

# Transformers

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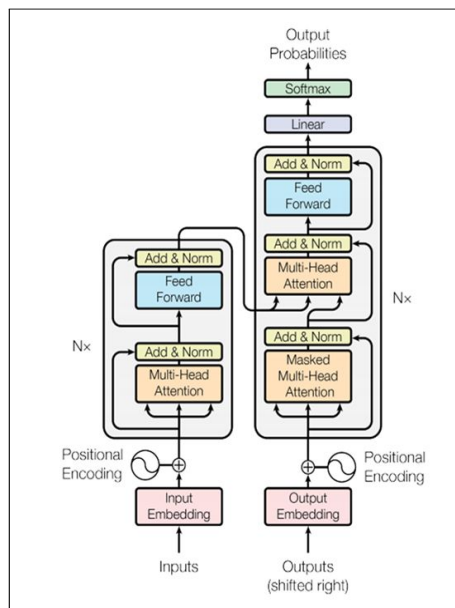
*Amazing video regarding transformers with great visuals available and recommended here: [\[1\]](#)*

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# 1 Transformers



- There are  $n$  amounts of encoders and  $n$  amounts of decoders.
- Within one layer (encoder or decoders) we have multiple sub-layers
- In the encoder, we have 2 sub-layers, which processes multi-head attention and the add and norm, the second sub-layer has a feed forward network and add & norm.
- In the decoder we have 3 sublayers, which is the masked multi-head attention, sublayer 2 (which is also known as cross attention) and sublayer three which is a feed-forward network.




The original paper utilizes this as an encoder decoder network.

**Transformer Encoder**

**Tasks:**

- Classification
- Masked language modelling
- Named entity recognition

**Popular models:**

- BERT 
- RoBERTa 
- DeBERTa 




(a) Classification tasks, feeding in a sequence and get a prediction over full input (sentiment classification) or a subset (entity recognition).

**Transformer Encoder-decoder**

**Tasks:**

- Translation
- Summarization
- Free-form QA

**Popular models:**

- Original Transformer 
- T5 
- BART 


(b) Sequence to sequence tasks

**Transformer Decoder**

**Tasks:**

- Causal language modelling
- Text generation

**Popular models:**

- GPT (1-3) 




(c) For language specific task such as text generation or language modelling

**Vision Transformers**

**Tasks:**

- Visual classification
- Object detection
- Image generation

**Popular models:**

- ViT 
- DINO 
- DETR 




(d) Use in place of CNNs, object detection or generation

**Multimodal Transformers**

**Tasks:**

- Image captioning/descriptions
- Language-based image querying
- Generating images from text descriptions

**Popular models:**

- ViLBERT 
- CLIP 
- DALL-E 



(e) Incorporating more than one modality (e.g. text, image, sound). So, generating images from text, or image captioning from an image.

**Other Uses**

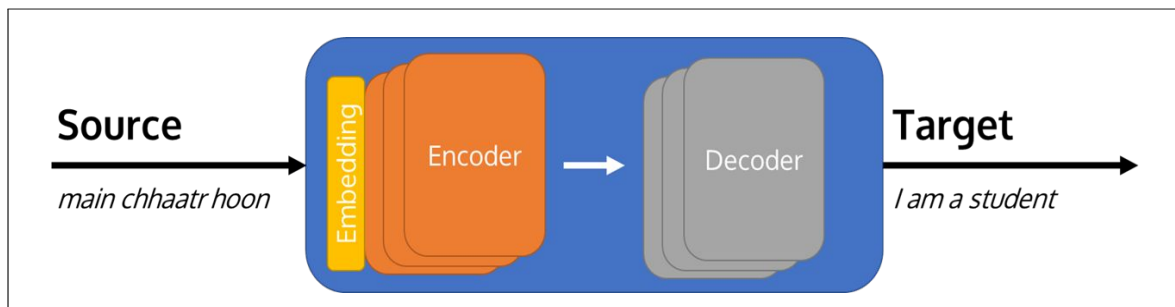
**Tasks:**

- Predicting protein structures
- Basic reasoning tasks

**Popular models:**

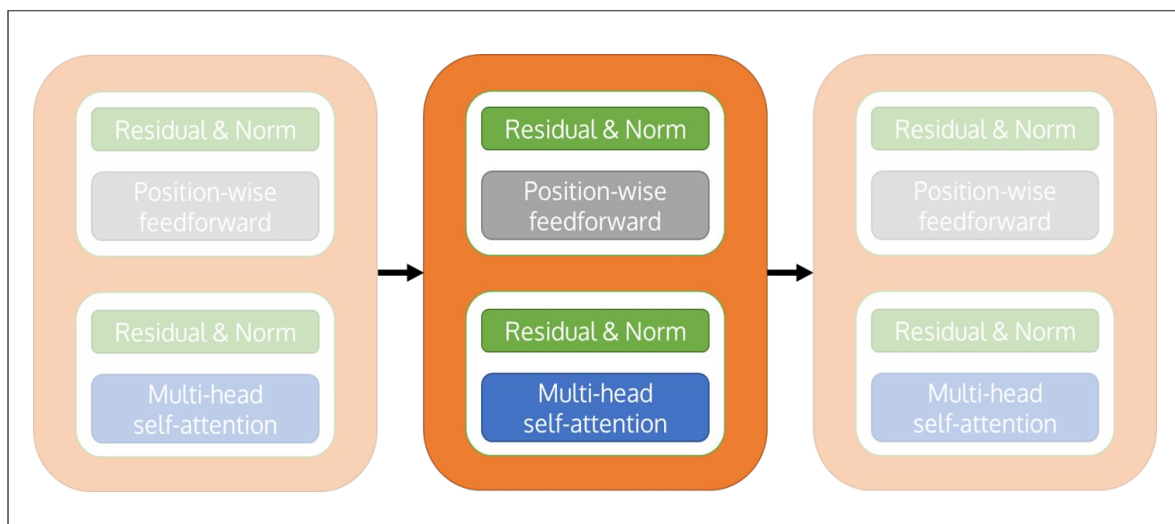
- AlphaFold 
- Maths word problems 

(f)

