

Ventas de Apple

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Introducción

Se debe elegir el modelo ETS y el modelo ARIMA que mejor predice las ventas, habiendo dejado fuera de la estimación los trimestres del 2017.

Cargamos los datos:

```
apple <- read.csv("IngresosApple.csv", sep = ";")
head(apple)
```

```
##   Trimestre Ingresos
## 1   Q2 2008      7980
## 2   Q3 2008      7561
## 3   Q4 2008     11520
## 4   Q1 2009     11880
## 5   Q2 2009      9084
## 6   Q3 2009      9734
```

Cargamos las librerías que vamos a necesitar:

```
require(forecast)
require(xts)
require(ggplot2)
library(ggfortify) #Plot Monthplot
library(dplyr)
```

Como las fechas están representadas por trimestres, debemos escribirlas en formato fecha para poder continuar con el análisis:

```
fechas <- seq(as.Date("2008-04-01"), as.Date("2017-09-30"), by = "quarter")
fechas
```

```
## [1] "2008-04-01" "2008-07-01" "2008-10-01" "2009-01-01" "2009-04-01"
## [6] "2009-07-01" "2009-10-01" "2010-01-01" "2010-04-01" "2010-07-01"
## [11] "2010-10-01" "2011-01-01" "2011-04-01" "2011-07-01" "2011-10-01"
## [16] "2012-01-01" "2012-04-01" "2012-07-01" "2012-10-01" "2013-01-01"
## [21] "2013-04-01" "2013-07-01" "2013-10-01" "2014-01-01" "2014-04-01"
## [26] "2014-07-01" "2014-10-01" "2015-01-01" "2015-04-01" "2015-07-01"
## [31] "2015-10-01" "2016-01-01" "2016-04-01" "2016-07-01" "2016-10-01"
## [36] "2017-01-01" "2017-04-01" "2017-07-01"
```

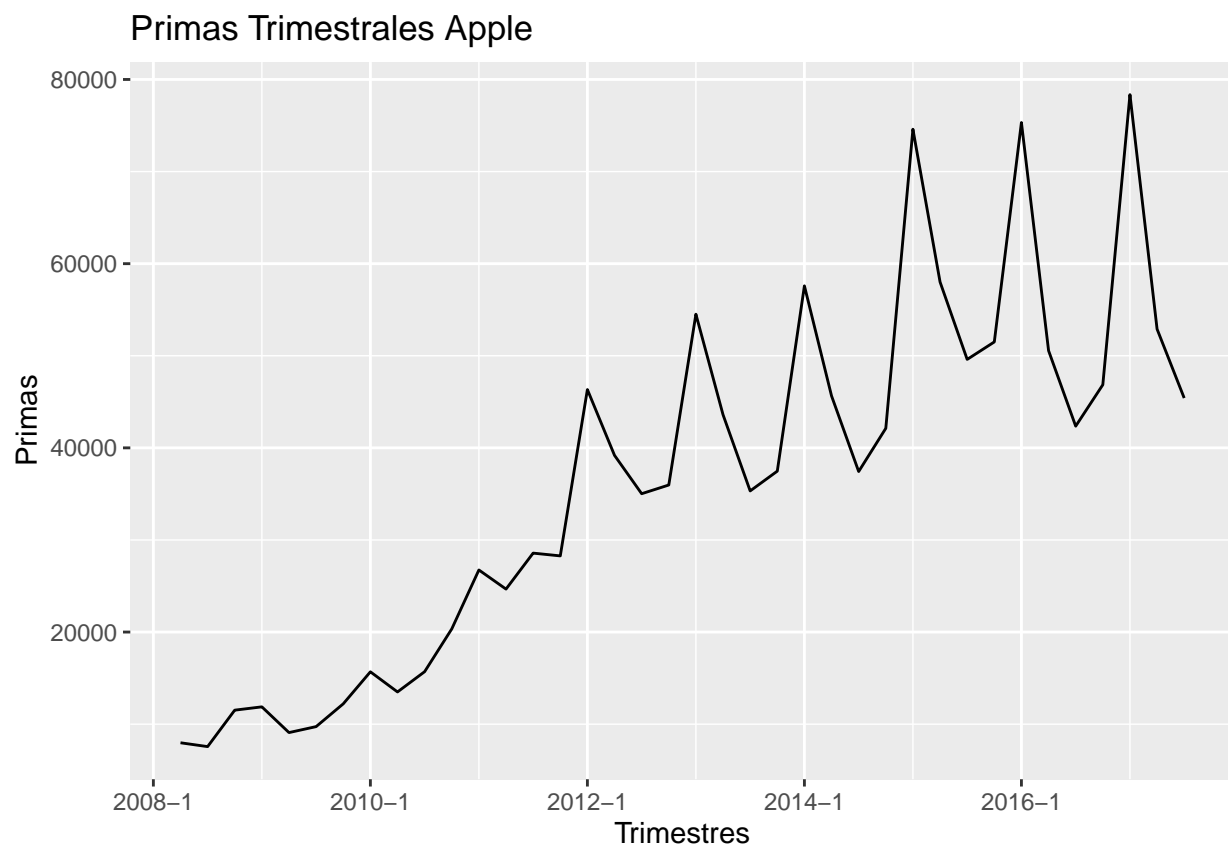
```
apple <- mutate(apple, Date =fechas)
```

Comprobamos que las fechas se han cambiado correctamente:

