\frac{\sqrt{21}}{4\sqrt{2\pi}} (5\cos^2\theta - 1)\sin\theta\sin\varphi$
3	4	fz(x2-y2)	$\frac{\sqrt{105}}{4\sqrt{\pi}}\sin^2\theta\cos\theta\cos2\varphi$
3	5	fxyz	$\frac{\sqrt{105}}{4\sqrt{\pi}}\sin^2\theta\cos\theta\sin2\varphi$
3	6	fx(x2-3y2)	$\frac{\sqrt{35}}{4\sqrt{2\pi}}\sin^3\theta(\cos^2\varphi - 3\sin^2\varphi)\cos\varphi$
3	7	fy(3x2-y2)	$\frac{\sqrt{35}}{4\sqrt{2\pi}}\sin^3\theta(3\cos^2\varphi-\sin^2\varphi)\sin\varphi$

Table 3.1: Angular functions $\Theta_{lm_r}(\theta,\varphi)$ associated with particular values of l and m_r for $l \geq 0$.

l	$m_{ m r}$	Name	$\Theta_{lm_{ m r}}(heta,arphi)$
-1	1	sp-1	$\frac{1}{\sqrt{2}}$ s $+\frac{1}{\sqrt{2}}$ px
-1	2	sp-2	$\frac{1}{\sqrt{2}}\mathbf{s} - \frac{1}{\sqrt{2}}\mathbf{p}\mathbf{x}$
-2	1	sp2-1	$\frac{1}{\sqrt{3}}\mathbf{s} - \frac{1}{\sqrt{6}}\mathbf{p}\mathbf{x} + \frac{1}{\sqrt{2}}\mathbf{p}\mathbf{y}$
-2	2	sp2-2	$\frac{1}{\sqrt{3}}$ s $-\frac{1}{\sqrt{6}}$ px $-\frac{1}{\sqrt{2}}$ py
-2	3	sp2-3	$\frac{1}{\sqrt{3}}$ s $+\frac{2}{\sqrt{6}}$ px
-3	1	sp3-1	$\frac{1}{2}(s + px + py + pz)$
-3	2	sp3-2	$\frac{1}{2}(\mathtt{s}+\mathtt{px}-\mathtt{py}-\mathtt{pz})$
-3	3	sp3-3	$\frac{1}{2}(\mathtt{s}-\mathtt{px}+\mathtt{py}-\mathtt{pz})$
-3	4	sp3-4	$\frac{1}{2}(\mathtt{s}-\mathtt{px}-\mathtt{py}+\mathtt{pz})$
-4	1	sp3d-1	$\frac{1}{\sqrt{3}}s - \frac{1}{\sqrt{6}}px + \frac{1}{\sqrt{2}}py$
-4	2	sp3d-2	$\frac{1}{\sqrt{3}}$ s $-\frac{1}{\sqrt{6}}$ px $-\frac{1}{\sqrt{2}}$ py
-4	3	sp3d-3	$\frac{1}{\sqrt{3}}$ s $+\frac{2}{\sqrt{6}}$ px
-4	4	sp3d-4	$rac{1}{\sqrt{2}}$ pz $+rac{1}{\sqrt{2}}$ dz2
-4	5	sp3d-5	$-rac{1}{\sqrt{2}}$ pz $+rac{1}{\sqrt{2}}$ dz2
-5	1	sp3d2-1	$\frac{1}{\sqrt{6}}s - \frac{1}{\sqrt{2}}px - \frac{1}{\sqrt{12}}dz^2 + \frac{1}{2}dx^2y^2$
-5	2	sp3d2-2	$\frac{1}{\sqrt{6}}s + \frac{1}{\sqrt{2}}px - \frac{1}{\sqrt{12}}dz^2 + \frac{1}{2}dx^2y^2$
-5	3	sp3d2-3	$\frac{1}{\sqrt{6}}s - \frac{1}{\sqrt{2}}py - \frac{1}{\sqrt{12}}dz^2 - \frac{1}{2}dx^2y^2$
-5	4	sp3d2-4	$\frac{1}{\sqrt{6}}s + \frac{1}{\sqrt{2}}py - \frac{1}{\sqrt{12}}dz^2 - \frac{1}{2}dx^2y^2$
-5	5	sp3d2-5	$\frac{1}{\sqrt{6}}s - \frac{1}{\sqrt{2}}pz + \frac{1}{\sqrt{3}}dz2$
-5	6	sp3d2-6	$\frac{1}{\sqrt{6}}s + \frac{1}{\sqrt{2}}pz + \frac{1}{\sqrt{3}}dz2$

Table 3.2: Angular functions $\Theta_{lm_r}(\theta,\varphi)$ associated with particular values of l and m_r for l < 0, in terms of the orbitals defined in Table 3.1.

r	$R_{ m r}(r)$
1	$2\alpha^{3/2}\exp(-\alpha r)$
2	$\frac{1}{2\sqrt{2}}\alpha^{3/2}(2-\alpha r)\exp(-\alpha r/2)$
3	$\sqrt{\frac{4}{27}}\alpha^{3/2}(1 - 2\alpha r/3 + 2\alpha^2 r^2/27)\exp(-\alpha r/3)$

Table 3.3: One possible choice for the radial functions $R_r(r)$ associated with different values of r: the set of solutions to the radial part of the hydrogenic Schrödinger equation for l=0, i.e., the radial parts of the 1s, 2s, 3s... orbitals, where $\alpha=Z/a=$ zona.

Code Overview

wannier90 can operate in two modes:

- 1. Post-processing mode: read in the overlaps and projections from file as computed inside a first-principles code. We expect this to be the most common route to using wannier90, and is described in Ch. 5;
- 2. Library mode: as a set of library routines to be called from within a first-principles code that passes the overlaps and projections to the wannier90 library routines and in return gets the unitary transformation corresponding to MLWF. This route should be used if the MLWF are needed within the first-principles code, for example in post-LDA methods such as LDA+U or SIC, and is described in Ch. 6.

