Semantica big-step

$$(B-Num) \frac{-}{\langle n,s\rangle \Downarrow n} \qquad (B-Loe) \frac{-}{\langle l,s\rangle \Downarrow s(l)} \qquad (B-Skip) \frac{-}{\langle skip,s\rangle \Downarrow s} \qquad (B-Add) \frac{\langle E_1,s\rangle \Downarrow n_1}{\langle E_1+E_2\rangle \Downarrow n_3} n_3 = add(n_1,n_2)$$

$$(B-Assign) \frac{\langle E_2,s\rangle \Downarrow n}{\langle l:=e,s\rangle \Downarrow s[l\mapsto n]} \qquad (B-Assign.s) \frac{\langle E_3\rangle \Downarrow n}{\langle l:=e,s\rangle \Downarrow \langle skip,s[l\mapsto n]\rangle} \qquad (B-Seq) \frac{\langle C_1,s\rangle \Downarrow s_1}{\langle C_1;C_2,s\rangle \Downarrow s'} \qquad (B-Seq.s) \frac{\langle C_1,s\rangle \Downarrow s_1}{\langle C_1;C_2,s\rangle \Downarrow s'} \qquad (B-Seq.s) \frac{\langle C_1,s\rangle \Downarrow \langle skip,s_1\rangle \langle C_2,s_1\rangle \Downarrow \langle r,s'\rangle}{\langle C_1;C_2,s\rangle \Downarrow \langle r,s'\rangle}$$

$$(B-If.T) \frac{\langle B_2,s\rangle \Downarrow true \langle C_1,s\rangle \Downarrow s'}{\langle if B then C_1 else C_2,s\rangle \Downarrow s'} \qquad (B-If.F) \frac{\langle B_2,s\rangle \Downarrow false \langle C_2,s\rangle \Downarrow s'}{\langle if B then C_1 else C_2,s\rangle \Downarrow s'} \qquad (B-If.F) \frac{\langle B_2,s\rangle \Downarrow false \langle C_2,s\rangle \Downarrow s'}{\langle if B then C_1 else C_2,s\rangle \Downarrow \langle r,s'\rangle}$$

$$(B-While.T) \frac{\langle B_2,s\rangle \Downarrow true \langle C_2,s\rangle \Downarrow s'}{\langle shile B do C_2,s\rangle \Downarrow s'} \qquad (B-While.F) \frac{\langle B_2,s\rangle \Downarrow false \langle C_2,s\rangle \Downarrow s'}{\langle shile B do C_2,s\rangle \Downarrow s'} \qquad (B-Do) \frac{\langle B_2,s\rangle \Downarrow r_1 \langle C_2,s\rangle \Downarrow r_2}{\langle do E return C_2,s\rangle \Downarrow r_2}$$

$$(B-While.UN) \frac{\langle if B then \langle C_2,s\rangle \Downarrow s'}{\langle shile B do C_2,s\rangle \Downarrow r_2,s'} \qquad (B-Await) \frac{\langle B_2,s\rangle \Downarrow true,s_1}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-Await) \frac{\langle B_2,s\rangle \Downarrow true,s_1}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBV) \frac{\langle B_2,s\rangle \Downarrow r_1}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-App-CBN) \frac{\langle B_2,s\rangle \Downarrow r_2}{\langle shile B do C_2,s\rangle \Downarrow r_2} \qquad (B-A$$

Semantica small-step

Grammatica delle espressioni

op :: = +
$$| \ge |$$

 $e \in \mathrm{Exp} \ :: = \mathsf{n} \ | \ \mathsf{b} \ | \ \mathsf{e} \ \mathsf{op} \ \mathsf{e} \ | \ \mathsf{if} \ \mathsf{e} \ \mathsf{then} \ \mathsf{e} \ \mathsf{else} \ \mathsf{e} \ | \ \mathsf{l} \ ! \ \mathsf{e} \ \mathsf{e} \ | \ \mathsf{e} \$

