810 Team Project

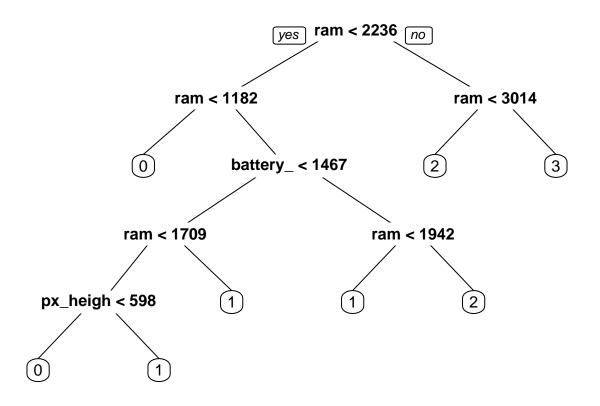
Bo Li U24425931

2/24/2021

```
library(data.table)
library(ggplot2)
library(ggthemes)
library(glmnet)
## Loading required package: Matrix
## Loaded glmnet 4.1
theme_set(theme_bw())
library(MASS)
library(rpart)
library(rpart.plot)
library(ipred)
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
## Attaching package: 'randomForest'
## The following object is masked from 'package:ggplot2':
##
##
       margin
library(caret)
## Loading required package: lattice
library(e1071)
library(caTools)
data <- fread("C:/Users/boli0/Downloads/train.csv")</pre>
str(data)
```

```
## Classes 'data.table' and 'data.frame': 2000 obs. of 21 variables:
## $ battery_power: int 842 1021 563 615 1821 1859 1821 1954 1445 509 ...
                  : int 0 1 1 1 1 0 0 0 1 1 ...
## $ clock_speed : num
                        2.2 0.5 0.5 2.5 1.2 0.5 1.7 0.5 0.5 0.6 ...
## $ dual sim
                  : int
                        0 1 1 0 0 1 0 1 0 1 ...
## $ fc
                  : int 1 0 2 0 13 3 4 0 0 2 ...
## $ four_g
                 : int 0 1 1 0 1 0 1 0 0 1 ...
## $ int_memory
                  : int
                        7 53 41 10 44 22 10 24 53 9 ...
## $ m dep
                  : num 0.6 0.7 0.9 0.8 0.6 0.7 0.8 0.8 0.7 0.1 ...
## $ mobile_wt
                  : int 188 136 145 131 141 164 139 187 174 93 ...
## $ n_cores
                 : int 2 3 5 6 2 1 8 4 7 5 ...
                        2 6 6 9 14 7 10 0 14 15 ...
## $ pc
                  : int
## $ px_height
                : int 20 905 1263 1216 1208 1004 381 512 386 1137 ...
## $ px_width
                : int 756 1988 1716 1786 1212 1654 1018 1149 836 1224 ...
## $ ram
                        2549 2631 2603 2769 1411 1067 3220 700 1099 513 ...
                  : int
## $ sc_h
                 : int 9 17 11 16 8 17 13 16 17 19 ...
## $ sc_w
                 : int 7 3 2 8 2 1 8 3 1 10 ...
## $ talk_time
                : int 19 7 9 11 15 10 18 5 20 12 ...
                 : int 0 1 1 1 1 1 1 1 1 1 ...
## $ three_g
## $ touch screen : int 0 1 1 0 1 0 0 1 0 0 ...
                 : int 1000001100...
## $ wifi
## $ price_range : int 1 2 2 2 1 1 3 0 0 0 ...
## - attr(*, ".internal.selfref")=<externalptr>
set.seed(810)
split = sample.split(data$price_range, SplitRatio = 0.7)
data_train = subset(data, split == TRUE)
data_test = subset(data, split == FALSE)
# 1-1. Build linear regression model
linreg = lm(price_range ~., data = data_train)
summary(linreg)
##
## Call:
## lm(formula = price_range ~ ., data = data_train)
## Residuals:
##
                    Median
       Min
                 1Q
                                  3Q
                                          Max
## -1.01082 -0.24804 0.00676 0.24155 0.84015
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                -1.532e+00 7.328e-02 -20.901 < 2e-16 ***
## battery_power 5.100e-04 1.930e-05 26.426 < 2e-16 ***
## blue
                -6.726e-03 1.723e-02 -0.390 0.69637
## clock speed -2.043e-02 1.054e-02 -1.937 0.05289 .
## dual sim
               -2.722e-02 1.726e-02 -1.577 0.11503
## fc
                                      0.488 0.62587
                1.262e-03 2.587e-03
## four_g
                -3.044e-02 2.114e-02 -1.439 0.15027
## int_memory
                8.259e-04 4.743e-04
                                      1.741 0.08184
## m_dep
                -3.580e-02 2.991e-02 -1.197 0.23152
```

```
## mobile_wt -7.184e-04 2.430e-04 -2.957 0.00316 **
## n_cores 1.126e-03 3.769e-03 0.299 0.76517
## pc
                -3.519e-04 1.809e-03 -0.195 0.84575
## px_height 2.498e-04 2.236e-05 11.171 < 2e-16 ***
## px_width 2.866e-04 2.294e-05 12.493 < 2e-16 ***
## ram
               9.477e-04 7.942e-06 119.326 < 2e-16 ***
                7.565e-04 2.380e-03 0.318 0.75065
## sc h
## sc_w -1.125e-03 2.285e-03 -0.493 0.62243
## touch_screen 7.650e-03 1.714e-02 0.446 0.65536
                -1.956e-02 1.719e-02 -1.138 0.25538
## wifi
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.3196 on 1379 degrees of freedom
## Multiple R-squared: 0.9195, Adjusted R-squared: 0.9183
## F-statistic: 787.5 on 20 and 1379 DF, p-value: < 2.2e-16
# 1-2. linear regression sse is 63.55421
linreg.pred = predict(linreg, newdata = data_test)
linreg.sse = sum((linreg.pred - data_test$price_range)^2)
linreg.sse
## [1] 63.55421
# 2-1. Build single decision tree classification
tree = rpart(price_range ~ .,method = "class", data = data_train,control = rpart.control(minsplit = 1)
prp(tree)
```



