

# **TRANSFER LEARNING FOR ONE-CLASS RECOMMENDATION BASED ON MATRIX FACTORIZATION**

by

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The Hong Kong University of Science and Technology  
in Partial Fulfillment of the Requirements for  
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18 June 2013

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This is to certify that I have examined the above M.Phil. thesis  
and have found that it is complete and satisfactory in all respects,  
and that any and all revisions required by  
the thesis examination committee have been made.

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18 June 2013

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# TABLE OF CONTENTS

<b>Title Page</b>	<b>i</b>
<b>Authorization Page</b>	<b>ii</b>
<b>Signature Page</b>	<b>iii</b>
<b>Acknowledgments</b>	<b>iv</b>
<b>Table of Contents</b>	<b>v</b>
<b>List of Figures</b>	<b>vii</b>
<b>List of Tables</b>	<b>viii</b>
<b>Abstract</b>	<b>ix</b>
<b>Chapter 1 Introduction</b>	<b>1</b>
1.1 Motivation	1
1.2 Contributions	2
1.3 Thesis Outline	3
<b>Chapter 2 Background</b>	<b>4</b>
2.1 Collaborative Filtering	4
2.1.1 Memory-based CF	5
2.1.2 Model-based CF	6
2.1.3 Hybrid models	7
2.2 Matrix Factorization	7
2.2.1 Singular Value Decomposition	8
2.2.2 Non-negative Matrix Factorizaion	8
2.2.3 Non-negative Matrix Tri-factorizaion	9
2.3 Transfer Learning	10
2.3.1 Transfer Learning for Collaborative Filtering	10
2.3.2 Large Scale Transfer Learning	11

<b>Chapter 3</b>	<b>Transfer Learning in One Class CF for Shopping Prediction</b>	<b>13</b>
3.1	Problem settings	13
3.1.1	Background	13
3.1.2	Problem definition	13
3.2	TRIMF	14
3.2.1	Weighting scheme of TRIMF	14
3.2.2	Transfer learning in TRIMF	14
3.2.3	Object function	15
3.3	Solution to TRIMF & Algorithm	17
3.4	Experiment	18
3.4.1	Datasets	18
3.4.2	Metrics	19
3.4.3	Baseline methods	19
3.4.4	Results	21
3.5	Performance comparison & analysis	23
<b>Chapter 4</b>	<b>Conclusion and Future work</b>	<b>25</b>
<b>References</b>		<b>27</b>

# **LIST OF FIGURES**

3.1	Graphical model of TRIMF	16
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## LIST OF TABLES

2.1	Overview of TRIMF in Cross-Domain Collaborative Filtering context.	4
3.1	Top 10 click items and top 10 purchase items in Yixun	15
3.2	Baseline methods.	19
3.3	Performance of TRIMF and other baseline methods on short-term users who have deal data.	21
3.4	Performance of TRIMF and other baseline methods on short-term users who have deal data.	22
3.5	Performance of TRIMF and other baseline methods on long-term users.	22
3.6	The effect of sharing	24



# **TRANSFER LEARNING FOR ONE-CLASS RECOMMENDATION BASED ON MATRIX FACTORIZATION**

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## **ABSTRACT**

One Class Recommender System aims at predicting users' future behaviors according to their historical actions. In these problems, the training data usually contain only binary data reflecting the behavior is happened or not. Thus, the data is sparser than traditional rating prediction problems. Recently, there are two ways to tackle the problem. 1, using knowledge transferred from other domains to mitigate the data sparsity problem. 2, providing methods to distinguish negative data and unlabeled data. However, it's not easy to simply transfer knowledge from source domain to target domain since their observations may be inconsistent. And without data from external source, distinguishing negative and unlabeled data is sometimes infeasible.

In this paper, we propose a novel matrix tri-factorization method to transfer the useful information from source domain to target domain. Then we embed this method to a cluster-based SVD(singular value decomposition) framework. In several real-world datasets, we show our method achieve better prediction precision than other state-of-the-art methods. The cluster-based SVD method has been online for 2 months in a online shopping site, and its performance is among the best.

# CHAPTER 1

## INTRODUCTION

### 1.1 Motivation

Recommendation systems have become extremely common in recent years, typical recommendation system recommends items (movies, music, books, etc.) that users may be interested in. Collaborative filtering approaches build a model from users' past behavior to predict items that the user may have an interest in. In real-world recommendation systems, users and items are all very large, so users can only rate a small fraction of items. Thus, the user-item matrix can be extremely sparse. What's more, sometimes we can't observe explicit ratings, only implicit feedback is provided(e.g click, pageview and purchase). Such problem may lead to poor performance in CF models.

Recently, different transfer learning methods have been developed to improve the performance of the model. In [14, 15], they use a rating-pattern sharing scheme to share user-item ratings pattern across different domains. In [24, 21], implicit feedback data is available, knowledge is transferred via latent-feature sharing. In [35, 8] they try to exploit correlations among multiple domains. However, most of the methods are developed for rating prediction problems. For example, in a music & book rating website, a user can have high or low rating for an album. The ratings are usually trustful, thus can be used to recommend books to the same users. But in a website where only implicit feedback is available(e.g advertisement), the behavior can be much more noisy and with less information. So to achieve better performance, we must transfer more knowledge from source domain while be very careful about the noise.