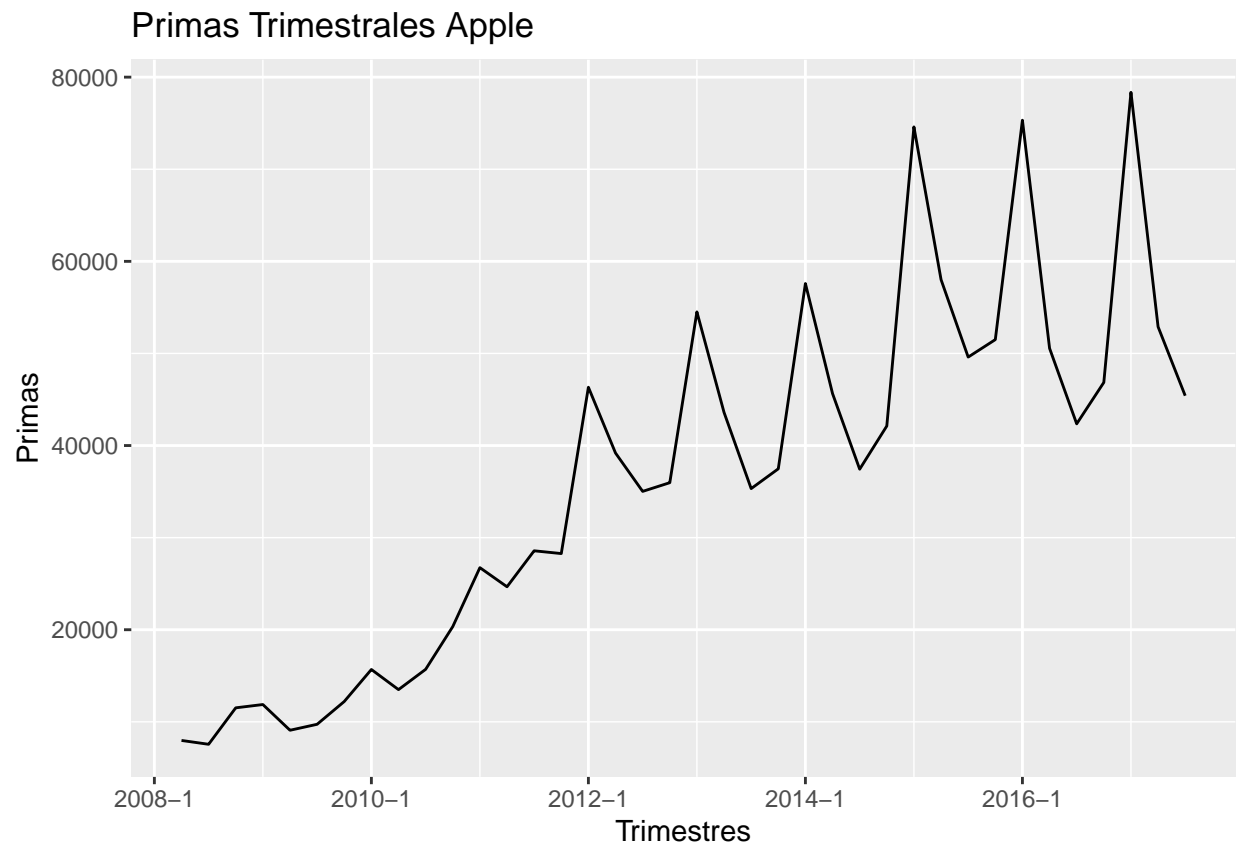
```
head(apple)
```

```
##   Trimestre Ingresos      Date
## 1   Q2 2008      7980 2008-04-01
## 2   Q3 2008      7561 2008-07-01
## 3   Q4 2008     11520 2008-10-01
## 4   Q1 2009     11880 2009-01-01
## 5   Q2 2009      9084 2009-04-01
## 6   Q3 2009      9734 2009-07-01
```

```
#Convert data to XTS
xapple=xts(apple$Ingresos, order.by = as.Date(apple$Date),frequency=4)
xapple=to.quarterly(xapple)
zapple=as.zoo(xapple$xapple.Close)
autoplot(zapple)+ggtitle("Primas Trimestrales Apple")+xlab("Trimestres")+ylab("Primas")
```



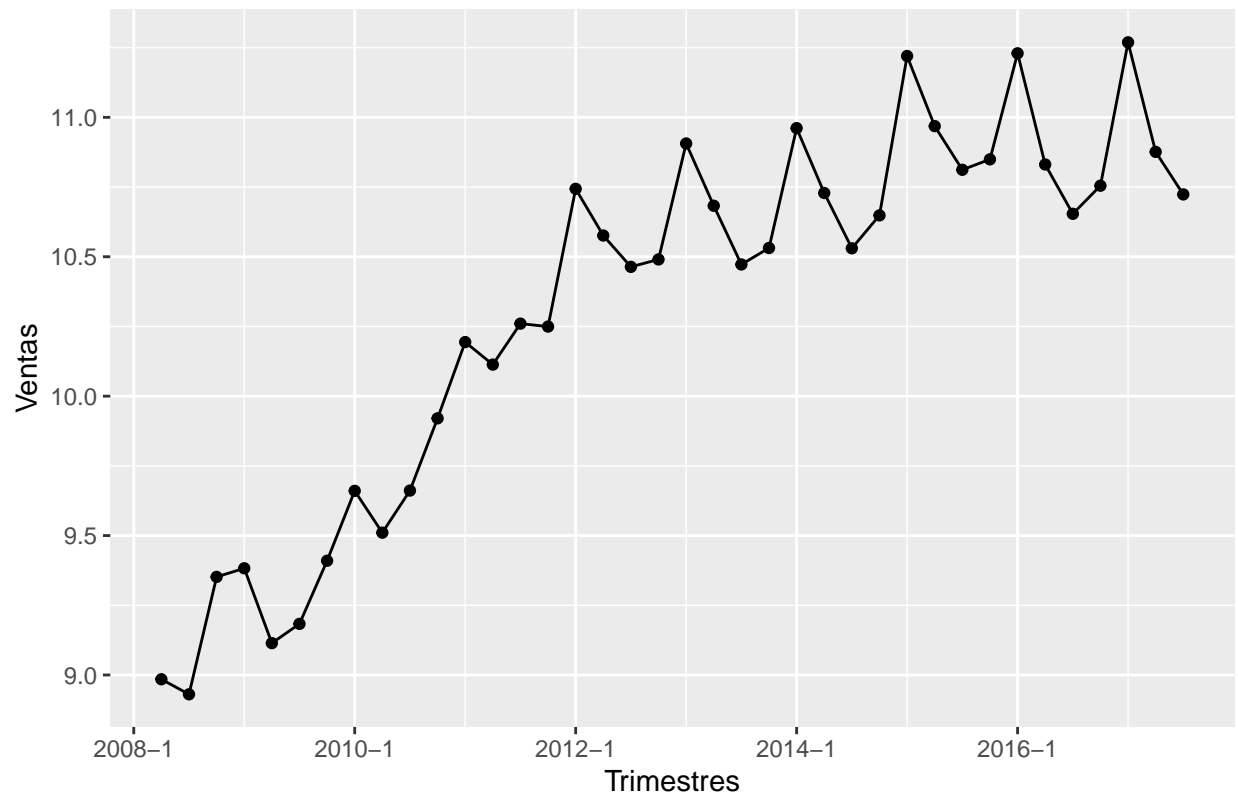
```
#Convert data to XTS
xapple=xts(apple$Ingresos, order.by = as.Date(apple$Date),frequency=4)
xapple=to.quarterly(xapple)
zapple=as.zoo(xapple$xapple.Close)
autoplot(zapple)+ggtitle("Primas Trimestrales Apple")+xlab("Trimestres")+ylab("Primas")
```



