

Self-Study Summary Collection
Volume 1
Electronics

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Contents

1	Digital Technology and Electronics	5
1.1	Circuit Theory	6
1.1.1	Basic electrical quantities	6
1.1.2	Prefixes	7
1.1.3	Unit grammar	7
1.1.4	Ohm's law	7
1.1.5	Circuit elements	7
1.1.6	Circuit terminology	7
1.1.7	Series Resistor	8
1.1.8	Parallel resistor	9
1.1.9	Simplify resistor network	10
1.1.10	Voltage divider	11
1.1.11	Kirchhoff's laws	11
1.1.12	Node voltage method	12
1.1.13	Mesh current method	14
1.1.14	Capacitor i-v equation	14
1.1.15	inductor i-v equation	14
1.1.16	RC circuit	16
1.2	Semiconductors	19
1.2.1	Diodes	19
1.2.2	Transistors	24
1.3	Digital Circuits: Combinatorial and Sequential Networks	27
1.3.1	Combinational	28
1.3.2	Sequential	30
1.3.3	Shift registers	34
1.3.4	Multiplexer	34
1.4	AC Circuit Analysis & Filtering	35
1.4.1	Impedance	38
1.4.2	Filters	38
2	Op-Amp	43
2.1	Inside Op-Amp	43
2.2	Implementation of Op-Amp	44
2.2.1	Non inverting (with feedback loop)	44
2.2.2	Voltage follower	45
2.2.3	Inverting	46
2.2.4	Summing	47
2.3	General example	48

Chapter 1

Digital Technology and Electronics

Resorcess

- <https://www.falstad.com/circuit/circuitjs.html>
- <http://www.32x8.com/var4kmapx.html>
- <https://www.tinkercad.com/dashboard?type=circuits&collection=designs>
- <https://www.symbolab.com/solver/system-of-equations-calculator>

1.1 Circuit Theory

1.1.1 Basic electrical quantities

Current

$i(A)$: amps

Positive repels Positive. Negative repels Negative. Positive and Negative force of attraction. Copper is commonly used in wires since there is only one electron in last orbital. This makes it easy to move therefore it is highly conductive.

$I = q^- / \text{sec}$ Current is charge per second.

Current is written from Positive to Negative. Since back in history Ben Franklin who studied electricity and came up with theories. However, they were unaware that electrons existed and therefore made the false assumption that the current goes from positive to negative. With infact the electron is attracted to the positive end and therefore flows that way. Ben Franklin 1747. JJ Thompson 1897 e^- . However positive charge does exist like in your body then it would be true.

Electron current is from negative to positive. Conventional current (the current we know as) is from positive to negative.

Voltage

$v(V)$: volt

Voltage is simmular to gravity. It is the potential difference in the two pols, in otherwords like potatial enegy like in the gravity analagy.

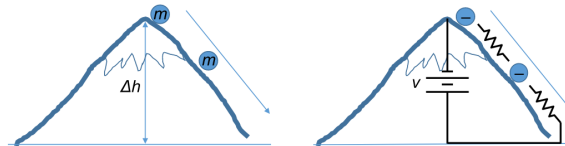


Figure 1.1: volt. From **de**

$$V = \frac{\Delta U}{q} \text{ Where } \Delta U \text{ is the potational energy diffrent and } q \text{ is charge particle}$$

Power

Power is defined as the rate energy (U) is transformed or transferred over time. We measure power in units of joules/second, also known as watts. 1 watt = 1 joules / second)

An electric circuit is capable of transferring power. Current is the rate of flow of charge, and voltage measures the energy transferred per unit of charge. We can insert these definitions into the equation for power: $p = \frac{dU}{dt} = \frac{dU}{dq} \cdot \frac{dq}{dt}$. ($dU = \Delta U$)

$$p = v * i \quad (1.1)$$

1.1.2 Prefixes

Number	Prefix	Symbol	Note
10^{+10}	tera-	T	
10^{+9}	giga-	G	
10^{+6}	mega-	M	
10^{+3}	kilo-	k	the only > 1 prefix in lower case
10^0			
10^{-3}	milli-	m	
10^{-6}	micro-	μ	be careful μ <i>mu</i> doesn't turn into "m"
10^{-9}	nano-	n	
10^{-12}	pico-	p	

1.1.3 Unit grammar

Symbol name	example names	Symbol	example symbols	Named after
second	1 millisecond	s	$2ns$	
meter	300 kilometer	m	$35nm$	
hertz	10 kilohertz	Hz	$100MHz$	Hertz
ohm	2 megohm	Ω	$47k\Omega$	Ohm
farad	10 picofarad	F	$220pF$	Faraday
ampere	35 microamp	A	$65mA$	Ampère
volt	11 kilovolt	V	$5\mu V$	Volta

1.1.4 Ohm's law

- V (Voltage): V (volt)
- I (Current): A (amps)
- R (Resistance): Ω (omega)

$$V = IR \quad (1.2)$$

1.1.5 Circuit elements**1.1.6 Circuit terminology**

- *Closed circuit* – A circuit is closed if the circle is complete if all currents have a path back to where they came from.

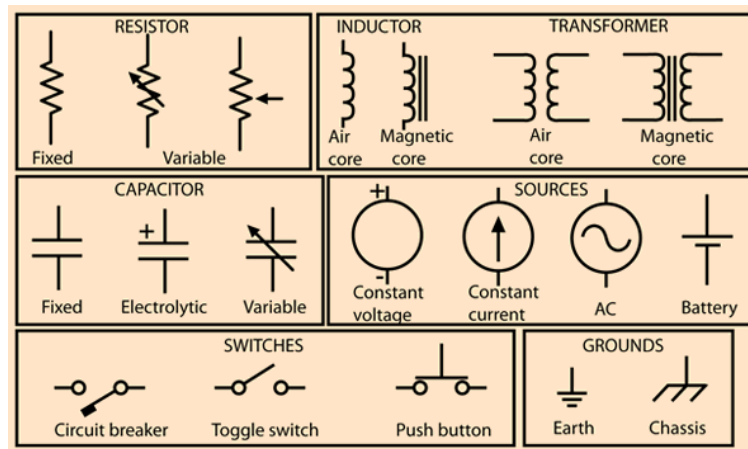


Figure 1.2: From Circuit elements

- *Open circuit* – A circuit is open if the circle is not complete if there is a gap or opening in the path.
- *Short circuit* – A short happens when a path of low resistance is connected (usually by mistake) to a component. The resistor shown below is the intended path for current, and the curved wire going around it is the short. Current is diverted away from its intended path, sometimes with damaging results. The wire shorts out the resistor by providing a low-resistance path for current (probably not what the designer intended).
- *Node* - Between elements
- *Branch* - path between two nodes.
- *Loop* - Close path in a circuit (Branch - Nodes + 1)

1.1.7 Series Resistor

$$R_{series} = R_1 + R_2 + \dots + R_n \quad (1.3)$$

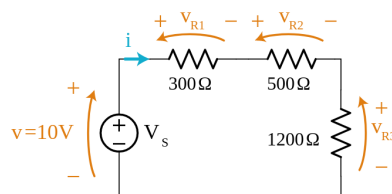


Figure 1.3: voltage distributes between resistors in series. From

$$R_{series} = 300\Omega + 500\Omega + 1200\Omega = 2000\Omega$$

$$i = \frac{v}{R_{series}} = \frac{10V}{2000\Omega} = 5mA$$

$$v_{R1} = i \cdot R1 = 5mA \cdot 300\Omega = 1.5V$$

$$v_{R2} = i \cdot R2 = 5mA \cdot 500\Omega = 2.5V$$

$$v_{R3} = i \cdot R3 = 5mA \cdot 1200\Omega = 6.0V$$

$$10V - 1.5V - 2.5V - 6.0V = 0V \text{ Therefore correct}$$

1.1.8 Parallel resistor

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} \quad (1.4)$$

$$R_{parallel} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}} \quad (1.5)$$

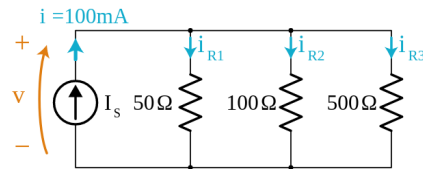


Figure 1.4: current distributes between resistors in parallel. From

$$R_{parallel} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

$$R_{parallel} = \frac{1}{\frac{1}{0.02} + \frac{1}{0.01} + \frac{1}{0.002}} = \frac{1}{0.032} = 31.25\Omega$$

$$v = i \cdot R_{parallel} = 100mA \cdot 31.25\Omega = 3.125V$$

$$i_{R1} = \frac{v}{R1} = \frac{3.125V}{50\Omega} = 62.5mA$$

$$i_{R2} = \frac{v}{R2} = \frac{3.125V}{100\Omega} = 31.25mA$$

$$i_{R3} = \frac{v}{R3} = \frac{3.125V}{500\Omega} = 6.25mA$$

$$100mA - 62.5mA - 31.25mA - 6.25mA = 0mA \text{ Therefore correct}$$

1.1.9 Simplify resistor network

Start from the furthest point. Make parallel and serial resistors become one.