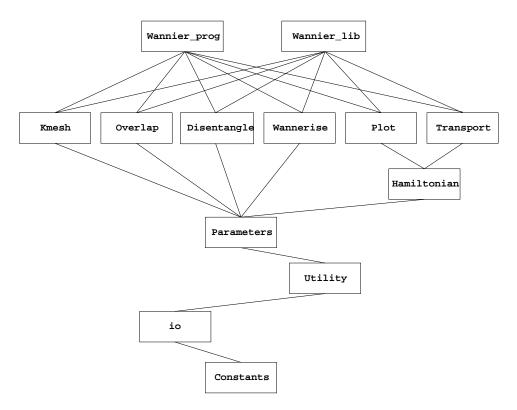


Figure 4.1: Schematic overview of the module structure of wannier90. Modules may only use data and subroutines from lower modules.

wannier90 as a post-processing tool

This is a description of how to use wannier90 as a post-processing tool.

The code must be run twice. On the first pass either the logical keyword postproc_setup must be set to .true. in the input file seedname.win or the code must be run with the command line option -pp. Running the code then generates the file seedname.nnkp which provides the information required to construct the $M_{mn}^{(\mathbf{k},\mathbf{b})}$ overlaps (Ref. [1], Eq. (25)) and $A_{mn}^{(\mathbf{k})}$ (Ref. [1], Eq. (62); Ref. [2], Eq. (22)).

Once the overlaps and projection have been computed and written to files seedname.mmn and seedname.amn, respectively, set postproc_setup to .false. and run the code. Output is written to the file seedname.wout.

5.1 seedname.nnkp file

OUTPUT, if postproc_setup = .true.

The file seedname.nnkp provides the information needed to determine the required overlap elements $M_{mn}^{(\mathbf{k},\mathbf{b})}$ and projections $A_{mn}^{(\mathbf{k})}$. It is written automatically when the code is invoked with the -pp command-line option (or when postproc_setup=.true. in seedname.win. There should be no need for the user to edit this file.

Much of the information in seedname.nnkp is arranged in blocks delimited by the strings begin block_name...end block_name, as described below.

5.1.1 Keywords

The first line of the file is a user comment, e.g., the date and time:

File written on 12Feb2006 at 15:13:12

The only logical keyword is calc_only_A, eg,

calc_only_A : F

5.1.2 Real_lattice block

```
begin real_lattice
2.250000 0.000000 0.000000
0.000000 2.250000 0.000000
0.000000 0.000000 2.250000
end real_lattice
```

The real lattice vectors in units of Angstrom.

5.1.3 Recip_lattice block

```
begin recip_lattice
2.792527 0.000000 0.000000
0.000000 2.792527 0.000000
0.000000 0.000000 2.792527
end recip_lattice
```

The reciprocal lattice vectors in units of inverse Angstrom.

5.1.4 Kpoints block

```
begin kpoints
8
0.00000 0.00000 0.00000
0.00000 0.50000 0.00000
.
.
.
0.50000 0.50000 0.50000
end kpoints
```

The first line in the block is the total number of k-points num_kpts. The subsequent num_kpts lines specify the k-points in crystallographic co-ordinates relative to the reciprocal lattice vectors.

5.1.5 Projections block

```
begin projections
  n_proj
  centre l mr r
   z-axis x-axis zona
  centre l mr r
```

```
z-axis x-axis zona
.
.
end projections
```

Notes:

n_proj: integer; the number of projection centres, equal to the number of MLWF num_wann.

centre: three real numbers; projection function centre in crystallographic co-ordinates relative to the direct lattice vectors.

1 mr r: three integers; l and m_r specify the angular part $\Theta_{lm_r}(\theta,\varphi)$, and r specifies the radial part $R_r(r)$ of the projection function (see Tables 3.1, 3.2 and 3.3).

z-axis: three real numbers; default is 0.0 0.0 1.0; defines the axis from which the polar angle θ in spherical polar coordinates is measured.

x-axis: three real numbers; must be orthogonal to z-axis; default is 1.0 0.0 0.0 or a vector perpendicular to z-axis if z-axis is given; defines the axis from with the azimuthal angle φ in spherical polar coordinates is measured.

zona: real number; the value of $\frac{Z}{a}$ associated with the radial part of the atomic orbital. Units are in reciprocal Angstrom.

5.1.6 nnkpts block

```
begin nnkpts
    10
    1    2    0    0    0
    .
    .
end nnkpts
```

First line: nntot, the number of nearest neighbours belonging to each k-point of the Monkhorst-Pack mesh

Subsequent lines: nntot×num_kpts lines, ie, nntot lines of data for each k-point of the mesh.

Each line of consists of 5 integers. The first is the k-point number nkp. The second to the fifth specify it's nearest neighbours k+b: the second integer points to the k-point that is the periodic image of the k+b that we want; the last three integers give the G-vector, in reciprocal lattice units, that brings the k-point specified by the second integer (which is in the first BZ) to the actual k+b that we need.

5.1.7 exclude_bands block

begin exclude_bands

```
8
1
2
.
end exclude_bands
```

To exclude bands (independent of k-point) from the calculation of the overlap and projection matricies, for example to ignore shallow-core states. The first line is the number of states to exclude, the following lines give the states for be excluded.

5.1.8 An example of projections

As a concrete example: one wishes to have a set of four sp^3 projection orbitals on, say, a carbon atom at (0.5,0.5,0.5) in fractional co-ordinates relative to the direct lattice vectors. In this case $\mathtt{seedname.win}$ will contain the following lines:

```
begin projections
C:1=-1
end projections
```

and seedname.nnkp, generated on the first pass of wannier90 (with postproc_setup=T), will contain:

```
begin projections
   0.50000
              0.50000
                         0.50000
                                            1
                                    -1
                                         1
     0.000
           0.000 1.000
                            1.000
                                  0.000 0.000
                                                  2.00
                         0.50000
   0.50000
              0.50000
                                     -1
                                         2
                                            1
     0.000
            0.000
                   1.000
                           1.000
                                  0.000 0.000
                                                  2.00
   0.50000
              0.50000
                         0.50000
                                     -1
                                         3
     0.000
            0.000 1.000
                           1.000
                                  0.000
                                         0.000
                                                  2.00
   0.50000
              0.50000
                         0.50000
                                     -1
                                         4
     0.000 0.000 1.000
                           1.000 0.000 0.000
                                                  2.00
end projections
```

where the first line tells us that in total four projections are specified, and the subsquent lines provide the projection centre, the angular and radial parts of the orbital (see Section 3.3 for definitions), the z and x axes, and the diffusivity and cut-off radius for the projection orbital.

PWSCF, or any other *ab initio* electronic structure code, then reads **seedname.nnkp** file, calculates the projections and writes them to **seedname.amn**.