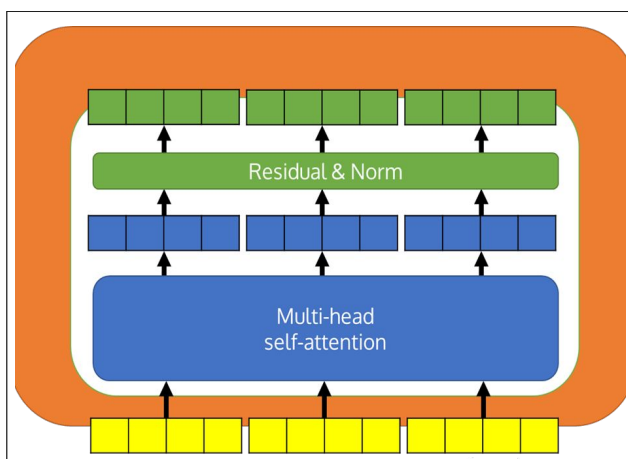


Like with other translation, the Transformer takes in a source sentence and generates a target. Inside, the transformer, we have a stack of encoder layers and a stack of decoder layers. At some point, we use the encoded output to help us generate the target. Note that the output of one encoder layer is sent as input to the next encoder layer. Similarly, the output of one decoder layer is sent to the next decoder layer as input

## 2 Transformer — Encoder



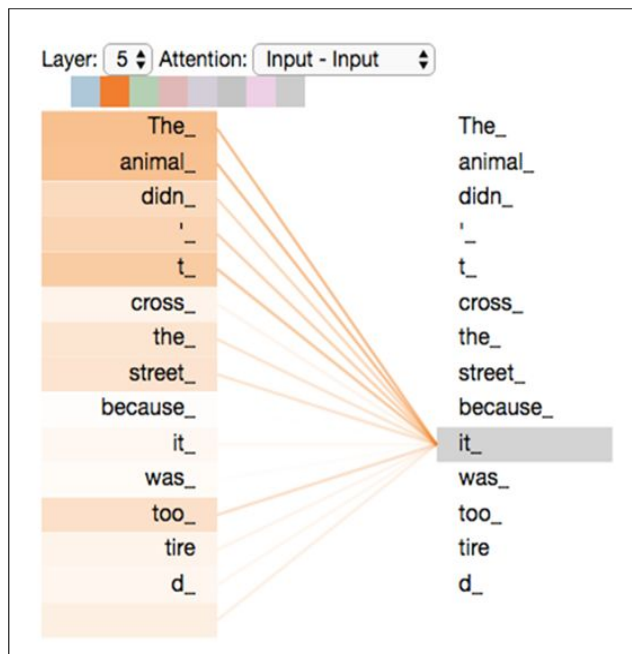
The output of the first encoder serves as the input for the second encoder. There are two sublayers. The first sublayer contains a multi-head self-attention module, and the second contains a position-wise feed forward network. A common theme in Transformers is that each sublayer will have a residual connection and layer normalization



- The multi-head self-attention receives some input, the yellow, which are some word representations (here, with 4 dimensions each). Generally, we have  $S$  words, each with  $D$  dimensions.
- The multi-head self-attention layer processes the input and outputs another set of  $S \times D$  encodings.
- These encodings get sent to the Residual & Norm, which outputs another set of  $S \times D$  encodings
- Conceptually this should make transformers easy to work with -mostly everything in the encoder stays as  $S \times D$ .

## 2.1 Self-attention

The self-attention mechanism allows each input in a sequence to look at the whole sequence to compute a representation of the sequence. Each word therefore gets a representation based on all the other words in the input sequence. Each  $S$  in an  $S \times D$  input has looked at every other word to compute its  $D$ -dimensional representation.



- As an example: “the animal didn’t cross the street because it was too tired”
- If we were processing this sequence, we would have some hidden state representation for the word “it”.
- In an RNN, the word “it” hasn’t been explicitly forced to look at other words in the sequence to align itself within them; the importance of words would be equal where we don’t want them to be
- Transformers are designed such that the hidden state representation of the word “it” would be influenced more by “animal” than “because”.
- For self-attention, each input (e.g. “it”) looks at the whole sequence and then computes a representation of that word, based on how important each of the other words are to it.s

The attention function consists of 3 variables

$$\text{Attention}(Q, K, V) = \sigma\left(\frac{QK^T}{\sqrt{d_h}}\right)V, \quad \text{Q: Queries, K: Keys, V: Values, } \sigma : \text{softmax} \quad (2.1.1)$$

### 2.1.1 Vector form

1. Define a Q
2. Calculate similarity of Q against the Ks
3. Output is the weighted sum of Vs

#### Q = Yellow

- Exact match with K = Yellow
- Therefore value = (255, 255, 0)

#### Q = Orange

- 50% K = Red, 50% K = Yellow
- Value =  $0.5(255, 0, 0) + 0.5(255, 255, 0)$   
= (255, 128, 0)

Colour (K)	RGB (V)
Red	(255, 0, 0)
Green	(0, 255, 0)
Blue	(0, 0, 255)
Yellow	(255, 255, 0)
Black	(0, 0, 0)
White	(255, 255, 255)

Think of it as a look-up in a dictionary (color to RGB value)

1. The query is the colour we want to find.
2. We would index the dictionary and receive a direct match
3. If the query is “orange” we want 50% red and 50% yellow and combine them

<b>Q = [0, 10, 0]</b> <ul style="list-style-type: none"> <li>Exact match with [0, 10, 0]</li> <li>V = [10, 0, 2]</li> </ul>	Key	Value
	[10, 0, 0]	[1, 0, 1]
	[0, 10, 0]	[10, 0, 2]
	[0, 0, 10]	[100, 5, 0]
	[0, 0, 10]	[1000, 6, 0]

