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Answer the question number-1

QuickSort (A, Left, Right)

- ① If $\text{Left} \leq \text{Right}$
- ② then $q = \text{Partition}(A, \text{Left}, \text{Right})$
- ③ QuickSort (A, Left, $q-1$)
- ④ QuickSort (A, $q+1$, Right)
- ⑤ END

Partition (A, Left, Right)

- ① $x = A[\text{Right}]$
- ② $i = \text{Left} - 1$
- ③ For $j = \text{Left}$ to $\text{Right} - 1$
- ④ do if $A[j] \leq x$
- ⑤ then $i = i + 1$
- ⑥ swap ($A[i], A[j]$)

⑦ Swap ($A[i+1]$, $A[\text{right}]$)

⑧ Return ($i+1$)

Analyze 3 case of complexities

① Worst Case : The worst case occurs if the input is presented in reverse order and if the first or the last element is chosen as pivot. In this case pivot provides a poor partition because all elements go into one partition and the other partition is empty. The worst case running time is $O(n^2)$.

2. Average Case : The average running time of Quick sort is obtained by averaging the run time of all possible

subproblems sizes. that means it occurs from the fact that on average each reduction step of the algorithm produces two subsets. So, the average running time is $O(n \log n)$

③ Best Case;

The best case occurs when the partition always splits into two subsets with equal no. of elements. So, the running time is $O(n \log n)$

Answer the question numbers

The main difference between divide and conquer and dynamic programming is that the divide and conquer combines

the solutions of the subproblems to obtain the solution of the main problem while dynamic programming uses the result of the subproblems to find the optimum solution of the main problem

conquer technique is used by fibonacci search. fibonacci search works on sorted array as the binary search, in fibonacci there is no use of \wedge operator instead of \wedge , it uses $+$ and $-$ operator,

$F(n) = F(n-1) + F(n-2)$, $F(0) = 0$, $F(1) = 1$ is the way to define fibonacci number recursively.