Transformacion Logarítmica

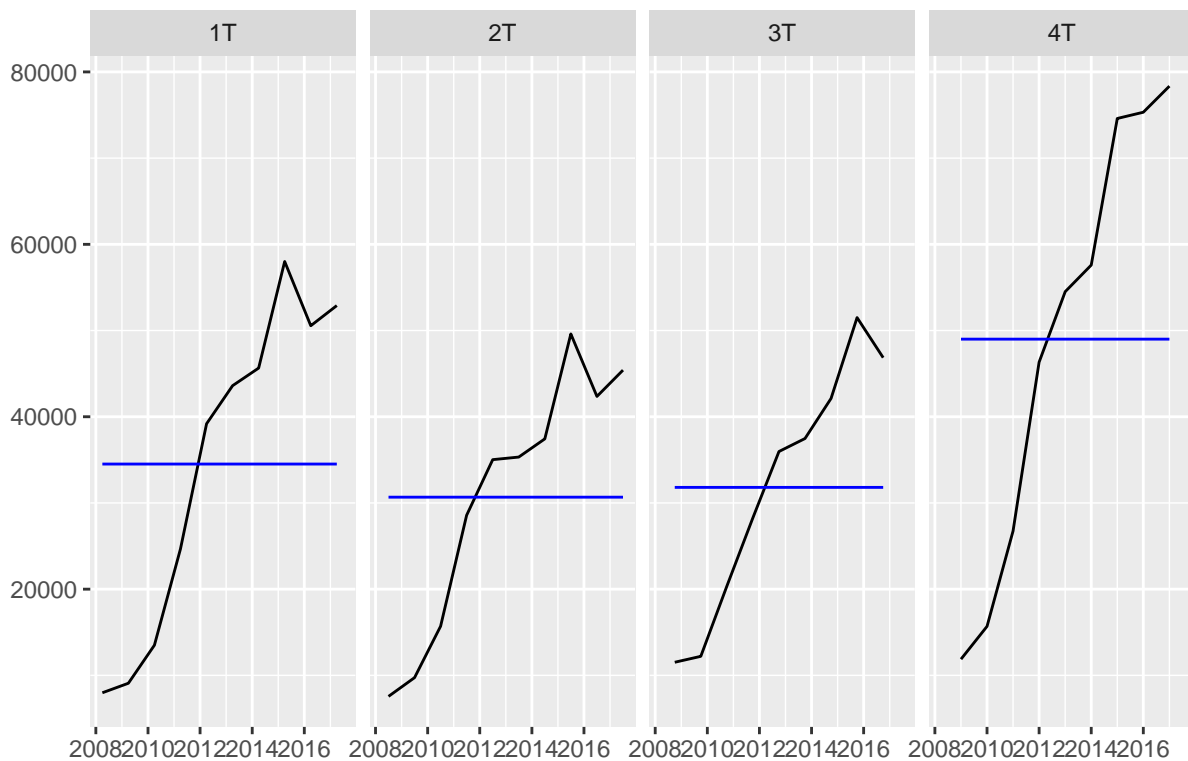
```
zlapple=log(zapple)
df_new1 <- data.frame(value = as.vector(zlapple),
                      time = time(zlapple))
ggplot(df_new1)+geom_point(aes(x=time,y=value))+geom_line(aes(x=time,y=value))+ylab("Ventas")+ggtitle("Ventas")
```

Ventas Trimestrales LOG Apple



```
#Transform to ts data
tsapple=ts(coredata(zapple), start = c(2008, 2), frequency = 4)
#Seasonal Plot
ggfreqplot(tsapple,freq=4,nrow=1,facet.labeller=c("1T","2T","3T","4T"))+ggtitle("Primas Trimestrales")
```