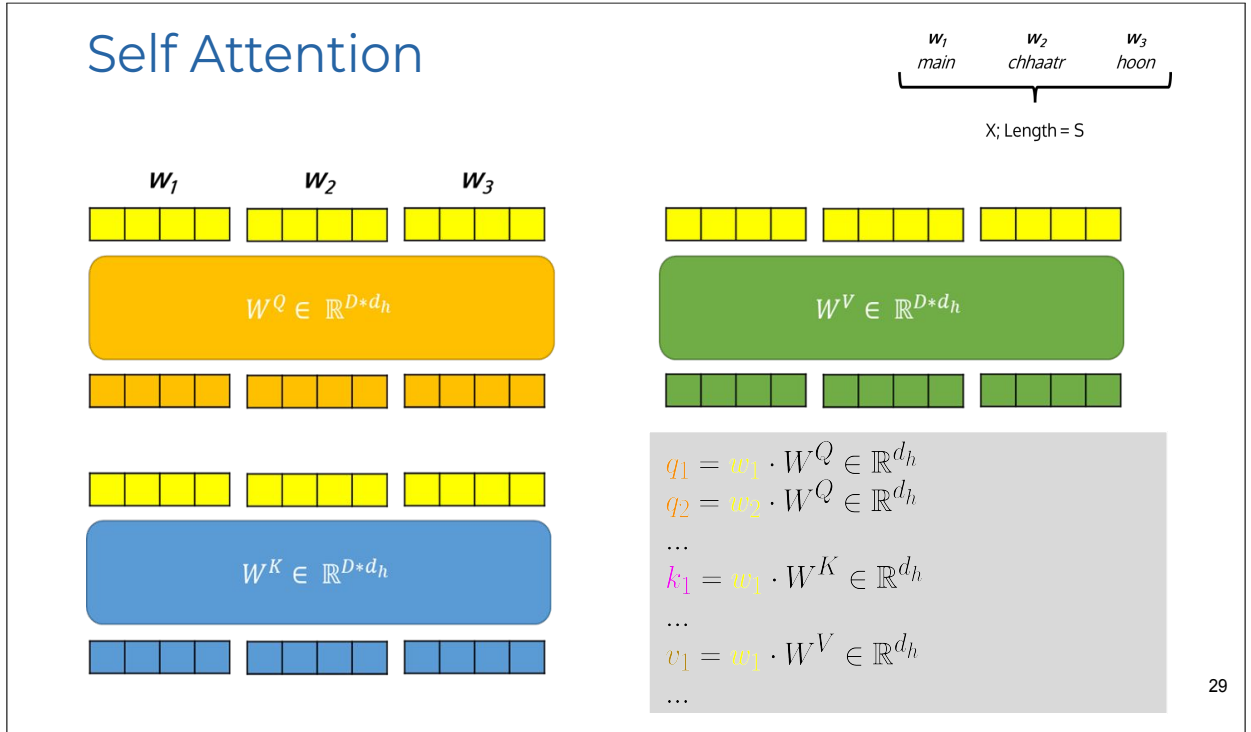
(g) direct match

<b>Q = [0, 0, 10]</b> <ul style="list-style-type: none"> <li>Matches the two [0, 0, 10]'s</li> <li>V = 0.5*[100, 5, 0] + 0.5*[1000, 6, 0]</li> <li>= [550, 5.5, 0]</li> </ul>	Key	Value
	[10, 0, 0]	[1, 0, 1]
	[0, 10, 0]	[10, 0, 2]
	[0, 0, 10]	[100, 5, 0]
	[0, 0, 10]	[1000, 6, 0]

(h) matches two keys

<b>Q = [10, 10, 0]</b> <ul style="list-style-type: none"> <li>Matches [10, 0, 0] and [0, 10, 0]</li> <li>V = 0.5*[1, 0, 1] + 0.5*[10, 0, 2]</li> <li>= [5.5, 0, 1.5]</li> </ul>	Key	Value
	[10, 0, 0]	[1, 0, 1]
	[0, 10, 0]	[10, 0, 2]
	[0, 0, 10]	[100, 5, 0]
	[0, 0, 10]	[1000, 6, 0]

(i) matches two keys, but in a combination



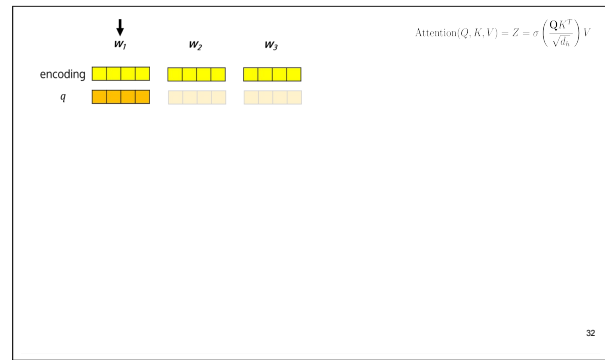
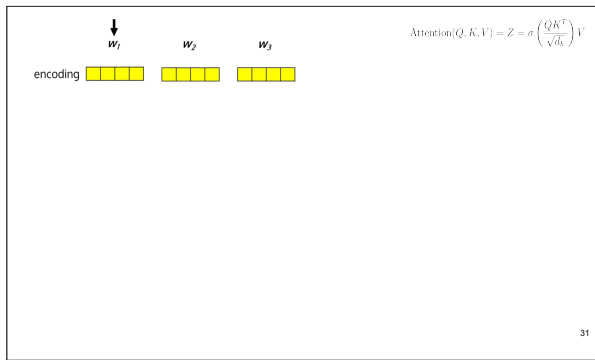
First, we take our word embeddings and project them through a learnt weight matrix, to a representation  $D \times d_h$ . Firstly, we set  $d_h$  equal to  $D$ . We do the same for our keys and values.

We can simplify the above to do everything in matrix form:

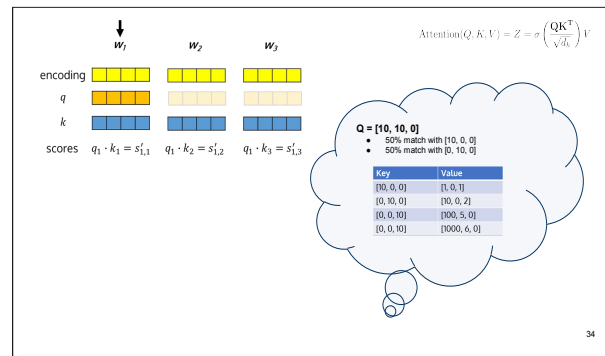
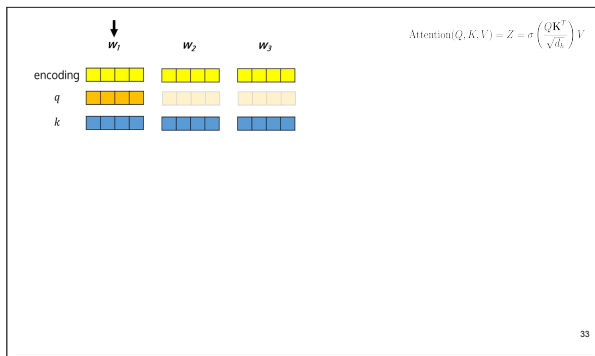
$$Q = W \cdot W^Q \in \mathbb{R}^{S \times d_h} \quad (2.1.2)$$