Some works have been done on solving one-class recommendation problem [11, 19]. They all try to model the frequency of actions by a confidence matrix. For example, if you clicked an item A for 10 times, item B for 1 time. It's more confident that you like A, but not quite sure that you like B. On the other side, if you are a heavy user and you didn't click a popular item A, then it's highly possible that you don't like A. But these works only explore the original matrix, in real-world there are many other useful informations which can be used to improve performance.

We collect several users' clicking and purchasing behaviors from two online shopping site. After taking careful analysis, we find that users' behaviors on clicking and purchasing are similar, but not the same. Based on that, we develop a matrix tri-factorization method(TRIMF) to transfer knowledge from side to side. TRIMF can be used to achieve different goals, (e.g optimize for Ctr(Cvr)).

Further, to make the method online, we develop a clustering-based matrix factorization method(CBMF) using hadoop. CBMF collect all kinds of user data and convert them into a single matrix per task. For cold-start users, a weighted recommendation from their neighbors will be provided. While for registered users, results are mixed with direct matrix factorization and CBMF.

## 1.2 Contributions

Our main contributions are summarized as follows:

- First, we find that in implicit datasets, more data must be shared to achieve better performance. To transfer more knowledge, a matrix tri-factorization method is proposed to transfer knowledge from user side and item side(TRIMF).
- Second, implicit datasets can consist many noises. To transfer useful knowledge, we

develop a clustering-pattern transfer function. For each task, a base clustering pattern matrix is provided, the function only do some cluster-level transformation. Thus we can share knowledge more accurately without losing too much information.

- Third, we propose a modified version of TRIMF which can be used for large scale recommendation. And it is used in an Internet company, it's performance is among the best in all online algorithms.

## 1.3 Thesis Outline

The rest of the thesis is organized as follows: we first provide the background of the research on Transfer Learning, Collaborative Filter and Matrix Factorization in Chapter 2. Then, we discuss the technique grounds of the proposed matrix tri-factorization method in Chapter 3. We present the details of our proposed STLCF framework in Chapter ?? and the experiments in Chapter ??. Finally, we share our thoughts of possible future work and conclude the thesis in Chapter 4.

# CHAPTER 2

## BACKGROUND

In this chapter, we would like to give a brief review of the related literatures. We classify our work to be most related to the works in the areas of cross-domain collaborative filtering.

In Table 2.1, we summarize the related works under the cross-domain collaborative filtering context. To the best of our knowledge, no previous work for collaborative filtering has ever focused on knowledge transfer between implicit datasets and utilize both latent factor and rating pattern transfer.

In the following, we would like to discuss the state-of-the-art methods for both Collaborative Filtering, Matrix Factorization and Transfer Learning.

Table 2.1: Overview of TRIMF in Cross-Domain Collaborative Filtering context.

	Rating-Pattern Sharing	Latent-Feature Sharing	Other
<i>Rating</i> $\rightarrow$ <i>Rating</i>	RMGM [14]	CMF [33]	
<i>Implicit</i> $\rightarrow$ <i>Rating</i>		CST [23], TCF [22]	TIF [24]
<i>Implicit</i> $\rightarrow$ <i>Implicit</i>	TRIMF		

### 2.1 Collaborative Filtering

Collaborative filtering ([13], [27]) as an intelligent component in recommender systems ([36], [17]) has gained extensive interest in both academia and industry.

Collaborative filtering(CF) methods are based on collecting and analyzing a large amount of information on users' behaviors, activities or preferences and predicting what users will like in the future based on their similar users. The underlying assumption of the collaborative filtering

approach is that, if a person A has the same opinion as B on an issue, A is more likely to have B's opinion on a different issue x than to have the opinion on x of a randomly chosen person. For example, a collaborative filtering recommendation system for television tastes could make predictions about which television show a user should like given a partial list of this user's tastes (likes or dislikes, ratings, etc).

There are three types of CF: memory-based, model-based and hybrid.

### **2.1.1 Memory-based CF**

This mechanism uses user rating data to compute the similarity between users or items. The similarity is then used for making recommendations. The memory-based method is used in many commercial systems, because it is easy to implement and is effective given plenty of records and doesn't produce a model. Typical examples of this mechanism are neighborhood based CF and item-based/user-based top-N recommendations[34].

The advantages of this approach include:

- The explainability of the results, which is an important aspect of recommendation systems.
- It is easy to setup and use.
- New data can be added easily and incrementally.
- It need not consider contents of the items being recommended.
- The mechanism scales well with co-rated items.

However, there are several disadvantages with this approach:

- It requires plenty of human ratings.

- Its performance decreases when data gets sparse, which is a common phenomenon with web related items.
- Although it can efficiently handle new users, adding new items becomes more complicated since that representation usually relies on a specific vector space. That would require to include the new item and re-insert all the elements in the structure. This prevents the scalability of this approach.

### 2.1.2 Model-based CF

Models are developed using data mining, machine learning algorithms to find patterns based on training data. This approach has a more holistic goal to uncover latent factors that explain observed ratings. Most of the models are based on creating a classification or clustering technique to identify the users in the test set. Various models have been proposed, including factorization models [13, 24, 25, 27], probabilistic mixture models [10, 12], Bayesian networks [26] and restricted Boltzman machines [30].

