Language ambiguity (has multiple precise meanings): Lexicon – morph(eme)ological analysis (stem and affix e.g. 'car'+'s') word 'bring me the file' (resolve w/ POS) syntactic 'I shot an elephant in my pjs' abstract functions instead Word segmentation (tokenization) syntactic 'I shot an elephant in my pjs' semantic 'the rabbit is ready for lunch' Word normalization (case/acronyms/spelling) of rules based on

maintenance of intuitive

Lemmatization 'sing, sung, sang' → 'sing Stemming (common root, above 's')
Part-Of-Speech (tag words with noun, verb...) Context-Free Grammar: <u>Derive</u> sentence structure through a <u>parse tree</u> $S \to NP \ VP, NP \to Det \ N, VP \to V \ NP, VP \to V, VP \to V \ PP, PP \to P \ NP$ <u>Discourse</u>: meaning of a text (relationship between sentences) <u>Pragmatics</u>: intentions/comman Corpus: a collection of documents Document: one item of corpus (sequence) Token: atomic word unit Vocabulary: unique tokens across coropus. One-Hot Encoding: sparse (wasted space), orthogonal vectors (every word is equidistant), cannot represent out of vocab well

linguistic rules. Sigmoid (binary class.) $\frac{1}{1+e^{-x}}$, ReLU: $\max(0,x)$, Tanh: $\frac{e^x-e^{-x}}{e^x+e^{-x}}$, Softmax (k-class): $\begin{array}{l} \text{Softmax} \left(\text{k-class} \right) : \sum_{k} \frac{e^{-y}}{e^{+k}} \\ \text{MSE } \left(\text{regression} \right) \frac{1}{N} \sum_{i=1}^{N} (y_i - \hat{y}_i)^2, \text{Binary cross-entropy:} \\ -\frac{1}{N} \sum_{i=1}^{N} (y^{(i)} \log(\hat{y}^{(i)}) + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})) \right) \text{Categorical cross} \\ \text{entropy } \left(\text{k-class} \right) : -\frac{1}{N} \sum_{i=1}^{N} \sum_{c=1}^{C} y_c^{(i)} \log(\hat{y}_c^{(i)}) \end{array}$

referential 'Pavarotti is a big opera star'

non-literal 'it's raining cats and dogs'

Euclidean Distance: $\sqrt{\sum_{i=1}^{n}(q_{d}-d_{i})^{2}}$ Cosine Similarity: $\cos(\theta)=\frac{p_{1}\cdot p_{2}}{\|p_{1}\|\cdot x\|p_{2}\|}$ Analogy Recovery: offset of the vectors reflect their relationship. $a - b \approx c - d \iff d \approx c - a + b$

Window: window consists of target and context (surrounding), Window size = radius Continuous Bag Of Words: context — target, Skip-gram: target — context (give as one-hot, get word representation, map embedding to target words using weight matrix, apply softmax). Train with list of pairs (target, context) by

Byte-Pair Encoding: Instead of manually specfying rules for lemmatisation or stemming, lets learn from data which character sequences occur together frequently. 1) Start with a vocabulary of all individual characters 2) Split the words in your training corpus also into individual characters + '_' at end 3) Find which two vocabulary items occur together most frequently in the trianing corpus 4) Add that combination as a new vocabulary item 5) Merge all occurrences of that combination in your corpus 6) Repeat until a desired numbe of merges has been performed. For unknown words follow above and apply replacements in order discovered.