$$K = W \cdot W^K \in \mathbb{R}^{S \times d_h} \quad (2.1.3)$$

$$V = W \cdot W^V \in \mathbb{R}^{S \times d_h} \quad (2.1.4)$$

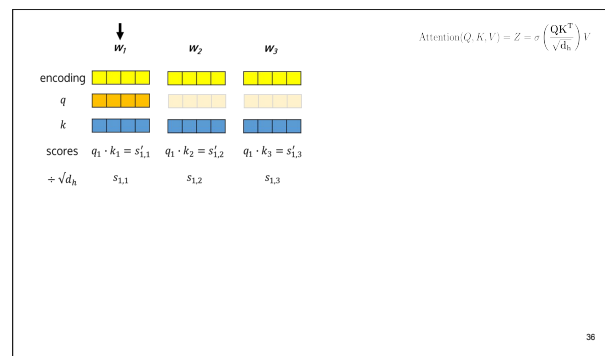
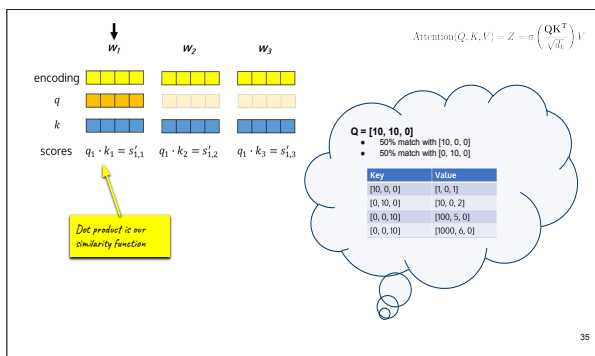


(j) Looking at attention in vector form first, we're going to (k) Due to the projections above, we have query vectors for work out our attention-ized representation for each word. all words. Right now, we only need the query vector for  $w_1$ . Let's start with  $w_1$



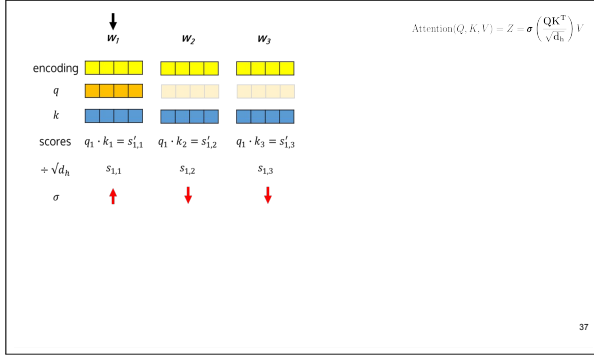
(l) Thinking back to the intuition, we want to compare how similar the query is to all keys we have. This is done by the query vector we have, and ALL the key vectors. We some similarity function. So here, we want to get a representation for  $w_1$ . We will get this representation by comparing our query vector to all our keys.

(m) Now we're going to work out the similarity between the query vector we have, and ALL the key vectors. We then obtained a weighting for how similar each of the key vectors were to the query vector. The score here is NOT the weighting, whoever, we need it in our calculation of the weighting

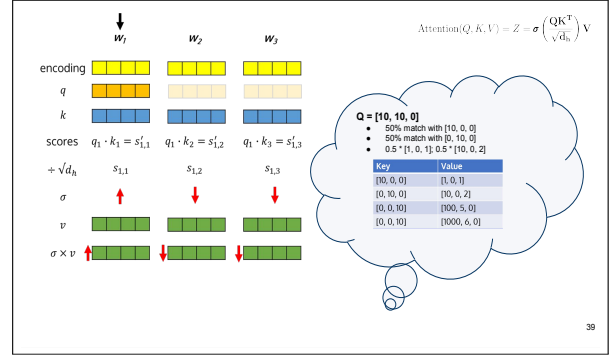


(n) Lets say the similarity is the dot product, so we get an un-normalized similarity between the given query vector and key vectors.

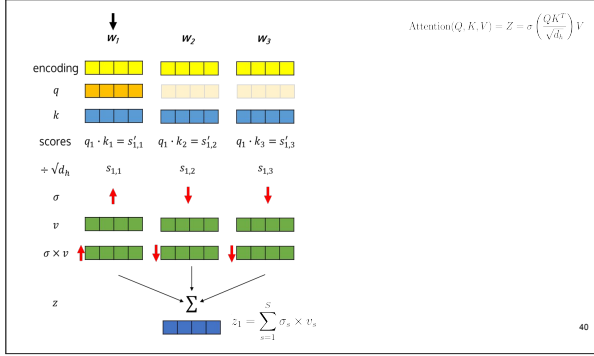
(o) In the next step, apply softmax, but before we do this, divide by  $\sqrt{d_h}$ . Post-division values are now closer to 0. This makes the softmax operation less peaky. That means that the outputs of the softmax operation will ideally not have an individual value which dominates the weightings



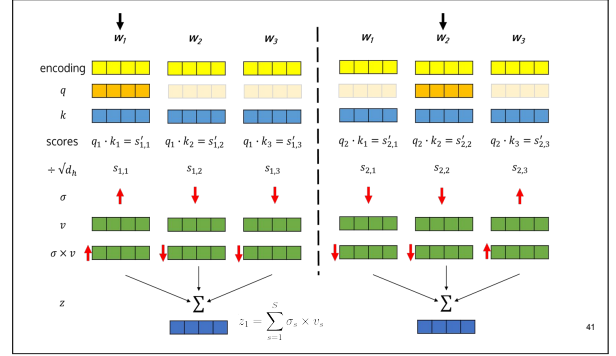
(p) Arrows indicate strong and weak weightings.



(q) The first step is simply retrieving the value vectors we obtained previously. The second step is actually performing the weighting on each of our value vectors. So our value vectors retain more information if the softmax value for that index is high, and retain less information if the softmax value for that index is low. The softmax here is the way we normalize similarity scores



(r) Finally we obtain our contextual representation for the first word. This is the sum over our weighted value vectors.