Primas Trimestrales



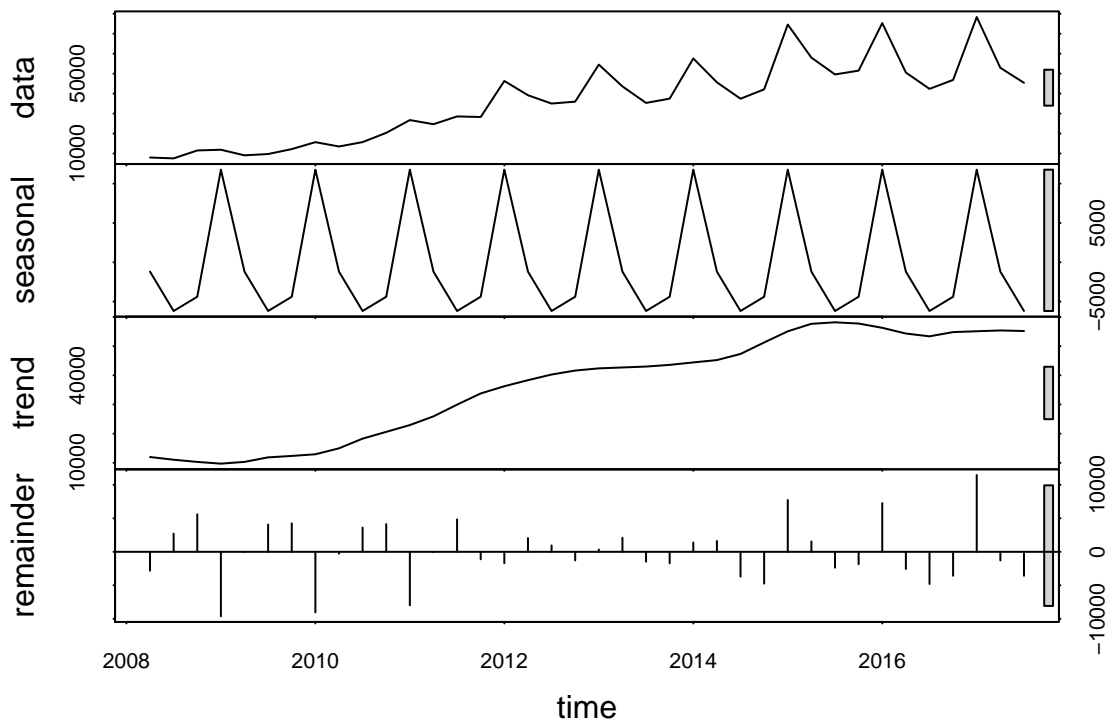
Descomposicion

```
stl(tsapple[, 1], s.window = "periodic")
```

```
## Call:
## stl(x = tsapple[, 1], s.window = "periodic")
##
## Components
##      seasonal      trend  remainder
## 2008 Q2 -1191.515 11987.713 -2816.19786
## 2008 Q3 -6202.795 11054.647  2709.14756
## 2008 Q4 -4388.396 10306.954  5601.44193
## 2009 Q1 11782.720  9712.795 -9615.51515
## 2009 Q2 -1191.515 10313.378   -37.86329
## 2009 Q3 -6202.795 11865.051  4071.74373
## 2009 Q4 -4388.396 12348.763  4246.63276
## 2010 Q1 11782.720 12927.130 -9026.85026
## 2010 Q2 -1191.515 14968.422  -277.90712
## 2010 Q3 -6202.795 18282.820  3619.97453
## 2010 Q4 -4388.396 20608.629  4122.76624
## 2011 Q1 11782.720 22936.090 -7977.81022
## 2011 Q2 -1191.515 25917.203   -58.68777
## 2011 Q3 -6202.795 29940.698  4833.09640
```

```
## 2011 Q4 -4388.396 33777.770 -1119.37412
## 2012 Q1 11782.720 36249.530 -1699.24976
## 2012 Q2 -1191.515 38326.357 2051.15766
## 2012 Q3 -6202.795 40267.415 958.37982
## 2012 Q4 -4388.396 41633.253 -1278.85770
## 2013 Q1 11782.720 42379.047 350.23228
## 2013 Q2 -1191.515 42689.157 2105.35767
## 2013 Q3 -6202.795 42998.839 -1473.04409
## 2013 Q4 -4388.396 43579.104 -1718.70816
## 2014 Q1 11782.720 44414.890 1396.39005
## 2014 Q2 -1191.515 45222.672 1614.84282
## 2014 Q3 -6202.795 47330.414 -3695.61937
## 2014 Q4 -4388.396 51256.536 -4745.14062
## 2015 Q1 11782.720 55088.745 7727.53443
## 2015 Q2 -1191.515 57657.107 1544.40748
## 2015 Q3 -6202.795 58173.837 -2366.04237
## 2015 Q4 -4388.396 57747.384 -1857.98841
## 2016 Q1 11782.720 56283.309 7257.97053
## 2016 Q2 -1191.515 54318.201 -2569.68577
## 2016 Q3 -6202.795 53365.704 -4804.90925
## 2016 Q4 -4388.396 54818.937 -3578.54150
## 2017 Q1 11782.720 55104.114 11464.16602
## 2017 Q2 -1191.515 55382.281 -1294.76586
## 2017 Q3 -6202.795 55190.924 -3580.12898
```

```
plot(stl(tsapple[, 1], s.window = "periodic"))
```



Modelos ETS

Eliminamos los últimos 3 trimestres. Estimamos y predecimos con modelo no estacionales.