1.1.10 Voltage divider

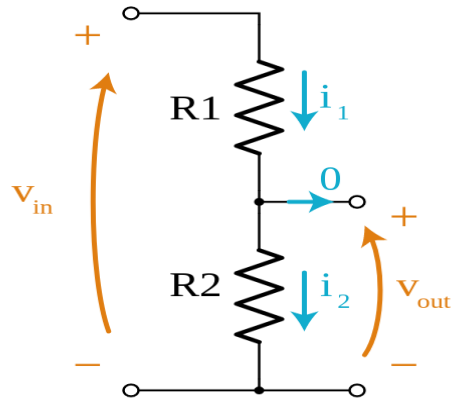


Figure 1.5: voltage-divider. From

$$v_{in} = i(R_1 + R_2) \Rightarrow I = \frac{1}{R_1 + R_2} v_{in}$$

$$v_{out} = iR_2 \Rightarrow v_{out} = \frac{R_2}{R_1 + R_2} v_{in}$$

$$= \frac{1}{\frac{R_1}{R_2} + 1} v_{in}$$

1.1.11 Kirchhoff's laws

Kirchhoff's current law

KCL

$$\sum i_{in} = \sum i_{out} \quad (1.6)$$

Kirchhoff's voltage law

KVL

$$\sum_n V_n = 0 \quad (1.7)$$

$$\sum V_{rise} = V_{drop} \quad (1.8)$$

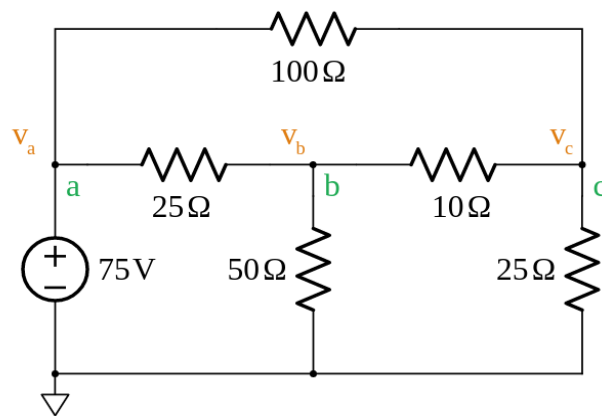
1.1.12 Node voltage method

Figure 1.6: Example node voltage method. From

1. Assign a reference node (ground).

Assign it under Voltage source

2. Assign node voltage names to the remaining nodes.

See image for v_a , v_b , v_c , a , b , c

3. Solve the easy nodes first, the ones with a voltage source connected to the reference node.

V_a is the easiest since it is the same as the input $v_a = 75V$

4. Write Kirchhoff's Current Law for each node. Do Ohm's Law in your head.

$$\text{Node } b: + \frac{v_a - v_b}{25} - \frac{v_b}{50} + \frac{v_c - v_b}{10} = 0$$

$$\text{Node } c: + \frac{v_a - v_c}{100} - \frac{v_b - v_c}{10} + \frac{v_c}{25} = 0$$

5. Solve the resulting system of equations for all node voltages.

$$\text{Node } b: - \frac{v_b}{25} - \frac{v_b}{50} - \frac{v_b}{10} + \frac{v_c}{10} = - \frac{v_a}{25}$$

$$\Rightarrow - \frac{8}{50} v_b + \frac{1}{10} v_c = - \frac{75}{25} = -3$$

$$\text{Node } c: + \frac{v_b}{10} - \frac{v_c}{100} - \frac{v_c}{10} + \frac{v_c}{25} = - \frac{v_a}{100}$$

$$\Rightarrow + \frac{1}{10} v_b - \frac{15}{100} v_c = - \frac{75}{100} = - \frac{3}{4}$$

Solve by gauselimination and then get $v_b = +37.5V$, $v_c = +30V$

6. Solve for any currents you want to know using Ohm's Law.

$$i_{ab25\Omega} = \frac{75 - 37.5}{25} = 1.5A \text{ arrow pointing right}$$

$$i_{b50\Omega} = \frac{37.5}{50} = 0.75A \text{ arrow pointing down}$$

$$i_{bc10\Omega} = \frac{37.5 - 30}{10} = 0.75A \text{ arrow pointing right}$$

$$i_{ac100\Omega} = \frac{75 - 30}{100} = 0.45A \text{ arrow pointing right}$$

$$i_{c25\Omega} = \frac{30}{25} = 1.2A \text{ arrow pointing down}$$

1.1.13 Mesh current method

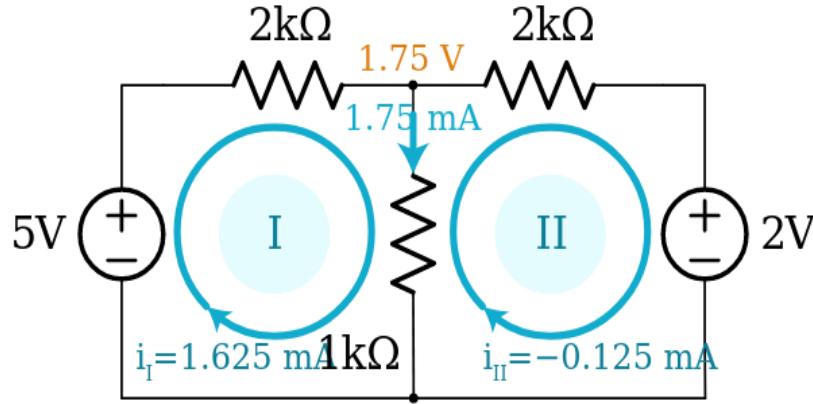


Figure 1.7: Mesh current method. From

Mesh I:

- + The voltage source – voltage drop over first resistor – voltage over second resistor = 0 (KVL)
- + $5V - 2000i_I - 1000(i_I - i_{II}) = 0$

Mesh II:

- + Voltage over first resistor – Voltage over second resistor – Voltage source
- + $1000(i_I - i_{II}) - 2000i_{II} - 2V = 0$

Gauselimination gives us $i_{II} = -0.125mA$, $i_I = +1.625mA$

1.1.14 Capacitor i-v equation

$$i = C \frac{dv}{dt}, \quad v = \frac{1}{C} \int_0^T i dt + v_0 \quad (1.9)$$

- C is the capacitance, a physical property of the capacitor (ex: $10\mu F$)
- $\frac{dv}{dt}$ reate of change for volt over time (ex: $100volts/second$)

1.1.15 inductor i-v equation

$$v = L \frac{di}{dt}, \quad \frac{1}{L} \int_0^T v dt + i_0 \quad (1.10)$$

- L is the inductance, a physical property of the inductor (ex: $1mH$)

- $\frac{di}{dt}$ is the reate of change for the current over time (ex: 300*ampere/second*)

1.1.16 RC circuit

RC natural response

When initializes the circuit with a voltage and the capacitor will then be charged. Then we disconnect the voltage source, the capacitor will act as a battery and edvenshula discharge.

$$v(t) = v_0 e^{-t/RC} \quad (1.11)$$

- Time constant: $\tau = RC$. It is the time it takes to charge the capacitor, through the resistor.
- v_0 is the voltage at $t = 0$

Example:

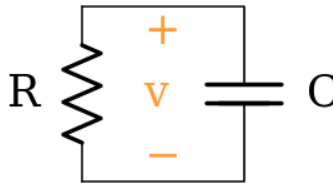


Figure 1.8: EX RC natural response. From

a. Write the expression for $v(t)$

$$v(t) = V_0 e^{-t/RC} = 1.4 e^{-t/(3k\Omega \cdot 1\mu F)} = 1.4 e^{-t/3ms}$$

b. What is $v(t)$ when $t = RC$?

$$\tau = RC = 3 \times 10^3 \cdot 1 \times 10^{-6} = 3ms$$

$$v(3ms) = 1.4 e^{-3ms/3ms} = 1.4 \cdot 1.4 \cdot 0.3679 = 0.515V$$

c. Plot $v(t)$

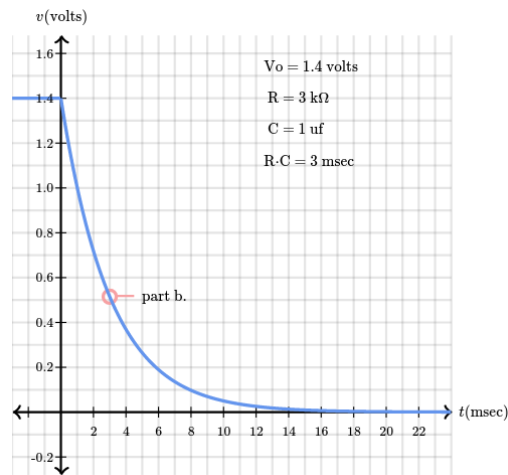


Figure 1.9: Plot RC natural response. From

RC step response

$$\text{Total} = \text{Forced response} + \text{Natural response} \quad (1.12)$$

- Forced response: No start charge on capacitor and connected voltage supply
- Total response: what the circuit actually response.