5.2 seedname.mmn file

INPUT.

The file seedname.mmn contains the overlaps $M_{mn}^{(\mathbf{k},\mathbf{b})}$

First line: a user comment, e.g., the date and time

Second line: 3 integers: num_bands, num_kpts, nntot

Then: num_kpts × nntot blocks of data:

First line of each block: 5 integers. The first specifies the \mathbf{k} (i.e., gives the ordinal corresponding to its position in the list of k-points in seedname.win). The 2nd to 5th integers specify $\mathbf{k} + \mathbf{b}$. The 2nd integer, in particular, points to the k-point on the list that is a periodic image of $\mathbf{k} + \mathbf{b}$, and in particular is the image that is actually mentioned in the list. The last three integers specify the \mathbf{G} vector, in reciprocal lattice units, that brings the k-point specified by the fourth integer, and that thus lives inside the first BZ zone, to the actual $\mathbf{k} + \mathbf{b}$ that we need.

Subsequent num_bands × num_bands lines of each block: two real numbers per line. These are the real and imaginary parts, respectively, of the actual scalar product $M_{mn}^{(\mathbf{k},\mathbf{b})}$ for $m,n\in[1,\text{num_bands}]$. The order of these elements is such that the first index m is fastest.

5.3 seedname.amn file

INPUT.

The file seedname.amn contains the projection $A_{mn}^{(\mathbf{k})}$.

First line: a user comment, e.g., the date and time

Second line: 3 integers: num_bands, num_kpts, num_wann

Subsequently num_bands × num_wann × num_kpts lines: 3 integers and 2 real numbers on each line. The first two integers are the band indices m and n. The third integer specifies the k by giving the ordinal corresponding to its position in the list of k-points in seedname.win. The real numbers are the real and imaginary parts, respectively, of the actual $A_{mn}^{(k)}$.

5.4 seedname.eig file

INPUT.

Required if any of disentanglement, plot_bands, plot_fermi_surface or hr_plot are .true.

The file seedname.eig contains the Kohn-Sham eigenvalues $\varepsilon_{n\mathbf{k}}$ (in eV) at each point in the Monkhorst-Pack mesh.

Each line consist of two integers and a real number. The first integer is the band index, the second integer gives the ordinal corresponding to the k-point in the list of k-points in seedname.win, and the real number is the eigenvalue.

E.g.,

1	1	-6.43858831271328
2	1	19.3977795287297
3	1	19.3977795287297
4	1	19.3977795287298

5.5 Interface with PWSCF

There is a seamless interface between wannier90 and PWSCF, a plane-wave DFT code that comes as part of the quantum-espresso package (see www.quantum-espresso.org or www.pwscf.org). At the time of writing, interfaces to other electronic structure codes are in progress, e.g., CASTEP (www.castep.org), ABINIT (www.abinit.org) and FLEUR (www.fleur.de). But, for the time being, you will need to download and compile PWSCF (i.e., the pw.x code) and the post-processing interface pw2wannier90.x. Please refer to the documentation that comes with the quantum-espresso distribution for instructions.

- 1. Run 'scf'/'nscf' calculation(s) with pw
- 2. Run wannier90 with postproc_setup = .true. to generate seedname.nnkp
- 3. Run pw2wannier90. First it reads an input file, e.g., seedname.pw2wan, which defines prefix and outdir for the underlying 'scf' calculation, as well as the name of the file seedname.nnkp, and does a consistency check between the direct and reciprocal lattice vectors read from seedname.nnkp and those defined in the files specified by prefix. pw2wannier90 generates seedname.mmn, seedname.amn and seedname.eig
- 4. Run wannier90 with postproc_setup = .false. to disentangle bands (if required), localise MLWF, and use MLWF for plotting, bandstructures, Fermi surfaces etc.

Examples of how the interface with PWSCF works are given in the wannier90 Tutorial.

5.5.1 seedname.pw2wan

A number of keywords may be specified in the pw2wannier90 input file:

- outdir Location to write output files. Default is './'
- prefix Prefix for the PWSCF calculation. Default is ','
- seedname Seedname for the wannier90 calculation. Default is 'wannier'

- spin_component Spin component. Takes values 'up', 'down' or 'none' (default).
- wan_mode Either 'standalone' (default) or 'library'
- write_unk Set to .true. to write the periodic part of the Bloch functions for plotting in wannier90. Default is .false.
- reduce_unk Set to .true. to reduce file-size (and resolution) of Bloch functions by a factor of 8. Default is .false. (only relevant if write_unk=.true.)¹
- wvfn_formatted Set to .true. to write formatted wavefunctions. Default is .false. (only relevant if write_unk=.true.)
- write_amn Set to .false. if $A_{mn}^{(k)}$ not required. Default is .true.
- ullet write_mmn Set to .false. if $M_{mn}^{(\mathbf{k},\mathbf{b})}$ not required. Default is .true.

For examples of use, refer to the wannier90 Tutorial.

¹Note that there is a small bug with this feature in v3.2 (and subsequent patches) of quantum-espresso. Please use a later version (if available) or the CVS version of pw2wannier90.f90, which has been fixed.

wannier90 as a library

This is a description of the interface between any external program and the wannier code. There are two subroutines: wannier_setup and wannier_run. Calling wannier_setup will return information required to construct the $M_{mn}^{(\mathbf{k},\mathbf{b})}$ overlaps (Ref. [1], Eq. (25)) and $A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}} | g_n \rangle$ projections (Ref. [1], Eq. (62); Ref. [2], Eq. (22)). Once the overlaps and projection have been computed, calling wannier_run activates the minimisation and plotting routines in wannier90.

6.1 Subroutines

6.1.1 wannier_setup

- character(len=*), intent(in) :: seed_name
 The seedname of the current calculation.
- integer, dimension(3), intent(in) :: mp_grid The dimensions of the Monkhorst-Pack k-point grid.
- integer, intent(in) :: num_kpts

 The number of k-points on the Monkhorst-Pack grid.
- real(kind=dp), dimension(3,3), intent(in) :: real_lattice The lattice vectors in Cartesian co-ordinates in units of Angstrom.
- real(kind=dp), dimension(3,3), intent(in) :: recip_lattice

 The reciprocal lattice vectors in Cartesian co-ordinates in units of reciprocal Angstrom.