Como debemos dejar fuera de la estimación los trimestres de 2017 y en nuestro dataset encontramos 3 trimestres de 2017, nuestro c0mit será igual a 3.

```
#Select number of observation to compare forecast
c0mit=3

#Data Size
nObs=length(zapple)

#sub_sample
oapple <- window(zapple,start=index(zapple[1]),end=index(zapple[nObs-c0mit]))

#Fit Simple Exponential Smoothing
fit1 <- ses(oapple)

#Fit Holt
fit2 <- holt(oapple)

#Fit Holt- exponential
fit3 <- holt(oapple ,exponential=TRUE,initial="simple")

#Fit Holt - damped
fit4 <- holt(oapple,damped=TRUE)

#Fit Holt - (exponential+damped)
fit5 <- holt(oapple,exponential=TRUE,damped=TRUE)
```

Resultados de los modelos:

```
fit1$model

## Simple exponential smoothing
##
## Call:
## ses(y = oapple)
##
## Smoothing parameters:
##   alpha = 0.4288
##
## Initial states:
##   l = 9016.5881
##
## sigma: 10303.87
##
##      AIC      AICc      BIC
## 775.1970 775.9712 779.8631
```

```
fit2$model
```

```
## Holt's method
##
## Call:
## holt(y = oapple)
##
## Smoothing parameters:
##   alpha = 1e-04
##   beta  = 1e-04
##
## Initial states:
##   l = 7035.2209
##   b = 1512.4299
##
## sigma: 9428.668
##
##      AIC      AICc      BIC
## 770.7953 772.8642 778.5720
```

```
fit3$model
```

```
## Holt's method with exponential trend
##
## Call:
## holt(y = oapple, initial = "simple", exponential = TRUE)
##
## Smoothing parameters:
##   alpha = 0.3725
##   beta  = 0.2346
##
## Initial states:
##   l = 7980
##   b = 0.9475
##
## sigma: 0.2622
```

```
fit4$model
```

```
## Damped Holt's method
##
## Call:
## holt(y = oapple, damped = TRUE)
##
## Smoothing parameters:
##   alpha = 0.2198
##   beta  = 1e-04
##   phi   = 0.98
##
## Initial states:
##   l = 7035.3965
##   b = 1512.5793
##
## sigma: 10020.06
##
```



```
##      AIC      AICc      BIC
## 775.9060 778.9060 785.2381
```

```
fit5$model
```

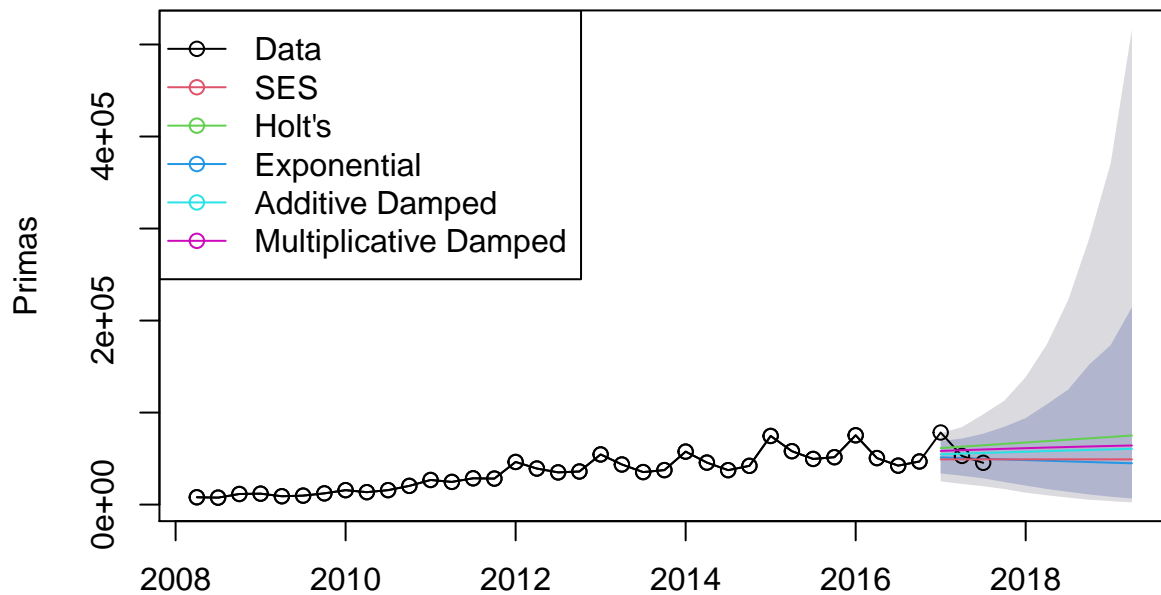
```
## Damped Holt's method with exponential trend
##
## Call:
## holt(y = oapple, damped = TRUE, exponential = TRUE)
##
## Smoothing parameters:
##   alpha = 1e-04
##   beta  = 1e-04
##   phi   = 0.9357
##
## Initial states:
##   l = 7821.9792
##   b = 1.1643
##
## sigma: 0.2466
##
##      AIC      AICc      BIC
## 757.2782 760.2782 766.6103
```

De acuerdo con el AIC, el modelo 5 (exponential+damped) sería la mejor opción

Representación gráfica de los modelos

```
plot(fit3, type="o", ylab="Primas", flwd=1, plot.conf=FALSE)
lines(window(zapple), type="o")
lines(fit1$mean, col=2)
lines(fit2$mean, col=3)
lines(fit4$mean, col=5)
lines(fit5$mean, col=6)
legend("topleft", lty=1, pch=1, col=1:6,
      c("Data", "SES", "Holt's", "Exponential",
        "Additive Damped", "Multiplicative Damped"))
```