There are several advantages with this paradigm:

- It handles the sparsity better than memory based ones.
- This helps with scalability with large data sets.
- It improves the prediction performance.
- It gives an intuitive rationale for the recommendations.

The disadvantage of this approach is the expensive model building. On the one hand, the modern recommendation system usually have petabytes of records as input; On the other hand, the convergence of most models requires intensive computation. One needs to have a tradeoff between prediction performance and scalability.

Given the accuracy of model-based CF, how to overcome the scalability issue has attracted much concern. With the rapid development of parallel computation, researchers have been exploring the use of parallel system to speed up the complex model building. For example in [3], the authors showed that a variety of machine learning algorithms including k-means, logistic regression, naive Bayes, SVM, PCA, gaussian discriminant analysis, EM and backpropagation (NN) could be speeded up by Google's map-reduce [5] paradigm. In [32], the authors showed there is an inverse dependency of training set size and training speed in SVM(linear kernel). That is, if you get more training instances, you can speed up your training speed.

In our method TRIMF, it's hard to parallellize the update step, so we develop a modified version of TRIMF and put it online.

### **2.1.3 Hybrid models**

A number of applications combine the memory-based and the model-based CF algorithms. These overcome the limitations of native CF approaches. It improves the prediction performance. Importantly, it overcomes the CF problems such as sparsity and loss of information. However, they have increased complexity and are expensive to implement. Usually most of the commercial recommender systems are hybrid, for example, Google news recommender system [4].

## **2.2 Matrix Factorization**

In the mathematical discipline of linear algebra, a matrix decomposition or matrix factorization is a factorization of a matrix into a product of matrices. There are many different matrix decompositions; each finds use among a particular class of problems. In CF, usually user-item matrix



is very sparse, we can decompose the original matrix into different low-rank matrix and then recover the dense matrix by multiply the low-rank matrix to produce recommendation results. There are two main methods of matrix factorizaion which are widely applied. 1. Singular value decomposition(SVD), 2. Non-negative matrix factorization(NMF).

### 2.2.1 Singular Value Decomposition

In linear algebra, the singular value decomposition (SVD) is a factorization of a real or complex matrix, with many useful applications in signal processing and statistics.

Formally, the singular value decomposition of an  $m * n$  real or complex matrix  $M$  is a factorization of the form  $M = U \Sigma V$ , where  $U$  is an  $m * m$  real or complex unitary matrix,  $\Sigma$  is an  $m * n$  rectangular diagonal matrix with non-negative real numbers on the diagonal, and  $V$  is an  $n * n$  real or complex unitary matrix. Singular value decomposition is used in recommender systems to predict people's item ratings [31].  $\Sigma$  consists of singular values of  $M$ , and we can select the  $k$ -biggest values and set other entries of  $\Sigma$  to zero. Then put  $M' = U \Sigma V$ ,  $M'$  is our recommendation result.

### 2.2.2 Non-negative Matrix Factorizaion

Non-negative matrix factorization (NMF) is a group of algorithms in multivariate analysis and linear algebra where a matrix  $V$  is factorized into (usually) two matrices  $W$  and  $H$ , with the property that all three matrices have no negative elements. It can be regard as a latent factor model [13].

Latent factor models are an alternative approach that tries to explain the ratings by characterizing both items and users on, say, 20 to 100 factors inferred from the ratings patterns. In movie recommendation, the discovered factors might measure obvious dimensions such as comedy versus drama, amount of action, or orientation to children. For users, each factor measures how

much the user likes movies that score high on the corresponding movie factor. For movies, each factor measures the property of that movie.

NMF decompose an original matrix  $V$  into two matrices  $W$  and  $H$ , s.t  $V = WH$ .  $V$  is a  $m * n$  matrix,  $W$  is a  $m * d$  matrix,  $H$  is a  $d * n$  matrix. Usually  $d \ll m, n$ , is the dimension of latent factor, NMF methods put users and items into one common latent space. When judging whether a user likes an item, we can simply calculate by inner product.

### 2.2.3 Non-negative Matrix Tri-factorizaion

As a transformation of NMF, Non-negative Matrix Tri-factorizaion(NMTF) decompose a matrix  $X$  into three non-negative part :  $X = USV$ . Instead of mapping users and items to a same latent space, the three parts of NMTF can be interpreted as:

- $U$  users' soft-clustering matrix
- $S$  users' clusters vs items' clusters(cluster relationship matrix)
- $V$  items' soft-clustering matrix

In [7], the authors proved that NMF is equivalent to k-means clustering. In [6] the authors also proved that NMTF can be regarded as a way of clustering. NMTF is well known in document processing, [16] uses prior knowledge in lexical and NMTF to tackle the sentiment analysis problem, [37] exploits the relationship between word clusters and document classes in text classification problem.

Because the property of NMTF, if we get some prior knowledge(e.g word cluster, document class), we can easily adopt them in the model. Thus can acheive better performance than traditional NMF methods. Our method(TRIMF) uses NMTF to leverage auxiliary data, align cluster and do cluster-level sharing. NMTF is also very common in the field of transfer learning, where clusters can be shared across different domains.