sliding window over input. Loss: $p(w_{t+j}|w_t) = \frac{\exp(u_{w_{t+j}}^T h w_t)}{\sum_{w'=1}^W \exp(u_{w'}^T h w_t)}$, the aim: $\max \prod_t \prod_j p(w_{t+j}|w_t) \rightarrow \min_{\theta} - \sum_t \sum_j \log p(w_{t+j}|w_t;\theta) \rightarrow \frac{1}{T} \sum_{t=1}^T \sum_{-c \le j \le c, j \ne 0} \log p(w_{t+j}|w_t;\theta)$ over all elems in corpus. However, the bottom term in the $p(w_{t+j}|w_t)$ is inefficient to compute across the entire corpus vocabulary. Therefore, train a Negative Sampling model to predict whether a word appears in the context of another: $\log p(D=1|w_t,w_{t+1})+k\mathbb{E}_{\widetilde{c}\sim P_{noise}}[\log p(D=0|w_t,\widetilde{c})]$ where $p(D=1|w_t,w_{t+1})$ is a binary logistic regression probability of seeing the word w_t in the context w_{t+1} . Approximate the expectation by drawing random words from vocabulary, and on left choose positive pairs. Thus the equation is replaced: $p(D=1|w_t,w_{t+1})=\frac{1}{1+\exp{-u_{w_{t+1}}h_{w_t}}}$. We can sample k (5-10 words) with frequency or random sampling.

Classification: $\hat{y} = \arg \max_{y} P(y|x)$ predict which y is most likely given input x. In the MultiNLI corpus we are given pairs of sentences (premise, hypothesis) with classification problem

(Entailment: If hypothesis is implied by premise, Contradiction: If hypothesis contradicts the premise, Neutral: otherwise). $\overline{Accuracy} = \frac{TP + TN}{TP + FP + TN + FN}, f1 = 2 \times \frac{precision \times recall}{precision + recall} = \frac{TP}{TP + 0.5(FP + FN)},$ Macro average: averaging of

each class F1 scores: increases the emphasis on less frequent classes. Micro average: TPs, TNs, FNs. FPs are each class F1 scores: increases the emphasized states are summed across each class e.g. $\frac{\sum_{i}^{C}TP_{i}}{\sum_{i}^{C}TP_{i}+\frac{1}{2}(\sum_{i}^{C}FP_{i}+\sum_{i}^{C}FN_{i})}=Accuracy$

Language Models: Assign probabilities to sequence of words, like predicting the next word in a sentence. Uni-directional: use information from left to generate predictions about words on the right. Bi-directional: use information from both sides to fill the target.

N-gram: need because language is flexible, and a natural extension of a sentence may no appear in corpus. $P(w_n|w_1^{n-1}) \approx P(w_n|w_{n-N+1}^{n-1}) = \frac{C(w_{n-N+1}^{n-1}w_n)}{C(w_{n-N+1}^{n-1})}.$ If certain words absent the probability is 0.

$$\begin{split} S(w_i|w_{i-2}w_{i-1}) &= \begin{cases} \frac{C(w_{i-2}w_{i-1}w_i)}{C(w_{i-2}w_{i-1})}, & if \ C(w_{i-2}w_{i-1}w_i) > 0 \\ 0.4 \cdot S(w_i|w_{i-1}), & otherwise \end{cases} \\ S(w_i|w_{i-1}) &= \begin{cases} \frac{C(w_{i-1}w_i)}{C(w_{i-1})}, & if \ C(w_{i-1}w_i) > 0 \\ 0.4 \cdot S(w_i), & otherwise \end{cases} \\ s(w_i) &= \frac{C(w_i)}{N} \end{split}$$

 $\begin{cases} \frac{C(w_{i-2}w_{i-1}w_i)}{C(w_{i-2}w_{i-1})}, & \text{if } C(w_{i-2}w_{i-1}w_i) > 0 \\ 0.4 \cdot S(w_i|w_{i-1}), & \text{otherwise} \end{cases}$ Change this with **add-one smoothing**: $P_{add-1}(w_n|w_{n-1}) = \frac{C(w_{n-1}w_n)+1}{C(w_{n-1})+1} \text{ however, this influences the less frequent words (not the following of the context of the context$ more). Therefore, implement backoff Interpolation: $P_{interp}(w_i|w_{i-2}w_{i-1}) = \lambda_1 P(w_i|w_{i-2}w_{i-1})$