(s) We repeat the process for every word in our input sequence. Our overall representation for our input sequence would then be all of our  $z$  vectors stacked together. Each  $z$ -vector is  $D$ -dimensional, and obviously we have  $S$  amounts of them.

### 2.1.2 Matrix Form

$$\text{Attention}(Q, K, V) = Z = \underbrace{\sigma\left(\frac{\overbrace{Q}^{\in \mathbb{R}^{S \times d_h}} \overbrace{K^T}^{\in \mathbb{R}^{d_h \times S}}}{\sqrt{d_h}}\right)}_{\text{attention matrix} \in \mathbb{R}^{S \times S}} V, \quad S = \text{source sequence length}$$

## 2.2 Multi-head attention

### Multi-head attention

- Multi-head self-attention is basically just self-attention
  - But it performs self-attention head amount of times
- The original Transformer used 8 heads
  - This means we run self-attention 8 times over 8 *different* Q, K, Vs
- Our final representation concatenates and projects the self-attention outputs
- Each head has dimensionality  $D/\text{heads}$

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We perform self-attention *head* amount of times. Each head may refer to different parts of the sequence. The number of heads needs to be equally divisible by the model dimensionality

$d_h$  therefore represents the model dimensionality divided by the number of heads.

## 2.3 Normalization

### 2.3.1 Layer normalization

Data fed into a neural network should be normalized e.g.  $\hat{x} = \frac{x - \mu}{\sigma}$ . There are also normalization techniques within the activations or layers of a network

### Layer Normalization

- Layer normalization normalizes the features of **one sample in one batch**
  - $B = \{x_1, x_2, \dots, x_N\} \quad x_n \in \mathbb{R}^d$
- Two key steps:
  - 1.  $\hat{x}_n = \text{normalize}(x_n)$
  - 2. Transform  $\hat{x}_n$  with learned parameters  $\gamma, \beta$

$$LN(\hat{x}_n) = \gamma \hat{x}_n + \beta$$

$\gamma \in \mathbb{R}^d$   
 $\beta \in \mathbb{R}^d$

$$\hat{x} = \frac{x - \mu}{\sigma}$$

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It normalizes the feature of one sample in one batch. The first step is that we normalize each one of the items in our batch respective to that item itself. Then transform the variable with learnable parameters  $(\gamma, \beta)$



### 2.3.2 Residual Connections

You would assume that if you want to stack layers, we should get a lower training error. In practice this doesn't happen; as you increase the number of layers, what you see is an increase in the training error that you will see.

Residual connections help mitigate the vanishing gradient problem, where Vanishing gradients = tiny weight changes. Residual connections provide a shortcut for information to flow to layer layers of the network, where the output of an earlier layer is added directly to the output of a layer layer. (see ResNet in Deep Learning lectures).

The reason this works so well: it lets each weight matrix to focus on only learning the difference between the previous layer and the current layer instead of learning an entire transformation as what happens in the traditional case.

## 2.4 Position-wise Feed forward Network

### Position-wise Feedforward Network

- A position-wise feedforward network is an NLP
- *Position-wise* just means it is applying the same transformation to every element in the sequence
  - i.e. same weights applied to all tokens in the sequence

$$\text{FNN}(x) = \max(0, xW_1 + b)W_2 + b_2$$

$$W_1 \in \mathbb{R}^{D \times d_{ff}} \quad W_2 \in \mathbb{R}^{d_{ff} \times D} \quad d_{ff} = 2048$$

- Two layered network, with a ReLU activation function

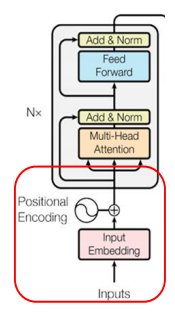
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**network is an NLP** → **network is an MLP**. Transformation is applied to all weights in a sequence. In the above example, there are 2 layers, with a ReLU activation function. We project  $x$  from  $d_{ff}$  into  $D$ . Then  $W_2$  projects it down again.

## 2.5 Positional Encoding

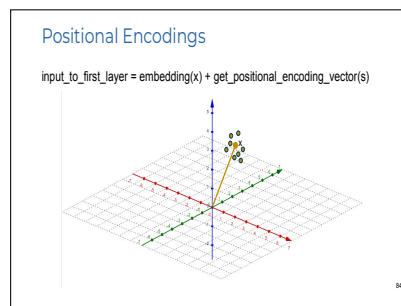
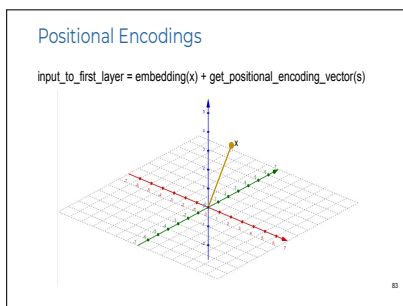
### Positional Encodings

- Our diagram indicates that the output of one layer forms the input to the next
  - But what about the first layer? What is this thing called positional encoding?
- **Transformers are position invariant by default**
  - The cat sat = sat the cat
- Differs from RNNs, which are inherently sequential
- Positional encodings are a way to inject position information into the embeddings



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This is inherently different to RNN which processes things in the order they arrive in.



Positional Encodings

- Multiple ways of incorporating positional embeddings
  - Authors propose using sinusoids
  - You can also learn the positional embeddings (more in BERT)

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The positional encoding vector is independent of the word, but only to the position in the sequence. The addition, permute the vector by small amounts. In vector space, the offset remains the same for any embedding given the same position.