Regole per la semantica

S-Left
$$E_1 \rightarrow E_1'$$

 $E_1 + E_2 \rightarrow E_1' + E_2$

S-Left
$$\frac{E_1 \rightarrow_{ch} E_1'}{E_1 + E_2 \rightarrow_{ch} E_1' + E_2}$$

$$op\text{-geq}\frac{-}{\langle \mathfrak{n}_1 \geqslant \mathfrak{n}_2, \mathfrak{s} \rangle \rightarrow \langle \mathfrak{b}, \mathfrak{s} \rangle}b = geq(\mathfrak{n}_1, \mathfrak{n}_2)$$

op1b
$$\frac{\langle e_2, s \rangle \rightarrow \langle e'_2, s' \rangle}{\langle e_1 + e_2, s \rangle \rightarrow \langle e_1 + e'_2, s' \rangle}$$

$$deref2 \frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle !e, s \rangle \rightarrow \langle !e', s' \rangle}$$

$$\mathbf{assign1} \frac{-}{\langle l := v, s \rangle \rightarrow \langle \text{skip}, s[l \mapsto v] \rangle} \text{if } l \in \text{dom}(s)$$

$$\text{if-tt} \frac{-}{ \langle \text{if true then } e_1 \text{ else } e_2, s \rangle \Rightarrow \langle e_1, s \rangle }$$

while
$$\frac{-}{\langle \text{while } e \text{ do } e_1, s \rangle \rightarrow \langle \text{if } e \text{ then } (e_1; \text{while } e \text{ do } e_1) \text{ else } \text{skip}, s \rangle}$$

$$seq.skip \frac{-}{\langle skip; e_2, s \rangle \rightarrow \langle e_2, s \rangle}$$

S-N.Right
$$\frac{E_2 \rightarrow E_2'}{n_1 + E_2 \rightarrow n_1 + E_2'}$$

S-Right
$$\frac{E_2 \rightarrow_{ch} E'_2}{E_1 + E_2 \rightarrow_{ch} E_1 + E'_2}$$

$$\mathbf{op1} \frac{\langle e_1, s \rangle \rightarrow \langle e_1', s' \rangle}{\langle e_1 + e_2, s \rangle \rightarrow \langle e_1' + e_2, s' \rangle}$$

$$\mathbf{op2b} \frac{\langle e_1, s \rangle \rightarrow \langle e'_1, s' \rangle}{\langle e_1 + \nu, s \rangle \rightarrow \langle e'_1 + \nu', s' \rangle}$$

$$\mathbf{ref1} \frac{-}{\langle \operatorname{ref} \nu, s \rangle \to \langle l, s[l \mapsto \nu] \rangle} l \notin dom(s)$$

$$\mathbf{assign2} \frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle l := e, s \rangle \rightarrow \langle l := e', s \rangle}$$

$$\text{if-ff} \dfrac{-}{\left\langle \text{if false then } e_1 \text{ else } e_2, \mathsf{s} \right\rangle \to \left\langle e_2, \mathsf{s} \right\rangle }$$

$$\mathbf{S\text{-}N.Right} \frac{\mathsf{E}_2 \Rightarrow \mathsf{E}_2'}{\mathsf{n}_1 + \mathsf{E}_2 \Rightarrow \mathsf{n}_1 + \mathsf{E}_2'} \qquad \qquad \mathbf{S\text{-}Add} \frac{-}{\mathsf{n}_1 + \mathsf{n}_2 \Rightarrow \mathsf{n}_3} \mathsf{n}_3 = \mathsf{add}(\mathsf{n}_1, \mathsf{n}_2)$$

$$\mathbf{S-Right} \frac{\mathsf{E}_2 \to_{\mathtt{ch}} \mathsf{E}_2'}{\mathsf{E}_1 + \mathsf{E}_2 \to_{\mathtt{ch}} \mathsf{E}_1 + \mathsf{E}_2'} \qquad \mathbf{op} + \frac{-}{\langle \mathsf{n}_1 + \mathsf{n}_2, \mathsf{s} \rangle \to \langle \mathsf{n}, \mathsf{s} \rangle} \mathsf{n} = \mathsf{add}(\mathsf{n}_1, \mathsf{n}_2)$$

$$op2 \frac{\langle e_2, s \rangle \rightarrow \langle e_2', s' \rangle}{\langle v + e_2, s \rangle \rightarrow \langle v + e_2', s \rangle}$$