$$v(t) = V_s + (V_0 - V_s)e^{-t/RC} \quad (1.13)$$

- V_s is the height of the voltage step
- V_0 is the initial voltage on the capacitor

LC natural response

$$s^2 + 1/LC = 0 \quad (1.14)$$

Euler's identities

$$e^{+jx} = \cos x + j \sin x$$

$$e^{-jx} = \cos x - j \sin x$$

where j is the name for $\sqrt{-1}$

Current function of time

$$i(t) = \sqrt{\frac{C}{L}} V_0 \sin \omega_0 t \quad (1.15)$$

Natural frequency of LC circuit

$$\omega_0 \equiv \sqrt{\frac{1}{LC}} \quad (1.16)$$

RLC

The RLC end text circuit is the electronic equivalent of a swinging pendulum with friction.

$$s = \frac{-R \pm \sqrt{R^2 - 4L/C}}{2L} \quad (1.17)$$

$$s = -\alpha \pm \sqrt{\alpha^2 - \omega_o^2} \quad (1.18)$$

where $\alpha = \frac{R}{2L}$ and $\omega_o = \frac{1}{\sqrt{LC}}$

1.2 Semiconductors

Semiconductors electrical conductivity is between conductors and insulators. The material becomes more “conductivity” or less resistance when the temprature rises. This behavior is oposite to that of metals.

1.2.1 Diodes

Ideal diodes

Cundoct electriscity only one way. Current flowes threow Anode (A) to Cathode (K).

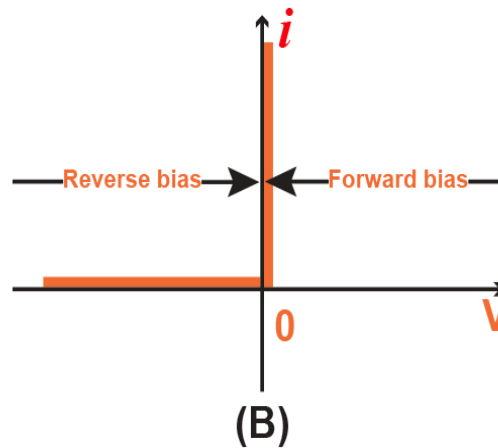


Figure 1.10: ideal diode iv-curv. From

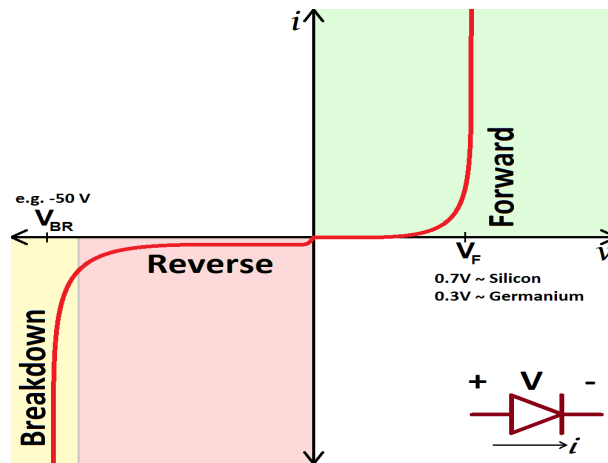
Real diodes

reverse brakedown is when the diode lets negative current. On normal diodes it will perminantly fail, probably melts.

$$i = I_s(e^{qv_d/kT} - 1) \quad (1.19)$$

- k is boltsmans constant ($1.38 * 10^{-23} J/K$ Jouls/Kelvin) $0K = -273^{\circ}C$
- T is tempreture of device (kelvin)
- I_s is structual current (silicon $10^{-12}A$), the small reverse current
- q is the charge of an electron ($1.1609 * 10^{-19}C$)

Difficult to use formula unless numerical analasys.

Figure 1.11: real diode i - v -curv. From

The DC model of a diode

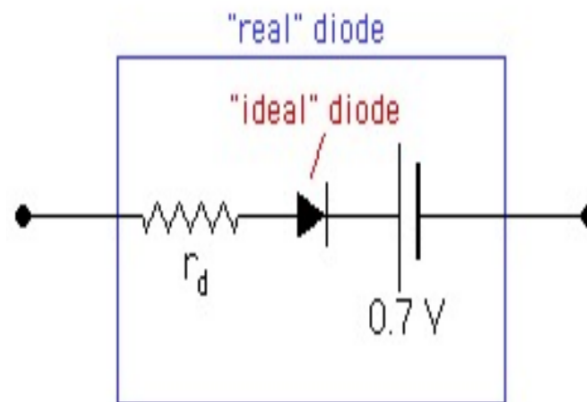


Figure 1.12: real diode dc model. From

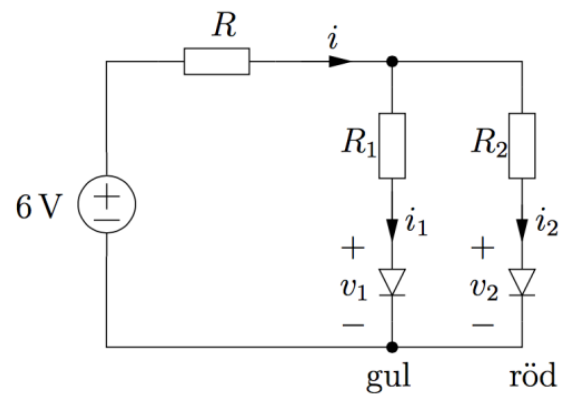
Example: diode

Figure 1.13: diodes example. From

$$i_1 = 40mA, v_1 = 2v$$

$$i_2 = 50mA, v_2 = 1.6v$$

Kirchhoffs strömlag: $i = i_1 + i_2 = 40mA + 50mA = 90mA = 0.09A$

Kirchhoffs spänningslag: (Loop 1)

$$+ 6 - iR - R_1 i_1 - 2 = 0$$

Kirchhoffs spänningslag: (Loop 2)

$$+ 6 - Ri - R_2 i_2 - 1.6 = 0$$

Vi har 3 okända och 2 eqvationer. Närmed så kan vi sätta ett värde på R sådant att motstånden är större än noll

$$R = 20\Omega \Rightarrow R_1 = 55\Omega; R_2 = 52\Omega$$

Zener Diodes

Allows to enter and reenter the reverse breakdown without permanently failing. symbol. Usually lower voltage for reverse breakdown used for analog to digital conversion and vice versa and a voltage regulator.

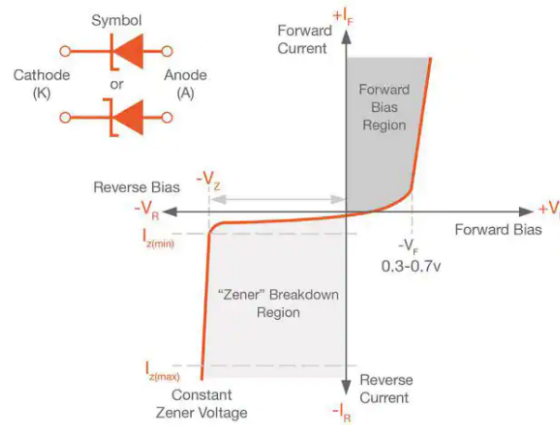


Figure 1.14: zener diode iv-curve. From

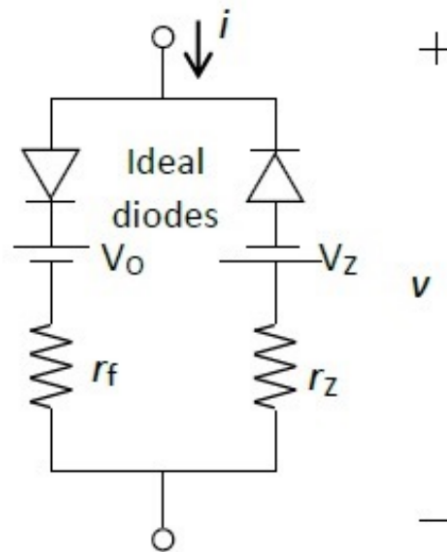


Figure 1.15: zener diode dc model. From

Example Let $V_{in} = 9V$ and $V_z = 5V$. Determent the minimum value of R if the maximum current is $20mA$ threw R , assume $R_L = \text{inf}$. Then determan the minimum resistance for R_L

