

```

diff --git a/cal_step1_solution.py b/cal_step1_solution.py
index 17d9dc2..e511adf 100644
--- a/cal_step1_solution.py
+++ b/cal_step1_solution.py
@@ -1,131 +1,151 @@
+
+
+## Please put everything in the docstring also the comments
+
+%%
+=====
+# CA 1: STEP 1
+=====
+''' Group 26:
+    Anton Gusarov
+    Martin Gustavsson
+'''
+import re
+import numpy as np
+import h5py
+import matplotlib
+from matplotlib import pyplot as plt
+from itertools import islice
+
+%% Simply reading the first 2 lines:
+with open('cal_step1_input_data.txt', 'r', errors='strict') as file: # opener is a custom callable
+    lines = list()
+    for i in range(2):
+        lines = file.readline()
+
+# %% Parse the main header of the file (first 2 lines):
+with open('cal_step1_input_data.txt', 'r', errors='strict') as file:
+    # read the header only i.e. the first 2 lines
+    # reg. expr. used where assumed that ',' or ';' are the separators:
+    lines = [re.split(r'[;,]', line) for line in islice(file.readlines(), 2)]
+
+header_keys = tuple(i.strip() for i in lines[0]) # remove trailing spaces by .strip()
+header_keys = tuple(re.sub(r'[\s#]', '', i) for i in header_keys)
+header_keys = tuple(re.sub(r'[\(\)]', '_', i) for i in header_keys)
+
+# %% remove all space characters from header line 2 and tx to float:
+header_values = [float(i.strip()) for i in lines[1]]
+header_values[0] = int(header_values[0]) # time_steps to be int
+header_values[4] = int(header_values[4]) # N_particles to be int
+
+# %% Create a dict {header_key -> header_value}:
+header = {}
+
+## Please use pythonic looping with zip, i.e.
+## for key, value in zip(header_keys, header_values):
+
+for i in range(len(header_keys)):
+    header[header_keys[i]] = header_values[i] # build dict incrementally
+
+locals().update(header) # unzip the dict to a set of variables
+
+# %% You need to identify the start of each time step by looking for the
+# time-step header # time_step. And then parse the N_particles rows
+# of position and velocity data in each time-step block
+
+# First task: print headers for time_step:
+with open('cal_step1_input_data.txt', 'r', errors='strict') as file:
+    for line in islice(file.readlines(), 4):
+        if '# time_step ' in line: print(line)
+
+# %%
+# Parse the data in each time-step block.
+# Store the data in a (three level) nested list called data.
+# 1. The first level should be the time step index,
+# 2. the second level the particle index,
+# 3. third level a list of the four values of the x, y position-
+# and v_x, v_y velocity-components stored as floating point numbers (float).
+
+inner_list_particle = []
+data = []
+particle_count = 0
+
+# The parser:
+with open('cal_step1_input_data.txt', 'r', errors='strict') as file:
+    for line in islice(file.readlines(), 3, None, None): # start from third line - skip the header
+        if (not line) or line.isspace(): # skip empty line: no symbols or only spaces
+            #print('empty string')
+            continue
+
+        if '# time_step ' in line:
+            time_step_index = int(''.join(re.findall(r'\d', line))) # parsed time-step index
+            #print('time step:', time_step_index, '\n')
+
+            if re.search(r'# ', line) is None: # find a line without '#' symbol i.e. with position and speeds numbers
+                inner_list_particle.append([float(i.strip()) for i in re.split(r'[;,]', line)])
+                particle_count += 1

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+
+         # Please do not hard code the number of particles
+
+         if particle_count == 400:
+
+             # This works, but is extra work for the computer
+             # Please do not copy the data and then remove the original
+
+             # Just pass the data along by appending it
+             # and set inner_list_particle to a new empty list []
+
+             data.append(inner_list_particle.copy())
+             inner_list_particle.clear()
+             particle_count = 0
+
+
+ print('data list size:', len(data), len(data[0]), len(data[0][0])) # check data list dimensions
+
+ # %% Convert a nested list to a multidimensional (NumPy) array
+ data = np.array(data)
+ print(type(data))
+ print(data.dtype)
+ print(data.shape)
+
+ # %% Split position vectors and velocity vectors
+ # To make the numerical analysis easier you want to store the final result in two separate ndarrays,
+ # one for the positions called R and one for the velocities called V
+ R = data[:, :, :2]
+ V = data[:, :, 2:]
+
+ print(R.shape)
+ print(V.shape)
+
+ # %% To swap the order of the axes use the NumPy "transpose-like" manipulation routines:
+ R = np.swapaxes(R, 1, 2)
+ V = np.swapaxes(V, 1, 2)
+
+ print(R.shape)
+ print(V.shape)
+
+ # %% Plot the first time step with Matplotlib
+ fig, axs = plt.subplots()
+ axs.set_aspect(aspect=1)
+ axs.scatter(R[0, 0, :], R[0, 1, :],
+             c='red', s=50.0, alpha=0.4, edgecolors='none')
+ plt.xlim(-1, 1)
+ plt.ylim(-1, 1)
+ plt.show(fig)
+
+ # %% Storing data using the hdf5 file format
+ # use its h5py.File class together with the 'with'-statement to open the file cal_step1_output_data.h5 file.