$$\mathbf{op2b} \frac{\langle e_1, s \rangle \to \langle e_1', s' \rangle}{\langle e_1 + \nu, s \rangle \to \langle e_1' + \nu', s' \rangle} \qquad \qquad \mathbf{deref1} \frac{-}{\langle !l, s \rangle \to \langle \nu, s \rangle} \mathrm{if} \ l \in \mathsf{dom}(s) \land s(l) = \nu$$

ref2
$$\frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle \text{ref } e, s \rangle \rightarrow \langle \text{ref } e', s \rangle}$$

if
$$\frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle \text{if } e \text{ then } e_1 \text{ else } e_2, s \rangle \rightarrow \langle \text{if } e' \text{ then } e_1 \text{ else } e_2, s \rangle}$$

$$-\frac{-}{\langle l := n, s \rangle \Rightarrow \langle n, s[l \mapsto n] \rangle} l \in dom(s)$$

$$\frac{-}{\langle \nu; e_2, s \rangle \rightarrow \langle e_2, s \rangle}$$

$$\operatorname{par-L} \frac{\langle e_1, s \rangle \to \langle e_1', s' \rangle}{\langle e_1 \| e_2, s \rangle \to \langle e_1' \| e_2, s' \rangle}$$

$$\operatorname{par-R} \frac{\langle e_2, s \rangle \to \langle e_2', s' \rangle}{\langle e_1 \| e_2, s \rangle \to \langle e_1 \| e_2', s' \rangle} \qquad \operatorname{end-L} \frac{-}{\langle \operatorname{skip} \| e, s \rangle \to \langle e, s \rangle} \qquad \operatorname{end-R} \frac{-}{\langle e \| \operatorname{skip}, s \rangle \to \langle e, s \rangle}$$

end-L
$$\frac{-}{\langle \text{skip} || e, s \rangle \rightarrow \langle e, s \rangle}$$

end-R
$$\frac{-}{\langle e || \text{skip}, s \rangle \rightarrow \langle e, s \rangle}$$

$$\textbf{ChoiceL} \frac{\langle e_1, \mathsf{s} \rangle \to \langle e_1', \mathsf{s}' \rangle}{\langle e_1 \oplus e_2, \mathsf{s} \rangle \to \langle e_1', \mathsf{s}' \rangle}$$

ChoiceR
$$\frac{\langle e_2, s \rangle \rightarrow \langle e'_2, s' \rangle}{\langle e_1 \oplus e_2, s \rangle \rightarrow \langle e'_2, s' \rangle}$$

Grammatica dei tipi

$$T::=\mathrm{int}\ |\ \mathrm{bool}\ |\ \mathrm{unit}\ |\ T_1\to T_2\ |\ T_1+T_2\ |\ T_1*T_2\ |\ \mathrm{ref}\ T\ |\ \{lab_1:T_1,\ldots,lab_k:T_k\}$$

Regole per il Tipaggio

Tipi primitivi e operatori

(int)
$$\frac{-}{\Gamma \vdash \mathfrak{n} : \text{int}}$$
 for $\mathfrak{n} \in \mathbb{Z}$

$$(int) \frac{-}{\Gamma \vdash n : int} \text{ for } n \in \mathbb{Z}$$

$$(bool) \frac{-}{\Gamma \vdash b : bool} \text{ for } n \in \{true, false\}$$

$$(op +) \frac{\Gamma \vdash e_1 : int}{\Gamma \vdash e_1 + e_2 : int}$$

$$(op *) \frac{\Gamma \vdash e_1 : int}{\Gamma \vdash e_1 * e_2 : int}$$

$$(\mathbf{op} +) \frac{\Gamma \vdash e_1 \colon \mathrm{int} \qquad \Gamma \vdash e_2 \colon \mathrm{int}}{\Gamma \vdash e_1 + e_2 \colon \mathrm{int}}$$

$$(\text{op *}) \frac{\Gamma \vdash e_1 \colon \text{int} \qquad \Gamma \vdash e_2 \colon \text{int}}{\Gamma \vdash e_1 * e_2 \colon \text{int}}$$

$$(op or) \frac{\Gamma \vdash e_1 \colon bool \qquad \Gamma \vdash e_2 \colon bool}{\Gamma \vdash e_1 \text{ or } e_2 \colon bool}$$