To make a prediction $P(w_1)$, where $\lambda_1 + \lambda_2 + \lambda_3 = 1$ to combine evidence from multiple n-grams. To make a prediction $P(w_1, \dots, w_n) = \prod_{k=1}^n P(w_k|w_k^{k-1})$ we switch into log space $\log P[\cdot] = \sum_{k=1}^n \log(P(w_k|w_k^{k-1}))$ however the longer the sentence the lower its likelihood. Switch to

Perplexity: where n is the number of words: $PPL(w) = \sqrt[n]{\frac{1}{\prod_{k=1}^{n} P(w_k|w_k^{k-1})}}$ the higher the conditional

probability of the word sequence, the lower the perplexity. Thus, minimizing perplexity is equivalent to maximizing the test set probability according to the language model. It is a measure of surprise in an LM when seeing new text. For a single word, the score is 1.

If the goal of the language model is to support with another task, the best choice of language model is the one that improves downstream task performance the most (extrinsic evaluation). Perplexity is less useful in this case (intrinsic evaluation).

Cross Entropy Loss: The cross-entropy is useful when we don't know the actual probability distribution p that generated some data. $\mathrm{H}(\mathrm{T},\mathrm{q}) = -\sum_{i=1}^N \frac{1}{N} \ln q(x_i)$. To convert to perplexity take the base of the logarithm and perform $PPL(M) = base^H$.

Statistical Machine Translation: a pipeline of Alignment model (responsible for extracting the phrase pairs) <u>Translation model</u> (contains phrases alongside their translation lookup table) <u>Language model</u> (contains the probability of target language phrases). The objective is p(t|s) given a source sentence predict a sentence t. $\arg\max_t p(t|s) = p(t)p(s|t)$. Downsides: Sentence Alignment (In parallel corpora single sentences in one language can be translated into several sentences in the other and vice versa) Word Alignment (no clear equivalent in the target language) Statistical anomalies (Real-world training sets may override translations) Idioms (Only in specific contexts do we want idioms to be translated) Out-of-vocabulary words.

Implementing Attention+RNN: For each hidden state in the encoder, $c_t = \sum_{i=1}^{I} \alpha_i h_i$ combine these into a context vector, it is dynamic and contextualised representation. We then feed a decoder this context vector and

the <init> token. This is the **energy**, and it is calculated with $e_i = a(s_{t-1}, h_i) = v^T \tanh(Ws_{t-1} + Uh_i)$ where $e_i \in \mathbb{R}^1$ is the unnormalized energy score, and a is a learnt neural network. $s_{t-1} \in \mathbb{R}^{D \times 1}$ is the previous decoder hidden state, $h_i \in \mathbb{R}^{2D \times 1}$ encoder hidden state for the ith word, $v^T \in \mathbb{R}^{D \times 1} \wedge v \in \mathbb{R}^{1 \times D}, W \in \mathbb{R}^{D \times D}$ $W \in \mathbb{R}^{D \times D}$ then the energy gets normalized with a softmax to form the α .

BLEU: reports a modified precision metric for each level of n-gram Modified Precision score $p_n = \frac{\text{Total Unique Overlap}_n}{\text{Total n-erams}}$ where Total n-grams is the 'total n-grams' in the produced sentence (not unique), and 'total unique overlap' is the unique set of unique tokens appearing in the output have appeared in the union of the reference sentences. **BLEU-4:** BP $(\prod_n^4 p_n)^{\frac{1}{4}}$, $BP = \min(1, \frac{MT \ Output \ Length}{Reference \ Length})$ where p_n defined above. Used to mostly encourage the hypothesis to be of a similar length to the reference. A shortcoming of BLEU is that it focuses a lot on the precision between Hyp and Ref, but not the recall. Chr-f: character n-gram F_{β} score. Balances character precision (percentage of n-grams in the hypothesis which have a counterpart in the reference) and character recall (percentage of character n-grams in the reference which are also present in the hypothesis). $CHRF_1 = \frac{2\cdot CHRP\cdot CHRR}{CHRP+CHRR}$ where CHRP: percentage of n-grams in the hypothesis which have a counterpart in the reference, CHRR: percentage of character n-grams in the reference which are also present in the hypothesis. Good for morphologically rich languages. **TER** translation error rate: Minimum # of edits required to change a hypothesis into one of the references. TER is performed at the word level, and the "edits" can be a: Shift, Insertion, Substitution and Deletion. **ROGUE** F-1 score n-gram, ROGUE-L: F-score of longest common subsequence e.g. source: The cat is on the mat hyp: The cat and the dog so LCS: the cat the, precision = 3/5, recall = 3/6. **METEOR**: summarization and captioning, more robust than BLEU. <u>Downside: cannot capture</u> <u>context of sentence to return a higher score.</u> **BERT-score**: a trained language model that can give contextual representations of tokens/words. May return different scores when evaluated against different models.