+ # Use '.create_dataset' method to store the ndarrays R and V,
+ # and store the other parameters as attributes using the .attrs.create method.
+
+ with h5py.File('cal_step1_output_data.h5', 'w') as hfile:
+     dset1 = hfile.create_dataset('R', data=R)
+     dset1 = hfile.create_dataset('V', data=V)
+
+ +     # Please store the attributes in the root of the hdf5 file not in dset1
+ +     # using the function pointed out in the description
+ +
+     dset1.attrs['N_particles'] = N_particles
+     dset1.attrs['time_steps'] = time_steps
+     dset1.attrs['time_step_s'] = time_step_s
+     dset1.attrs['radius'] = radius
+     dset1.attrs['v_variance'] = v_variance
+
+ diff --git a/cal_step3_solution.py b/cal_step3_solution.py
+ index a8bfdff..502ecaa 100644
+ --- a/cal_step3_solution.py
+ +++ b/cal_step3_solution.py
+ @@ -1,216 +1,235 @@
+ +
+ +## use docstring here not comments
+ +
+ +##%
+ + # =====
+ + #         CA 1: STEP 3
+ + # =====
+ + import os
+ + import itertools
+ + import h5py
+ + from scipy import stats
+ + from scipy.spatial import distance
+ + import numpy as np
+ + from numpy import random
+ + from matplotlib import pyplot as plt
+ + import matplotlib.animation as animation
+
+ from scipy.spatial import distance
+ from scipy.spatial import cKDTree

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```

from cal_step_2_solution import animate_particles
from cal_step_2_solution import plot_statistical_analysis

+# Please move all functions here and put the other code after them
+
%%
# 1. Particle system initialization
#-----
N_particles = 400
sigma_v = 0.1
r0 = 2 * random.rand(2, N_particles) - 1
v0 = sigma_v * random.randn(2, N_particles)

print(r0.shape, v0.shape) # shape check

# sanity check plot of initial positions:
x0, y0 = r0[0, :], r0[1, :]
fig, axs = plt.subplots()
axs.set_aspect(aspect=1)
axs.scatter(x0, y0, color='green', s=50.0, alpha=0.4, edgecolors='none')
plt.xlim(-1.1, 1.1)
plt.ylim(-1.1, 1.1)
plt.show(fig)

# %%
# 2. Time propagation
#-----
time_step = 0.02 # 50 steps/sec

def time_propagation(r, v, time_step):
    r = r + v * time_step # broadcasting was used to implement this in a single line
    return r, v

r, v = time_propagation(r0, v0, time_step) # call the function

# sanity check plot of time propagation:
x, y = r[0, :], r[1, :]
fig, axs = plt.subplots()
axs.set_aspect(aspect=1)
axs.scatter(x, y, color='blue', s=50.0, alpha=0.4, edgecolors='none')
plt.xlim(-1.1, 1.1)
plt.ylim(-1.1, 1.1)
plt.show(fig)