print(tree)

```
## n= 1400
##
## node), split, n, loss, yval, (yprob)
         * denotes terminal node
##
##
   1) root 1400 1050 0 (0.250000000 0.250000000 0.250000000 0.250000000)
      2) ram< 2235.5 727 377 0 (0.481430536 0.416781293 0.101788171 0.000000000)
##
                           41 0 (0.878338279 0.121661721 0.000000000 0.000000000) *
##
        4) ram< 1182 337
        5) ram>=1182 390 128 1 (0.138461538 0.671794872 0.189743590 0.000000000)
##
                                         68 1 (0.216867470 0.726907631 0.056224900 0.000000000)
##
         10) battery_power< 1466.5 249
                                 53 1 (0.430894309 0.569105691 0.000000000 0.000000000)
##
           20) ram< 1708.5 123
                                     17 0 (0.721311475 0.278688525 0.000000000 0.000000000) *
##
             40) px_height< 598 61
                                      9 1 (0.145161290 0.854838710 0.000000000 0.000000000) *
             41) px_height>=598 62
##
                                 15 1 (0.007936508 0.880952381 0.1111111111 0.000000000) *
##
           21) ram>=1708.5 126
                                         60 1 (0.00000000 0.574468085 0.425531915 0.000000000)
##
         11) battery power>=1466.5 141
##
           22) ram< 1941.5 110
                                 30 1 (0.000000000 0.727272727 0.272727273 0.000000000) *
                                 1 2 (0.00000000 0.032258065 0.967741935 0.000000000) *
##
           23) ram>=1941.5 31
##
      3) ram>=2235.5 673 323 3 (0.000000000 0.069836553 0.410104012 0.520059435)
##
        6) ram< 3013.5 318 98 2 (0.000000000 0.147798742 0.691823899 0.160377358) *
                             56 3 (0.000000000 0.000000000 0.157746479 0.842253521) *
##
        7) ram>=3013.5 355
```