There are multiple ways of incorporating positional embeddings, such as sinusoids or learning the positional embeddings. Applying positional encoding depends **ONLY** on the index the word appears in.

$$PE_{pos,2i} = \sin\left(\frac{pos}{10000^{\frac{2i}{d}}}\right)$$

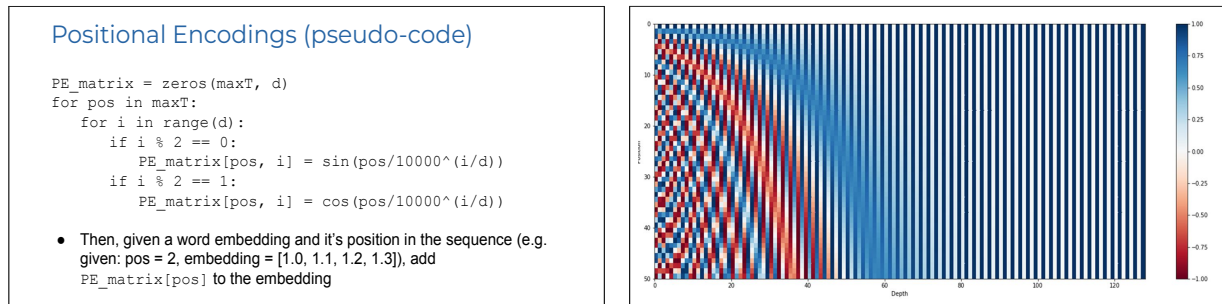
$$PE_{pos,2i+1} = \cos\left(\frac{pos}{10000^{\frac{2i}{d}}}\right)$$

$pos$  : position of the word,  $i$  : index of  $d$

The only difference between the functions is whether we use a sin or cosine. Note that when we're early on in looping over  $d$ ,  $i$  will be small. The resulting exponent would be therefore be small. This makes the denominator small. Thus the overall value of  $\frac{pos}{10000^{(2i/d)}}$  would be larger than when we're later in our loop over  $d$

The  $2i$  and  $2i + 1$  impl that we're going to be looping over the indexes in range of  $d$ . E.g. consider we had a vector of 512 dimension. We would be looping over it. At an even index (e.g 0) we'd apply the sin variant of PE. At an odd index (e.g. 1), we would apply the cos variant.

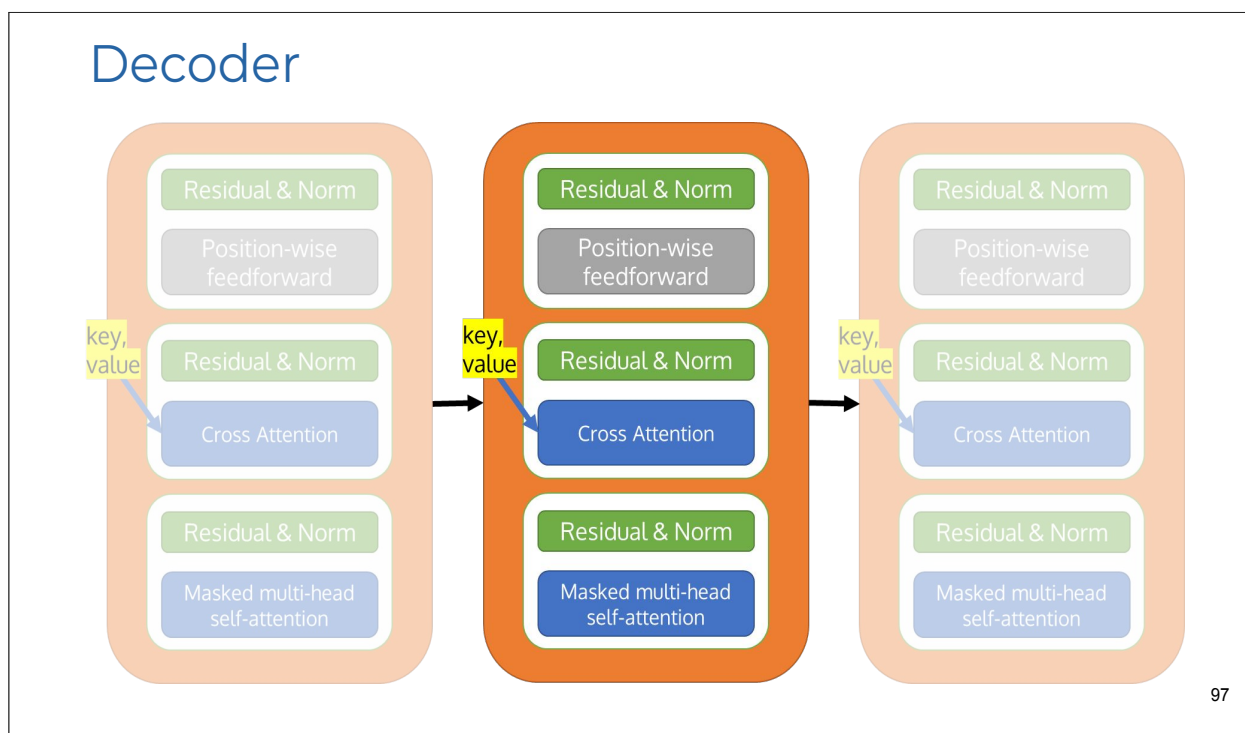
### 2.5.1 Pseudo-code



Consider position 0, i.e. the first word in the sequence, positional encoding function means no manipulation is done to the vector. At position 1, the positional encoding function shows that indexes up to 10 have values close to 1 added to them. At position 22 the encoding function shows that the first few indexes are affected heavily by positional encoding. some indexes have values close to -1 added to them, followed shortly by a value +1 added to them.

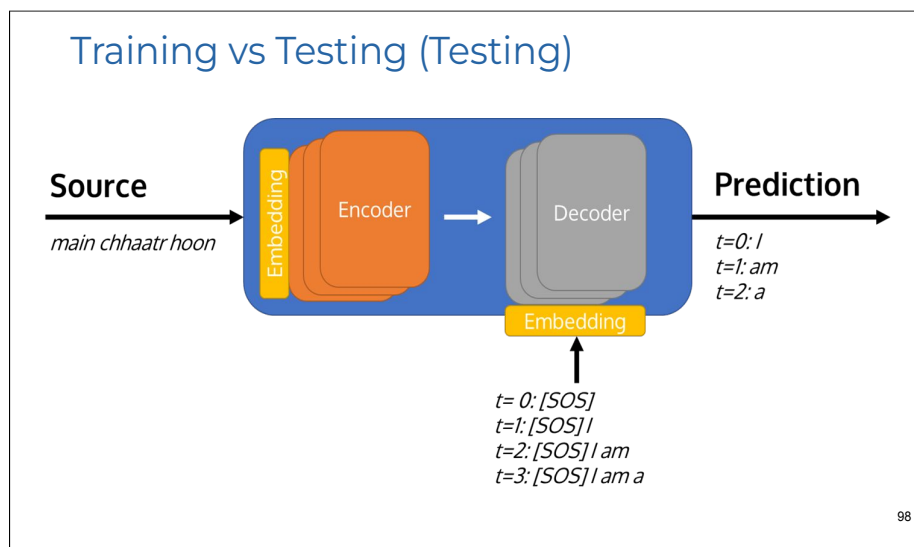
We don't just add another dimension to indicate the position because that draws the samples away from the 0 mean. Also, there is less generability because if during training, the model hasn't seen that word in that position then during testing it won't be very good.