## 2.3 Transfer Learning

Pan and Yang [20] surveyed the field of transfer learning. A major assumption in many machine learning and data mining algorithms is that the training and future data must be in the same feature space and have the same distribution. However, in many real-world applications, this assumption may not hold. For example, we have a task in recommendation, users and items form a joint distribution in training data. But in test data, users may be different with the training as well as items, their relationship may varies too. Thus the latter data has different feature spaces or distribution than the training data. In such cases, knowledge transfer, if done successfully, would greatly improve the performance of learning by avoiding much expensive data-labeling effort.

### 2.3.1 Transfer Learning for Collaborative Filtering

Some works on transfer learning are in the context of collaborative filtering. Mehta and Hofmann [18] consider the scenario involving two systems with shared users and use manifold alignment methods to jointly build neighborhood models for the two systems. They focus on making use of an auxiliary recommender system when only part of the users are aligned, which does not distinguish the consistency of users' preferences among the aligned users. [33] designed a collective matrix factorizaion framework, where two matrix  $M, N$  are factorized into  $M = UV^T, N = US^T$ . The sharing part  $U$  can be a bridge to transfer knowledge from  $M$  to  $N$ (or  $N$  to  $M$ ), base on that, there are some following work in cross-domain collaborative filtering using matrix factorization tecnique. Li *et al.* [15] designed a regularization framework to transfer knowledge of cluster-level rating patterns, they use matrix tri-factorization and cluster level rating patterns are shared. Pan *et al.* [22], [23] used a matrix factorization framework to

transfer knowledge in latent feature space. Knowledge is transferred from an implicit feedback dataset to a rating dataset, but this method can deal with knowledge transfer in both implicit domains. Cao *et al.* [2] exploited correlations among different CF domains via learning. E.g we factorize each matrix  $X_d$  by  $X_d = F_d G_d^T$  where  $F_d$  and  $G_d$  are the user and the item latent features, respectively. This approach tries to explore the correlations between user domains  $F_d$  and/or item domains  $G_d$  and the knowledge can be transferred across domains through the correlation matrices.

Our method(TRIMF) leverage rating pattern sharing and latent feature sharing carefully by designing a matrix tri-factorization framework. TRIMF can handle knowledge transfer from implicit(explicit) dataset A to implicit(explicit) dataset B. Also, TRIMF can be set to suit different tasks.

### 2.3.2 Large Scale Transfer Learning

So far, transfer learning has been mostly considered in the off-line learning settings, which do not emphasize the scalability and computation speed. Due to the rapid development of storage technique and flourish of internet services, the real world problems in recent recommendation systems are mostly based on some large data sets. Little work on large scale transfer learning has been published in previous literature, though it is badly desirable. To cope with the growing needs of today's recommendation system, we would like to discover the parallelizing possibility in our experiments. There are already some researchers working on the large scale collaborative filtering, [4] designed a map-reduce framework for online news recommendation. In our approach, we investigate the parallel framework and put them on an online shopping site.

## Map-Reduce Framework

MapReduce is a framework for processing parallelizable problems in huge datasets using a large number of computers (nodes). A MapReduce program comprises a Map() procedure that performs filtering and sorting (such as sorting students by first name into queues, one queue for each name) and a Reduce() procedure that performs a summary operation (such as counting the number of students in each queue, yielding name frequencies).

- **“Map” step:** The master node takes the input, divides it into smaller sub-problems, and distributes them to worker nodes. A worker node may do this again in turn, leading to a multi-level tree structure. The worker node processes the smaller problem, and passes the answer back to its master node.
- **“Sort” step:** The master node sort all key-value pairs according to their key. Thus in the reduce step, same key appears sequentially.
- **“Reduce” step:** The master node then collects the answers to all the sub-problems and combines them in some way to form the output, i.e. the answer to the problem it was originally trying to solve.

We will show that our methods(modified version of TRIMF) can be plugged into the Map-Reduce framework for parallelization.

## CHAPTER 3

# TRANSFER LEARNING IN ONE CLASS CF FOR SHOPPING PREDICTION

### 3.1 Problem settings

#### 3.1.1 Background

In real-world, a person usually has different kinds of behaviour before buying one thing. For online shopping sites, Their goal is to let users buy their products, but the user-item matrix for deal is extremely sparse( less than 0.001% ). So if we only use the information of deal, we can't achieve good even reasonable performance.

In Yixun(Tencent's online shopping site), there are two main actions - click and purchase, both consists only binary data(1-action happened, 0-unknown). We know that deal matrix  $X_d$  is very sparse, although click matrix  $X_c$  is also sparse, but is much denser than  $X_d$ . So we developed a transfer learning algorithm(TRIMF) that leverage these data to predict a user's future purchasing. Compared with former methods which shares rating patterns or latent features only, our method shares both rating patterns and latent features through cluster-level transform and overlapping matrix. Experiments show that my algorithm performs better than other baseline(Transfer) methods.