summary(tree)

```
## Call:
## rpart(formula = price_range ~ ., data = data_train, method = "class",
       parms = list(split = "information"), control = rpart.control(minsplit = 1))
     n = 1400
##
##
             CP nsplit rel error
##
                                    xerror
                                                 xstd
                     0 1.0000000 1.0495238 0.01458632
## 1 0.33333333
                     1 0.6666667 0.6676190 0.01781740
## 2 0.19809524
## 3 0.16095238
                     2 0.4685714 0.4771429 0.01708226
                     3 0.3076190 0.3257143 0.01531097
## 4 0.01380952
## 5 0.01285714
                     5 0.2800000 0.3038095 0.01494703
## 6 0.01000000
                     7 0.2542857 0.2752381 0.01442290
## Variable importance
##
             ram battery_power
                                   px_height
                                                  px_width
                                                                     sc_w
##
              78
                             7
                                           5
                                                          2
                                                                        2
##
      int_memory
                     mobile_wt
                                          fc
                                                                 dual_sim
                                                        рс
##
               2
                                           1
                                                          1
##
## Node number 1: 1400 observations,
                                        complexity param=0.3333333
##
     predicted class=0 expected loss=0.75 P(node) =1
##
       class counts:
                      350
                             350
##
      probabilities: 0.250 0.250 0.250 0.250
     left son=2 (727 obs) right son=3 (673 obs)
##
##
     Primary splits:
##
         ram
                       < 2235.5 to the left, improve=650.760600, (0 missing)
##
         battery_power < 1332.5 to the left, improve= 37.065280, (0 missing)
                       < 1630.5 to the left, improve= 25.439830, (0 missing)
##
         px_width
##
                       < 1212 to the left, improve= 18.147350, (0 missing)
         px_height
##
         mobile_wt
                       < 104.5 to the left, improve= 9.566532, (0 missing)
##
     Surrogate splits:
##
         px_height
                       < 280.5 to the right, agree=0.549, adj=0.062, (0 split)
##
         battery_power < 1721.5 to the left, agree=0.534, adj=0.031, (0 split)
##
                                to the left, agree=0.534, adj=0.031, (0 split)
                       < 10.5
         sc_w
##
                       < 13.5
                                to the left, agree=0.528, adj=0.018, (0 split)
         fc
                       < 42.5
##
                                to the left, agree=0.528, adj=0.018, (0 split)
         int_memory
##
## Node number 2: 727 observations,
                                       complexity param=0.1980952
     predicted class=0 expected loss=0.5185695 P(node) =0.5192857
##
                       350
##
                             303
                                    74
       class counts:
     probabilities: 0.481 0.417 0.102 0.000
##
     left son=4 (337 obs) right son=5 (390 obs)
##
##
     Primary splits:
##
                       < 1182
                                to the left, improve=231.36100, (0 missing)
         ram
                                to the left, improve= 47.93258, (0 missing)
##
         battery_power < 1455</pre>
                       < 639.5 to the left, improve= 33.61836, (0 missing)
##
         px_height
##
         px_width
                       < 1144.5 to the left, improve= 29.33494, (0 missing)
##
                       < 186.5 to the left, improve= 4.38501, (0 missing)
         mobile_wt
##
     Surrogate splits:
##
         px_width
                    < 684.5 to the left, agree=0.567, adj=0.065, (0 split)
##
                             to the left, agree=0.557, adj=0.045, (0 split)
                    < 1.5
         рс
##
         mobile_wt < 100.5 to the left, agree=0.556, adj=0.042, (0 split)
##
         px_height < 286.5 to the left, agree=0.554, adj=0.039, (0 split)
                             to the left, agree=0.550, adj=0.030, (0 split)
##
         int memory < 6.5
```

```
##
                                       complexity param=0.1609524
## Node number 3: 673 observations,
##
    predicted class=3 expected loss=0.4799406 P(node) =0.4807143
##
       class counts:
                         0
                             47
                                   276
                                         350
##
      probabilities: 0.000 0.070 0.410 0.520
##
     left son=6 (318 obs) right son=7 (355 obs)
##
     Primary splits:
##
         ram
                       < 3013.5 to the left, improve=180.93670, (0 missing)
##
         battery_power < 1352.5 to the left, improve= 46.75949, (0 missing)
##
         px_width
                       < 1283 to the left, improve= 31.47901, (0 missing)
##
        px_height
                       < 955
                                to the left, improve= 24.86811, (0 missing)
                       < 10.5 to the left, improve= 7.02468, (0 missing)
##
         int_memory
##
     Surrogate splits:
##
         battery_power < 589
                               to the left, agree=0.548, adj=0.044, (0 split)
##
                               to the right, agree=0.544, adj=0.035, (0 split)
         sc_h
                       < 18.5
##
                       < 4.5
                                to the left, agree=0.541, adj=0.028, (0 split)
         int_memory
##
                       < 1074
                               to the left, agree=0.541, adj=0.028, (0 split)
         px_width
##
         dual sim
                       < 0.5
                                to the left, agree=0.536, adj=0.019, (0 split)
##
## Node number 4: 337 observations
##
     predicted class=0 expected loss=0.1216617 P(node) =0.2407143
       class counts: 296
##
                             41
                                     0
##
      probabilities: 0.878 0.122 0.000 0.000
##
## Node number 5: 390 observations,
                                       complexity param=0.01380952
##
     predicted class=1 expected loss=0.3282051 P(node) =0.2785714
##
       class counts:
                       54
                             262
                                    74
      probabilities: 0.138 0.672 0.190 0.000
##
##
     left son=10 (249 obs) right son=11 (141 obs)
##
     Primary splits:
##
         battery_power < 1466.5 to the left, improve=57.255060, (0 missing)
##
                       < 1508.5 to the left, improve=47.743900, (0 missing)
##
                       < 674.5 to the left, improve=31.980610, (0 missing)
        px_height
##
                       < 1113.5 to the left, improve=29.405230, (0 missing)
        px_width
                               to the left, improve= 3.540274, (0 missing)
##
        n cores
                       < 4.5
##
     Surrogate splits:
##
        px height < 1639.5 to the left, agree=0.649, adj=0.028, (0 split)
##
        talk_time < 3.5
                           to the right, agree=0.646, adj=0.021, (0 split)
##
         px_width < 530.5 to the right, agree=0.644, adj=0.014, (0 split)
##
                   < 1203.5 to the right, agree=0.641, adj=0.007, (0 split)
        ram
##
## Node number 6: 318 observations
##
     predicted class=2 expected loss=0.3081761 P(node) =0.2271429
##
                                   220
       class counts:
                         0
                              47
##
      probabilities: 0.000 0.148 0.692 0.160
##
## Node number 7: 355 observations
     predicted class=3 expected loss=0.1577465 P(node) =0.2535714
##
##
       class counts:
                         0
                               0
                                    56
##
      probabilities: 0.000 0.000 0.158 0.842
##
## Node number 10: 249 observations,
                                        complexity param=0.01285714
##
    predicted class=1 expected loss=0.2730924 P(node) =0.1778571
##
      class counts:
                       54 181
                                    14
```

```
##
      probabilities: 0.217 0.727 0.056 0.000
##
     left son=20 (123 obs) right son=21 (126 obs)
##
     Primary splits:
##
         ram
                       < 1708.5 to the left, improve=46.820460, (0 missing)
##
         px_width
                       < 1479.5 to the left, improve=24.350920, (0 missing)
##
                       < 736
                                to the left, improve=20.883800, (0 missing)
         px height
         battery_power < 1027.5 to the left, improve=15.672300, (0 missing)
##
                                to the right, improve= 6.621616, (0 missing)
##
         sc h
                       < 11.5
##
     Surrogate splits:
##
         sc_w
                       < 4.5
                                to the left, agree=0.574, adj=0.138, (0 split)
##
                       < 1779
                                to the right, agree=0.570, adj=0.130, (0 split)
         px_width
                                to the left, agree=0.558, adj=0.106, (0 split)
##
         battery_power < 558
                                to the left, agree=0.554, adj=0.098, (0 split)
##
                       < 0.5
##
                       < 161.5 to the right, agree=0.554, adj=0.098, (0 split)
         mobile_wt
##
## Node number 11: 141 observations,
                                        complexity param=0.01380952
##
     predicted class=1 expected loss=0.4255319 P(node) =0.1007143
##
       class counts:
                         0
                              81
                                    60
                                           0
##
      probabilities: 0.000 0.574 0.426 0.000
##
     left son=22 (110 obs) right son=23 (31 obs)
##
     Primary splits:
##
         ram
                       < 1941.5 to the left, improve=27.291620, (0 missing)
                                to the left, improve=13.931310, (0 missing)
##
                       < 696
         px_height
                                to the left, improve=12.786660, (0 missing)
##
         px width
                       < 1240
##
                                to the left, improve= 2.607385, (0 missing)
         battery_power < 1990</pre>
##
         int memory
                       < 47.5
                                to the left, improve= 2.351360, (0 missing)
##
  Node number 20: 123 observations,
                                        complexity param=0.01285714
##
     predicted class=1 expected loss=0.4308943 P(node) =0.08785714
##
##
       class counts:
                        53
                              70
##
      probabilities: 0.431 0.569 0.000 0.000
##
     left son=40 (61 obs) right son=41 (62 obs)
##
     Primary splits:
##
                                to the left, improve=22.302360, (0 missing)
         px_height
                       < 598
##
         px width
                       < 994.5 to the left, improve=19.697840, (0 missing)
##
         battery_power < 1027.5 to the left, improve=19.114670, (0 missing)
##
         ram
                       < 1515.5 to the left, improve= 5.609121, (0 missing)
##
                       < 3.5
                                to the left, improve= 4.698548, (0 missing)
         рс
##
     Surrogate splits:
##
                               to the left, agree=0.667, adj=0.328, (0 split)
         px_width
                       < 1085
##
                                to the left, agree=0.626, adj=0.246, (0 split)
         battery_power < 919
                                to the right, agree=0.610, adj=0.213, (0 split)
##
         clock speed
                       < 1.65
                                to the right, agree=0.593, adj=0.180, (0 split)
##
         dual sim
                       < 0.5
##
                                to the right, agree=0.585, adj=0.164, (0 split)
         four_g
                       < 0.5
##
## Node number 21: 126 observations
     predicted class=1 expected loss=0.1190476 P(node) =0.09
##
##
       class counts:
                         1
                             111
                                    14
##
      probabilities: 0.008 0.881 0.111 0.000
##
## Node number 22: 110 observations
    predicted class=1 expected loss=0.2727273 P(node) =0.07857143
##
##
       class counts:
                         0
                              80
                                    30
##
      probabilities: 0.000 0.727 0.273 0.000
```

```
##
## Node number 23: 31 observations
##
    predicted class=2 expected loss=0.03225806 P(node) =0.02214286
##
      class counts: 0 1
                                  30
##
     probabilities: 0.000 0.032 0.968 0.000
##
## Node number 40: 61 observations
    predicted class=0 expected loss=0.2786885 P(node) =0.04357143
##
##
      class counts: 44 17 0
##
     probabilities: 0.721 0.279 0.000 0.000
## Node number 41: 62 observations
    predicted class=1 expected loss=0.1451613 P(node) =0.04428571
##
                            53
      class counts:
                       9
##
     probabilities: 0.145 0.855 0.000 0.000
```