Forecasts from Holt's method with exponential trend

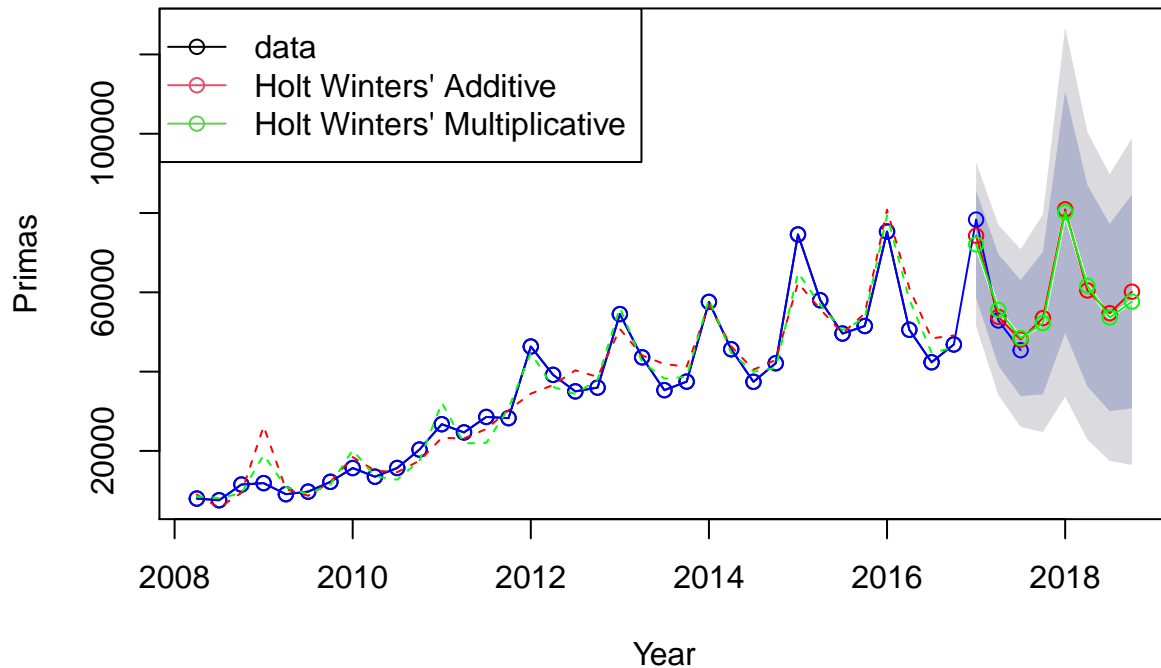


A continuación estimamos modelos no estacionales:

```
#seasonal model Holt-winters
fit6 <- hw(oapple,seasonal="additive")
fit7 <- hw(oapple,seasonal="multiplicative")

#Plot models
plot(fit7,ylab="Primas",
     plot.conf=FALSE, type="o", fcol="white", xlab="Year")
lines(window(zapple),type="o",col="blue")
lines(fitted(fit6), col="red", lty=2)
lines(fitted(fit7), col="green", lty=2)
lines(fit6$mean, type="o", col="red")
lines(fit7$mean, type="o", col="green")
legend("topleft",lty=1, pch=1, col=1:3,
      c("data","Holt Winters' Additive","Holt Winters' Multiplicative"))
```

Forecasts from Holt–Winters' multiplicative method



Seleccionamos de forma automática el modelo ETS

```
## Select automatic ETS
etsfit<-ets(oapple)
#forecast model
fventas.ets=forecast(etsfit)
#Results
summary(fventas.ets)
```

```
##
## Forecast method: ETS(M,A,M)
##
## Model Information:
## ETS(M,A,M)
##
## Call:
## ets(y = oapple)
##
## Smoothing parameters:
##   alpha = 0.493
##   beta  = 0.493
##   gamma = 0.507
##
## Initial states:
```

```

##      l = 7125.3462
##      b = 1485.7975
##      s = 1.1511 1.1163 0.8322 0.9004
##
##      sigma: 0.1222
##
##      AIC      AICc      BIC
## 703.9538 711.1538 717.9519
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set -41.934 4120.155 2883.262 -0.297759 8.677434 0.4160202 0.1438481
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## 2017 Q1      69439.83 58568.387 80311.27 52813.394 86066.26
## 2017 Q2      53347.98 41773.016 64922.95 35645.598 71050.37
## 2017 Q3      48972.04 33884.613 64059.47 25897.811 72046.27
## 2017 Q4      54176.09 31475.035 76877.14 19457.824 88894.35
## 2018 Q1      80540.07 32680.293 128399.85 7344.857 153735.28
## 2018 Q2      61619.03 17211.212 106026.85 -6296.866 129534.93
## 2018 Q3      56344.41 7869.773 104819.05 -17791.151 130479.97
## 2018 Q4      62103.80 -718.363 124925.97 -33974.410 158182.02

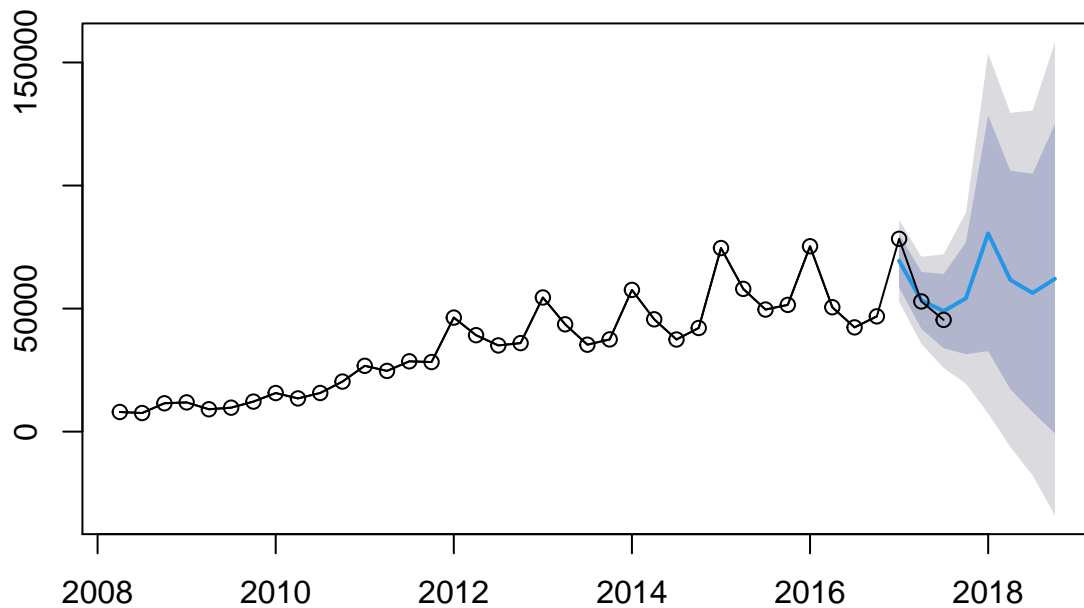
```

```

#Plot
plot(fventas.ets)
lines(window(zapple),type="o")