Inference: Greedy Decoding: Outputs the most likely word at each time step (i.e. an argmax) fast but doesn't look into the future; can get weird later. **Beam Search**: Instead of choosing the best token to generate at each time-step we keep k possible tokens at each step. Maintain the log probability of each hypothesis in beam by incrementally adding logprob of generating each next token. Only the top k paths are kept. **Temperature Sampling**: problem with above is determinism. Therefore, divide logits by T and run run softmax $\frac{e^{y_i}}{\sum_i^N e}$

Improving Performance: Back-translation: translate the source into one language and translate it back. The hope is, that once translated back the semantics is the same but syntactically it may be different. Synonym Replacement: Use dictionary & syntax trees to find appropriate synonyms/ Use word embeddings & nearest

together in the batch or train your model on simpler/smaller sequence lengths first.

TF-IDF: Problem: words in a query are weighted equally. Term Frequency – Measures how often a term occurs in a document. Inverse Document Frequency - Measures how common or rare a term is across all documents in the corpus. (Terms that appear in many different documents are less significant than those that appear in a smaller number of

Multinomial sample over softmax probabilities.

 $TF_{w,d} = \frac{count(w,d)}{\sum_{w'} count(w',d)}$ (frequency of w occurring together with d). $IDF_{w,D}=\log \frac{|D|}{[\{d\in D: w\in d\}]}$ down-weighs words that appear everywhere. $TF-IDF_{w,d}, D=TF_{w,d}IDF_{w,D}$

neighbours to find synonyms. Batching, Padding and Sequence Length: Group similar length sentences

 $\hat{y} = \arg\max_y P(y|x) = \arg\max_y P(x|y)P(y)$ since evidence doesn't change. $\underbrace{\frac{P(x|y)}{P(y)}}_{P(x)}\underbrace{\frac{y}{P(y)}}_{Naive Bayes Classifier:}_{P(x_1|y)...P(x_I|y)}$ P(y|x) $\hat{y} = \arg\max_{y} P(x_1, \dots, x_I | y) P(y) = \arg\max_{y} P(y) \prod_{i=1}^{I} P(x_i | y)$

In a Bag of Words count the number of times a token appears in the vocabulary per class. In One smoothed Naive Bayes: $P(x_i|y) = \frac{count(x_i,y)+1}{c\sum_{x \in V} count(x_i,y)+1} = \frac{1}{(c\sum_{x \in V} count(x_i,y)+1)}$ Binary Naive Bayes: only consider if a feature is present, rather than considering every time it occurs. **Controlling for negation**: pre-pend 'NOT_'

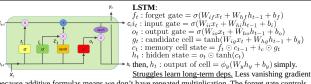
<u>Discriminative</u> algorithms directly learn P(Y|X) without considering likelihood. <u>Generative</u>: consider likelihood **Logistic Regression**: apply sigmoid/softmax with $s = w \cdot x + b$ with loss $H(P,Q) = -\sum_i P(y_i) \log Q(y_i)$.

