

Semantica big-step

$$\begin{array}{c}
\text{(B-Num)} \frac{-}{\langle n, s \rangle \Downarrow n} \quad \text{(B-Loc)} \frac{-}{\langle l, s \rangle \Downarrow s(l)} \quad \text{(B-Skip)} \frac{-}{\langle \text{skip}, s \rangle \Downarrow s} \quad \text{(B-Add)} \frac{\langle E_1, s \rangle \Downarrow n_1 \quad \langle E_2, s \rangle \Downarrow n_2}{\langle E_1 + E_2 \rangle \Downarrow n_3} n_3 = \text{add}(n_1, n_2) \\
\\
\text{(B-Assign)} \frac{\langle E, s \rangle \Downarrow n}{\langle l := e, s \rangle \Downarrow s[l \mapsto n]} \quad \text{(B-Assign.s)} \frac{\langle E, s \rangle \Downarrow n}{\langle l := e, s \rangle \Downarrow \langle \text{skip}, s[l \mapsto n] \rangle} \quad \text{(B-Seq)} \frac{\langle C_1, s \rangle \Downarrow s_1 \quad \langle C_2, s_1 \rangle \Downarrow s'}{\langle C_1; C_2, s \rangle \Downarrow s'} \quad \text{(B-Seq.s)} \frac{\langle C_1, s \rangle \Downarrow \langle \text{skip}, s_1 \rangle \quad \langle C_2, s_1 \rangle \Downarrow \langle r, s' \rangle}{\langle C_1; C_2, s \rangle \Downarrow \langle r, s' \rangle} \\
\\
\text{(B-If.T)} \frac{\langle B, s \rangle \Downarrow \text{true} \quad \langle C_1, s \rangle \Downarrow s'}{\langle \text{if } B \text{ then } C_1 \text{ else } C_2, s \rangle \Downarrow s'} \quad \text{(B-If.T)} \frac{\langle B, s \rangle \Downarrow \text{true} \quad \langle C_1, s \rangle \Downarrow \langle r, s' \rangle}{\langle \text{if } B \text{ then } C_1 \text{ else } C_2, s \rangle \Downarrow \langle r, s' \rangle} \quad \text{(B-If.F)} \frac{\langle B, s \rangle \Downarrow \text{false} \quad \langle C_2, s \rangle \Downarrow s'}{\langle \text{if } B \text{ then } C_1 \text{ else } C_2, s \rangle \Downarrow s'} \quad \text{(B-If.F)} \frac{\langle B, s \rangle \Downarrow \text{false} \quad \langle C_2, s \rangle \Downarrow \langle r, s' \rangle}{\langle \text{if } B \text{ then } C_1 \text{ else } C_2, s \rangle \Downarrow \langle r, s \rangle} \\
\\
\text{(B-While.T)} \frac{\langle B, s \rangle \Downarrow \text{true} \quad \langle C, s \rangle \Downarrow s_1 \quad \langle \text{while } B \text{ do } C, s_1 \rangle \Downarrow s'}{\langle \text{while } B \text{ do } C, s \rangle \Downarrow s'} \quad \text{(B-While.F)} \frac{\langle B, s \rangle \Downarrow \text{false}}{\langle \text{while } B \text{ do } C, s \rangle \Downarrow s} \quad \text{(B-Do)} \frac{\langle B, s \rangle \Downarrow v_1 \quad \langle C, s \rangle \Downarrow v_2}{\langle \text{do } E \text{ return } C, s \rangle \Downarrow v_2} \\
\\
\text{(B-While.UN)} \frac{\langle \text{if } B \text{ then } (C; \text{while } B \text{ do } C) \text{ else skip}, s \rangle \Downarrow r, s'}{\langle \text{while } B \text{ do } C, s \rangle \Downarrow r, s'} \quad \text{(B-Await)} \frac{\langle B, s \rangle \Downarrow \text{true}, s_1 \quad \langle C, s_1 \rangle \rightarrow^* \langle \text{skip}, s' \rangle}{\langle \text{await } B \text{ protect } C \text{ end}, s \rangle \rightarrow \langle \text{skip}, s' \rangle} \\
\\
\text{(B-Let-CBV)} \frac{P \Downarrow m \quad E\{m/x\} \Downarrow n}{\text{let } x = P \text{ in } E \Downarrow n} \quad \text{(B-Let-CBN)} \frac{E\{P/x\} \Downarrow n}{\text{let } x = P \text{ in } E \Downarrow n} \quad \text{(B-Fn)} \frac{-}{\langle \text{fn } x: T \Rightarrow e, s \rangle \rightarrow \langle \text{fn } x: T \Rightarrow e, s \rangle} \\
\\
\text{(B-App-CBV)} \frac{E_1 \Downarrow \text{fn } x: T \Rightarrow E \quad E\{E_2/x\} \Downarrow n}{E_1 E_2 \Downarrow n} \quad \text{(B-App-CBN)} \frac{E_1 \Downarrow \text{fn } x: T \Rightarrow E \quad E_2 \Downarrow v \quad E\{v/x\} \Downarrow n}{E_1 E_2 \Downarrow n}
\end{array}$$

