

Problem: We will be provided with 4 integers. By using plus, minus, multiply and divide, we need to manipulate these 4 integers to obtain a final result – 24.

Firstly, we need to find out all possible permutations of these 4 integers. For 4 different integers, we will get $A_4^4 = 24$ possible answers. And we also need to consider about the arrangements of brackets. In this situation, we have only 5 possible ways to arrange the brackets:

$$((A \cdot B) \cdot C) \cdot D$$

$$(A \cdot (B \cdot C)) \cdot D$$

$$A \cdot ((B \cdot C) \cdot D)$$

$$A \cdot (B \cdot (C \cdot D))$$

$$(A \cdot B) \cdot (C \cdot D)$$

And since we have 4 operations $(+, -, \times, \div)$, we will get in total $24 \times 5 \times 4 \times 4 \times 4 = 7680$ possible results. Then we only need to check out whether the result equals to 24.

Input: 4 integers num1, num2, num3, num4

Output: A way to manipulate 4 integers to obtain 24

1. $numbers \leftarrow \{num1, num2, num3, num4\}$

2. $ops \leftarrow \{+, -, *, /\}$

3. $perm \leftarrow \{numbers\}$

4. **For** $i \leftarrow 1$ to 24 **Do**

5. $perm \leftarrow \text{Next_permutation}(numbers) \cup perm$

/* Next_permutation() is a function to get next permutation of *numbers* */

6. **End**

7. **For every** $\{num1, num2, num3, num4\} \in perm$

/**perm* is a set of all possible permutations, for each permutation in this set...*/

8. **For every** $i \in ops$ **Do**

9. **For every** $j \in ops$ **Do**

10. **For every** $k \in ops$ **Do**

/**i, j, k* means a kind of operation – plus, minus, multiply or divide*/

11. **If** $((num1 \ i \ num2) \ j \ num3) \ k \ num4 == 24$

12. **Then Return** $((num1 \ i \ num2) \ j \ num3) \ k \ num4)$

13. **Elseif** $((num1 \ i \ (num2 \ j \ num3)) \ k \ num4) == 24$

14. **Then Return** $((num1 \ i \ (num2 \ j \ num3)) \ k \ num4)$

15. **Elseif** $(num1 \ i \ ((num2 \ j \ num3) \ k \ num4)) == 24$

16. **Then Return** $(num1 \ i \ ((num2 \ j \ num3) \ k \ num4))$

17. **Elseif** $(num1 \ i \ (num2 \ j \ (num3 \ k \ num4))) == 24$

18. **Then Return** (*num1* i (*num2* j (*num3* k *num4*)))

19. **Elseif** ((*num1* i *num2*) j (*num3* k *num4*)) == 24

20. **Then Return** ((*num1* i *num2*) j (*num3* k *num4*))

/*5 possible ways to arrange the brackets*/

21. **Else**

22. **Then Print**('No solution.')

23. **End**

24. **End**

25. **End**

26. **End**

27.**End**

Please input 4 numbers:
1, 2, 3, 4 1 2 3 4 : ((1 + 2)+ 3)* 4

Please input 4 numbers:
1, 4, 5, 8 1 5 8 4 : (1 + 5)*(8 - 4)

Please input 4 numbers:
5, 9, 8, 3 3 9 5 8 : ((3 * 9)+ 5)- 8

Please input 4 numbers:
1, 3, 4, 6 6 1 3 4 : 6 /(1 -(3 / 4))

Please input 4 numbers:
1, 5, 4, 6 6 5 4 1 : 6 /((5 / 4)- 1)

num1	num2	num3	num4	Result
1	2	3	4	$((1 + 2) + 3) * 4$
1	4	5	8	$(1 + 5) * (8 - 4)$
5	9	8	3	$((3 * 9) + 5) - 8$
1	3	4	6	$6 / (1 - (3 / 4))$
1	5	4	6	$6 / ((5 / 4) - 1)$