#### 3.1.2 Problem definition

- Input: [0-1 matrix:user click matrix  $X_c(m_c * n_c)$ , user deal matrix  $X_d(m_d * n_d)$ ],  $m_c, m_d$  denote the number of users,  $n_c, n_d$  denote the number of items. Users and items are partially shared.

- Output: Two prediction matrix  $P_C(m_c * n_c)$ ,  $P_d(m_d * n_d)$ , which predict users' purchasing behaviour.

## 3.2 TRIMF

### 3.2.1 Weighting scheme of TRIMF

Former one-class CF methods [11], [19] use weighted low-rank approximation to tackle the problem that all observed ratings are 1. Given a rating matrix  $R = (R_{ij})_{m*n} \in \{0, 1\}^{m*n}$  with  $m$  users and  $n$  items and a corresponding non-negative weight matrix  $W = (W_{ij})_{m*n} \in R^{m*n+}$ , weighted low-rank approximation aims at finding a low rank matrix  $X = (X_{ij})_{m*n}$  minimizing the objective of a weighted Frobenius loss function as follows :  $L(X) = w(R_{ij} - X_{ij})$ .

In [11], the authors consider actions that happens more than once (e.g click an item multiple times). Negative entries are ignored, for each positive entry, its weight is propotional to its frequency, since more frequent can mean that we are more confident about the entry. In [19], positive entries are all with the same weight 1, while negative entries are considered in different ways. According to their experiments, user-oriented weighting scheme can acheive best performance. That is, for negative entries  $W_{ij} \propto \sum_j R_{ij}$ , it's idea is that if a user has more positive examples, it is more likely that she does not like the other items, that is, the missing data for this user is negative with higher probability.

In our method we adopt this weighting scheme to give missing values proper weights, i.e for positive entries we use the weighting scheme in [11] and negative entries we use user-oriented weighting.

### 3.2.2 Transfer learning in TRIMF

User's deal data is very sparse, e.g users will buy  $n_d$  items one day while click  $n_c$  items. Then  $n_d \ll n_c$ . So only use deal data is not sufficient. Traditional transfer learning methods use

matrix factorization and share a certain part of low-rank matrix(e.g user-latent factor, rating pattern). But none of them apply multi-selective-sharing schme.

In TRIMF, rating matrix are factorized into three parts :  $X = USV^T$ . We want to use users' click data to learn a better cluster-level rating pattern  $S$ , compared with only using users' purchase data. And for overlap users and items, we want their latent vector  $U, V$  to be the same, too. That it, we share their rating patterns and latent vectors. But what a user like to click is not always the item he wants to buy. So these rating pattern should be somehow related but not the same. In Yixun, there are only 2 common items in top-10 click items and top-10 purchase items (Table 3.2.2). So we can't simply apply the same pattern in prediction.

Top click items	Top purchase items
iPhone 5s	Tissue
Xiaomi 3	Laundry soap powder
Thinkpad	Xiaomi 3
CPU	Snacks
Hard disk	Battery
Router	iPhone 5s
Earphone	Mouse

Table 3.1: Top 10 click items and top 10 purchase items in Yixun

However, after careful observation we found that there are some items which belongs to the same category with higher conversion rate(user tends to buy after clicking), but some categories not. And there are some users who like window-shopping while others will buy it right after clicking. These are all cluster-level features, we design a mapping function to let the learnt  $S$  suit data better.

### 3.2.3 Object function

We use a weighted non-negative matrix tri-factorization method to deal with the problem as illustrated below.



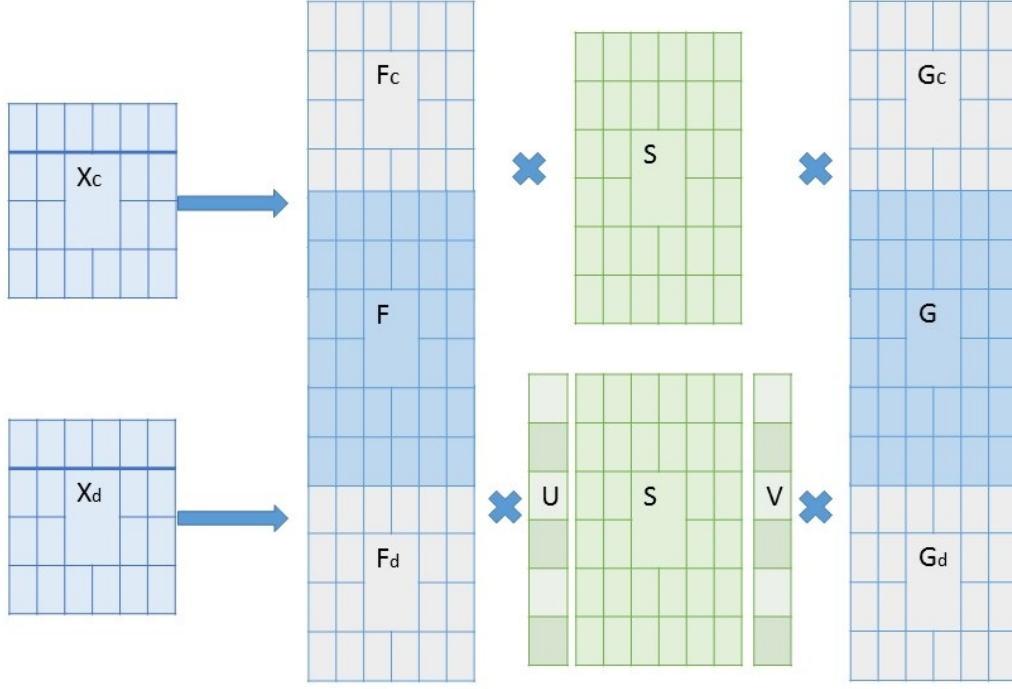


Figure 3.1: Graphical model of TRIMF

Objective Function:

$$\min_{F,G,S,U,V} W_c \odot \|X_c - (F; F_c)S(G; G_c)'\|_2 + W_d \odot \|X_d - (F; F_d)(USV)(G; G_d)'\|_2$$