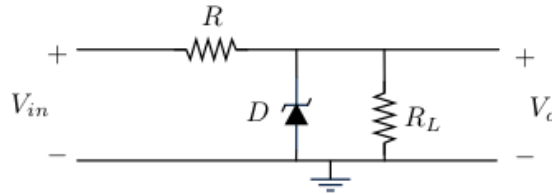


Figure 1.16: zener diode example. From

Let I be the current over R , I_1 the current over the zener diode and I_2 be the current over R_L .

$$I = \frac{V_{in} - V_o}{R}$$

$$\Rightarrow R > \frac{9 - 5}{20 \cdot 10^{-3}} \Omega = 200 \Omega$$

$$\text{KCL: } I = I_1 + I_2$$

$$I_1 = 0 \text{ if } R_L \text{ is to low}$$

$$I_2 = \frac{V_o - 0}{R_L}$$

$$\Rightarrow I = I_2 \Rightarrow 20mA = \frac{5v}{R_L}$$

$$\Rightarrow R_L > \frac{5}{20 \cdot 10^{-3}} \Omega = 250 \Omega$$

1.2.2 Transistors

All Semiconductors are non linier. But we can use transistors with linjer modules.
NPN and PNP symbols. Base (B), Collector (C) and Emitter (E)

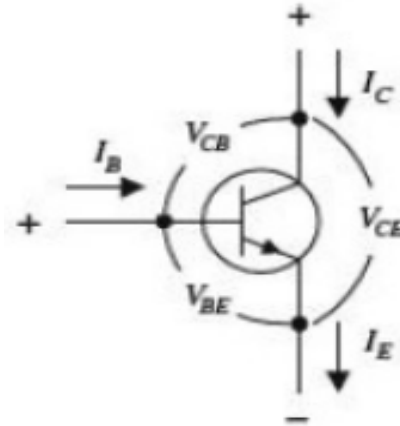


Figure 1.17: Transistor NPN. From

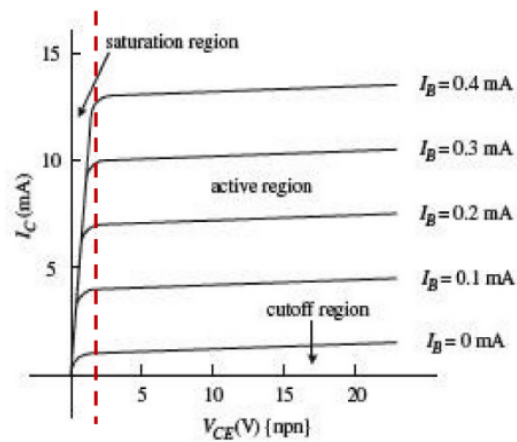


Figure 1.18: Transistor Operational mode. From

Transistor modes**Cutoff:** Open switch

$$I_B = I_E = I_C = 0$$

$$V_{BE}, V_{BC} < 0$$

Saturation: Closed switch

$$V_{CE} \leq V_{CEsat}, I_B > 0$$

Active: Dependent current source

$$I_E = I_B + I_C, I_C = h_{FE} I_B = \beta I_B$$

$$V_{CE} > V_{CEsat}, I_B > 0, V_{BC} = V_B - V_C < 0$$

Example: Transistor What is the largest value that R_B can have so that the transistor behaves as a switch (saturation mode)? The transistor has a current gain h_{FE} between 100 and 300. Suppose that $V_{CEsat} = 0.2V$ and $V_{BEsat} = 0.7V$.

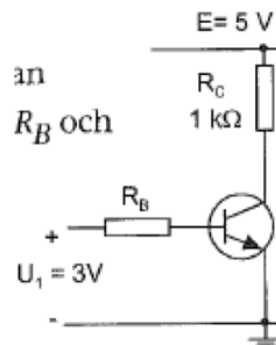


Figure 1.19: Transistor example. From

Om transistorn är bottnad (max current) gäller det att potentialen i C (mellan R_C och transistorn)

$$V_{CE} = V_C - V_E = V_C - 0 = V_{CEsat}$$

$$V_C = V_{CEsat} = 0.2V$$

\Rightarrow Vi har då ett spänningsfall över R_C på $5 - 0.2 = 4.8V$.

$$R_C \cdot I_C = 4.8V \quad \text{Ohm's law} \Rightarrow I_C = \frac{4.8}{10^3} = 4.8mA$$

Vi vet att $I_C = \beta \cdot I_B$ men är ej säkra på β 's värde. Det kan vara så långt som 100.

Vi kan behöva $I_B = \frac{I_C}{100} = 48\mu A$ för att inte I_C ska bli för liten. Alltså: $I_B > 48\mu A$ för att garantera bottnad transistor.

Betrakta nu slingan där I_B går.

Potentialvandring: $U_1 - R_B I_B - V_{BE,sat} = 0, 3 - R_B I_B - 0.7 = 0$

eller $2.3 = R_B I_B \Leftrightarrow I_B = \frac{2.3}{R_B}$

Använd olikhet $I_B > 48\mu A \Rightarrow \frac{2.3}{R_B} > 48\mu A \Rightarrow \frac{2.3}{48 \cdot 10^{-6}} > R_B$ eller $R_B < 47.9k\Omega$

1.3 Digital Circuits: Combinatorial and Sequential Networks

Logic Gates








Name	NOT	AND	NAND	OR	NOR	XOR	XNOR																																																																																																
Alg. Expr.	\overline{A}	AB	\overline{AB}	$A+B$	$\overline{A+B}$	$A\oplus B$	$\overline{A\oplus B}$																																																																																																
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Figure 1.20: Logic Gates. From

Boolean algebra (or: +), (and: ·)

$(x')' = x$

$x + x = x$

$x \cdot x = x$ $x + (y + x) = (x + y) + z$

$x(yz) = (xy)z$

$x + x' = 1$

$x \cdot x' = 0$ $x(y + z) = xy + xz$

$x + yz = (x + y)(x + z)$

$x + 1 = 1$

$x + xy = x$

$x \cdot 0 = 0$

$xy + \overline{x}z = xy + \overline{x}z + yz$

$x + 0 = x$ $(x + y)(\overline{x} + z) = (x + y)(\overline{x} + z)(y + z)$

$x \cdot 1 = x$ $\overline{(x + y)} = \overline{x} \overline{y}$

$\overline{(xy)} = \overline{x} + \overline{y}$

1.3.1 Combinational

$$f(x_6, x_5, x_4, x_3, x_2, x_1, x_0) = x_6 x_4 (x_5 + x_3 + x_0) + x_2 x_1$$

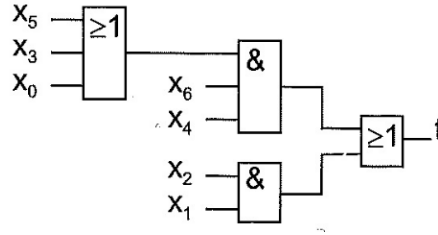


Figure 1.21: Boolean factorization. From

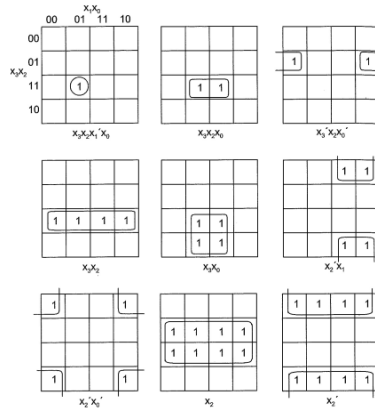


Figure 1.22: KMap patterns. From

KMaps works from 4 variables.

Delays, there is a small delay for each gate.

