

# Risk Management

Exercises for participants of the programme **Quantitative Finance**

## C-Exercise 16

- (a) Write a *scilab*-function

$$e = \text{MEF}(x, u),$$

that evaluates the empirical mean excess function  $e_n$  at  $u < \max\{x_i : i = 1, \dots, n\}$  for  $n \in \mathbb{N}$  observations  $x = (x_1, \dots, x_n)$ .

- (b) Write a *scilab*-function

$$\text{MEP}(x),$$

that draws the mean excess plot for observations  $x = (x_1, \dots, x_n)$ .

- (c) Generate  $n = 500$  simulations for

- the t-distribution with  $\nu = 3$  degrees of freedom,
- the t-distribution with  $\nu = 6$  degrees of freedom,
- the exponential distribution with parameter  $\lambda = 1$ ,

and draw the corresponding mean excess plot.

- (d) Write a *scilab*-function

$$[\text{beta}, \text{gamma}] = \text{PoT\_Est}(x, u)$$

that estimates the parameters  $\beta, \gamma$  via maximum likelihood according to section 3.3.2

- (e) Write a *scilab*-function

$$[\text{VaR}, \text{ES}] = \text{VaR\_ES\_PoT}(x, p, u)$$

that computes the VaR and ES estimates from section 3.3.5 and 3.3.6 for  $n \in \mathbb{N}$  independent observations  $x = (x_1, \dots, x_n)$ ,  $u \in (0, \infty)$  and level  $p \in (0, 1)$ .

- (f) Take the data set from C-Exercise 15 and use a mean excess plot for a reasonable choice of  $u$ . Compute the estimates for VaR and ES at level  $p = 0.99$ .