RNN: $h_{t+1} = f(h_t, x_t) = \tanh(Wh_t + Ux_t), W \in \mathbb{R}^{H \times H}, U \in \mathbb{R}^{H \times E}$ The model is less able to learn from earlier inputs, better for long ranged **CNN**: CNNs can perform well if the task involves key phrase recognition

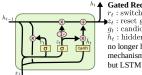
Feed-Forward LM (FFLM); get word embeddings for words and concat them together embedding; $V \times E$. concat: $c_k \in \mathbb{R}^{C \times E}$ with a output layer $CE \times V$ then softmax. **RNN**: $h_{t+1} = f(h_t, x_t) = \tanh(Wh_t + Ux_t), y_t = W_{hy}h_t + B_y$. **Teacher Forcing**: if there is an incorrect

label we force it to use the actual expected label. The ratio can be 100% (i.e. full teacher forcing), 50%, or you can even anneal it during training. This may cause Exposure Bias where it never actually uses its own predictions during training. **Bidirectional RNN**: When comparing the number of parameters in this vs a single directional rnn, it doubles. The output layer also doubles (because we are given a matrix $H \times O$ twice from each direction making the output layer have dimension $H \times H \times O$). This extends to **multi-layered RNNs**

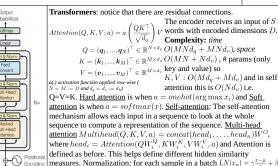
Naive translation: minimise negative log likelihood loss $-\sum_{t=1}^{T} \log p(\hat{y}_t|y_{< t}, c)$. Take hidden vector encoding from encoder RNN into the decoder. This limits amount of information it can retain for longer vectors, as more words get decoded the hidden layer continues through the decoder and looses its information.



because additive formulas means we don't have repeated multiplication. The forget gate controls when to preserve gradients or not. $W_{ii}=(H\times E)$ and $W_{hi}=(H\times H)$ since we go from mbeddings to hidden representation



Gated Recurrent Unit: r_t : switch gate = $\sigma(W_{ir}x_t + W_{hr}h_{t-1} + b_r)$ $\blacktriangleright z_t$: reset gate = $\sigma(W_{ix}x_t + W_{hz}h_{t-1} + b_z)$ g_t : candidate state = $\tanh(W_{ig}x_t + r_t * (W_{hg}h_{t-1} + b_g))$ h_t : hidden state = $(1 - z_t) * g_t + z_t * h_{t-1}$ no longer has input/output gate but maintains forgetting mechanism. GRU more efficient computing & less over-fitting but LSTM good default choice.



with learnable params to scale. Residual connections: Residual connections help mitigate the vanishing gradient problem, where Vanishing gradients = tiny weight changes. Residual connections

provide a shortcut for information to flow to layer layers of the

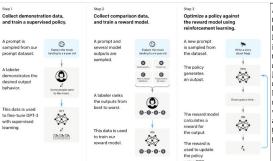
network, where the output of an earlier layer is added directly to the output of a layer layer. Positional Encodings transformers are position invariant by default; positional encoding vector is independent of the word, but only to the position in the sequence it is either learnt or where pos=position of word, d=dimension of output space, i = column indices $PE_{pos,2i}=\sin\left(rac{pos}{10000^{rac{2i}{d}}}
ight)$ and $PE_{pos,2i+1}=\cos\left(rac{pos}{10000^{rac{2i}{d}}}
ight)$ smaller early on, larger later on (iterating i over d). Masked Attention: mask out some attention values by adding matrix with 0s and set upper triangle to $-\infty$ (useful for sequence prediction with a given ordering: in test time "future" is not available for the "current" to attend). <u>Cross Attention</u>: In self-attention, we work with the same input sequence. In cross-attention, we mix or combine two *different* input sequences. In the case of the original transformer architecture above, that's the sequence returned by the encoder module on the left and the input sequence being processed by the decoder part on the right. with i: current global step, warmup hyperparameter (4000), d: model dimensionality <u>Decaying learning rate</u>: $lr = \sqrt{\frac{1}{d}} \times min \left(\sqrt{\frac{1}{d}}, i \times warmup^{-1.5} \right)$