- $W_c, W_d$  is the weight for  $X_c, X_d$ , every observed entry has weight  $1 + \log(\text{frequency})$ . while others have weight  $W_{ij} = \sum_j I(R_{ij})$ .
- $F, G$  is the soft clustering result matrix for overlapped users(items), they are forced to have the same cluster distributions. Others are unique users(items).
- $U, V$  are two diagonal matrix,  $U_{ii}$  scales every  $S_{i*}$  to  $U_{ii}S_{i*}$ , it models the users' tranform from click to deal. While  $V_{jj}$  scales every  $S_{*j}$  to  $S_{*j}V_{jj}$ , it models the items' tranform from click to deal.
- When predicting, we use  $(F; F_d)(USV)(G; G_d)$  to predict users who have deal data. And since we got two mapping matrix  $U, V$ , we apply  $U, V$  back to click matrix to predict users who have click data, i.e we use  $(F; F_c)(USV)(G; G_c)$  to predict.

### 3.3 Solution to TRIMF & Algorithm

Follow the update rules in [37], we use an alternately iterative algorithm to solve the objective function.

Firstly, we declare some denotions:

- $I_c, I_{cc}, I_{cd}, I_d : (I_c, I_{cc}) * (F; F_c) = I * (F; F_c)$  and  $(I_{cd}, I_d) * (F; F_d) = I * (F; F_d)$
- $sg : S * G' * G * S'$
- $F_1, F_2 : [F; F_c], [F; F_d]$

In each round of iteration these matrixes are updated as :

$$F \leftarrow F * \sqrt{\frac{I_{cc}' * (W_c * X_c) * G * S' + I_{cd}' * (W_d * X_d) * G * S'}{(I_{cc}' * I_{cc} * F + I_{cc}' * I_c * F_c + I_{cd}' * (I_{cd} * F + I_d * F_d)) * sg}}$$

$$F_c \leftarrow F_c * \sqrt{\frac{I_c' * (W_c * X_c) * G * S'}{I_c' * (I_{cc} * F + I_c * F_c) * sg}}$$

$$F_d \leftarrow F_d * \sqrt{\frac{I_d' * (W_d * X_d) * G * S'}{I_d' * (I_{cd} * F + I_d * F_d) * sg}}$$

$$G \leftarrow G * \sqrt{\frac{W_c * X_c * F_1 * S + (W_d * X_d)' * F_2 * S}{(G * (S' * F_1' * F_1 * S + S' * F_2' * F_2 * S))}}$$

$$U \leftarrow U * \sqrt{\frac{F_2' * (W_d * X_d) * G * V' * S'}{F_2' * F_2 * U * S * V * G' * G * V' * S'}}$$

$$V \leftarrow V * \sqrt{\frac{S' * F_2' * (W_d * X_d) * G}{S' * F_2' * F_2 * S * V * G' * G}}$$

The user-item matrix is typically very sparse with  $z \ll nm$  non-zero entries while  $k$  is typically also much smaller than  $n, m$ . By using sparse matrix multiplications and avoiding dense intermediate matrices, the updates can be very efficiently and easily implemented. In

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**Algorithm 1:** Algorithm for TRIMF.

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**Input:**  $\mathbf{X}_c, \mathbf{X}_d$   
 $\mathbf{X}_c \in \mathbb{R}^{m_c \times n_c}$ : the purchase data  
 $\mathbf{X}_d \in \mathbb{R}^{m_d \times n_d}$ : the click data  
**Initialize:** Initialize  $W_c, W_d : (1 + \log(freq))$  for observed,  $\sum_j I(R_{ij})$  for unseen,  
 $F, G, S, U, V : random$ , Set overlap numbers for users and items  
**for**  $i = 1$  to  $T$  **do**  
  update  $F$   
  update  $F_c, F_d$   
  update  $G$   
  update  $S$   
  update  $U, V$   
**end for**  
**Output:**  $F, G, S, U, V$

---

particular, updating  $F, S, G$  each takes  $O(k^2(m + n) + kz)$ , and the algorithm usually reach convergence in less than 200 iterations.

## 3.4 Experiment

### 3.4.1 Datasets

We select real data from an online shopping site: yixun.com<sup>1</sup>. We collect data for 6 months, the entire dataset consists 5,324,231 users and 643,123 items. The sparsity in click matrix is 0.06%, in purchase matrix is 0.0003%.

To check the effectiveness of TRIMF in short time and long time, we construct two smaller datasets.