Semantica small-step

Grammatica delle espressioni

$$\text{op} ::= = + \mid \geq$$

$$e \in \text{Exp} ::= n \mid b \mid e \text{ op } e \mid \text{if } e \text{ then } e \text{ else } e \mid l := e \mid !l \mid \text{skip} \mid e; e \mid \text{while } e \text{ do } e \mid \text{fn } x: T \Rightarrow e \mid e_1 e_2 \mid \text{let } x: T = e \text{ in } e \mid e \oplus e \mid e \| e \mid \\ \text{await } e \text{ protect } e \text{ end} \mid \# \text{lab } e$$

Regole per la semantica

$$\text{S-Left} \frac{E_1 \rightarrow E'_1}{E_1 + E_2 \rightarrow E'_1 + E_2}$$

$$\text{S-Left} \frac{E_1 \rightarrow_{\text{ch}} E'_1}{E_1 + E_2 \rightarrow_{\text{ch}} E'_1 + E_2}$$

$$\text{op-geq} \frac{-}{\langle n_1 \geq n_2, s \rangle \rightarrow \langle b, s \rangle} b = \text{geq}(n_1, n_2)$$

$$\text{op1b} \frac{\langle e_2, s \rangle \rightarrow \langle e'_2, s' \rangle}{\langle e_1 + e_2, s \rangle \rightarrow \langle e_1 + e'_2, s' \rangle}$$

$$\text{deref2} \frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle !e, s \rangle \rightarrow \langle !e', s' \rangle}$$

$$\text{assign1} \frac{-}{\langle l := v, s \rangle \rightarrow \langle \text{skip}, s[l \mapsto v] \rangle} \text{if } l \in \text{dom}(s)$$

$$\text{if-tt} \frac{-}{\langle \text{if true then } e_1 \text{ else } e_2, s \rangle \rightarrow \langle e_1, s \rangle}$$

$$\text{while} \frac{-}{\langle \text{while } e \text{ do } e_1, s \rangle \rightarrow \langle \text{if } e \text{ then } (e_1; \text{while } e \text{ do } e_1) \text{ else skip}, s \rangle}$$

$$\text{seq.skip} \frac{-}{\langle \text{skip}; e_2, s \rangle \rightarrow \langle e_2, s \rangle}$$

$$\text{S-N.Right} \frac{E_2 \rightarrow E'_2}{n_1 + E_2 \rightarrow n_1 + E'_2}$$

$$\text{S-Right} \frac{E_2 \rightarrow_{\text{ch}} E'_2}{E_1 + E_2 \rightarrow_{\text{ch}} E_1 + E'_2}$$

$$\text{op1} \frac{\langle e_1, s \rangle \rightarrow \langle e'_1, s' \rangle}{\langle e_1 + e_2, s \rangle \rightarrow \langle e'_1 + e_2, s' \rangle}$$

$$\text{op2b} \frac{\langle e_1, s \rangle \rightarrow \langle e'_1, s' \rangle}{\langle e_1 + v, s \rangle \rightarrow \langle e'_1 + v', s' \rangle}$$

$$\text{ref1} \frac{-}{\langle \text{ref } v, s \rangle \rightarrow \langle l, s[l \mapsto v] \rangle} l \notin \text{dom}(s)$$