# %%
# 3. Simulation function
#-----
# The function uses the time_propagation function to compute
# the time evolution of the particles for a given number of 'time_steps'
# and returns the positions R and velocities V of all particles for all time steps.

def simulate(r0, v0, time_step, time_steps, update_function, **kwargs):
    # Allocate R and V:
    R = np.empty((time_steps, r0.shape[0], r0.shape[1]))
    V = np.empty((time_steps, v0.shape[0], v0.shape[1]))

    # Initialize R[0] and V[0] using r0 and v0:
    R[0, :, :] = r0
    V[0, :, :] = v0

    # Loop over all time steps and call:
    for t in range(1, time_steps):
        R[t, :, :], V[t, :, :] = update_function(R[t-1, :, :], V[t-1, :, :], time_step, **kwargs)
    return R, V

simulation1 = simulate(
    r0, v0, time_step, time_steps=400,
    update_function=time_propagation)

%%
# call the animation:
animate_particles(simulation1[0], time_step, filename='cal_step3_movie1.mp4')

# %%
# 4. Hard wall boundary collisions
#-----
# -- check if the position coordinates (x and y) are out of bounds and
# -- the particle at the same time has a velocity component going in the wrong direction (relative to the "wall").
# -- In this case change the sign of the corresponding velocity component (v_x or v_y)

# Use numpy boolean arrays for indexing so that each line of code treats all particles at the same time.
# Modify the velocity vector v in-place so that the function does not have to return anything.

def boundary_collisions(r, v):
    ''' Modifies the velocity vector according to the hard wall boundary conditions.
    '''

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+ # Please add the check of the velocity components
+ # Without it particles tend to get stuck at the boundaries and even go outside it
+
boundary = np.full(r.shape, 1) # defines the abs value of coordinates |x| or |y|
boundary_check = np.greater(np.absolute(r), boundary) # returns True if any module of coordinate > 1
boundary_check = -2 * boundary_check.astype(int) + 1 # True/False to -1/1
v = np.multiply(boundary_check, v) # changes the sign of v components for where boundary_check is True
return r, v

def update_with_boundaries(r, v, time_step):
    ''' Time propagation with boundary conditions.
    '''
    r, v = time_propagation(r, v, time_step)
    r, v = boundary_collisions(r, v)
    return r, v

simulation2 = simulate(
    r0, v0, time_step, time_steps=400,
    update_function=update_with_boundaries)

animate_particles(simulation2[0], time_step, 'cal_step3_movie2.mp4')

# %%
# 5. Particle-particle collision
#-----
# -- loops over all pairs of particles,
# -- check if they are closer to each other than 2*radius and are travelling towards each other.
# -- If yes then modify their velocity vectors according to a momentum conserving collision.

radius = 0.05
def particle_collisions(r, v, radius):
    dist = distance.pdist(np.swapaxes(r, 0,1), metric='euclidean') # returns condensed vector of distances
    dist = distance.squareform(dist) # find pairs closer to each other than 2*radius

    check_dist = np.less(dist, 2*radius)
    np.fill_diagonal(check_dist, False) # fill diagonal
    check_dist = np.triu(check_dist) # remove duplicates due to symmetry
    indx = np.asarray(np.where(check_dist==True)) # return indices of pairs where distance is smaller than 2*r

    indx = np.split(indx, indx.shape[1], axis=1)
    for i in indx: # i - pair of indexes of the colliding particles
+
+         # Please add the check on the velocities that ensures that the
+         # particles are travelling towards each other.
+
+         # Please work with vector expressions instead of treating the x and y
+         # components separately
+
        # v_i = v[:, i[0]] # i-particle pair of v components (x, y)
        # v_j = v[:, i[1]] # j-particle pair of v components (x, y)

        v_i_x = v[:, i[0]][0] - (v[:, i[0]][0] - v[:, i[1]][0])
        v_i_y = v[:, i[0]][1] - (v[:, i[0]][1] - v[:, i[1]][1])

        v_j_x = v[:, i[1]][0] + (v[:, i[0]][0] - v[:, i[1]][0])
        v_j_y = v[:, i[1]][1] + (v[:, i[0]][1] - v[:, i[1]][1])

        v[:, i[0]] = [v_i_x, v_i_y]
        v[:, i[1]] = [v_j_x, v_j_y]
    return r, v

def update_with_interactions_slow(r, v, time_step, radius):
    r, v = time_propagation(r, v, time_step)
    r, v = boundary_collisions(r, v)
    r, v = particle_collisions(r, v, radius)
    return r, v

simulation3 = simulate(
    r0, v0, time_step, time_steps=100,
    update_function=update_with_interactions_slow, radius=radius)

animate_particles(simulation3[0], time_step, 'cal_step3_movie3.mp4')