- real(kind=dp), dimension(3,num_kpts), intent(in) :: kpt_latt

 The positions of the k-points in fractional co-ordinates relative to the reciprocal lattice vectors.
- integer, intent(in) :: num_bands_tot

 The total number of bands in the first-principles calculation (note: including semi-core states).
- integer, intent(in) :: num_atoms

 The total number of atoms in the system.
- character(len=20), dimension(num_atoms), intent(in) :: atom_symbols The elemental symbols of the atoms.
- real(kind=dp), dimension(3,num_atoms), intent(in) :: atoms_cart The positions of the atoms in Cartesian co-ordinates in Angstrom.
- logical, intent(in) :: gamma_only Set to .true. if the underlying electronic structure calculation has been performed with only Γ -point sampling and, hence, if the Bloch eigenstates that are used to construct $A_{mn}^{(\mathbf{k})}$ and $M_{mn}^{(\mathbf{k},\mathbf{b})}$ are real.
- integer, intent(out) :: nntot
 The total number of nearest neighbours for each k-point.
- integer, dimension(num_kpts,num_nnmax), intent(out) :: nnlist The list of nearest neighbours for each k-point.
- integer, dimension (3, num_kpts, num_nnmax), intent (out) :: nncell The vector, in fractional reciprocal lattice co-ordinates, that brings the nn^{th} nearest neighbour of k-point nkp to its periodic image that is needed for computing the overlap $M_{mn}^{(k,b)}$.
- integer, intent(out) :: num_bands

 The number of bands in the first-principles calculation used to form the overlap matricies
 (note: excluding eg. semi-core states).
- integer, intent(out) :: num_wann
 The number of MLWF to be extracted.
- real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_site Projection function centre in crystallographic co-ordinates relative to the direct lattice vectors.
- integer, dimension(num_bands_tot), intent(out) :: proj_1 l specifies the angular part $\Theta_{lm_r}(\theta,\varphi)$ of the projection function (see Tables 3.1, 3.2 and 3.3).
- integer, dimension(num_bands_tot), intent(out) :: proj_m $m_{\rm r}$ specifies the angular part $\Theta_{lm_{\rm r}}(\theta,\varphi)$, of the projection function (see Tables 3.1, 3.2 and 3.3).

- integer, dimension(num_bands_tot), intent(out) :: proj_radial r specifies the radial part $R_r(r)$ of the projection function (see Tables 3.1, 3.2 and 3.3).
- real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_z
 Defines the axis from which the polar angle θ in spherical polar coordinates is measured.
 Default is 0.0 0.0 1.0.
- real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_x
 Must be orthogonal to z-axis; default is 1.0 0.0 0.0 or a vector perpendicular to proj_z if proj_z is given; defines the axis from with the azimuthal angle φ in spherical polar coordinates is measured.
- real(kind=dp), dimension(num_bands_tot), intent(out) :: proj_zona The value of $\frac{Z}{a}$ associated with the radial part of the atomic orbital. Units are in reciprocal Angstrom.
- integer, dimension(num_bands_tot), intent(out) :: exclude_bands Kpoints independant list of bands to exclude from the calculation of the MLWF (e.g., semi-core states).

Conditions:

```
\star num_kpts = mp_grid(1) \times mp_grid(2) \times mp_grid(3).
```

 \star num_nnmax = 12

This subroutine returns the information required to determine the required overlap elements $M_{mn}^{(\mathbf{k},\mathbf{b})}$ and projections $A_{mn}^{(\mathbf{k})}$, i.e., M_matrix and A_matrix, described in Section 6.1.2.

For the avoidance of doubt, real_lattice(1,2) is the y-component of the first lattice vector \mathbf{A}_1 , etc.

The list of nearest neighbours of a particular k-point nkp is given by nnlist(nkp,1:nntot).

Additionally, the parameters num_shells and shell_list may be specified in the wannier90 input file.

6.1.2 wannier_run

• character(len=*), intent(in) :: seed_name
The seedname of the current calculation.

- integer, dimension(3), intent(in) :: mp_grid The dimensions of the Monkhorst-Pack k-point grid.
- integer, intent(in) :: num_kpts

 The number of k-points on the Monkhorst-Pack grid.
- real(kind=dp), dimension(3,3), intent(in) :: real_lattice The lattice vectors in Cartesian co-ordinates in units of Angstrom.
- real(kind=dp), dimension(3,3), intent(in) :: recip_lattice

 The reciprical lattice vectors in Cartesian co-ordinates in units of inverse Angstrom.
- real(kind=dp), dimension(3,num_kpts), intent(in) :: kpt_latt

 The positions of the k-points in fractional co-ordinates relative to the reciprocal lattice vectors.
- integer, intent(in) :: num_bands
 The total number of bands to be processed.
- integer, intent(in) :: num_wann
 The number of MLWF to be extracted.
- integer, intent(in) :: nntot
 The number of nearest neighbours for each k-point.
- integer, intent(in) :: num_atoms

 The total number of atoms in the system.
- character(len=20), dimension(num_atoms), intent(in) :: atom_symbols The elemental symbols of the atoms.
- real(kind=dp), dimension(3,num_atoms), intent(in) :: atoms_cart The positions of the atoms in Cartesian co-ordinates in Angstrom.
- logical, intent(in) :: gamma_only Set to .true. if the underlying electronic structure calculation has been performed with only Γ -point sampling and, hence, if the Bloch eigenstates that are used to construct $A_{mn}^{(\mathbf{k})}$ and $M_{mn}^{(\mathbf{k},\mathbf{b})}$ are real.
- complex(kind=dp), dimension(num_bands,num_bands,nntot,num_kpts), intent(in) :: M_matrix

 The matrices of overlaps between neighbouring periodic parts of the Bloch eigenstates at each k-point, $M_{mn}^{((\mathbf{k},\mathbf{b}))}$ (Ref. [1], Eq. (25)).
- complex(kind=dp), dimension(num_bands,num_wann,num_kpts), intent(in) :: A_matrix

 The matrices describing the projection of num_wann trial orbitals on num_bands Bloch states at each k-point, $A_{mn}^{(k)}$ (Ref. [1], Eq. (62); Ref. [2], Eq. (22)).
- real(kind=dp), dimension(num_bands,num_kpts), intent(in) :: eigenvalues The eigenvalues $\varepsilon_{n\mathbf{k}}$ corresponding to the eigenstates, in eV.