Contextual Word Representations: there is one word representation per word, even though in different contexts it may mean different things. RNNs capture this. **ELMO**: two directions: $p(t_1, t_2, \dots, t_N) = \prod_{k=1}^{N} p(t_k|t_1, t_2, \dots, t_{k-1})$ and $p(t_1, t_2, \dots, t_N) = \prod_{k=1}^{N} p(t_k|t_{k+1}, t_{k+2}, \dots, t_N)$. Uses LSTMs with multiple layers of bidirectional slices. Intermediate representation + second layer allows for more complex second-level reasoning about words. Use ELMO to enhance. **BERT**: Bidirectional Encoder Representations from Transformers: Advantage from self-attention is that every word is just one hop away from every other word. In LSTMs or RNNs, if we wanted to get information from one word to another, we'd have to step through every word in the sequence and keep information in memory. Unlike Self-attention which combines directly information from every other word. Segment Embeddings, Position Embeddings, Token Embeddings. Train with Masked Language Modelling, too little masking = difficult to train, too much = not enough context. Next sentence prediction did these two sentences appear in this order? Using Pre-trained models: for sentence classification, insert <CLS> token and attach new layer to the output for this token. Token labelling: put classification pairs on each token. Pair classification: separate two sentences with a token + add classification head on top 'does sentence 1 entail sentence 2 or vice versa?' Question answering: We can structure the task with an input, and a paragraph of text which may contain some answers. Then train the model to label individual tokens to indicate which tokens are the answer, then simply extract these

- · BERT: Trained with masked language modelling and next sentence prediction.
- RoBERTa: Got rid of next sentence prediction, optimized hyperparameters.
- DeBERTa: Focused on improvements to positional
- SpanBERT: mask contiguous tokens instead of random. Makes the task harder.
- . DistilBERT | ALBERT: training a small model to behave similarly to the bigger version
- BigBird | LongFormer: Self attention has O(N²) complexity. Models with sparse attention mechanisms have been proposed to extend the input length
- ClinicalBert | MedBert | PubMedBert | BEHRT: BERT-like models trained on specific domains
- ERNIE: add special entity embeddings into transforme
- for added benefit. Multi-lingual Models
- Multi-modal Models: combine text + visual
- ImageBERT: encodes objects as additional tokens.
 VilBERT: two parallel BERT encoders, interact using co-attention module, Image features are extracted using pre-trained Faster R-CNN
- Masked Image modelling: mask parts of image.
- Masked Protein modelling: AlphaFold.

Pre-training encoder-decoder models: Without parallel data: prefix language modelling give it half a sentence and predict the second half. Shuffle words and the task is to recover the original sentence masking just predict the full sentence. Instruction Tuning: took annotated datasets and phrased it as a Seq2Seq task. Place the query into a template into a conversational-sounding instruction.

Pre-training decoder models: train to optimize $p_{\theta}(w_t|w_{1:t-1})$ Great for tasks where the output has the same vocabulary as the pre-training data. **Fine tuning:** put a new layer on top and fine-tune the model for a desired task. **Zero-shot learning:** Give the model a natural language description of the task, have it generate the answer as a continuation. One-shot learning: In addition to the description of the task, give one example of solving the task. No gradient updates are performed. Few-shot learning: In addition to the task description, give a few examples of the task as input. No gradient updates are performed.



Advanced prompting and learning from human feedback: Chain of thought to show reasoning. Zero-shot chain of-thought: ask it to 'think step

Retrieval Based language models: NNs aren't a great place to store factual information because everything is distributed and smooth embeddings. Th the language model acts as the controller, and the factual retrieval model finds relevant texts from any databases you have. This allows for citations PROBLEMS: language models trained with instruction finetuning use manually created ground-truth data to follow instructions. Therefore, 1) tasks like open-ended creative generation have no right answer, 2) language modelling penalizes all token-level mistakes equally, but some errors are worse than others. Therefore introduce human feedback by giving possible answer. However, human-in-the-loop is expensive. Therefore, write a model to predict the scores of humans or to avoid noisy scores, write them to rank the answers instead.