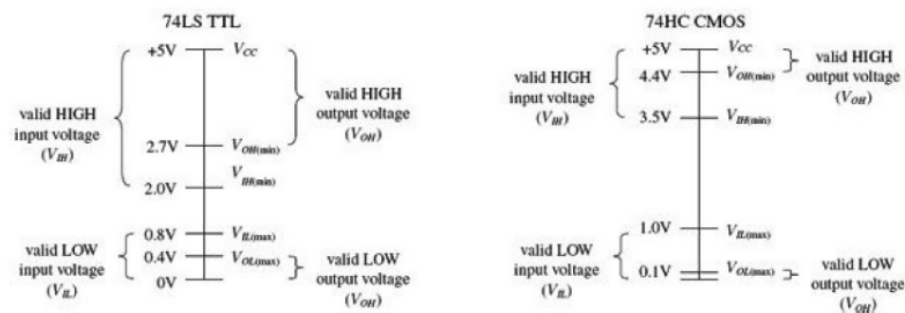


Figure 1.23: Logic families. From

Example: design circuit

$f(x_3, x_2, x_1, x_0) = \sum(0, 2, 4, 5, 6, 7) + d(8, 10, 12, 14)$ - sum-of-products (1.20)

- 0 = 0000
- 2 = 0010
- 4 = 0100
- 5 = 0101
- 6 = 0110
- 7 = 0111

- 8 = 1000
- 10 = 1010
- 12 = 1100
- 14 = 1110

		X_1X_0			
		00	01	11	10
X_3X_2	00	1	0	0	1
	01	1	1	1	1
	11	-	0	0	-
	10	-	0	0	-

$f = \overline{x_0} + \overline{x_3}x_2$ (1.21)

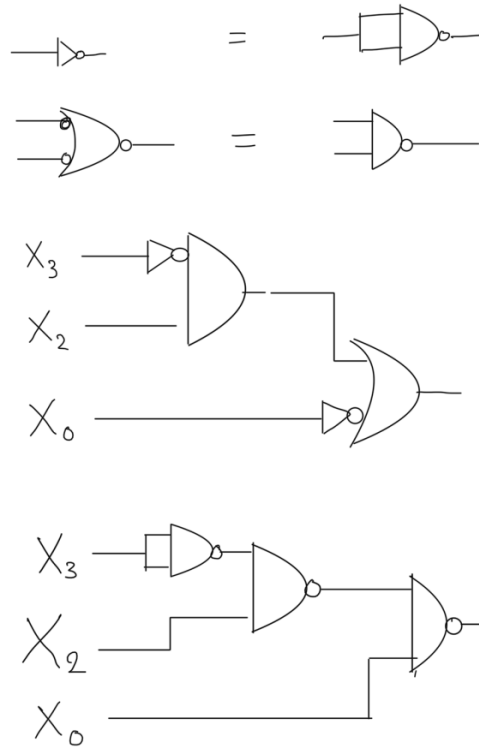


Figure 1.24: lodgic Combinational lodgic.

1.3.2 Sequential

Remembers the state what happend before.

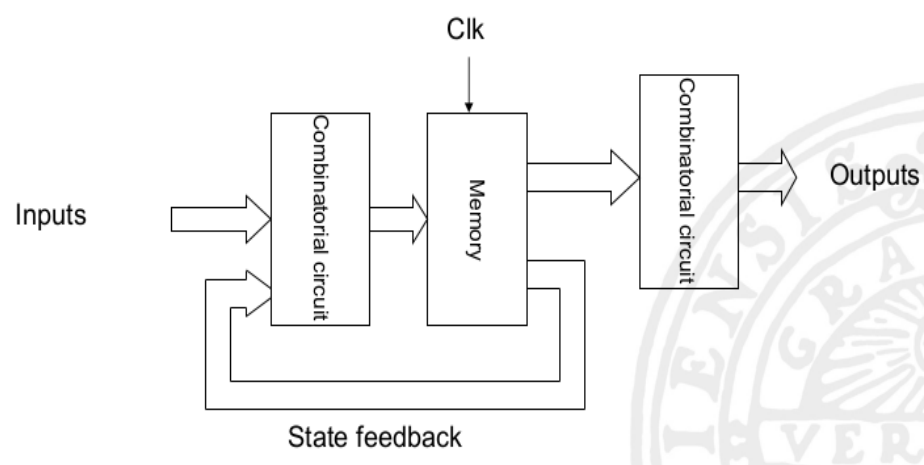


Figure 1.25: Sequential circuits moore type. From

Memory

Description	Circuit
SR-latch (memory cell)	
Gated SR-latch	
Gated D-latch	
D Flip Flops	

Table 1.1: Memory. From

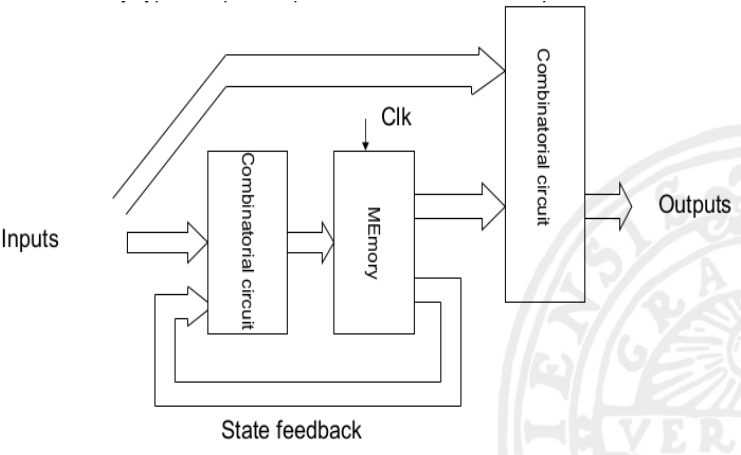


Figure 1.26: Sequential circuits mealy type. From

Timind diagram

State diagram

State code

State name	q_1	q_0
S0	0	0
S1	0	1
S2	1	0
S3	1	1

State Table In sequential circuits we use *state table* instead of *truth table*. ex of state table format:

Previus state	Input	Next state	Output
0 0	0	0 0	0
0 0	1	0 1	0
0 1	0	0 1	1
0 1	1	1 0	1

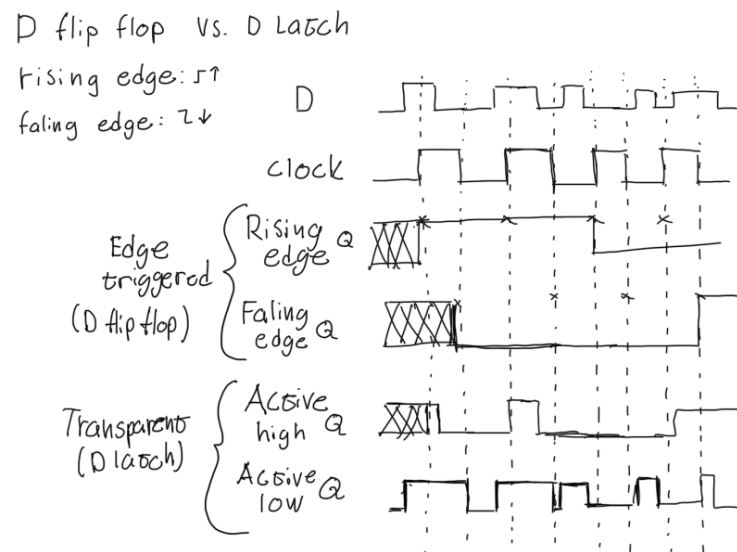


Figure 1.27: Timing diagram.

Moore-circuit Note: in more machine we need a end state for output 1

Mealy-circuit Note: in mealy machine we dont need that.

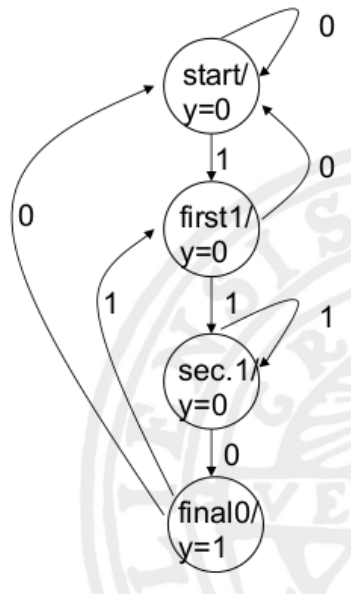


Figure 1.28: State diagram moore. From

1.3.3 Shift registers

Each bit is processed simultaneously. Makes much simpler circuit.

1.3.4 Multiplexer

$$f(A, B, C) = \sum(0, 1, 5, 6)$$

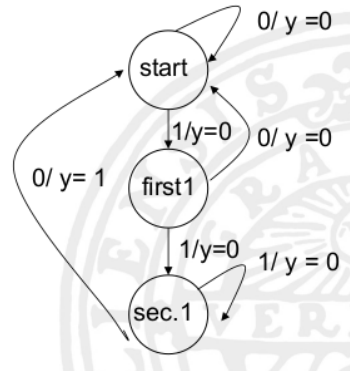


Figure 1.29: State diagram mealy. From

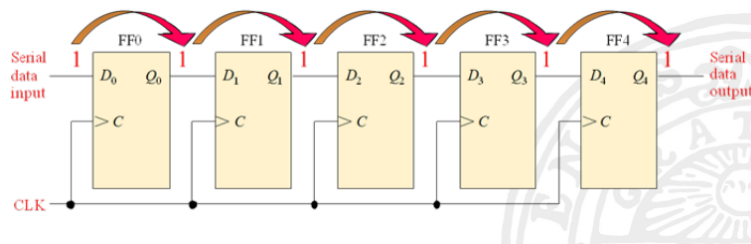


Figure 1.30: Shift register. From

1.4 AC Circuit Analysis & Filtering

Note: $G(\omega) = H(\omega)$

- *sinusoidal steady state* same as AC (analysis)
- *phasor* a complex number representation of sinusoid
- *transfer function* relationship with input and output voltage $G(j\omega) = \frac{V_{out}}{V_{in}}$
- *Impedance* representation of $\frac{V_{in}}{i}$ (z)
- *Angular frequency* $\omega = 2\pi f$ where f is frequency in Hz with is cycles per second
- *Operational frequency* $\frac{1}{\sqrt{2}}$