2-2. Single decision tree classification see is 7021.066

```
tree.pred = predict(tree, newdata = data_test)

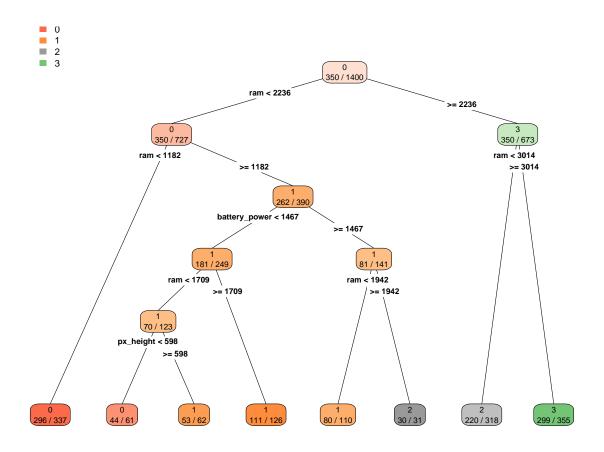
tree.sse = sum ((tree.pred - data_test$price_range)^2)

tree.sse

## [1] 7021.066

# 2-3. Build decision tree while cp = 0.01000000
# E1 is 0.1907143.

tree2 <- prune(tree, cp = 0.01000000)
rpart.plot(tree2, type = 4, branch = 0, extra = 2)</pre>
```



```
CFit1 <- predict(tree2, data_train, type = "class")
ConfM1 <- table(data_train$price_range, CFit1)
(E1 <- (sum(ConfM1) - sum(diag(ConfM1)))/sum(ConfM1))</pre>
```