Part of Speech Tagging: tokenizing sentences with type (adj, noun, etc.). The task is to estimate $P(T|W), T=t_1,\ldots,t_n \wedge W=w_1,\ldots,w_n$ as an instance of many to many classification. $P(T|W)=\frac{p(W|T)P(T)}{p(W)}=P(W|T)P(T)$ where $P(T) \approx P(t_1)P(t_2|t_2)\dots P(t_n|t_{n-1})$ by chain rule/bigram assumption and $P(W|T) \approx P(w_1|t_n)\dots P(w_n|t_n)$ where we estimate $P(t_i|t_{i-1}) = \frac{C(w_i,t_i)}{C(t_{i-1})} \wedge P(w_i|t_i) = \frac{C(w_i,t_i)}{C(t_i)}$. Generate two tables with this data including tags <s> and <\s> in the tag table. The table should be down: given I see Y, across what is the probability that I will see X. Then calculate with $P(T|W) \approx \sum_i P(t_i|t_{i-1}) \cdot P(w_i|t_i)$ for each cell. This is greedy.

		_
$Q=q_1q_2\dots q_N$	A set of N states (tags)	
$A=a_{11}a_{ij}\ldots a_{NN}$	A transition probability matrix A, each $a_{\bar{i}}$ representing the probability P of moving from state i to state j , s.t. $\sum_{j=1}^{N} a_{ij} = 1 \forall i$	l
$O = o_1 o_2 \dots o_T$	a sequence of T observations (words), each one drawn from a vocabulary $v_1 = v_1, v_2, \dots, v_V$	E
$B=b_i(o_t)$	a sequence of observation likelihoods (emission probabilities), each expressing the probability of an observation $\mathbf{o}_{\mathbf{i}}$ being generated from a state i	1
$\pi=\pi_1,\ldots,\pi_N$	π_i is the probability that the chain will start in state $i - \sum_{i=1}^N \pi_i = 1$	

function VITERBI(observations of len T.state-graph of len N) returns best-path, path-prob

create a path probability matrix viterbi[N,T] for each state s from 1 to N do : initialization step viterbi[s,1] $\leftarrow \pi_s * b_s(o_1)$ backpointer[s,1] $\leftarrow 0$ for each time step t from 2 to T do for each state s from 1 to N do $viterbi[s,t] \leftarrow \max_{s'=1}^{N} viterbi[s',t-1] * a_{s',s} * b_s(o_t)$ $\textit{backpointer}[s,t] \leftarrow \underset{}{\text{argmax}} \ \textit{viterbi}[s',t-1] * \textit{a}_{s',s} * \textit{b}_{s}(o_{t})$ $bestpathprob \leftarrow \max_{s}^{N} viterbi[s, T]$; termination step

 $bestpathpointer \leftarrow \underset{}{\operatorname{argmax}} viterbi[s, T]$; termination step

bestpath←the path starting at state bestpathpointer, that follows backpointer[] to states back in time

Dependency Parsing: (like in Alexa) how do words modify/link together? Head: origin/governer/ argument and dependent: modifier/destiny. The root is the governer of the entire sentence. Advantages: Ability to deal with languages that are morphologically rich (some languages words change place but sentence stays the same), the dependency link abstracts away the word order, Can be directly used to solve problems such as co-reference resolution, question answering. It is a directed graph G(V,A) where V is a set of verticies, A is a set of ordered pairs of verticies (Arcs). It has a single root, a vertex has exactly one incoming arc, unique path from ROOT to each vertex, no cycles MALT parser (transition-based): greedy → linear time. Reads sentence word by word, left to right + Greedy decision as to how to attach each word as it is read. σ stack (which starts with root), β buffer (which starts with all the words in the sentence) A set of arcs (which starts empty). There is a shift, left arc, right arc.