## 3 Transformer — Decoder



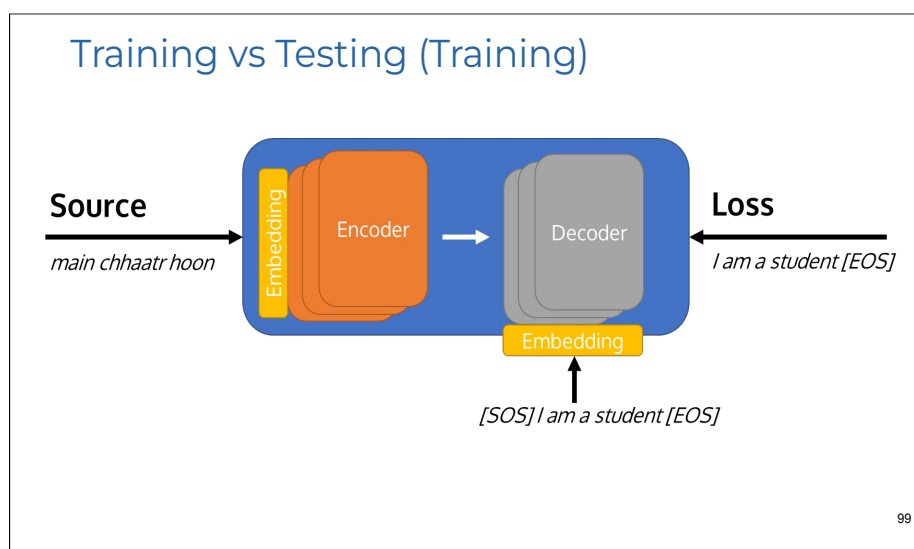
### 3.1 Pipeline

#### 3.1.1 Testing



Our source sentence gets encoded via our encoder. We feed an SOS token to our decoder, which then predicts the first word. We append the prediction to our SOS token, and then use this to predict the next word. At some point our decoder will predict an EOS token and we'll know that this is the end of the generation.

#### 3.1.2 Training



However, during training, we won't get the model to generate auto-regressively. We're going to feed the whole target sequence as input to the decoder and decode the sentence in one go. This means we can run the decoder stack once. As opposed to running it for as many tokens as we have in the target sequence (Which is what we do when performing inference). If we feed in the whole sequence to the decoder, we need a way to tell the decoder not to look at future tokens when computing attention for one of the tokens. E.g. when trying to compute the attention-based representation for "am" we should not be allowed to look at "a" or "student", since these tokens are in the future. We enforce this uni-directionality with masking.

### 3.2 Masked Multi-head Self attention

When we looked at attention in the encoder, the bidirectionality meant that each word looked at every other word, including future tokens for the word which we are trying to calculate the attention for. Masked multi-head means that we're not looking at future tokens.

**Masked Multi-head Self-attention**

- Our mask is going to be  $\in \mathbb{R}^{T \times T}$ 
  - i.e. a square matrix
  - Here,  $T$  is the target sequence length
- For every token, an illegal location will be all future tokens we're not meant to have access to.
  - So at  $t=1$ , we don't have access to any words  $t>1$ ,
  - At  $t=2$ , we don't have access to any words  $t>2$

	I	am	a	student
I	✓	✗	✗	✗
am	✓	✓	✗	✗
a	✓	✓	✓	✗
student	✓	✓	✓	✓

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We enforce uni-directionality with a mask. We set the values in the upper triangle to negative infinity. The mask is a  $T \times T$  matrix.

### 3.3 Cross Attention

**Cross Attention**

- The decoder needs to know the encoded representation
- Every time we're decoding a token, we need to know which encoded words we should look at to decode the token
  - Achieved via cross attention
- We use the **key**, **value** tensors from the **last encoder layer**, and send them to all the decoder layers.
  - So, **query** comes from the **current decoder layer**
- Cross attention matrix shape =  $T \times S$

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Thinking back to the dictionary analogy, we have a query vector (in target-language embedding space). We're then looking to find the similar key vectors from the encoder. In other words, which encoded words are most similar to this current decoding word. Then, using the softmax weighted similarities, we obtain some aggregated value indicating which words are most important.

$T \times S$  is the similarity between target words and source words.

### 3.4 Conclusion

Our overall decoder is similar to the encoder layer in construction. We create a decoder and decoder layer class, the decoder layer class contains one decoder layer, and the decoder class contains embeddings + PE and a for loop over the desired number of decoder layers.

## 4 Tricks

### 4.1 Decaying learning rate

$$lr = \sqrt{\frac{1}{d}} \times \min \left( \sqrt{\frac{1}{d}}, i \times warmup^{-1.5} \right), \quad \begin{cases} i : & \text{current global step} \\ warmup : & \text{hyperparameter (default: 4000)} \\ d : & \text{model dimensionality} \end{cases} \quad (4.1.1)$$