- logical, dimension(num_bands,num_kpts), intent(out) :: lwindow
 The element lwindow(nband,nkpt) is .true. if the band nband lies within the outer
 energy window at kpoint nkpt.
- real(kind=dp), dimension(3,num_wann), intent(out) :: wann_centres
 The centres of the MLWF in Cartesian co-ordinates in Angstrom.
- real(kind=dp), dimension(num_wann), intent(out) :: wann_spreads The spread of each MLWF in \mathring{A}^2 .
- real(kind=dp), dimension(3), intent(out) :: spread The values of Ω , Ω_I and $\tilde{\Omega}$ (Ref. [1], Eq. (13)).

Conditions:

- \star num_wann \leq num_bands
- * $num_kpts = mp_grid(1) \times mp_grid(2) \times mp_grid(3)$.

If num_bands = num_wann then U_matrix_opt is the identity matrix and lwindow=.true.

For the avoidance of doubt, real_lattice(1,2) is the y-component of the first lattice vector \mathbf{A}_1 , etc.

```
\begin{array}{lcl} \texttt{M\_matrix(m,n,nkp,nn)} &=& \langle u_{m\mathbf{k}} | u_{n\mathbf{k}+\mathbf{b}} \rangle \\ \\ \texttt{A\_matrix(m,n,nkp)} &=& \langle \psi_{m\mathbf{k}} | g_n \rangle \\ \\ \texttt{eigenvalues(n,nkp)} &=& \varepsilon_{n\mathbf{k}} \end{array}
```

where

```
\begin{array}{lcl} \mathbf{k} & = & \texttt{kpt\_latt(1:3,nkp)} \\ \mathbf{k} + \mathbf{b} & = & \texttt{kpt\_latt(1:3,nnlist(nkp,nn))} + \texttt{nncell(1:3,nkp,nn)} \end{array}
```

and $\{|g_n\rangle\}$ are a set of initial trial orbitals. These are typically atom or bond-centred Gaussians that are modulated by appropriate spherical harmonics.

Additional parameters should be specified in the wannier90 input file.

Files

7.1 seedname.win

INPUT. The master input file; contains the specification of the system and any parameters for the run. For a description of input parameters, see Chapter 2; for examples, see Section 9.1 and the wannier90 Tutorial.

7.1.1 Units

The following are the dimensional quantities that are specified in the master input file:

- Direct lattice vectors
- Positions (of atomic or projection) centres in real space
- Energy windows
- Positions of k-points in reciprocal space
- Convergence thresholds for the minimisation of Ω
- zona (see Section 3.1)
- wannier_plot_cube: cut-off radius for plotting WF in Gaussian cube format

Notes:

- The units (either ang (default) or bohr) in which the lattice vectors, atomic positions or projection centres are given can be set in the first line of the blocks unit_cell_cart, atoms_cart and projections, respectively, in seedname.win.
- Energy is always in eV.
- \bullet Convergence thresholds are always in \mathring{A}^2

- Positions of k-points are always in crystallographic coordinates relative to the reciprocal lattice vectors.
- zona is always in reciprocal Angstrom (Å⁻¹)
- The keyword length_unit may be set to ang (default) or bohr, in order to set the units in which the quantities in the output file seedname.wout are written.
- wannier_plot_radius is in Angstrom

The reciprocal lattice vectors $\{\mathbf{B}_1, \mathbf{B}_2, \mathbf{B}_3\}$ are defined in terms of the direct lattice vectors $\{\mathbf{A}_1, \mathbf{A}_2, \mathbf{A}_3\}$ by the equation

$$\mathbf{B}_1 = \frac{2\pi}{\Omega} \mathbf{A}_2 \times \mathbf{A}_3 \quad \text{etc.}, \tag{7.1}$$

where the cell volume is $V = \mathbf{A}_1 \cdot (\mathbf{A}_2 \times \mathbf{A}_3)$.

7.2 seedname.mmn

INPUT. Written by the underlying electronic structure code. See Chapter 5 for details.

7.3 seedname.amn

INPUT. Written by the underlying electronic structure code. See Chapter 5 for details.

7.4 seedname.eig

INPUT. Written by the underlying electronic structure code. See Chapter 5 for details.

7.5 seedname.nnkp

OUTPUT. Written by wannier90 when postproc_setup=.TRUE. (or, alternatively, when wannier90 is run with the -pp command-line option). See Chapter 5 for details.

7.6 seedname.wout

OUTPUT. The master output file. Here we give a description of the main features of the output. The verbosity of the output is controlled by the input parameter iprint. The higher the value, the more detail is given in the output file. The default value is 1, which prints minimal information.

7.6.1 Header

The header provides some basic information about wannier90, the authors, and the execution time of the current run.

```
WANNIER90

Welcome to the Maximally-Localized
Generalized Wannier Functions code
http://www.wannier.org

Authors:
Arash A. Mostofi (Imperial College London)
Jonathan R. Yates (University of Cambridge)
Young-Su Lee (KIST, S. Korea)

Copyright (c) 1997-2007 J. Yates, A. Mostofi,
Y.-S. Lee, N. Marzari, I. Souza, D. Vanderbilt

Release: 1.1 1st Sep 2007

Execution started on 10Sep2007 at 12:46:57
```

7.6.2 System information

This part of the output file presents information that wannier90 has read or inferred from the master input file seedname.win. This includes real and reciprocal lattice vectors, atomic positions, k-points, parameters for job control, disentanglement, localisation and plotting.

SYSTEM

Lattice Vectors (Ang)

				·0/		
	a_1	3.938486	0.00000	0.000	000	
	a_2	0.000000	3.93848	6 0.0000	000	
	a_3	0.000000	0.00000	0 3.9384	186	
	Unit	Cell Volume:	61.0	9251 (Ang	g^3)	
		Reciprocal-Spa	ace Vecto	rs (Ang^-	1)	
	b_1	1.595330	0.00000	0.000	000	
	b_2	0.000000	1.59533	0.000	000	
	b_3	0.000000	0.00000	0 1.595	330	
Site	Fractio	nal Coordinate		Cartesia	n Coordina	te (Ang)
		.00000 0.0000				
		.50000 0.5000				
		K-POII	NT GRID			
	Grid size	= 4 x 4 x 4	Т^+	al nointe	= 64	
	GIIU SIZE		100	ar hornes	- 04	
		,				

*-	MAIN			*
	Number of Wannier Functions	:	9	- 1
	Number of input Bloch states	:	9	- 1
	Output verbosity (1=low, 5=high)	:	1	- 1
	Length Unit	:	Ang	- 1
	Post-processing setup (write *.nnkp)	:	F	- 1
		•		

7.6.3 Nearest-neighbour k-points

This part of the output files provides information on the b-vectors and weights chosen to satisfy the condition of Eq. 2.1.