Start:
$$\sigma = [ROOT], \beta = w_1, ..., w_n, A = \emptyset$$
1. Shift $\sigma, w_i | \beta, A \rightarrow \sigma | w_i, \beta, A$

2. Left-Arc_r $\sigma|w_i|w_j$, β , $A \rightarrow \sigma|w_j$, β , $A \cup \{r(w_j, w_i)\}$

3. Right-Arc, $\sigma|w_i|w_i$, β , $A \rightarrow \sigma|w_i$, β , $A \cup \{r(w_i, w_i)\}$

Finish: $\sigma = [w]$, $\beta = \emptyset$

A machine learning classifier learns the actions to perform. The model can have categories (like subject, object, etc.), and the total number of operations is 2* categories + 1. Follow up work uses embeddings instead of sparse 1-hot encoded words, then softmax at the end. Accuracy and recall calculated (evaluating parsers) as above. Neural Parsing: RNN gives a flattened tree with brackets to indicate branches.

Hidden Markov Model Tagger: before, we don't consider all possible paths. How: $\hat{T} = \arg\max_x P(T|W)$. Assume: Markov to predict the future tag all that matters is the current state. <u>Independence</u> the probability of an output observation (word) o_i depends only on the state that produced the observation q_i

Emission probability: $P(w_i|t_i)$ and Transition probability: $P(t_{i+1}|t_i)$ Viterbi algorithm: $v_t(j) = \max_{i=1}^{N} v_{t-1}(i)a_{ij}b_i(o_t) = \max_{i=1}^{N} v_{t-1}(i)P(q_i|q_i)P(o_t|q_j)$ where $v_{t-1}(i)$ is the previous viterbi path probably from the previous time step, a_{ij} is the transition probability from the previous state q_i to the current state q_j and $b_j(o_t)$ is the emission probability.

The number of possible paths grows exponentially with the length of the input Viterbi's running time is $O(SN^2)$, where S is the length of the input and N is the number of states in the mode. Maybe BeamSearch.

Maximum entropy classifier: a discriminative model to directly estimate the posterior. $\hat{T} = \arg \max_x \prod P(t_i|w_i, t_{i-1})$ by giving it contextual words surrounding the task.

RNN for POS tagging: input the word embedding, output the tag, train with cross-entropy loss and run inference by selecting the most likely tag from softmax at each step.

SOTA: use multilingual BERT.

Constituency Parsing: Grammar checking, semantic analysis, parsing, downstream tasks. Challenge that in the lexicon many possible trees exist. Define a <u>Context free grammar</u>: G=(T,N,S,R) with Terminals, Nonterminals, Start Symbol, Rules from non-terminal — sequence of terminals/non-terminals.

The CKY algorithm: $O(n^3|G|)$: n is the length of the parsed string; |G| is the size of the CNF grammar G. Create a matrix nxn, use upper triangular portion, start at diagonal and record rules word matches. Step up and use two surrounding cells below to see if it satisfies any other rules. Continue until the corner.

Use it for <u>recognition</u> (does it contain a sentence?) <u>parsing</u> (include backpointers to see which rules stem from what other rules) retrieve sentences. Can also do statistical parsing (**Probabilistic context free grammar**) by finding the probability of a grammar: $q(X \to \gamma) = \frac{c(X \to \gamma)}{c(X)}$ by counting. Then tree branches have a probability attached. Multiply along the branches to get probability of

The CKY Algorithm for PCFG: same algorithm but be careful that creating a new rule doesn't change the probability. $X \to Y$. Z

Base case:
$$\pi[i,i,X] = q(X \to w_i)$$
, recursive case: $\pi[i,j,X] = \begin{cases} X \to Y,Z \\ s \in \{i\dots(j-1)\} \end{cases} (q(X \to YZ) \times \pi[i,s,Y] \times \pi[s+1,j,Z])$

his is essentially the CKY algorithm where pi refers to the span, given that its root token is X. Evaluating the Parsers: precision = |correct in hyp|/|total in hyp|, recall |correct in hyp|/|total in ref| and F-1 = 2 P R / (P + R). Issues: poor independence assumption removes structural dependencies across the tree, Word is only dependent on its POS tag.

Lack of lexical conditioning (the immediate neighbour might not be the most 'attention'). **Probabilistic Lexicalised CFG:** Add annotations specifying the head of each rule where rules can be $X(h) \rightarrow Y(h)Z(w)$ or $X(h) \rightarrow Y(w)Z(h)$ or $X(h) \rightarrow h$