[1] 0.1907143

```
# 2-4. Utiltize bagging from ipred package to build combined decision tree 1
# Bagging classification trees with 25 bootstrap replications, E2 is 0.75.
BagM1 <- bagging(price_range ~., data = data_train, nbagg = 25, coob = TRUE, control = rpart.control(mix)
CFit2 <- predict(BagM1, data_train, type = "class")
ConfM2 <- table(data_train$price_range, CFit2)
(E2 <- (sum(ConfM2) - sum(diag(ConfM2)))/sum(ConfM2))</pre>
```

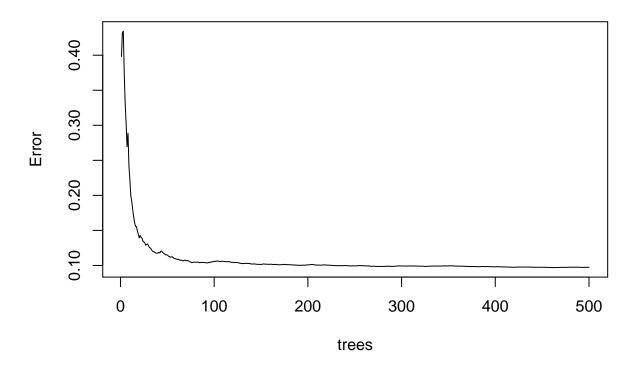
[1] 0.75

```
# 3-1. Random forest
# E3 is 0.9992.
rFM <- randomForest(price_range ~., data = data_train, importance = TRUE, proximity = TRUE)
## Warning in randomForest.default(m, y, ...): The response has five or fewer
## unique values. Are you sure you want to do regression?</pre>
```

```
print(rFM)
##
## Call:
   randomForest(formula = price_range ~ ., data = data_train, importance = TRUE,
                                                                                     proximity = TRUE
                 Type of random forest: regression
##
##
                       Number of trees: 500
## No. of variables tried at each split: 6
##
##
            Mean of squared residuals: 0.09728984
##
                      % Var explained: 92.22
summary(rFM)
                  Length Class Mode
##
## call
                        5 -none- call
                        1 -none- character
## type
## predicted
                    1400 -none- numeric
## mse
                     500 -none- numeric
                     500 -none- numeric
## rsq
                    1400 -none- numeric
## oob.times
                       40 -none- numeric
## importance
## importanceSD
                       20 -none- numeric
## localImportance
                       O -none- NULL
## proximity 1960000 -none- numeric
## ntree
                        1 -none- numeric
## mtry
                        1 -none- numeric
                      11 -none- list
## forest
                        O -none- NULL
## coefs
## y
                    1400 -none- numeric
                        O -none- NULL
## test
                        O -none- NULL
## inbag
                        3 terms call
## terms
```

plot(rFM)

rFM

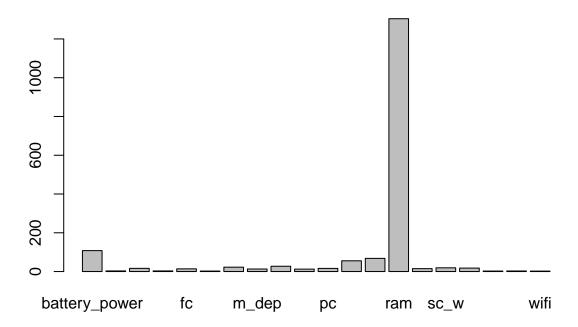


```
Fit3 <- predict(rFM, data_train)
ConfM3 <- table(data_train$price_range, Fit3)
(E3 <- (sum(ConfM3) - sum(diag(ConfM3)))/sum(ConfM3))</pre>
```