Distance to Nearest-Neighbour Shells				
Shell	Distance (Ang^-1)	Multiplicity		
1 2	0.398833 0.564034	6 12		
++ The b-vectors are chosen automatically The following shells are used: 1				
	Shell # Nearest-Neigh	bours		
	1 6			
Completeness relation	on is fully satisfied [Eq.	(B1), PRB 56, 12847 (1997)]		

7.6.4 Disentanglement

Then (if required) comes the part where $\Omega_{\rm I}$ is minimised to disentangle the optimally-connected subspace of states for the localisation procedure in the next step.

First, a summary of the energy windows that are being used is given:

**					
+					+
		Energy	Wind	lows	1
1					1
1	Outer:	2.81739	to	38.00000	(eV)
1	Inner:	2.81739	to	13.00000	(eV)
+					+

Then, each step of the iterative minimisation of $\Omega_{\rm I}$ is reported.

Extraction of optimally-connected subspace

+						+< DIS
	Iter	Omega_I(i-1)	Omega_I(i)	Delta (frac.)	Time	< DIS
+						+< DIS
	1	3.82493590	3.66268867	4.430E-02	0.36	< DIS
	2	3.66268867	3.66268867	6.911E-15	0.37	< DIS

.

```
<<< Delta < 1.000E-10 over 3 iterations >>>
</< Disentanglement convergence criteria satisfied >>>
```

Final Omega_I 3.66268867 (Ang^2)

+-----+

The first column gives the iteration number. For a description of the minimisation procedure and expressions for $\Omega_{\rm I}^{(i)}$, see the original paper [2]. The procedure is considered to be converged when the fractional difference between $\Omega_{\rm I}^{(i)}$ and $\Omega_{\rm I}^{(i-1)}$ is less than dis_conv_tol over dis_conv_window iterations. The final column gives a running account of the wall time (in seconds) so far. Note that at the end of each line of output, there are the characters "<--DIS". This enables fast searching of the output using, for example, the Unix command grep:

my_shell> grep DIS wannier.wout | less

7.6.5 Wannierisation

The next part of the input file provides information on the minimisation of $\widetilde{\Omega}$. At each iteration, the centre and spread of each WF is reported.

```
*----*
+-----+<-- CONV
| Iter Delta Spread RMS Gradient Spread (Ang^2) Time | <-- CONV
+-----+<-- CONV
Initial State
WF centre and spread 1 (0.000000, 1.969243, 1.969243) 1.52435832
WF centre and spread 2 ( 0.000000, 1.969243, 1.969243 ) 1.16120620
      0.29 <-- CONV
    Cycle:
WF centre and spread 1 (0.000000, 1.969243, 1.969243) 1.52414024
WF centre and spread 2 ( 0.000000, 1.969243, 1.969243 ) 1.16059775
Sum of centres and spreads (11.815458, 11.815458, 11.815458)
                                      12.62663472
      -0.313E-02
              0.0697660962
                         12.6266347170
                                    0.34 <-- CONV
         Delta: O_D= -0.4530841E-18 O_OD= -0.3133809E-02 O_TOT= -0.3133809E-02 <-- DLTA
```

gives

```
Cycle:
          2
WF centre and spread
                     1 ( 0.000000, 1.969243, 1.969243 ) 1.52414866
WF centre and spread
                     2 ( 0.000000, 1.969243, 1.969243 )
                                                        1.16052405
 Sum of centres and spreads (11.815458, 11.815458, 11.815458)
                                                       12.62646411
        -0.171E-03
                     0.0188848262
                                     12.6264641055
                                                      0.38 <-- CONV
     O_D=
              Delta: O_D= -0.2847260E-18 O_OD= -0.1706115E-03 O_TOT= -0.1706115E-03 <-- DLTA
Final State
WF centre and spread 1 (0.000000, 1.969243, 1.969243) 1.52416618
WF centre and spread 2 ( 0.000000, 1.969243, 1.969243 ) 1.16048545
Sum of centres and spreads (11.815458, 11.815458, 11.815458)
                                                        12.62645344
      Spreads (Ang^2)
                         Omega I
                                      12.480596753
     _____
                         Omega D
                                        0.000000000
                         Omega OD =
                                        0.145856689
  Final Spread (Ang^2)
                         Omega Total =
                                        12.626453441
```

It looks quite complicated, but things look more simple if one uses grep: my_shell> grep CONV wannier.wout

+					-+< CONV
Iter	Delta Spread	RMS Gradient	Spread (Ang^2)	Time	< CONV
+					-+< CONV
0	0.126E+02	0.000000000	12.6297685260	0.29	< CONV
1	-0.313E-02	0.0697660962	12.6266347170	0.34	< CONV
50	0.000E+00	0.000000694	12.6264534413	2.14	< CONA

The first column is the iteration number, the second is the change in Ω from the previous iteration, the third is the root-mean-squared gradient of Ω with respect to variations in the unitary matrices $\mathbf{U}^{(\mathbf{k})}$, and the last is the time taken (in seconds). Depending on the input parameters used, the procedure either runs for $\mathtt{num_iter}$ iterations, or a convergence criterion is applied on Ω . See Section 2.8 for details.

Similarly, the command

 $my_shell> grep SPRD wannier.wout$

gives

0_D=	0.0000000	0.1491718 O_TOT=	12.6297685 < SPRD
0_D=	0.0000000	0.1460380	12.6266347 < SPRD
0_D=	0.0000000	0.1458567 O_TOT=	12.6264534 < SPRD

which, for each iteration, reports the value of the diagonal and off-diagonal parts of the non-gauge-invariant spread, as well as the total spread, respectively. Recall from Section 1.1 that $\Omega = \Omega_{\rm I} + \Omega_{\rm D} + \Omega_{\rm OD}$.

