HPC Shallow Water project: Theoretical Analysis

Antoine Hoffmann Parallel and High Performance Computing MATH-454, EPFL E-mail: antoine.hoffmann@epfl.ch

May 14, 2018

1 Introduction

This project consist to parallelize a given finite volume solver MATLAB code which simulates the propagation of a Tsunami on the scale of an island in the shallow water modeling framework.

2 Presentation of the sequential C++ code

2.1 Sequential Algorithm

The MATLAB code has been firstly translated into a C++ sequential code. The main work consisted mainly in a structural reorganization of the algorithm by defining a collection of C++ functions. Those functions where written in a second C++ file linked to the main program with a hierarchical makefile in view to increase the readability and analysis of performance. The algorithm and the finite volume solver did not need to be deeply changed and one can read a pseudo code presentation of the sequential C++ implementation at Algorithm 1.

Algorithm 1 Sequential C++ Finite Volume Solver

```
n_x = 1D number of grid cells on one side of the domain
N = \text{Total number of grid cells}
dx = \text{Grid spacening in [km]}
Allocating (H, HU, HV, Z_{dx}, Z_{dy}, H_t, HU_t, HV_t)
                                                                                                            ▶ Memory allocation
(Z_{dx}, Z_{dy}) \Leftarrow \text{Topology data file}
                                                                    ▷ Load gradients of the topology from binary data file
(H, HU, HV) \Leftarrow \text{Initial state data file}
                                                         ▶ Load initial state of the height and the velocities of the water
while T < T_{\rm end} do
                                                                                          \triangleright Simulating until a given time T_{\rm end}
    dt \Leftarrow \text{new\_dt}(H, HU, HV, dx, N)
                                                                                    \triangleright Updating dt from finite volume scheme
   if T + dt > T_{\text{end}} then
        dt \Leftarrow T_{\text{end}} - T
                                                                                                       \triangleright To stop exactly at T_{\rm end}
    (H_t, HU_t, HV_t) \Leftarrow (H, HU, HV)
                                                                                (H_t, HU_t, HV_t) \Leftarrow \text{enforce\_BC}(H_t, HU_t, HV_t, dx)
                                                                                                ▶ Enforce boundary conditions
    (H, HU, HV) \Leftarrow \text{FV\_time\_step}(Z_{dx}, Z_{dy}, H_t, HU_t, HV_t, dt, nx)
                                                                                     ▶ Perform one time step of finite volume
    (H, HU, HV) \Leftarrow impose\_tolerances(H, HU, HV)
    T \Leftarrow T + dt
Save solution to disk
Free memory space
```

PHPC project Antoine Hoffmann

2.2 Validation

Some data are also taken from the C++ code such as the final state of the water level and an history of the time step evolution during the simulation. Those two results were used to verify the correctness of the C++ code. Figure 1 and Figure 2 confirm that the sequential C++ code is working correctly with a negligible error in comparison to the real values.

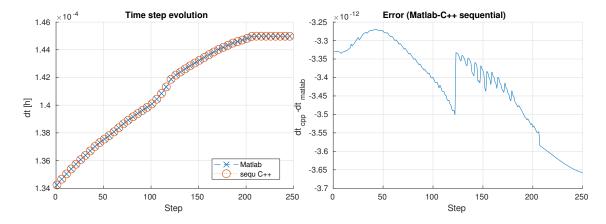


Figure 1: Comparison between the tracking of the time step in the Matlab and C++ sequential codes.

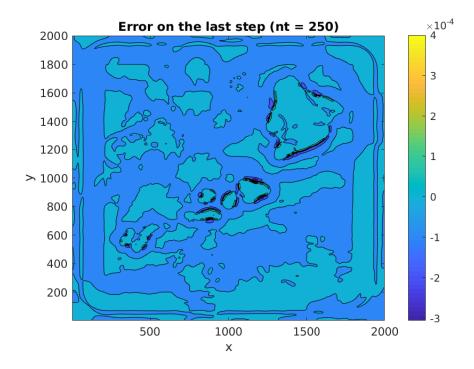


Figure 2: Error between the last step of the MATLAB code and sequential C++ one.

2.3 Performance comparison

Even if one could not expect an improvement in performance as great as the future parallelization of the algorithm, it can be interesting to figure out if the C++ language version performs already better the sequential algorithm than the Matlab version. The performances in computational time has been measured through six independent launch of compute.m and compute.cpp. These measurement are reported on Figure 3 where one can observe a $\approx 250\%$

PHPC project Antoine Hoffmann

increase of the performance just by transferring the solver from Matlab to C++. Of course the performance of the C++ code is related to the compilation process did with the most aggressive optimization option (-0fast). The least optimized compilation (-00) shows extremely reduced performances and take more than 300 seconds to run.

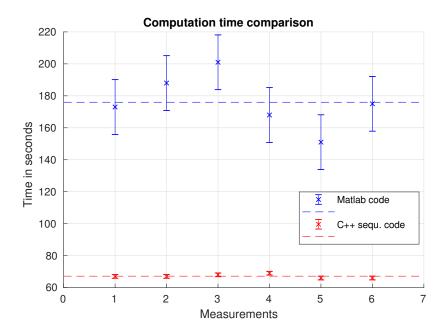


Figure 3: Performance comparison between MATLAB and sequential C++ code for 250 iterations and g++ -Ofast compilation option on an Intel(R) Core(TM) i7-6700HQ CPU @ 2.60GHz.

2.4 Computing time analysis

Before starting the parallelization of our sequential code, it is important to perform a profiling of the computational cost of each steps in the Algorithm 1. The Table 1 presents the computational times (expressed in ticks) taken by the main process of our sequential code and the percentage it represents w.r.t. the global computational time. One can notice that the most costly part of the algorithm is to compute the steps of the finite volume explicit scheme. Keeping this in mind, a parallelization of the function FV_time_step must be the priority.

Step	Comp. Time [ms]	Share of total time
Variable Initialization	0.0432 ± 0.0447	< 0.0001%
Initial state loading	57.021 ± 3.771	$0.0880 \pm 0.0073\%$
new_dt	3532.6 ± 79.5	$5.4466 \pm 0.0741\%$
Copy to temporary variables	2870.8 ± 51.017	$4.4271 \pm 0.0874\%$
enfore_BC	34.669 ± 1.9657	$0.0534 \pm 0.0017\%$
FV_time_step	57608 ± 1551.2	$88.8071 \pm 0.1638\%$
$impose_tolerances$	729.33 ± 21.124	$1.1245 \pm 0.0239\%$
Save output	25.334 ± 1.4030	$0.0390 \pm 0.0014\%$
Free memory space	9.1721 ± 0.3275	$0.0141 \pm 0.0002\%$

Table 1: Results for 10 manual profiling of the sequential C++ code for 250 step.

3 Parallelism Preview with CUDA

The GPU programming language CUDA has been chosen to implement a parallel version of the C++ sequential code.

The parallelization of the main while loop of Algorithm 1 can obviously not be parallelized since it needs the

PHPC project Antoine Hoffmann

results of the previous iteration at each steps. It is however not the case for the functions called inside the loop, i.e. new_dt, enforce_BC, FV_time_step and impose_tolerances.

3.1 Parallelization of FV_time_step

As demonstrated on Table 1, the FV_time_step function has the greatest potential of performance increase. Since the treated variables are two dimensional arrays, the most natural way to parallelize this function is to divide the grid in to N_b regions. Each region will be treated by one block containing $N_t = N/N_b$ threads. However the process updates the variables H, HU and HV by performing a computation similar to a second degree derivative finite difference scheme, thus some data must be transferred between the blocks on their borders.