[1] 0.9992857

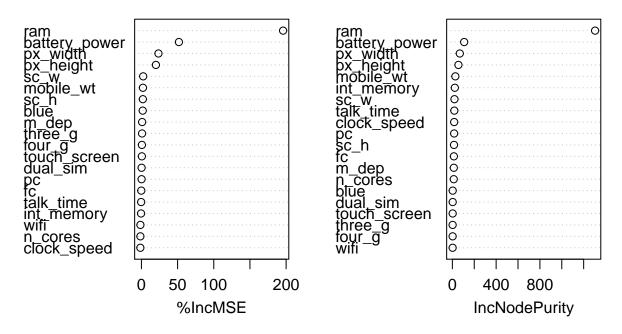
```
# 3-2. Random Forest Feature Importance Barplot
barplot(rFM$importance[,2], main = "Feature Importance Barplot")
```

Feature Importance Barplot



3-3. Random Forest Feature Importance ScatterPlot
varImpPlot(x = rFM, sort = TRUE, n.var = nrow(rFM\$importance), main = "Feature Importance ScatterPlot")

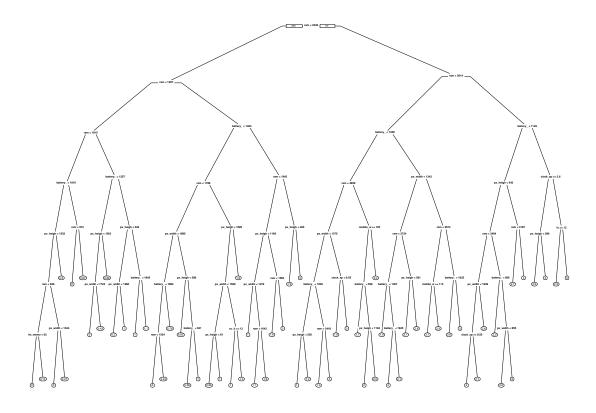
Feature Importance ScatterPlot



```
# 4-1. regression trees cross-validation
tr.control = trainControl(method = "cv", number = 10)
cp.grid = expand.grid(.cp = (0:10)*0.001)
tr = train(price_range ~., data = data_train, method = "rpart", trControl = tr.control, tuneGrid = cp.g
## CART
##
## 1400 samples
    20 predictor
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 1260, 1260, 1260, 1260, 1260, 1260, ...
## Resampling results across tuning parameters:
##
##
                      Rsquared
    ср
                                0.1825574
##
    0.000 0.3564032 0.8994784
##
    0.001
           0.3654180
                     0.8936930
                               0.1933365
##
    0.002 0.3805913 0.8849092 0.2138772
##
    0.003 0.3859357 0.8814569
                               0.2305825
##
    0.004 0.3940466 0.8769803 0.2473934
##
    0.005 0.4141426
                     0.8638818 0.2867955
##
    0.006  0.4267100  0.8553362  0.3193465
##
    0.008 0.4398649 0.8464382 0.3379351
##
```

```
## 0.009 0.4410306 0.8456274 0.3381416 ## 0.010 0.4410306 0.8456274 0.3381416 ## RMSE was used to select the optimal model using the smallest value. ## The final value used for the model was cp = 0.
```

```
# 4-2. plot best tree
best.tree = tr$finalModel
prp(best.tree)
```



```
# 4-3. best tree sse is 80.34064
best.tree.pred = predict(best.tree, newdata = data_test)
best.tree.sse = sum((best.tree.pred - data_test$price_range)^2)
best.tree.sse
```

[1] 80.34064