# %%
# 6. Fast hard spheres
#-----
# Use the KDTree class in scipy.spatial to rapidly find all pairs of particles
# closer than two times the radius to each other.

def particle_collisions_fast(r, v, radius):
    tree = cKDTree(np.swapaxes(r, 0,1))
    dist_set = tree.query_pairs(2*radius) # method; returns Python SET of pairs of points whose distance is at most r

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for i in list(dist_set): # i - pair of indexes of the colliding particles
+
+     # Please consider all the comments in the function `particle_collisions` above
+
    # v_i = v[:, i[0]] # i-particle pair of v components (x, y)
    # v_j = v[:, i[1]] # j-particle pair of v components (x, y)

    v_i_x = v[:, i[0]][0] - (v[:, i[0]][0] - v[:, i[1]][0])
    v_i_y = v[:, i[0]][1] - (v[:, i[0]][1] - v[:, i[1]][1])

    v_j_x = v[:, i[1]][0] + (v[:, i[0]][0] - v[:, i[1]][0])
    v_j_y = v[:, i[1]][1] + (v[:, i[0]][1] - v[:, i[1]][1])

    v[:, i[0]] = [v_i_x, v_i_y]
    v[:, i[1]] = [v_j_x, v_j_y]
return r, v

def update_with_interactions_fast(r, v, time_step, radius):
    r, v = time_propagation(r, v, time_step)
    r, v = boundary_collisions(r, v)
    r, v = particle_collisions_fast(r, v, radius)
    return r, v

simulation4 = simulate(
    r0, v0, time_step, time_steps=1000,
    update_function=update_with_interactions_fast, radius=radius)

animate_particles(simulation4[0], time_step, 'cal_step3_movie4.mp4')

# %%
# 7. Statistical analysis of interacting particles
#-----
plot_statistical_analysis(simulation4[0], simulation4[1], time_step, 'cal_step3_figure_summary.svg')

diff --git a/cal_step_2_solution.py b/cal_step_2_solution.py
index 446ebel..ebfaadd 100644
--- a/cal_step_2_solution.py
+++ b/cal_step_2_solution.py
@@ -1,219 +1,246 @@
+
+ # Please use a docstring here not comments
+
# %%
# =====
# CA 1: STEP 2
# =====
import os
import itertools
import h5py
from scipy import stats
from scipy.spatial import distance
import numpy as np
from matplotlib import pyplot as plt
import matplotlib.animation as animation

def plot_statistical_analysis(R, V, time_step, filename):
    """
    Analyzes R and V and plots statistical analysis results
    """
    time = np.arange(0, R.shape[0]*time_step, time_step) # [sec]

+
+ # General comment on reshaping of arrays
+
+ # Please do not hard code the dimensions in the reshaping of arrays
+ # This makes your function only work for 1000 timesteps with 400 particles
+
+ # Instead of doing reshaping with given shapes please use the ndarray method .flatten()
+
+ # It is also convenient to refrain from defining flattened variables and instead
+ # flatten the array when calling .fit and .hist, i.e.
+ # plt.hist(R[:, 0, :].flatten(), ...)