```

Forecasts from ETS(M,A,M)



Comparación entre los valores actuales y los valores predichos:

```
matrix(c(fventas.ets$mean[1:c0mit],zapple[(n0bs-c0mit+1):n0bs]),ncol=2)
```

```
##           [,1]  [,2]
## [1,] 69439.83 78351
## [2,] 53347.98 52896
## [3,] 48972.04 45408
```

Predicciones y Precisión

```
etsfit<-ets(window(tsapple,end=2016+4/4))
fventas.ets=forecast(etsfit,h=c0mit)
forecast:::testaccuracy(fventas.ets$mean>window(tsapple,start=2017),test = NULL, d = NULL, D = NULL)
```

```
##           ME           RMSE           MAE           MPE           MAPE           ACF1
## -9937.360471 10259.914274  9937.360471  -20.733460   20.733460   -0.500000
##   Theil's U
##    1.667969
```

Modelos ARIMA

```
#Select number of observation to compare forecast
cOmit=3

#Data Size
nObs=length(zapple)

#sub_sample
oapple <- window(zapple,start=index(zapple[1]),end=index(zapple[nObs-cOmit]))

#out sample (real data to forecast performance)
papple <- window(zapple,start=index(zapple[nObs-cOmit+1]),end=index(zapple[nObs]))
```

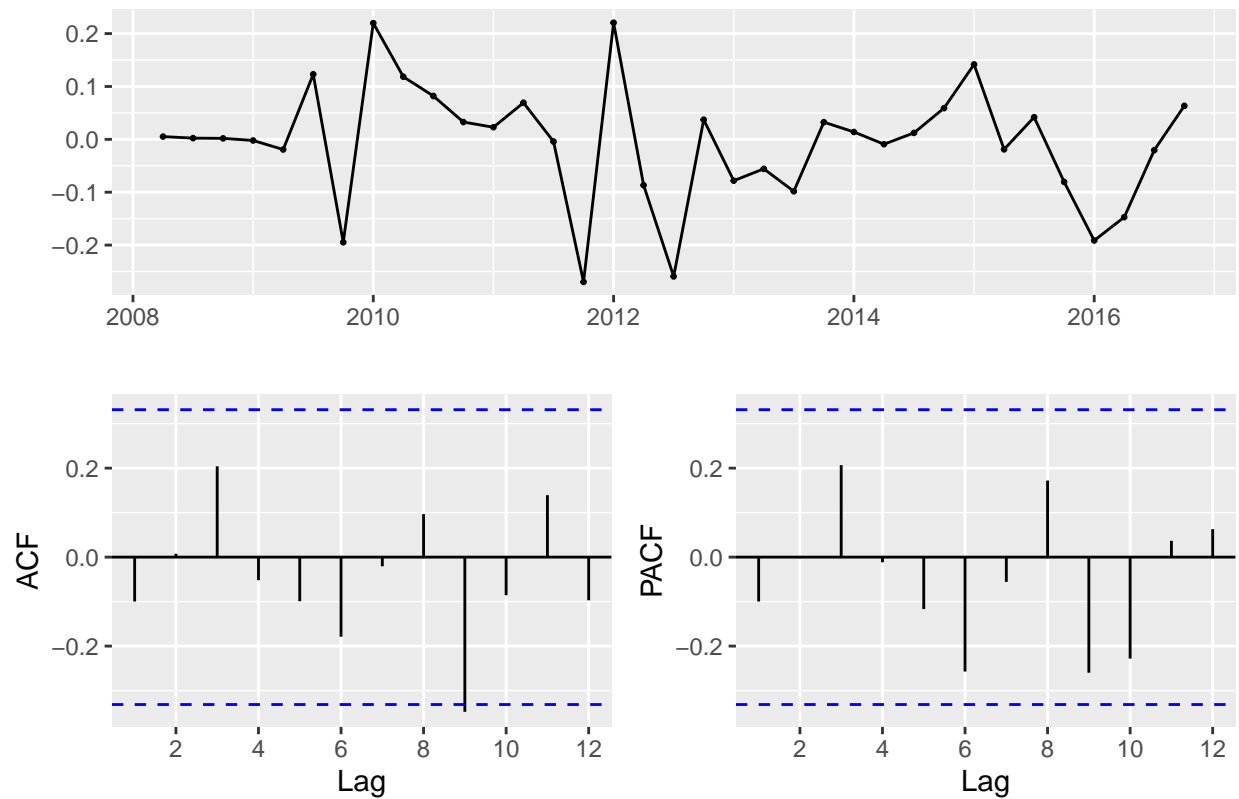
Creamos un modelo ARIMA

```
fit1=auto.arima(oapple,lambda=0)
summary(fit1)

## Series: oapple
## ARIMA(0,1,0)(0,1,0)[4]
## Box Cox transformation: lambda= 0
##
## sigma^2 estimated as 0.01472: log likelihood=20.72
## AIC=-39.45 AICc=-39.3 BIC=-38.04
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set -764.5058 4786.405 3054.054 -1.321616 8.284962 0.4406634 0.1269135
```

Análisis de los Residuos:

```
ggtstdisplay(fit1$residuals)
```



El gráfico del ACF no muestra correlación entre los residuos. Se observa en el gráfico del PACF que ningún lag es significativo.

