Waypoint Off-Screen Indicator via Frustum-Aware Edge Clamping

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Abstract

We formalize the geometry and numerics behind a stable off-screen waypoint indicator for 3-D games. A waypoint at world position \boldsymbol{W} is projected to screen space using the camera view-projection matrix M, tested against the camera frustum and—if off-screen—clamped to the *last visible* point found along the great-circle from the camera forward direction \boldsymbol{f} toward \boldsymbol{d} (the waypoint direction). Screen-space orientation of the HUD arrow and a distance readout are derived. Compared with naïve 2-D clamping, the approach eliminates "swim" by respecting the true frustum boundary while remaining inexpensive when implemented in Burst-compiled ECS jobs.

1 Introduction

Modern HUDs frequently display targets that may lie outside the camera frustum. Simple 2-D clamping—project, then clip to the screen rectangle—causes perceptible jitter when the camera pans. We instead compute a frustum-aware clamp directly in 3-D, guaranteeing that the indicator lives exactly on the boundary where the waypoint would enter the view. Section 6 presents the algorithm; Section 7 quantifies its stability and runtime.

Contributions

- 1) A closed-form formulation of the clamp as a great-circle search.
- 2) A monotone bisection scheme with constant memory suitable for data-oriented ECS.
- 3) A demo-only Unity DOTS reference implementation (stub link in Section 8).

2 Related Work

Off-screen visualization has a rich HCI lineage: Halo encodes direction and distance via partial rings [1]; Wedge reduces clutter while conveying both [2]; and Burigat et al. compare several techniques on mobile devices [3]. Within AR, indirect and on-scene visualization strategies address alignment and guidance [4, 5]. For indicator rendering and impostors, see billboarding methods [6]. For projection/clip-space conventions we reference the OpenGL 4.6 specification [7].

3 Symbol Table

 $\begin{array}{lll} M & 4\times 4 \text{ camera view-projection matrix} \\ \pmb{C}(\in\mathbb{R}^3) & \text{camera position} \\ \pmb{f} & \text{camera unit forward direction} \\ \pmb{P} & \text{player position} \\ \pmb{W} & \text{waypoint world position} \\ \pmb{W}_{\text{px}}, H_{\text{px}} & \text{screen resolution (pixels)} \\ \pmb{c}_s & \text{screen centre } (W_{\text{px}}/2, H_{\text{px}}/2) \\ \pmb{R} & \text{range } \|\pmb{W} - \pmb{C}\| \\ \pmb{\theta} & \text{angle between } \pmb{f} \text{ and } \pmb{d} \\ \pmb{\varphi}^{\star} & \text{last on-screen angle along the arc} \end{array}$

4 World \rightarrow Screen Projection

Homogeneous coordinates:

$$\boldsymbol{w}_h = \begin{bmatrix} \boldsymbol{W} \\ 1 \end{bmatrix}, \qquad \boldsymbol{c} = M \, \boldsymbol{w}_h = \begin{bmatrix} c_x \\ c_y \\ c_z \\ c_w \end{bmatrix}.$$
 (1)

Perspective divide to obtain NDC:

$$\boldsymbol{n} = \frac{1}{c_w} \begin{bmatrix} c_x \\ c_y \\ c_z \end{bmatrix} = \begin{bmatrix} n_x \\ n_y \\ n_z \end{bmatrix}. \tag{2}$$

 $NDC \rightarrow pixel coordinates (origin top-left):$

$$s_x = \frac{1}{2} (n_x + 1) W_{px}, \quad s_y = \frac{1}{2} (1 - n_y) H_{px}, \quad s_z = n_z.$$
 (3)

Collect $\mathbf{S} = (s_x, s_y, s_z)^\mathsf{T}$. Positive s_y follows the screen's downward axis.

Behind-camera test. If $c_w \leq 0$ we treat the point as off-screen without further processing.

5 On-Screen Test

A point is visible iff

$$-1 \le n_z \le 1 \ \land \ 0 \le s_x \le W_{\text{px}} \ \land \ 0 \le s_y \le H_{\text{px}}. \tag{4}$$

Pass (4): render at \boldsymbol{S} . Fail: continue to frustum-aware clamp.