$$v(t) = v_p \cos \omega t + \phi \quad (1.22)$$

Phasor 3 representations

- Rectangular form $z = x + jy$
- polar form
- exponential form $z = ze^{j\phi}$

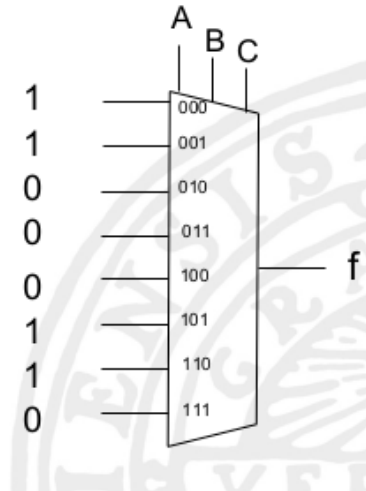


Figure 1.31: Mux. From

Phasor conversion

$$r = \sqrt{x^2 + y^2}$$

$$\phi = \arctan \frac{x}{y}$$

$$x = r \cos(\phi)$$

$$y = r \sin(\phi)$$

$$e^{j\phi} = \cos \phi + j \sin \phi$$

$$\cos \phi = \operatorname{Re}(e^{j\phi})$$

$$\sin \phi = \operatorname{Im}(e^{j\phi})$$

Phasor operations

$$\text{addition: } z_1 + z_2 = (x_1 + x_2) + j(y_1 + y_2)$$

$$\text{subtraction: } z_1 - z_2 = (x_1 - x_2) + j(y_1 - y_2)$$

$$\text{multiplication: } z_1 z_2 = r_1 r_2 / (\phi_1 + \phi_2)$$

$$\text{division: } \frac{z_1}{z_2} = \frac{r_1}{r_2} / (\phi_1 - \phi_2)$$

$$\text{inverse: } \frac{1}{z} = \frac{1}{r} / -\phi$$

$$\text{square root: } \sqrt{z} = \sqrt{r} / (\phi/2)$$

$$\text{complex conjugate: } z^* = x - jy$$

Transfer function

$$H(j\omega) = |H(j\omega)| / \angle H(j\omega)$$

$$H(w) = \frac{v_o(w)}{v_i(w)}$$

Euler formula

$$e^{jx} = \cos x + j \sin x$$

$$e^{-jx} = \cos x - j \sin x$$

They are used to represent sinus wave.

We instead calculate with complex exponentials with euler formula instead of sinus waves

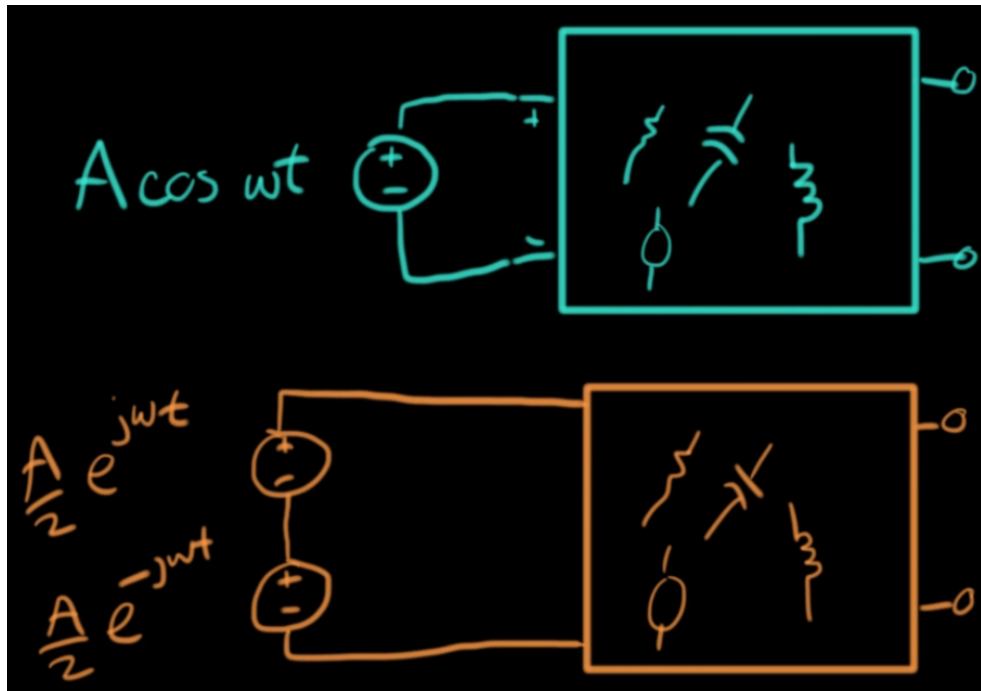


Figure 1.32: AC euler represent demonstration. From

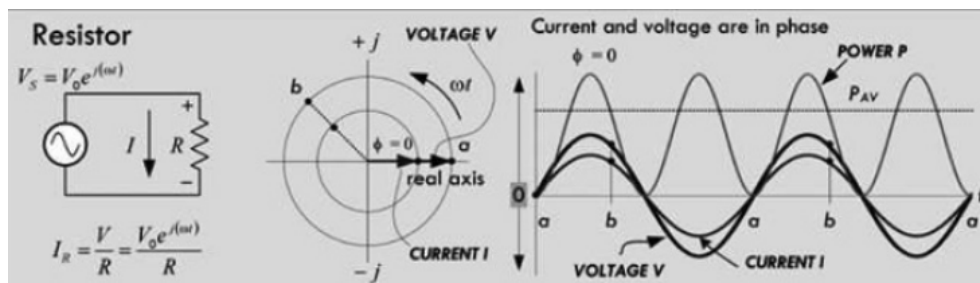
AC Resistor representation

Figure 1.33: AC resistor represent. From

1.4.1 Impedance

$$\text{Impedance } \frac{v_{in}}{i} (z)$$

$$\text{Resistor : } \frac{v}{i} = R$$

$$\text{Inductor : } \frac{v}{i} = j\omega l$$

$$\text{Capasitor : } \frac{v}{i} = \frac{1}{j\omega c}$$

1.4.2 Filters

The filter can eather be active and passive filters:

- *Passive filters* only use active components like resistor, capasitor and inductor
- *Active filters* use opamp (can amplify output)

There are 4 common filtering types:

- *High-pass filter (HP)* lets higher frequencys threow
- *Low-pass filter (LP)* lets lower frequencys threow
- *Bandpass filter (BP)* within a frequency spand. Can be comind with HP and LP in series
- *Notch filter* oposit of BP

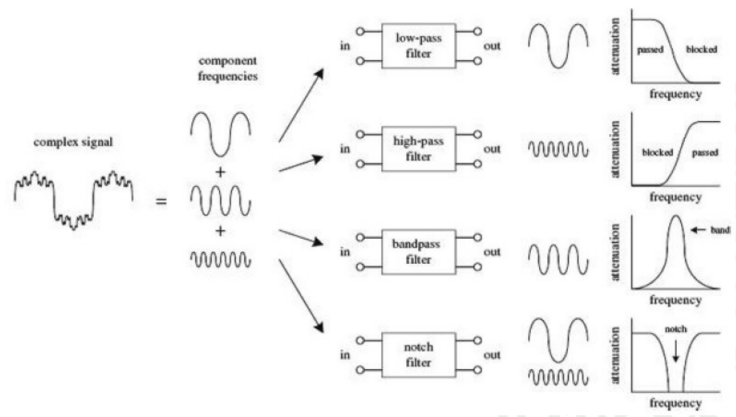


Figure 1.34: Signal filtering. From

Filters can be constructed as follows:

RC filter, RL Filter, LC filter, L-filter, π -filter and T-filter.