7.6.6 Plotting

After WF have been localised, wannier90 enters its plotting routines (if required). For example, if you have specified an interpolated bandstucture:



Calculating interpolated band-structure

7.6.7 Summary timings

At the very end of the run, a summary of the time taken for various parts of the calculation is given. The level of detail is controlled by the timing_level input parameter (set to 1 by default).

===========		====		=======
	TIMING INFORMATION			1
=========		====		=======
Tag			Ncalls	Time (s)
kmesh: get		:	1	0.212
overlap: read		:	1	0.060
wann: main		:	1	1.860
plot: main		:	1	0.168
*				*

All done: wannier90 exiting

7.7 seedname.chk

INPUT/OUTPUT. Information required to restart the calculation or enter the plotting phase. If we have used disentanglement this file also contains the rectangular matrices $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$.

7.8 seedname.r2mn

OUTPUT. Written if write_r2mn = true. The matrix elements $\langle m|r^2|n\rangle$ (where m and n refer to MLWF)

7.9 seedname_band.dat

OUTPUT. Written if bands_plot=.TRUE.; The raw data for the interpolated band structure.

7.10 seedname_band.gnu

OUTPUT. Written if bands_plot=.TRUE. and bands_plot_format=gnuplot; A gnuplot script to plot the interpolated band structure.

7.11 seedname_band.agr

OUTPUT. Written if bands_plot=.TRUE. and bands_plot_format=xmgrace; A grace file to plot the interpolated band structure.

7.12 seedname_band.kpt

OUTPUT. Written if bands_plot=.TRUE.; The k-points used for the interpolated band structure, in units of the reciprocal lattice vectors. This file can be used to generate a comparison band structure from a first-principles code.

7.13 seedname.bxsf

OUTPUT. Written if fermi_surface_plot=.TRUE.; A Fermi surface plot file suitable for plotting with XCrySDen.

7.14 seedname_w.xsf

OUTPUT. Written if wannier_plot=.TRUE. and wannier_plot_format=xcrysden. Contains the wth WF in real space in a format suitable for plotting with XCrySDen or VMD, for example.

7.15 seedname_w.cube

OUTPUT. Written if wannier_plot=.TRUE. and wannier_plot_format=cube. Contains the \mathbf{w}^{th} WF in real space in Gaussian cube format, suitable for plotting in XCrySDen, VMD, gopenmol etc.

7.16 UNKp.s

INPUT. Read if wannier_plot=.TRUE. and used to plot the MLWF.

The periodic part of the Bloch states represented on a regular real space grid, indexed by k-point p (from 1 to num_kpts) and spin s ('1' for 'up', '2' for 'down').

The name of the wavefunction file is assumed to have the form:

```
write(wfnname,200) p,spin
200 format ('UNK',i5.5,'.',i1)
```

The first line of each file should contain 5 integers: the number of grid points in each direction (ngx, ngy and ngz), the k-point number ik and the total number of bands num_band in the file. The full file will be read by wannier90 as:

```
read(file_unit) ngx,ngy,ngz,ik,nbnd
do loop_b=1,num_bands
  read(file_unit) (r_wvfn(nx,loop_b),nx=1,ngx*ngy*ngz)
end do
```

The file can be in formatted or unformatted style, this is controlled by the logical keyword wvfn_formatted.

7.17 seedname_centres.xyz

OUTPUT. Written if translate_home_cell=.TRUE.; xyz format atomic structure file suitable for viewing with your favourite visualiser (jmol, gopenmol, vmd, etc.).

7.18 seedname_hr.dat

OUTPUT. Written if hr_plot=.TRUE.. The first line gives the date and time at which the file was created. The subsequent lines each contain, respectively, the components of the vector \mathbf{R} in terms of the lattice vectors $\{\mathbf{A}_i\}$, the indices m and n, and the real and imaginary parts of the Hamiltonian matrix element $H_{mn}^{(\mathbf{R})}$ in the WF basis, e.g.,

Created	on	24May2007	at	23:32:09
---------	----	-----------	----	----------

0	0	-2	1	1	-0.001013	0.000000
0	0	-2	2	1	0.000270	0.000000
0	0	-2	3	1	-0.000055	0.000000
0	0	-2	4	1	0.000093	0.000000
0	0	-2	5	1	-0.000055	0.000000

.

Frequently Asked Questions

8.1 General Questions

8.1.1 What is wannier 90?

wannier90 is a computer package, written in Fortran90, for obtaining maximally-localised Wannier functions, using them to calculate bandstructures, Fermi surfaces, dielectric properties, sparse Hamiltonians and many things besides.

8.1.2 Where can I get wannier90?

The most recent release of wannier90 is always available on our website www.wannier.org.

8.1.3 Where can I get the most recent information about wannier90?

The latest news about wannier90 can be followed on our website www.wannier.org.

8.1.4 Is wannier90 free?

Yes! wannier90 is available for use free-of-charge under the GNU General Public Licence. See the file LICENCE that comes with the wannier90 distribution or the GNU hopepage at www.gnu.org.

8.1.5 Who wrote wannier90?

wannier90 is written by Arash A. Mostofi (Imperial College London), Jonathan. R. Yates (University of Cambridge) and Young-Su Lee (Korea Institute of Science and Technology). wannier90 is based on algorithms written in 1996-7 by Nicola Marzari (Massachusetts Institute of Technology) and David Vanderbilt (Rutgers University), and in 2000-1 by Ivo Souza

(University of California at Berkeley), Nicola Marzari and David Vanderbilt.

The interface to PWSCF was written by Stefano de Gironcoli (SISSA, Trieste).

8.2 Getting Help

8.2.1 Is there a Tutorial available for wannier90?

Yes! The examples directory of the wannier90 distribution contains input files for a number of tutorial calculations. The doc directory contains the accompanying tutorial handout.

8.2.2 Where do I get support for wannier90?

There are a number of options:

- 1. The wannier90 User Guide, available in the doc directory of the distribution, and from the webpage (www.wannier.org/user_guide.html)
- 2. The wannier90 webpage for the most recent announcements (www.wannier.org)
- 3. The wannier90 mailing list (see www.wannier.org/forum.html)

8.2.3 Is there a mailing list for wannier90?

Yes! You need to register: go to www.wannier.org/forum.html and follow the instructions.