## 5 Code

### 5.1 Self Attention

```

1  # %%
2  import torch
3  import torch.nn.functional as F
4  import math
5  import numpy as np
6
7  # %%
8
9
10 def scaled_dot_product_attention(Q, K, V, dk=4):
11     ## matmul Q and K
12     QK = Q @ K.T
13
14     ## scale QK by the sqrt of dk
15     matmul_scaled = QK / math.sqrt(dk)
16
17     attention_weights = F.softmax(matmul_scaled, dim=-1)
18
19     ## matmul attention_weights by V
20     output = attention_weights @ V
21
22     return output, attention_weights
23
24 # %%
25
26
27 def print_attention(Q, K, V, n_digits=3):
28     temp_out, temp_attn = scaled_dot_product_attention(Q, K, V)
29     temp_out, temp_attn = temp_out.numpy(), temp_attn.numpy()
30     print('Attention weights are:')
31     print(np.round(temp_attn, n_digits))
32     print()
33     print('Output is:')
34     print(np.around(temp_out, n_digits))
35
36
37 # %%
38 temp_k = torch.Tensor([[10, 0, 0],
39                        [0, 10, 0],
40                        [0, 0, 10],
41                        [0, 0, 10]]) # (4, 3)
42
43 temp_v = torch.Tensor([[1, 0, 1],
44                        [10, 0, 2],
45                        [100, 5, 0],
46                        [1000, 6, 0]]) # (4, 3)
47
48 # %%
49 # This 'query' aligns with the second 'key',
50 # so the second 'value' is returned.
51 temp_q = torch.Tensor([[0, 10, 0]]) # (1, 3)
52 print_attention(temp_q, temp_k, temp_v)
53
54 # %%
55 # This query aligns with a repeated key (third and fourth),
56 # so all associated values get averaged.
57 temp_q = torch.Tensor([[0, 0, 10]]) # (1, 3)
58 print_attention(temp_q, temp_k, temp_v)
59
60 # %%
61 # This query aligns equally with the first and second key,
62 # so their values get averaged.
63 temp_q = torch.Tensor([[10, 10, 0]]) # (1, 3)
64 print_attention(temp_q, temp_k, temp_v)

```

```

65
66 # %%
67 temp_q = torch.Tensor([[0, 10, 0], [0, 0, 10], [10, 10, 0]]) # (3, 3)
68 print_attention(temp_q, temp_k, temp_v)

```

code/self\_attention.py

## 5.2 MHA

```

1 # %%
2 import torch
3 import torch.nn as nn
4 import math as m
5 import torch.nn.functional as F
6
7 # %%
8
9
10 class MultiHeadAttention(nn.Module):
11     def __init__(self, d_model=4, num_heads=2, dropout=0.3):
12         super().__init__()
13
14         # d_q, d_k, d_v
15         self.d = d_model // num_heads
16
17         self.d_model = d_model
18         self.num_heads = num_heads
19
20         self.dropout = nn.Dropout(dropout)
21
22
23         self.linear_Qs = nn.ModuleList([nn.Linear(d_model, self.d)
24                                           for _ in range(num_heads)])
25         ## create a list of layers for K, and a list of layers for V
26         self.linear_Ks = nn.ModuleList([nn.Linear(d_model, self.d)
27                                           for _ in range(num_heads)])
28         self.linear_Vs = nn.ModuleList([nn.Linear(d_model, self.d)
29                                           for _ in range(num_heads)])
30
31         self.mha_linear = nn.Linear(d_model, d_model)
32
33     def scaled_dot_product_attention(self, Q, K, V):
34         # shape(Q, K, V) = [B x seq_len x D/num_heads]
35
36         # q => [b x seq_len x d_h]
37         # k => [b x seq_len x d_h]
38         # => [b x d_h x seq_len]
39         # q matmul k => [b x seq_len x seq_len]
40
41         Q_K_matmul = torch.matmul(Q, K.permute(0, 2, 1))
42         scores = Q_K_matmul / m.sqrt(self.d)
43         # shape(scores) = [B x seq_len x seq_len]
44
45         attention_weights = F.softmax(scores, dim=-1)
46         # shape(attention_weights) = [B x seq_len x seq_len]
47
48         output = torch.matmul(attention_weights, V)
49         # shape(output) = [B x seq_len x D/num_heads]
50
51         return output, attention_weights
52
53     def forward(self, x):
54         # shape(x) = [B x seq_len x D]

```

```

55 Q = [linear_Q(x) for linear_Q in self.linear_Qs]
56 K = [linear_K(x) for linear_K in self.linear_Ks]
57 V = [linear_V(x) for linear_V in self.linear_Vs]
58 # shape(Q, K, V) = [B x seq_len x D/num_heads] * num_heads
59
60
61 output_per_head = []
62 attn_weights_per_head = []
63 # shape(output_per_head) = [B x seq_len x D/num_heads] * num_heads
64 # shape(attn_weights_per_head) = [B x seq_len x seq_len] * num_heads
65 for Q_, K_, V_ in zip(Q, K, V):
66
67     ## run scaled_dot_product_attention
68     output, attn_weight = self.scaled_dot_product_attention(Q_, K_, V_)
69
70     # shape(output) = [B x seq_len x D/num_heads]
71     # shape(attn_weights_per_head) = [B x seq_len x seq_len]
72     output_per_head.append(output)
73     attn_weights_per_head.append(attn_weight)
74
75 # example output_per_head = [
76 # [
77 #     [0.00, 0.01],
78 #     [0.10, 0.11],
79 #     [0.20, 0.21]
80 # ], (tensor)
81 # [
82 #     [1.00, 1.01],
83 #     [1.10, 1.11],
84 #     [1.20, 1.21]
85 # ], (tensor)
86 # [
87 #     [2.00, 2.01],
88 #     [2.10, 2.11],
89 #     [2.20, 2.21]
90 #
91 # ] (tensor)
92 # ]
93
94 # example output = [
95 # [ 0.00, 0.01, 1.00, 1.01, 2.00, 2.01 ],
96 # [ 0.10, 0.11, 1.10, 1.11, 2.10, 2.11 ]
97 # [ 0.20, 0.21, 1.20, 1.21, 2.20, 2.21 ]
98 # ] # [3 x 6]
99
100 # [3 x 3]
101 # [
102 # [0.0, 0.1, 0.2]
103 # [1.0, 1.1, 1.2]
104 # []
105 # ]
106
107 # [2 x 2 x 3 x 3]
108 # [
109 # [
110 #     [0.0, 0.1, 0.2],
111 #     [1.0, 1.1, 1.2],
112 #     [2.0, 2.1, 2.2]
113 # ],
114 # []
115 #
116 # ]
117
118 output = torch.cat(output_per_head, -1)
119 attn_weights = torch.stack(attn_weights_per_head).permute(1, 0, 2, 3)

```



```
120     # shape(output) = [B x seq_len x D]
121     # shape(attn_weights) = [B x num_heads x seq_len x seq_len]
122
123     projection = self.dropout(self.mha_linear(output))
124
125     return projection, attn_weights
126
127 # %%%
```

code/mha.py

## References

- [1] The AI Hacker. *Illustrated Guide to Transformers Neural Network: A step by step explanation*. 2020.  
URL: <https://www.youtube.com/watch?v=4Bdc55j8018>.