$$\text{assign2} \frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle l := e, s \rangle \rightarrow \langle l := e', s' \rangle}$$

$$\text{if-ff} \frac{-}{\langle \text{if false then } e_1 \text{ else } e_2, s \rangle \rightarrow \langle e_2, s \rangle}$$

$$\text{assign1b} \frac{-}{\langle l := n, s \rangle \rightarrow \langle n, s[l \mapsto n] \rangle} l \in \text{dom}(s)$$

$$\text{seq} \frac{\langle e_1, s \rangle \rightarrow \langle e'_1, s' \rangle}{\langle e_1; e_2, s \rangle \rightarrow \langle e'_1; e_2, s' \rangle}$$

$$\text{S-Add} \frac{-}{n_1 + n_2 \rightarrow n_3} n_3 = \text{add}(n_1, n_2)$$

$$\text{op+} \frac{-}{\langle n_1 + n_2, s \rangle \rightarrow \langle n, s \rangle} n = \text{add}(n_1, n_2)$$

$$\text{op2} \frac{\langle e_2, s \rangle \rightarrow \langle e'_2, s' \rangle}{\langle v + e_2, s \rangle \rightarrow \langle v + e'_2, s' \rangle}$$

$$\text{deref1} \frac{-}{\langle !l, s \rangle \rightarrow \langle v, s \rangle} \text{if } l \in \text{dom}(s) \wedge s(l) = v$$

$$\text{ref2} \frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle \text{ref } e, s \rangle \rightarrow \langle \text{ref } e', s' \rangle}$$

$$\text{assign3} \frac{\langle e_1, s \rangle \rightarrow \langle e'_1, s' \rangle}{\langle e_1 := e_2, s \rangle \rightarrow \langle e'_1 := e_2, s' \rangle}$$

$$\text{if} \frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle \text{if } e \text{ then } e_1 \text{ else } e_2, s \rangle \rightarrow \langle \text{if } e' \text{ then } e_1 \text{ else } e_2, s \rangle}$$

$$\text{seq.skipb} \frac{-}{\langle v; e_2, s \rangle \rightarrow \langle e_2, s \rangle}$$

$$\begin{array}{c}
\text{record1} \frac{\langle e_i, s \rangle \rightarrow \langle e'_i, s' \rangle}{\langle \{\text{lab}_1 = v_1, \dots, \text{lab}_i = e_i, \dots, \text{lab}_k = e_k\}, s \rangle \rightarrow \langle \{\text{lab}_1 = v_1, \dots, \text{lab}_i = e'_i, \dots, \text{lab}_k = e_k\}, s' \rangle} \\
\\
\text{record2} \frac{-}{\langle \#\text{lab}_i \{\text{lab}_1 = v_1, \dots, \text{lab}_i = e_i, \dots, \text{lab}_k = e_k\}, s \rangle \rightarrow \langle v_i, s \rangle} \quad \text{record3} \frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle \#\text{lab } e, s \rangle \rightarrow \langle \#\text{lab } e', s' \rangle} \\
\\
\text{par-L} \frac{\langle e_1, s \rangle \rightarrow \langle e'_1, s' \rangle}{\langle e_1 \parallel e_2, s \rangle \rightarrow \langle e'_1 \parallel e_2, s' \rangle} \quad \text{par-R} \frac{\langle e_2, s \rangle \rightarrow \langle e'_2, s' \rangle}{\langle e_1 \parallel e_2, s \rangle \rightarrow \langle e_1 \parallel e'_2, s' \rangle} \quad \text{end-L} \frac{-}{\langle \text{skip} \parallel e, s \rangle \rightarrow \langle e, s \rangle} \quad \text{end-R} \frac{-}{\langle e \parallel \text{skip}, s \rangle \rightarrow \langle e, s \rangle} \\
\\
\text{await} \frac{\langle e_1, s \rangle \rightarrow^* \langle \text{true}, s' \rangle \quad \langle e_2, s' \rangle \rightarrow^* \langle \text{skip}, s'' \rangle}{\langle \text{await } e_1 \text{ protect } e_2 \text{ end}, s \rangle \rightarrow \langle \text{skip}, s'' \rangle} \quad \text{ChoiceL} \frac{\langle e_1, s \rangle \rightarrow \langle e'_1, s' \rangle}{\langle e_1 \oplus e_2, s \rangle \rightarrow \langle e'_1, s' \rangle} \quad \text{ChoiceR} \frac{\langle e_2, s \rangle \rightarrow \langle e'_2, s' \rangle}{\langle e_1 \oplus e_2, s \rangle \rightarrow \langle e'_2, s' \rangle}
\end{array}$$