8.3 Providing Help: Finding and Reporting Bugs

8.3.1 I think I found a bug. How do I report it?

- Check and double-check. Make sure it's a bug.
- Check that it is a bug in wannier90 and not a bug in the software interfaced to wannier90.
- Check that you're using the latest version of wannier90.
- Send an email to developers@wannier.org. Make sure to describe the problem and to attach all input and output files relating to the problem that you have found.

8.3.2 I have got an idea! How do I report a wish?

We're always happy to listen to suggestions. Email your idea to the wannier90 developers at developers@wannier.org.

8.3.3 I want to help! How can I contribute to wannier90?

Great! There's always plenty of functionality to add. Email us at developers@wannier.org to let us know about the functionality you'd like to contribute.

8.3.4 I like wannier90! Should I donate anything to its authors?

Our Swiss bank account number is... just kidding! There is no need to donate anything, please just cite our paper in any publications that arise from your use of wannier90:

[ref] A. A. Mostofi, J. R. Yates, Y.-S. Lee, I. Souza, D. Vanderbilt and N. Marzari, wannier90: A Tool for Obtaining Maximally-Localised Wannier Functions, *Comput. Phys. Commun.*, submitted (2007); http://arxiv.org/abs/0708.0650.

8.4 Installation

8.4.1 How do I install wannier90?

Follow the instructions in the file README.install in the main directory of the wannier90 distribution.

8.4.2 Are there wannier90 binaries available?

Not at present.

8.4.3 Is there anything else I need?

Yes. wannier90 works on top of an electronic structure calculation. At the time of writing, wannier90 is interfaced to the PWSCF code, a plane-wave, pseudopotential, density-functional theory code, which is part of the quantum-espresso package. You will need to download it from the webpage www.quantum-espresso.org or www.pwscf.org. Then compile PWSCF and the wannier90 interface program pw2wannier90. For instructions, please refer to the documentation that comes with the quantum-espresso distribution.

For examples of how to use PWSCF and wannier90 in conjunction with each other, see the wannier90 Tutorial.

Interfaces to other electronic structure codes, such as CASTEP,¹ FLEUR² and ABINIT,³ are currently in progress and should become available in the near future.

 $^{^{1}}$ www.castep.org

²www.flapw.de

³www.abinit.org

- 8.5 Compile-time Problems
- 8.6 Run-time Problems
- 8.7 Using wannier90

Sample Input Files

9.1 Master input file: seedname.win

```
: 4
num_wann
mp_grid
                : 4 4 4
                 : 100
num_iter
postproc_setup : true
begin unit_cell_cart
ang
-1.61 0.00 1.61
0.00 1.61 1.61
-1.61 1.61 0.00
end unit_cell_cart
begin atoms_frac
  -0.125 -0.125 -0.125
    0.125 0.125 0.125
end atoms_frac
bands_plot
             : true
bands_num_points : 100
bands_plot_format : gnuplot
begin kpoint_path
L 0.50000 0.50000 0.50000 G 0.00000 0.00000 0.00000
G 0.00000 0.00000 0.00000 X 0.50000 0.00000 0.50000
X 0.50000 0.00000 0.50000 K 0.62500 0.25000 0.62500
end kpoint_path
begin projections
C:1=0,1=1
```

```
begin kpoints
0.00 0.00 0.00
0.00 0.00 0.25
0.00 0.50 0.50
.
.
0.75 0.75 0.50
0.75 0.75 0.75
end kpoints
```

end projections

9.2 seedname.nnkp

Running wannier90 on the above input file would generate the following nnkp file:

```
File written on 9Feb2006 at 15:13: 9
calc_only_A
             : F
begin real_lattice
 -1.612340
            0.000000
                        1.612340
  0.000000
             1.612340
                        1.612340
  -1.612340
            1.612340
                        0.000000
end real_lattice
begin recip_lattice
  -1.951300 -1.951300
                        1.951300
  1.951300
             1.951300
                        1.951300
  -1.951300
            1.951300 -1.951300
end recip_lattice
begin kpoints
     64
  0.00000
           0.00000
                     0.00000
  0.00000
           0.25000
                    0.00000
  0.00000
           0.50000
                     0.00000
  0.00000
           0.75000
                     0.00000
  0.25000
           0.00000
                     0.00000
  0.50000
           0.75000
                     0.75000
```

```
0.75000 0.00000 0.75000

0.75000 0.25000 0.75000

0.75000 0.50000 0.75000

0.75000 0.75000 0.75000

end kpoints
```

begin projections

8 -0.12500 -0.12500 -0.12500 0 1 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 -0.12500 -0.12500 -0.12500 1 1 1 0.000 1.000 1.000 0.000 0.000 0.000 2.00 -0.12500 -0.12500 -0.12500 1 0.000 1.000 0.000 0.000 0.000 1.000 2.00 -0.12500 -0.12500 -0.12500 1 3 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 0.12500 0.12500 0.12500 0 1 1 0.000 0.000 0.000 1.000 1.000 0.000 2.00 0.12500 0.12500 0.12500 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 0.12500 0.12500 0.12500 1 2 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 0.12500 0.12500 0.12500 1 3 1 0.000 0.000 1.000 1.000 0.000 0.000 2.00 end projections

begin nnkpts

.

64	1	1	1	1
64	16	0	0	1
64	43	0	0	0
64	48	0	0	0
64	52	1	0	0
64	60	0	0	0
64	61	0	1	0
64	63	0	0	0
end	nnkpts			

begin exclude_bands

end exclude_bands

Bibliography

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- [2] I. Souza, N. Marzari and D. Vanderbilt, Maximally Localized Wannier Functions for Entangled Energy Bands, *Phys. Rev. B* **65**, 035109 (2001).
- [3] Gygi, F., Fattebert, J.-L., and Schwegler, E., Computation of Maximally Localized Wannier Functions using a simultaneous diagonalization algorithm, *Comp. Phys. Commun.* **155**, 1 (2003).
- [4] A. A. Mostofi, J. R. Yates, Y.-S. Lee, I. Souza, D. Vanderbilt and N. Marzari, wannier90: A Tool for Obtaining Maximally-Localized Wannier Functions, *Comput. Phys. Commun.*, submitted (2007); http://arxiv.org/abs/0708.0650.
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- [6] M. Posternak, A. Baldereschi, S. Massidda and N. Marzari, Maximally Localized Wannier Functions in Antiferromagnetic MnO within the FLAPW Formalism, *Phys. Rev. B* 65, 184422 (2002).