Some resources to construct filters

- RF tools
- Filterwizard

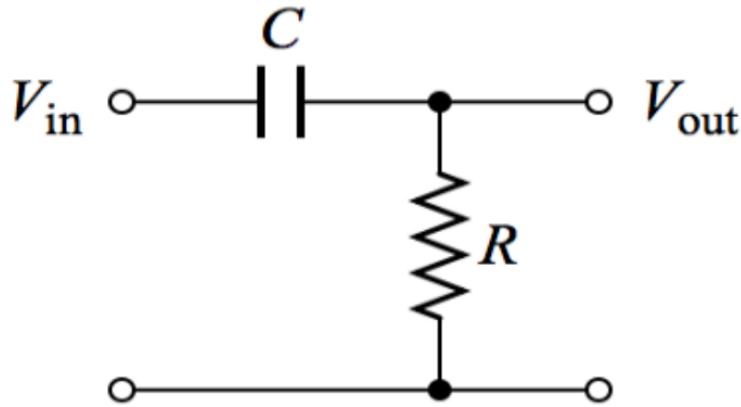
Example: HP filter

Figure 1.35: HP Filter Circuit.png. From

$$\begin{aligned}
 V_{out} &= V_{in} \frac{z_R}{z_C + z_R} \quad \text{-From voltage divider circuit} \\
 &= V_{in} \frac{R}{\frac{1}{j\omega C} + R} \quad \text{-From impedance axiom} \\
 &= V_{in} \frac{\frac{R}{1}}{\frac{R(j\omega C) + 1}{j\omega C}} = V_{in} \frac{R(j\omega C)}{R(j\omega C) + 1}
 \end{aligned}$$

Therefore we get $G_{HP} = \frac{R(j\omega C)}{R(j\omega C) + 1}$

$$\begin{aligned}
 |G_{HP}| &= \frac{1}{\sqrt{2}} = \frac{R\omega C}{\sqrt{R^2\omega^2 C^2 + 1}} \\
 &\Rightarrow \frac{\sqrt{R^2\omega^2 C^2 + 1}}{\sqrt{2}} = R\omega C \\
 &\Rightarrow \frac{R^2\omega^2 C^2 + 1}{2} = R^2\omega^2 C^2 \\
 &\Rightarrow R^2\omega^2 C^2 + 1 = 2R^2\omega^2 C^2 \\
 &\Rightarrow R^2\omega^2 C^2 = 1 \\
 &\Rightarrow R\omega C = 1 \\
 &\Rightarrow R = \frac{1}{\omega C}
 \end{aligned}$$

The following is given: $\omega = 2\pi f$, $1kHz$ for HP filter. The capacitor should not be larger than $2.2\mu F$. Therefore we chose $c = 1\mu F$, this gives us $R \approx 160\Omega$.

$$\begin{aligned}
 \arg(G_{HP}) &= \arg\left(\frac{160 \cdot 2 \cdot \pi \cdot 10^{-6} \cdot f \cdot j}{160 \cdot 2 \cdot \pi \cdot 10^{-6} \cdot f \cdot j + 1}\right) \\
 &= \arg(160 \cdot 2 \cdot \pi \cdot 10^{-6} \cdot f \cdot j) - \arg(160 \cdot 2 \cdot \pi \cdot 10^{-6} \cdot f \cdot j + 1) \\
 &= \frac{\pi}{2} - \arctan\left(\frac{160 \cdot 2 \cdot \pi \cdot 10^{-6} \cdot f}{1}\right) \\
 &= \frac{\pi}{2} - \arctan\left(\frac{\pi \cdot f}{3125}\right)
 \end{aligned}$$

$$\begin{aligned}
 \arg(G_{HP}) &= \arg\left(\frac{160 \cdot 2 \cdot \pi \cdot 10^{-6} \cdot f \cdot j}{160 \cdot 2 \cdot \pi \cdot 10^{-6} \cdot f \cdot j + 1}\right) \\
 \Rightarrow \frac{z_1}{z_2} &= \frac{r_1}{r_2} \angle \phi_1 - \phi_2 \\
 \Rightarrow \frac{z_1}{z_2} &= \frac{\sqrt{(0.32 \cdot 10^{-3} \cdot f\pi)^2}}{\sqrt{(0.32 \cdot 10^{-3} \cdot f\pi)^2 + 1}} \angle \arctan 0 - \arctan \frac{1}{0.32 \cdot 10^{-3} \cdot f\pi} \\
 \Rightarrow \arg\left(\frac{z_1}{z_2}\right) &= -\arctan \frac{1}{0.32 \cdot 10^{-3} \cdot f\pi} \\
 &= -\arctan \frac{1}{0.32 \cdot 10^{-3} \cdot f\pi} \\
 &= \frac{\pi}{2} - \arctan \frac{f\pi}{3125}
 \end{aligned}$$

Example: exponential representation

$$\begin{aligned}
 H(j\omega) &= \frac{j\pi}{1 + j2\pi} = |H(j\omega)|e^{j\arg(H(j\omega))} \\
 \Rightarrow |H(j\omega)| &= \frac{\sqrt{\pi^2}}{\sqrt{1^2 + 2^2\pi^2}} = \frac{\pi}{\sqrt{1 + 4\pi^2}} \\
 \arg(H(j\omega)) &= \arg\left(\frac{j\pi}{1 + j2\pi}\right) = \arctan\left(\frac{0}{\pi}\right) - \arctan\left(\frac{1}{2\pi}\right) \\
 &= \frac{\pi}{2} - \arctan(2\pi) \\
 \Rightarrow H(j\omega) &= \frac{\pi}{\sqrt{1 + 4\pi^2}} e^{j\arctan(2\pi)}
 \end{aligned}$$

Series of filter

One can commbind filters to create more complex filters. The *transfer function* will be the multiplication of

$$G_{tot} = G_1 \cdot G_2 \cdot \dots \cdot G_n \quad (1.23)$$

The *Gain* will be the gain for each individual transfer function multiplied

$$|G_{tot}| = |G_1| \cdot |G_2| \cdot \dots \cdot |G_n| \quad (1.24)$$

The phase function is the sum of the phase functions

$$Arg(G_{tot}) = Arg(G_1) + Arg(G_2) + \dots + Arg(G_n) \quad (1.25)$$

Chapter 2

Op-Amp

Op-Amp is a type of amplifier for data signals. Saturates mean that it will become a state line since it can not become more than the input nor can it be less than what is going in the opposite direction. $v_0 = A(v^+ - v^-)$

The current to v^- and v^+ will be close to zero and in an ideal circuit will be zero.
We can say $v^- = v^+$ when there is a feedback loop (negative terminal and non-inverting amp).

2.1 Inside Op-Amp

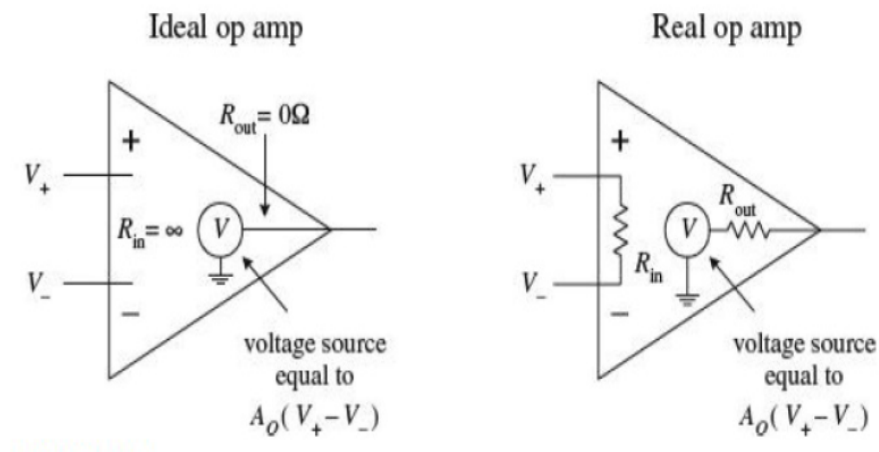


Figure 2.1: Inside opAmp. From

In ideal op amp the resistance will be infinity. However, the in reality there is no infinite resistance therefore if one would have a voltage divider with larger resistance then the internal resistance the current will go threw V_+ and V_- . The output in 0 Ohm so we will not have any voltage drop, not in reality, however.

2.2 Implementation of Op-Amp

Comparator

An op amp without negative feedback (a comparator)

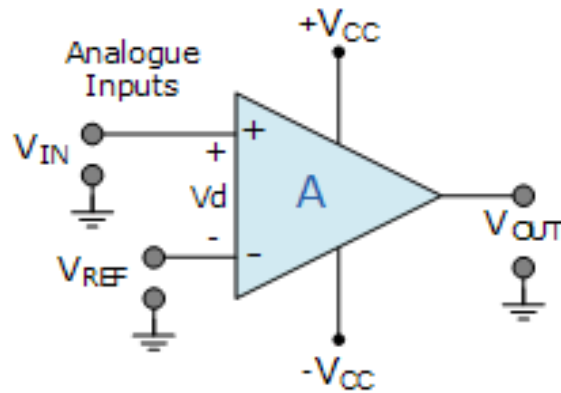


Figure 2.2: Op-Amp comparator. From

When $V_+ > V_-$ then $V_o = +V_{cc}$. When $V_+ < V_-$ then $V_o = -V_{cc}$

2.2.1 Non inverting (with feedback loop)

Amplifies the input but does not change its sign (non inverting). An op amp with negative feedback (a non-inverting amplifier)