Box-Ljung Test

```
Box.test(fit1$residuals,lag=4, fitdf=3, type="Lj")
```

```
##
## Box-Ljung test
##
## data: fit1$residuals
## X-squared = 2.1794, df = 1, p-value = 0.1399
```

```
Box.test(fit1$residuals,lag=8, fitdf=3, type="Lj")
```

```
##
## Box-Ljung test
##
## data: fit1$residuals
## X-squared = 4.501, df = 5, p-value = 0.4797
```

```
Box.test(fit1$residuals,lag=12, fitdf=3, type="Lj")
```

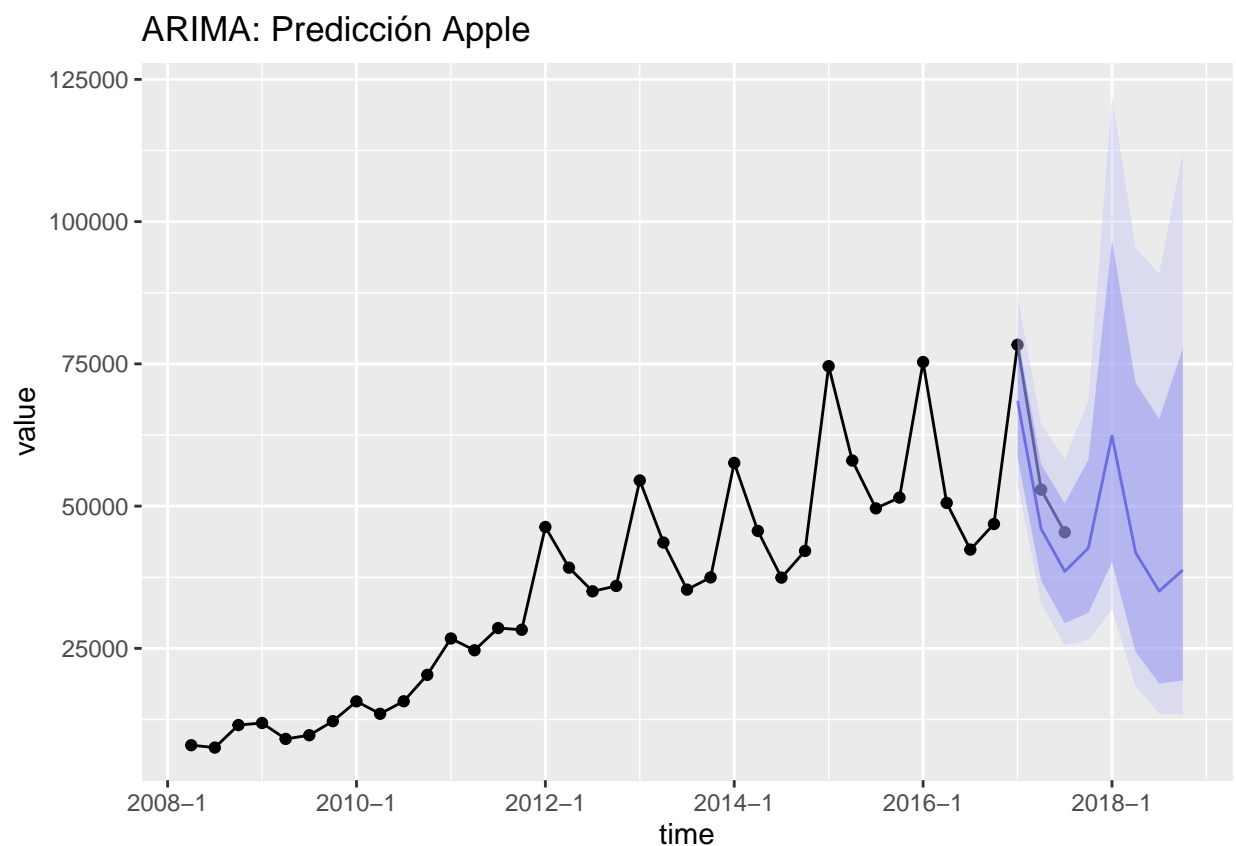
```
##
## Box-Ljung test
##
## data: fit1$residuals
## X-squared = 12.477, df = 9, p-value = 0.1877
```

La hipótesis nula del Test Box-Ljung implica que los residuos son ruido blanco, y como p-valor > 0.05 , se acepta la hipótesis nula.

```
fventas.arima=forecast(fit1)
```

```
df_new <- data.frame(value = as.vector(zapple),
                     time = time(zapple))
```

```
ggplot(df_new)+geom_point(aes(x=time,y=value))+geom_line(aes(x=time,y=value))+ geom_forecast(fventas.arima)
```



```
fventas.arima
```

##	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## 2017 Q1	68524.50	58656.57	80052.53	54021.77	86920.63
## 2017 Q2	45993.21	36914.17	57305.26	32857.77	64379.78
## 2017 Q3	38534.34	29436.35	50444.28	25525.07	58174.00
## 2017 Q4	42622.67	31230.74	58169.99	26490.28	68579.55
## 2018 Q1	62338.78	40156.60	96774.23	31816.09	122143.34

## 2018 Q2	41841.40	24416.21	71702.49	18358.80	95360.44
## 2018 Q3	35055.84	18821.04	65294.59	13541.05	90754.54
## 2018 Q4	38775.11	19344.31	77723.59	13387.03	112310.89

Comparación entre ARIMA y ETS

Si comparamos los MAPE de los modelos ETS y ARIMAS, escogeríamos ARIMAS ya que el MAPE DE ARIMAS (8.284962) es menor que el MAPE de ETS (8.677434).