Grammatica dei tipi

$$T :: = \text{int} \mid \text{bool} \mid \text{unit} \mid T_1 \rightarrow T_2 \mid T_1 + T_2 \mid T_1 * T_2 \mid \text{ref } T \mid \{\text{lab}_1 : T_1, \dots, \text{lab}_k : T_k\}$$

Regole per il Tipaggio

Tipi primitivi e operatori

$$\begin{array}{c}
(\text{int}) \frac{-}{\Gamma \vdash n : \text{int}} \text{ for } n \in \mathbb{Z} \quad (\text{bool}) \frac{-}{\Gamma \vdash b : \text{bool}} \text{ for } n \in \{\text{true}, \text{false}\} \quad (\text{op } +) \frac{\Gamma \vdash e_1 : \text{int} \quad \Gamma \vdash e_2 : \text{int}}{\Gamma \vdash e_1 + e_2 : \text{int}} \quad (\text{op } *) \frac{\Gamma \vdash e_1 : \text{int} \quad \Gamma \vdash e_2 : \text{int}}{\Gamma \vdash e_1 * e_2 : \text{int}} \\
\\
(\text{op or}) \frac{\Gamma \vdash e_1 : \text{bool} \quad \Gamma \vdash e_2 : \text{bool}}{\Gamma \vdash e_1 \text{ or } e_2 : \text{bool}} \quad (\text{op and}) \frac{\Gamma \vdash e_1 : \text{bool} \quad \Gamma \vdash e_2 : \text{bool}}{\Gamma \vdash e_1 \text{ and } e_2 : \text{bool}} \quad (\text{op } \geq) \frac{\Gamma \vdash e_1 : \text{int} \quad \Gamma \vdash e_2 : \text{int}}{\Gamma \vdash e_1 \geq e_2 : \text{bool}} \\
\\
(\text{skip}) \frac{-}{\Gamma \vdash \text{skip} : \text{unit}} \quad (\text{seq}) \frac{\Gamma \vdash e_1 : \text{unit} \quad \Gamma \vdash e_2 : T}{\Gamma \vdash e_1; e_2 : T} \quad (\text{if}) \frac{\Gamma \vdash e_1 : \text{bool} \quad \Gamma \vdash e_2 : T \quad \Gamma \vdash e_3 : T}{\Gamma \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 : T} \quad (\text{while}) \frac{\Gamma \vdash e_1 : \text{bool} \quad \Gamma \vdash e_2 : T}{\Gamma \vdash \text{while } e_1 \text{ do } e_2 : T} \\
\\
(\text{let}) \frac{\Gamma \vdash e_1 : T \quad \Gamma, x : T \vdash e_2 : T'}{\Gamma \vdash \text{let } x : T = e_1 \text{ in } e_2 : T'}
\end{array}$$

Referenze

$$\begin{array}{c}
(\text{ref}) \frac{\Gamma \vdash e : T}{\Gamma \vdash \text{ref } e : \text{ref } T} \quad (\text{deref}) \frac{\Gamma \vdash e : \text{ref } T}{\Gamma \vdash !e : T} \quad (\text{assign}) \frac{\Gamma \vdash e_1 : \text{ref } T \quad \Gamma \vdash e_2 : T}{\Gamma \vdash (e_1 = e_2) : \text{unit}} \quad (\text{loc}) \frac{-}{\Gamma \vdash l : \text{ref } T} \quad \Gamma(l) = \text{ref } T
\end{array}$$