- **Yixun short term data:** we select data from two weeks, 20130801-20130814. we sample a fraction of user by random, and remove those whose action frequency is too low(e.g only one click during this period). In the click matrix we have 16240 users and 1932 items. In the purchase matrix we have 2520 users and 1791 items. There are 2029 overlapped users and 1642 overlapped items. We train our model using data from first week and data from second week is used for testing.

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<sup>1</sup><http://www.yixun.com>

non-transfer methods	transfer methods
Most Popular, SVD, NMF, PMF, BPRMF, WRMF	CMF, TCF, TRIMF

Table 3.2: Baseline methods.

- **Yixun long term data:** we select 1012 active users through 6 months. In their long term actions, there are 6021 items which have been clicked and 1973 items bought. We select the five latest purchasing items per user as test data, others as training data. There are 1503 overlapped items.

### 3.4.2 Metrics

We use  $prec@5$  and  $prec@10$  as our evaluation measures.  $prec@n$  is the precision of top- $n$  results. Our main goal is to optimize for conversion rate(future purchase matrix), so the test is mainly done in the purchase matrix. However, since TRIMF can also optimize for source domain(click matrix), some test in click matrix is also conducted.

### 3.4.3 Baseline methods

We divide baseline methods into non-transfer methods and transfer methods. All baseline methods are shown in Table 3.2.

#### non-transfer methods

For all non-transfer methods, we use 3 combinations of matrix as our training matrix:deal, click, deal+click, and report their best performance. We choose parameters by cross validation.

- **Most Popular:** Most popular selects top- $n$  items in global, and provide same recommendation results for each user.
- **SVD [25]:** Singular Value Decomposition(SVD) is a typical method used in recommender system, here PureSVD from Matlab is used.

- rank = {5,10,20,30,40,50}
- NMF [13]: Non-negative Matrix Factorization(NMF) is also a typical method used in recommender system, here NMF from Matlab is used.
  - rank = {10,20,40,60,100}
- PMF [29]: Probabilistic Matrix Factorization(PMF) is a recently proposed method for missing value prediction. Previous work showed that this method worked well on the large, sparse and imbalanced data set.
  - rank = {10,20,30,40,50}
- BPRMF [28]: BPR is a generic optimization criterion for personalized ranking that is the maximum posterior estimator derived from a Bayesian analysis of the problem. Unlike traditional methods whose object function is point-wise, BPR is a pair-wise object function. BPRMF implements BPR using matrix factorization.
  - We initialized BPR with most popular results.
  - We set  $iteration = \#n * 100$ , ( $\#n$  in the number of observations)
- WRMF [19]: One-class collaborative filtering(WRMF) is a weighted low rank approximation method optimized for implicit dataset.
  - rank = {5,10,15,20,25}

## transfer methods

- CMF [33]: Collective Matrix Factorization is proposed for jointly factorizing two matrices. Being adopted as a transfer learning technique in several recent works, CMF has been proven to be an effective cross-domain recommendation approach. For each training and testing pairs, we make two matrix the same dimension(in order to share a latent factor) by padding rows & columns.

Method	Prec@5	Prec@10
Most Popular	0.0323	0.0289
SVD	0.0438	0.0367
NMF	0.0403	0.0324
PMF	0.0435	0.0372
BPRMF	0.0444	0.0364
WRMF	0.049	0.0403
CMF	0.0436	0.0350
TCF	0.0453	0.0369
TRIMF	<b>0.0525</b>	<b>0.0410</b>

Table 3.3: Performance of TRIMF and other baseline methods on short-term users who have deal data.

- Shared latent space dimension =  $\{5,10,15,20,25\}$
- TCF [22]: TCF is a transfer learning method to predict missing ratings via heterogeneous feedbacks. It’s originally designed for rating prediction, so we set the deal matrix with random sampled zeros as the rating matrix, click matrix as the implicit feed back matrix. Zero rows and colomns are also padded to make the two matrix in same dimension.
- TRIMF: our method.
  - We set latent factor = 30, iteration = 200.

### 3.4.4 Results

#### Yixun short term data

Since the user overlap of deal and click matrix are small, so we perform two test, one on deal matrix  $X_d$  and one on click matrix  $X_c$ .

Results are showed in Table 3.3 and Table 3.4.

#### Yixun long term data

Since the user are manually selected, we only test  $X_d$ . The result is showed in Table 3.5.

Method	Prec@5	Prec@10
Most Popular	0.0090	0.0085
SVD	0.0123	0.00113
NMF	0.0091	0.0089
PMF	0.0121	0.0112
BPRMF	0.0142	0.0130
WRMF	0.0174	0.0144
CMF	0.0176	0.0139
TCF	0.0158	0.0127
TRIMF	<b>0.0189</b>	<b>0.0153</b>
TRIMF(without remap)	0.0175	0.0146

Table 3.4: Performance of TRIMF and other baseline methods on short-term users who have deal data.

Method	Prec@5	Prec@10
Most Popular	0.00508	0.00405
SVD	0.00453	0.00413
NMF	0.00401	0.00389
PMF	0.00421	0.00312
BPRMF	0.00542	0.00430
WRMF	0.00485	0.00345
CMF	0.00512	0.00432
TCF	0.00534	0.00502
TRIMF	<b>0.00720</b>	<b>0.00606</b>

Table 3.5: Performance of TRIMF and other baseline methods on long-term users.