+
    # Prepare data for x,y velocities and coordinates plots:
    #-----
    # 1. x and y positions:
    R_resaped_x = np.reshape(R[:,0,:], (400*1000,))
    R_resaped_y = np.reshape(R[:,1,:], (400*1000,))
    V_resaped_x = np.reshape(V[:,0,:], (400*1000,))
    V_resaped_y = np.reshape(V[:,1,:], (400*1000,))

    v_x_loc, v_x_scale = stats.norm.fit(V_resaped_x) # fit model to the data
    v_x_pdf = stats.norm.pdf(np.arange(-0.5, 0.5, 0.01), loc=v_x_loc, scale=v_x_scale) # modelled distribution

    v_y_loc, v_y_scale = stats.norm.fit(V_resaped_y)
    v_y_pdf = stats.norm.pdf(np.arange(-0.5, 0.5, 0.01), loc=v_y_loc, scale=v_y_scale)

    x_loc, x_scale = stats.uniform.fit(R_resaped_x)
    x_pdf = stats.uniform.pdf(np.arange(-1.5, 1.5, 0.01), loc=x_loc, scale=x_scale)

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y_loc, y_scale = stats.uniform.fit(R_reshaped_y)
y_pdf = stats.uniform.pdf(np.arange(-1.5, 1.5, 0.01), loc=y_loc, scale=y_scale)

plt.subplots_adjust(left=None, bottom=None, right=None, top=None,
                    wspace=0.5, hspace=0.7) # Tune the subplot layout

# Prepare data for pair distance distribution function:
#-----
+
+ # Please use NumPy broadcasting to implement thie pair distances
+ # The goal is use the basic mechanism of broadcasting (not scipy.spatial.distance.pdist)
+

R_split_time = np.split(R, R.shape[0], axis=0)
def calculate_distances(R_split_time):
    dist = distance.pdist(np.swapaxes(np.squeeze(R_split_time), 0, 1),
                          metric='euclidean') # returns condensed vector of distances
    return dist
Dist = list(map(calculate_distances, R_split_time)) # produces the list of condensed distances
Dist = np.asarray(Dist) # (1000, 79800) ndarray

# Prepare data for velocity norm pdf:
#-----
V_norm = np.linalg.norm(V, ord=2, axis=1)
V_reshaped = np.reshape(V_norm, (400*1000,))
v_loc, v_scale = stats.rayleigh.fit(V_reshaped)
v_pdf = stats.rayleigh.pdf(np.arange(0, 0.5, 0.01), loc=v_loc, scale=v_scale)

# Prepare data for E_k and V_tot:
#-----
V_sum = np.sum(V, 2)
V_tot = np.linalg.norm(V_sum, ord=2, axis=1)

+ # This is the second time the function computes V_norm
+ # Please remove one of the calculations
+
V_norm = np.linalg.norm(V, ord=2, axis=1)
- V_norm.shape
+
+ # This row of code is not doing anything please clean up
+ V_norm.shape
+

E_k = np.sum(np.square(V_norm)/2, 1)

# PLOTS:
#=====
plt.figure(1, figsize=(20, 30)) # â\200\231figsize â\200\231 to make the figure larger
plt.subplots_adjust(left=None, bottom=None, right=None, top=None,
                    wspace=0.5, hspace=1.5) # Tune the subplot layout

# V_tot plot:
#-----
plt.subplot(4,2,1)
plt.plot(time, V_tot, color='blue', linewidth=1.5)
plt.xlabel('Time')
plt.ylabel('Total velocity')
plt.grid(True)

# E_k plot:
#-----
plt.subplot(4,2,2)
plt.plot(time, E_k, color='blue', linewidth=1.5)
plt.ylim(0, 5) # can be removed to look at the noisy component
plt.xlabel('Time')
plt.ylabel('Kinetic energy')
plt.grid(True)

# pair distance distribution function plot:
#-----
plt.subplot(4,2,3)
plt.hist(Dist[500], 70, density=True, facecolor='blue', alpha=0.75) # plot hist only at a single time-point
plt.xlabel('Pair distance, $d_{ij}$')
plt.ylabel('Probability')
plt.xlim(0, 3.0) # can be removed to look at the noisy component
plt.grid(True)

# Plot velocity norm pdf and hist:
#-----
plt.subplot(4,2,4)
plt.hist(V_reshaped, 70, density=True, facecolor='blue', alpha=0.75)
plt.plot(np.arange(0, 0.5, 0.01), v_pdf, linewidth=2, color='red')
plt.xlabel('Velocity norm')
plt.ylabel('Probability')
plt.xlim(0, 0.5) # can be removed to look at the noisy component