(op and)
$$\frac{\Gamma \vdash e_1 \colon \text{bool} \qquad \Gamma \vdash e_2 \colon \text{bool}}{\Gamma \vdash e_1 \text{ and } e_2 \colon \text{bool}}$$

$$(\mathbf{op} \geqslant) \frac{\Gamma \vdash e_1 \colon \text{int} \qquad \Gamma \vdash e_2 \colon \text{int}}{\Gamma \vdash e_1 \geqslant e_2 \colon \text{bool}}$$

$$(op \ or) \frac{\Gamma \vdash e_1 \colon bool \quad \Gamma \vdash e_2 \colon bool}{\Gamma \vdash e_1 \text{ or } e_2 \colon bool} \qquad (op \ and) \frac{\Gamma \vdash e_1 \colon bool \quad \Gamma \vdash e_2 \colon bool}{\Gamma \vdash e_1 \text{ and } e_2 \colon bool} \qquad (op \geqslant) \frac{\Gamma \vdash e_1 \colon int \quad \Gamma \vdash e_2 \colon int}{\Gamma \vdash e_1 \geqslant e_2 \colon bool} \qquad (assign) \frac{\Gamma \vdash e \colon int}{\Gamma \vdash l \coloneqq e \colon unit} \text{ if } \Gamma(l) = intref$$

$$(skip) \frac{-}{\Gamma \vdash skip : unit}$$

$$(\text{seq}) \frac{\Gamma \vdash e_1 \colon \text{unit} \qquad \Gamma \vdash e_2 \colon \Gamma}{\Gamma \vdash e_1 ; e_2 \colon \Gamma}$$

$$(\text{seq}) \frac{\Gamma \vdash e_1 \colon \text{unit} \quad \Gamma \vdash e_2 \colon \mathsf{T}}{\Gamma \vdash e_1 \colon e_2 \colon \mathsf{T}} \qquad \qquad (\text{if}) \frac{\Gamma \colon e_1 \colon \text{bool} \quad \Gamma \vdash e_2 \colon \mathsf{T} \quad \Gamma \vdash e_3 \colon \mathsf{T}}{\Gamma \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \colon \mathsf{T}} \qquad \qquad (\text{while}) \frac{\Gamma \vdash e_1 \colon \text{bool} \quad \Gamma \vdash e_2 \colon \mathsf{T}}{\Gamma \vdash \text{while } e_1 \text{ do } e_2 \colon \mathsf{T}}$$

(while)
$$\frac{\Gamma \vdash e_1 \colon \text{bool} \qquad \Gamma \vdash e_2 \colon \mathsf{T}}{\Gamma \vdash \text{while } e_1 \text{ do } e_2 \colon \mathsf{T}}$$

(let)
$$\frac{\Gamma \vdash e_1 \colon \mathsf{T} \qquad \Gamma, \mathsf{x} \colon \mathsf{T} \vdash e_2 \colon \mathsf{T}'}{\Gamma \vdash \text{let } \mathsf{x} \colon \mathsf{T} = e_1 \text{ in } e_2 \colon \mathsf{T}'}$$

Funzioni

$$(\mathbf{var}) \frac{-}{\Gamma \vdash \cdot T} \text{ if } \Gamma(x) = T$$

$$(\mathbf{fn}) \frac{\Gamma, x \colon T \vdash e \colon T'}{\Gamma \vdash (\mathbf{fn} \ x \colon T \ \Rightarrow \ e) \colon T \to T'}$$

$$(\operatorname{fn}) \frac{\Gamma, x \colon \mathsf{T} \vdash e \colon \mathsf{T}'}{\Gamma \vdash (\operatorname{fn} x \colon \mathsf{T} \ \Rightarrow \ e) \colon \mathsf{T} \to \mathsf{T}'} \qquad (\operatorname{app}) \frac{\Gamma \vdash e_1 \colon \mathsf{T} \to \mathsf{T}' \qquad \Gamma \vdash e_2 \colon \mathsf{T}}{\Gamma \vdash e_1 e_2 \colon \mathsf{T}'}$$