### 3.5 Performance comparison & analysis

First, we observed that TRIMF out-perform all other baseline non-transfer methods in three tests. In short-term deal test, we can see traditional CF method which aims at rating prediction (e.g SVD, NMF) can't achieve compatible performance than others. Because these methods is designed for matrix with multiple values, not for our binary matrix. while CF method designed for binary matrix(BPRMF, WRMF) can acheive significantly greater result. In long-term test the difference is not so significant, because the data here is less sparse than short-term data, every method has enough data to train a good model.

Second, TRIMF also out-perform other transfer methods. Since CMF, TCF are also designed for rating prediction problems. The information in our training set is limited, so both methods can't transfer enough knowledge from their framework. TRIMF is designed for one-class transfer learning, TRIMF combines one-class and transfer methods, so it inherits advantages from both side.

#### The effects of $UV$

In our assumption,  $UV$  are two mapping matrix that describe the difference in user-cluster and item-category. To see whether  $UV$  really reflects the phenomenon, we manually check entries in  $UV$  with high and low values.

We found that high value in  $V$  reflects item clusters that people tends to buy after clicking, e.g toothbrush, snacks. While low value of  $V$  more reflects that items are popular but people may not buy it immediately, e.g cell phones, laptops. High value in  $U$  reflects user-cluster who tends to buy after clicking, while users belong to low value user-clusters are all window-shopping fans.

In Table 3.4, we can see if we want to predict future purchasing items on users who have click data, we can map  $UV$  back. Thus the learned cluster-pattern  $S$  is transformed from click



Method	Prec@5	Prec@10
shareFG	<b>0.0436</b>	<b>0.0350</b>
not share	0.0335	0.0306
random share	0.0344	0.0299

Table 3.6: The effect of sharing

pattern to purchase pattern.

### The effects of sharing

To see that sharing  $F, G$  really works, we select another 6000 users to test, we tried 'not share', 'share' and 'random share', the  $prec@n$  here are not comparable with the first experiment (Table 3.3). Results show that we must share latent factor carefully, random share may do harm to performance. But sharing latent factor for overlapped users/items can achieve a significantly greater result.

## CHAPTER 4

### CONCLUSION AND FUTURE WORK

In this thesis, we proposed to perform *selective* knowledge transfer for CF problems and came up with a systematical study on how the factors such as variance of empirical errors could leverage the selection. We found although empirical error is effective to model the consistency across domains, it would suffer from the sparseness problem in CF settings. By introducing a novel factor - variance of empirical errors to measure how trustful this consistency is, the proposed criterion can better identify the useful source domains and the helpful proportions of each source domain. We embedded this criterion into a boosting framework to transfer the most useful information from the source domains to the target domain. The experimental results on real-world data sets showed that our selective transfer learning solution performs better than several state-of-the-art methods at various sparsity levels. Furthermore, comparing to existing methods, our solution works well on long-tail users and is more robust to overfitting.

However, we notice that there are limitations in the work. First, in STLCF, the knowledge transfer is item-based. That is, each item / user is evaluated independently. Therefore, the implicit relationships between items / users are omitted. Second, The computational cost of STLCF is expensive, even though the parallel implementation makes it possible to run on large clusters. Third, we require the full correspondence on either user set or the item set as a bridge for the knowledge transfer. This requirement limits the applications of STLCF in the real world, because most of the real system will not be able to provide the full correspondence information. Fourth, we are aware that although the STLCF performs well on the long-tails (target domain tasks with very limited observations, for example the experiment in Section ??), it still can not handle the case where no record of target domains is exist.

We believe the Selective Transfer Learning has practical applications in the real world and would be a promising research topic. STLCHF is our initial attempt on this topic. In the future to make Selective Transfer Learning be more robust, we propose the following approaches:

- **Model-based Selective Transfer Learning.** Instead of item-based knowledge transfer, we would like to explore the model-based transfer. That is, the domain information is first generalized as model and then be applied to later tasks. This will improve the universality of the source domain information and reduce the storage demand, as the information is generalized by models.
- **Relationship Regularized Selective Transfer Learning.** On the one hand, with the rapid growing of social networks in the internet, we have access to plenty of online user relationship. On the other hand, previous researches on taxonomy have made it possible to build relationship between items. Relationship regularized selection of helpful knowledge is naturally the next work.
- **Selection of Domain Correspondence.** Due to either record corruption or the absence of data in the industry, it is not always possible to obtain the full correspondence between the source domains and the target domain for knowledge transfer. To make Selective Transfer Learning be practical, we want to research on the selection of correspondence between domains when only part of it could be helpful. For example, in the settings where the user set is shared among the source and the target domains, we would like to select parts of the users during the transfer learning processes.
- **Boosting in Multi-Dimension.** The technique in this article can be viewed as boosting over either the item or user dimension. Can we extend it to multi-dimensional boosting? For example, would the interest of a user towards certain items evolve over time? With the evolution of user interests, is it possible to make a better prediction on the future ratings?

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