plt.grid(True)

# Plots for x,y velocities and coordinates:
#-----
plt.subplot(4,2,5) # Position number option
plt.hist(V_reshaped_x, 40, density=True, facecolor='blue', alpha=0.75)
plt.plot(np.arange(-0.5, 0.5, 0.01), v_x_pdf, linewidth=2, color='red')

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plt.xlabel('x velocities')
plt.ylabel('Probability')
plt.xlim(-0.4, 0.4) # can be removed to look at the noisy component
plt.grid(True)

plt.subplot(4,2,6) # Position number option
plt.hist(V_resaped_x, 40, density=True, facecolor='blue', alpha=0.75)
plt.plot(np.arange(-0.5, 0.5, 0.01), v_x_pdf, linewidth=2, color='red')
plt.xlabel('y velocities')
plt.ylabel('Probability')
plt.xlim(-0.4, 0.4) # can be removed to look at the noisy component
plt.grid(True)

plt.subplot(4,2,7)
plt.hist(R_resaped_x, 70, density=True, facecolor='blue', alpha=0.75)
plt.plot(np.arange(-1.5, 1.5, 0.01), x_pdf, linewidth=2, color='red')
plt.xlabel('x coordinates')
plt.ylabel('Probability')
plt.xlim(-1.5, 1.5) # can be removed to look at the noisy component
plt.grid(True)

plt.subplot(4,2,8)
plt.hist(R_resaped_y, 70, density=True, facecolor='blue', alpha=0.75)
plt.plot(np.arange(-1.5, 1.5, 0.01), y_pdf, linewidth=2, color='red')
plt.xlabel('y coordinates')
plt.ylabel('Probability')
plt.xlim(-1.5, 1.5) # can be removed to look at the noisy component
plt.grid(True)

plt.savefig(filename)
plt.show()

def animate_particles(R, time_step, filename='movie.mp4'):
    """Generates an mp4 movie with the particle trajectories
    using Matplotlib. """

    if os.path.isfile(filename):
        print('WARNING (animate_particles): The output file', filename, 'exists. Skipping animation.')
        return

    frames = R.shape[0]
    frames_per_second = 1. / time_step

    fig = plt.figure(figsize=(6, 6))
    ax = plt.subplot()

    plt.xlabel('x')
    plt.ylabel('y')
    plt.axis('image')
    plt.xlim([-1.0, 1.0])
    plt.ylim([-1.0, 1.0])

    markers = ax.scatter([], [], facecolor='red', s=180, alpha=0.5)
    text = plt.text(-0.9, 0.9, 'frame =', ha='left')

    def update(frame, markers, text):
        print('frame =', frame)
        r = R[frame]
        markers.set_offsets(r.T)
        text.set_text('frame = {}'.format(frame))

    anim = animation.FuncAnimation(
        fig, update,
        frames=frames, interval=50,
        fargs=(markers, text),
        blit=False, repeat=False,
    )

    writer = animation.writers['ffmpeg'](fps=frames_per_second)
    anim.save(filename, writer=writer, dpi=100)
    plt.close()

if __name__ == '__main__':
    # Read h5:
    with h5py.File('cal_step1_output_data.h5', 'r') as hfile:
        print(hfile.keys())

        dataset_R = hfile['R']
        R = dataset_R[:]
        dataset_V = hfile['V']
        V = dataset_V[:]

        time_step_s = dataset_V.attrs['time_step_s']
        radius = dataset_V.attrs['radius']
        v_variance = dataset_V.attrs['v_variance']

```

+
+ # Calling del on hfile is not required since you used the with statement
+

```
del dataset_R, dataset_V, hfile

# Plot the y-position of particle number 123 as a function of time t:
y_position_n123 = R[:, 1, 123]
time = np.arange(0, R.shape[0]*time_step_s, time_step_s) # [sec]

plt.plot(time, y_position_n123,
         color='red', linewidth=1.5)
plt.title('Particle 123 y-position')
plt.xlabel('Time')
plt.ylabel('y-position')
plt.grid(True)
plt.show()

# Call the statistical plots function:
plot_statistical_analysis(R, V, time_step_s, filename='cal_step2_figure_summary.svg')
# Call the animation function:
animate_particles(R, time_step_s, filename='cal_step1_movie.mp4')
```