Funzioni

$$\begin{array}{c} \text{(var)} \frac{-}{\Gamma \vdash: \top} \quad \text{if } \Gamma(x) = \top \qquad \text{(fn)} \frac{\Gamma, x: \top \vdash e: \top'}{\Gamma \vdash (\text{fn } x: \top \Rightarrow e): \top \rightarrow \top'} \qquad \text{(app)} \frac{\Gamma \vdash e_1: \top \rightarrow \top' \quad \Gamma \vdash e_2: \top}{\Gamma \vdash e_1 e_2: \top'} \end{array}$$

Record

$$\begin{array}{c} \text{(record)} \frac{\Gamma \vdash e_1: \top_1 \dots \Gamma \vdash e_k: \top_k}{\Gamma \vdash \{\text{lab}_1 = e_1, \dots, \text{lab}_k = e_k\} : \{\text{lab}_1: \top_1, \dots, \text{lab}_k: \top_k\}} \qquad \text{(recordproj)} \frac{\Gamma \vdash e: \{\text{lab}_1: \top_1, \dots, \text{lab}_k: \top_k\}}{\Gamma \vdash \# \text{lab}_i e: \top_i} \end{array}$$

Concorrenza

$$\begin{array}{c} \text{(T-sq1)} \frac{\Gamma \vdash e_1: \text{unit} \quad \Gamma \vdash e_2: \text{unit}}{\Gamma \vdash e_1; e_2: \text{unit}} \qquad \text{(T-sq2)} \frac{\Gamma \vdash e_1: \text{proc} \quad \Gamma \vdash e_2: \text{proc}}{\Gamma \vdash e_1; e_2: \text{proc}} \qquad \text{(T-par)} \frac{\Gamma \vdash e_1: \top_1 \quad \Gamma \vdash e_2: \top_2}{\Gamma \vdash e_1 \parallel e_2: \text{proc}} \quad \top_1, \top_2 \in \{\text{unit}, \text{proc}\} \\ \text{(T-await)} \frac{\Gamma \vdash e_1: \text{bool} \quad \Gamma \vdash e_2: \text{unit}}{\Gamma \vdash \text{await } e_1 \text{ protect } e_2 \text{ end: unit}} \qquad \text{(T-choice)} \frac{\Gamma \vdash e_1: \text{unit} \quad \Gamma \vdash e_2: \text{unit}}{\Gamma \vdash e_1 \oplus e_2: \text{unit}} \end{array}$$

Sottotipaggio

$$\begin{array}{c} \text{(sub)} \frac{\Gamma \vdash e: \top \quad \top <: \top'}{\Gamma \vdash e: \top'} \qquad \text{(s-refl)} \frac{-}{\top <: \top} \qquad \text{(s-trans)} \frac{\top <: \top' \quad \top' <: \top''}{\top <: \top''} \end{array}$$

Sottotipaggio dei record

$$\begin{array}{c} \text{(rec-perm)} \frac{\pi \text{ una permutazione di } 1, 2, \dots, k}{\{p_1: \top_1, \dots, p_k: \top_k\} <: \{p_{\pi(1)}: \top_{\pi(1)}, \dots, p_{\pi(k)}: \top_{\pi(k)}\}} \qquad \text{(rec-width)} \frac{-}{\{p_1: \top_1, \dots, p_k: \top_k, p_{k+1}: \top_{k+1}, \dots, p_z: \top_z\} <: \{p_1: \top_1, \dots, p_k: \top_k\}} \\ \text{(rec-depth)} \frac{\top_1 <: \top'_1 \dots \top_k <: \top'_k}{\{p_1: \top_1, \dots, p_k: \top_k\} <: \{p_1: \top'_1, \dots, p_k: \top'_k\}} \end{array}$$

Sottotipaggio delle funzioni

$$\text{(fun-sub)} \frac{\top_1 <: \top'_1 \quad \top_2 <: \top'_2}{\top_1 \rightarrow \top_2 <: \top'_1 \rightarrow \top'_2}$$

Sottotipaggio somma e prodotto

$$\begin{array}{c} \text{(prod-sub)} \frac{\top_1 <: \top'_1 \quad \top_2 <: \top'_2}{\top_1 * \top_2 <: \top'_1 * \top'_2} \qquad \text{(sum-sub)} \frac{\top_1 <: \top'_1 \quad \top_2 <: \top'_2}{\top_1 + \top_2 <: \top'_1 + \top'_2} \end{array}$$