Concorrenza

(T-sq1)
$$\frac{\Gamma \vdash e_1 : \text{unit} \qquad \Gamma \vdash e_2 : \text{unit}}{\Gamma \vdash e_1 : e_2 : \text{unit}}$$

$$(\mathbf{T}\text{-}\mathbf{sq2}) \frac{\Gamma \vdash e_1 \colon \operatorname{proc} \qquad \Gamma \vdash e_2 \colon \operatorname{proc}}{\Gamma \vdash e_1 \colon e_2 \colon \operatorname{proc}}$$

$$(\mathbf{T}\text{-}\mathbf{sq2}) \frac{\Gamma \vdash e_1 \colon \operatorname{proc} \quad \Gamma \vdash e_2 \colon \operatorname{proc}}{\Gamma \vdash e_1 \colon e_2 \colon \operatorname{proc}} \qquad \qquad (\mathbf{T}\text{-}\mathbf{par}) \frac{\Gamma \vdash e_1 \colon \mathsf{T}_1 \quad \Gamma \vdash e_2 \colon \mathsf{T}_2}{\Gamma \vdash e_1 \| e_2 \colon \operatorname{proc}} \quad \mathsf{T}_1, \mathsf{T}_2 \in \{\operatorname{unit}, \operatorname{proc}\}$$

(T-await)
$$\frac{\Gamma \vdash e_1 \colon \text{bool} \qquad \Gamma \vdash e_2 \colon \text{unit}}{\Gamma \vdash \text{await } e_1 \text{ protect } e_2 \text{ end} \colon \text{unit}}$$

(T-choice)
$$\frac{\Gamma \vdash e_1 : \text{unit} \qquad \Gamma \vdash e_2 : \text{unit}}{\Gamma \vdash e_1 \oplus e_2 : \text{unit}}$$

Sottotipaggio

(sub)
$$\frac{\Gamma \vdash e : T \qquad T <: T'}{\Gamma \vdash e : T'}$$

$$(s-refl) \frac{-}{T <: T}$$

$$(s\text{-refl}) \frac{-}{\mathsf{T} <: \mathsf{T}} \qquad \qquad (s\text{-trans}) \frac{\mathsf{T} <: \mathsf{T}' \qquad \mathsf{T}' <: \mathsf{T}''}{\mathsf{T} <: \mathsf{T}''}$$

Sottotipaggio dei record

$$\frac{-}{\{p_1\colon T_1,\dots,p_k\colon T_k,p_{k+1}\colon T_{k+1},\dots,p_z\colon T_z\}<\colon \{p_1\colon T_1,\dots,p_k\colon T_k\}}$$

$$(\text{rec-depth}) \frac{\mathsf{T}_1 <: \mathsf{T}_1' \ \dots \ \mathsf{T}_k <: \mathsf{T}_k'}{\{ \mathsf{p}_1 \colon \mathsf{T}_1, \dots, \mathsf{p}_k \colon \mathsf{T}_k \} <: \{ \mathsf{p}_1 \colon \mathsf{T}_1', \dots, \mathsf{p}_k \colon \mathsf{T}_k' \}}$$

Sottotipaggio delle funzioni

$$\textbf{(fun-sub)} \frac{\mathsf{T}_1\colon >\mathsf{T}_1' \quad \mathsf{T}_2<\colon \mathsf{T}_2'}{\mathsf{T}_1\to\mathsf{T}_2<\colon \mathsf{T}_1'\to\mathsf{T}_2'}$$

Sottotipaggio somma e prodotto

$$\textbf{(prod-sub)} \frac{ T_1 <: T_1' \quad T_2 <: T_2' }{ T_1 * T_2 <: T_1' * T_2' }$$

$$(\text{sum-sub}) \frac{\mathsf{T}_1 <: \mathsf{T}_1' \qquad \mathsf{T}_2 <: \mathsf{T}_2'}{\mathsf{T}_1 + \mathsf{T}_2 <: \mathsf{T}_1' + \mathsf{T}_2'}$$