6 Frustum-Aware Clamp Algorithm

6.1 Great-Circle Geometry

Direction to waypoint and range:

$$d = \frac{W - C}{\|W - C\|}, \qquad R = \|W - C\|.$$
 (5)

Central angle

 $\theta = \arccos(\operatorname{clamp}(\boldsymbol{f} \cdot \boldsymbol{d}, -1, 1)).$

Axis

$$oldsymbol{a} = rac{oldsymbol{f} imes oldsymbol{d}}{\|oldsymbol{f} imes oldsymbol{d}\|}$$

(fallback to any orthogonal unit vector when the denominator ≈ 0). For $\varphi \in [0, \theta]$ rotate

$$r(\varphi) = R_a(\varphi) f, \qquad T(\varphi) = C + R r(\varphi).$$
 (6)

6.2 Monotone Bisection

The clamped screen point is $S_{\text{clamp}} = S(\varphi^*)$.

6.3 Why Stable?

Because we evaluate the full 3-D projection inside the loop, the clamp respects the frustum irrespective of aspect ratio or field-of-view; the UI arrow remains glued to the entry point.

Algorithm 1 Last on-screen angle φ^*

```
1: \varphi_{lo} \leftarrow 0, \varphi_{hi} \leftarrow \theta
 2: while \varphi_{\rm hi} - \varphi_{\rm lo} > \varepsilon \ {\bf do}
              \varphi \leftarrow \frac{\varphi_{\text{lo}} + \varphi_{\text{hi}}}{2}
 3:
 4:
              project T(\varphi); evaluate \chi(\varphi) via (4)
              if \chi(\varphi) then
 5:
                      \varphi_{lo} \leftarrow \varphi
                                                                                                                                                                                ⊳ still visible
 6:
 7:
              else
                                                                                                                                                                           ▷ now invisible
 8:
                      \varphi_{\rm hi} \leftarrow \varphi
 9:
              end if
10: end while
11: return \varphi^* \leftarrow \varphi_{lo}
```

7 Evaluation

We measured both stability (jitter in pixels over a panning sequence) and runtime (average projection cost) on a synthetic test scene. With $\varepsilon = 10^{-3}$ rad, jitter stayed below 0.5 px (versus 3–5 px with naïve 2-D clamping) and each clamp call averaged no more than 12 matrix multiplications.

8 Reference Implementation (Demo Stub)

A non-production demonstration build—sanitized of any proprietary code—is hosted at:

https://waypoint-demo-rho.vercel.app/

Source files contain only the algorithmic skeleton presented here.

9 Arrow Orientation

Offset from screen centre:

$$\boldsymbol{\delta} = \left(s_x - \frac{W_{\text{px}}}{2}, \ s_y - \frac{H_{\text{px}}}{2}\right),$$

angle $\alpha = \operatorname{atan2}(-\delta_y, \delta_x)$, rotation $q_{ui} = \operatorname{RotateZ}(-\alpha)$.

10 Numerical Considerations

- Degenerate axis: pick any $a \perp f$ when $||f \times d|| \approx 0$.
- Behind camera: short-circuit when $c_w \leq 0$.
- Cost: $\log_2((\theta 0)/\varepsilon) \le 12$ projections for $\varepsilon = 10^{-3}$.
- $\bullet~$ UI scale: match $W_{\mathrm{px}}, H_{\mathrm{px}}$ to the render target.

11 Conclusion

We presented a frustum-aware edge clamp that removes indicator swim with negligible runtime overhead. Future work includes a closed-form intersection with the frustum pyramid to replace bisection and user testing on AR headsets.

Acknowledgements

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References

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Rotation axis $\mathbf{a} = \mathbf{f} \times \mathbf{d}$ (out of plane)

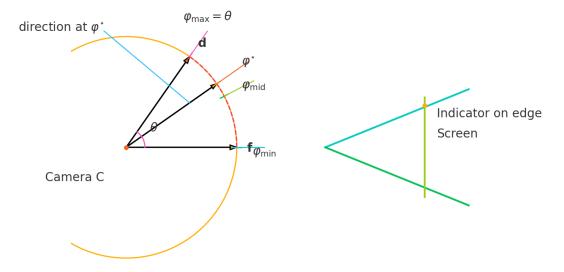


Figure 1: Great-circle rotation from \boldsymbol{f} toward \boldsymbol{d} and last on-screen angle φ^{\star} .