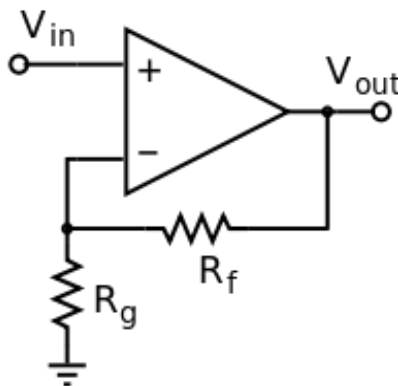


Figure 2.3: Op-Amp Feedback (Non inverting). From

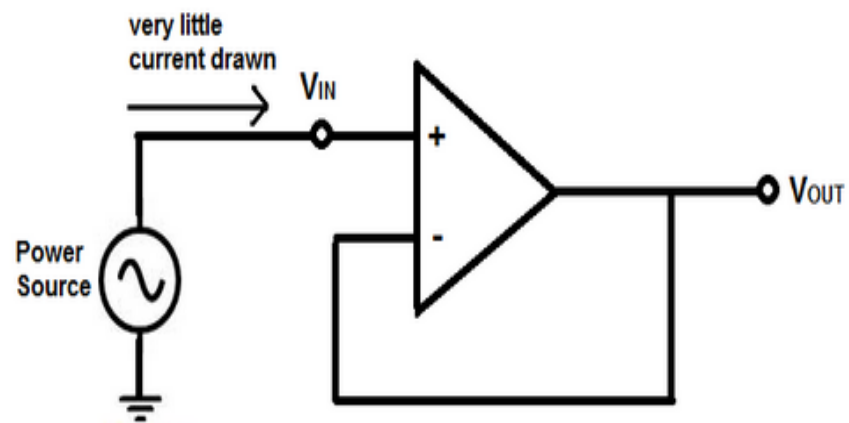
2.2.2 Voltage follower

Figure 2.4: Op-Amp voltage follower. From

$$v_+ = v_- = v_{in} = v_{out}$$

2.2.3 Inverting

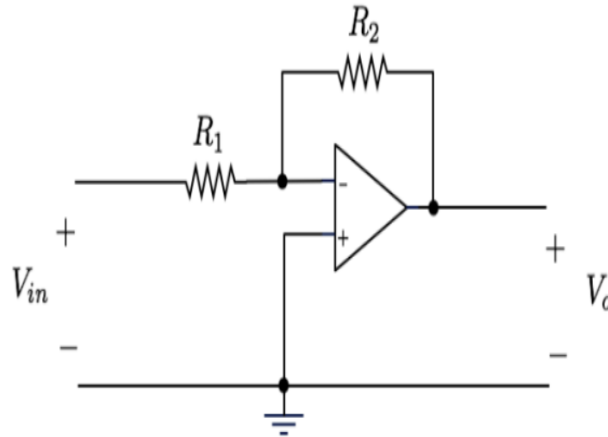


Figure 2.5: Op-Amp voltage follower. From

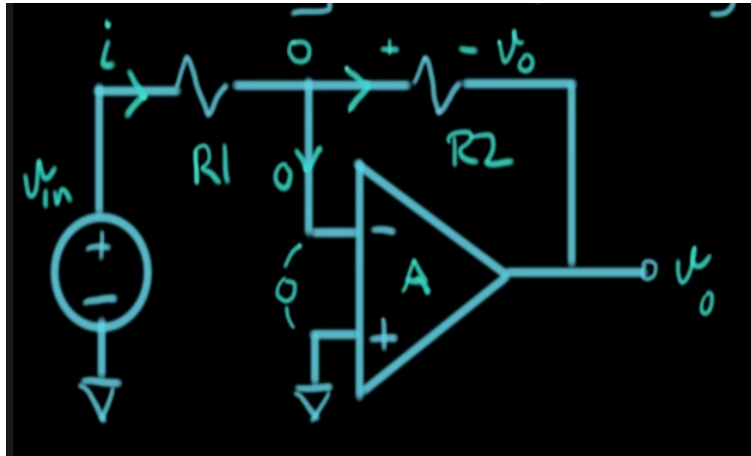


Figure 2.6: Op-Amp calculations for inverting. From

As seen from the image the current will be $i = v_{in}/R_1$ and $i = -v_o/R_2$. We combined them and get:

$$V_0 = \frac{-R_2}{R_1} V_{in}$$

2.2.4 Summing

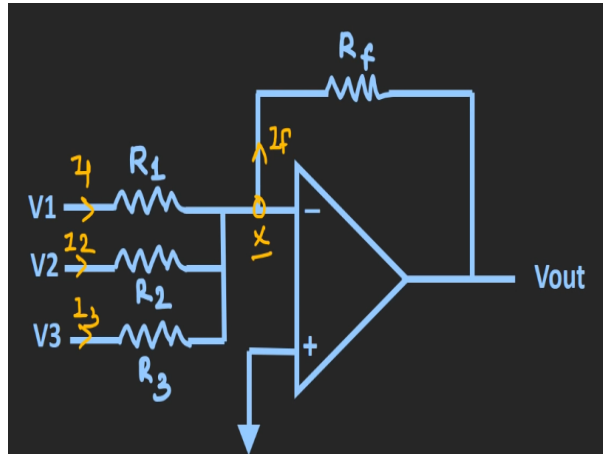


Figure 2.7: Op-Amp summing. From

Applying KCL we get: $I_f = I_1 + I_2 + I_3$ $\frac{v_1 - 0}{R_1} + \frac{v_2}{R_2} + \frac{V_3}{R_3} = \frac{0 - v_{out}}{R_f} \Rightarrow v_{out} = -(\frac{R_f}{R_1} V_1 + \frac{R_f}{R_2} V_2 + \frac{R_f}{R_3} V_3)$

2.3 General example

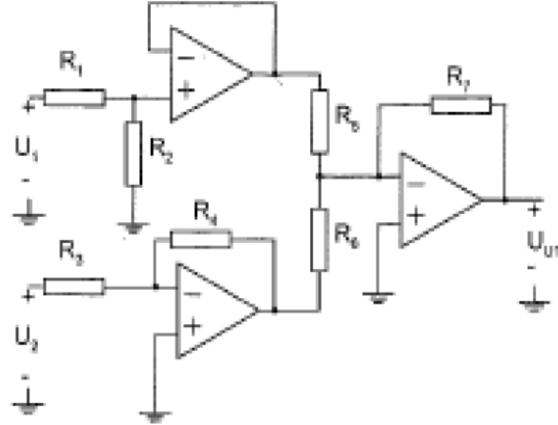


Figure 2.8: Op-Amp example. From

General observations: We can divide the circuit into three pieces. The one on the top is a *Voltage follower*, we can call it circuit 1. The one on the bottom is a *Inverting op-amp* as is the middle one. We can name the bottom one circuit 2 and the middle one is circuit 3.

We start with circuit 3:

We name node **A** between R_5 and R_6 . KCL: $I = I_5 + I_6$ and $I = I_7$ since there is no current in $-$ terminal.

$$I = \frac{-U_{out}}{R_7} = I_5 + I_6 = \frac{v_{O1}}{R_5} + \frac{v_{O2}}{R_6}$$

Because of Ohm's law and $v_{overresistor} = v_{head} - v_{tail}$.

To solve v_{O1} we need to solve circuit 1:

Applying KCL between R_1 and R_2 we get $I_1 = I_2 + I_3$ where $I_3 = 0$ since there is no current going in the $+$ terminal. $I_1 = I_2$ Ohm's law result in

$$\frac{U_1 - v_{O1}}{R_1} = \frac{v_{O1} - 0}{R_2} \text{ since in a voltage follow circuit}$$

$$v^- = v^+ = v_{out}. \text{ We then get } v_{out} = \frac{R_2}{R_1 + R_2} U_1$$

$$\text{then } I_5 = \frac{R_2}{(R_1 + R_2)R_5} U_1.$$

To solve v_{O2} we need to solve circuit 2:

KCL gives $I_3 = I_4$ since there is no current in $-$ terminal.

$$\text{Ohm's law } \frac{U_2 - v^-}{R_3} = \frac{v^- - v_{O2}}{R_4}.$$

$$v^- = v^+ = 0 \text{ with result in } \frac{U_2}{R_3} = \frac{-v_{O2}}{R_4}.$$

$$v_{O2} = \frac{-R_4}{R_3} U_2$$

$$\text{The current } I_6 = \frac{-R_4}{R_3 R_6} U_2$$

Going back to circuit 3:

$$I = I_5 + I_6 = \frac{R_2}{(R_1+R_2)R_5}U_1 + \frac{-R_4}{R_3R_6}U_2$$

$$\text{results in } \frac{-U_{out}}{R_7} = \frac{R_2}{(R_1+R_2)R_5}U_1 + \frac{-R_4}{R_3R_6}U_2.$$

$$\text{Final result: } U_{out} = -R_7\left(\frac{R_2}{R_5(R_1+R_2)}U_1 - \frac{R_4}{R_3R_5}U_2\right)$$