



$$\vec{q} = \underset{q}{\operatorname{argmin}} \sum_{i=0}^{|E|} \left(f_i - \sum_{\substack{j=0, \\ \text{if } e_i \in h_j}}^{|H|} q_j \right)^2 + \alpha \sum_{j=0}^{|H|} (q_j \neq 0)$$

haplotype (h_i)	frequency (q_i)
-C-A-T-	q_{CAT}
-C-A-A-	q_{CAA}
-C-C-T-	q_{CCT}
-C-C-A-	q_{CCA}
-A-A-T-	q_{AAT}
-A-A-A-	q_{AAA}
-A-C-T-	q_{ACT}
-A-C-A-	q_{ACA}

$$\begin{aligned} \delta_1 &= (0.40 - q_{CAT} - q_{CAA} - q_{CCT} - q_{CCA})^2 \\ \delta_2 &= (0.60 - q_{AAT} - q_{AAA} - q_{ACT} - q_{ACA})^2 \\ \delta_3 &= (0.65 - q_{CAT} - q_{CAA} - q_{AAT} - q_{AAA})^2 \\ \delta_4 &= (0.35 - q_{CCT} - q_{CCA} - q_{ACT} - q_{ACA})^2 \\ \delta_5 &= (0.75 - q_{CAT} - q_{CCT} - q_{AAT} - q_{ACT})^2 \\ \delta_6 &= (0.25 - q_{CAA} - q_{CCA} - q_{AAA} - q_{ACA})^2 \end{aligned} \Rightarrow \vec{q} = \begin{pmatrix} 0.40 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.35 \\ 0.25 \end{pmatrix}$$

$$\vec{q} = \underset{q}{\operatorname{argmin}} \sum_{i=0}^6 \delta_i + 0.3 \sum_{j=0}^8 (q_j \neq 0)$$