# The physica package

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## https://github.com/leedehai/typst-physics

Version 0.8.1, October 25, 2023 Doc updated: November 26, 2023

**NOTE (2023-04-02):** Typst is version 0.x and evolving, and this package evolves with it. Also, the package itself is under development and fine-tuning. While the major version stays 0, no backward compatibility is guaranteed.

Indexed at <a href="https://typst.app/docs/packages/">https://typst.app/docs/packages/</a>.

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## 1. Introduction

<u>Typst</u> is typesetting framework aiming to become the next generation alternative to LATEX. It excels in its friendly user experience and performance.

The physica package provides handy Typst typesetting functions that make academic writing for physics simpler and faster, by simplifying otherwise very complex and repetitive expressions in the domain of physics.

This manual itself was generated using the Typst CLI and the physica package, so hopefully this document is able to provide you with a sufficiently self evident demonstration of how this package shall be used.

## 2. Using physica

With typst's <u>package management</u>:

# 3. The symbols

Some symbols are already provided as a Typst built-in. They are listed here just for completeness with annotation like <sup>typst</sup> this, as users coming from LATEX might not know they are already available in Typst out of box.

All symbols need to be used in **math mode** \$...\$.

## 3.1. Braces

Symbol	Abbr.	Example	Notes
typst abs (content)		$\mathrm{abs}(\mathrm{phi}(\mathrm{x})) \to  \varphi(x) $	absolute
typst norm(content)		$\mathrm{norm}(\mathrm{phi}(\mathbf{x})) \to \ \varphi(x)\ $	norm
order(content)		$\operatorname{order}(\mathbf{x}^{2}) \longrightarrow \mathcal{O}(x^2)$	order of magnitude
Set(content)		$\begin{split} & \operatorname{Set}(\mathbf{a}_{-}\mathbf{n}),  \operatorname{Set}(\mathbf{a}_{-}\mathbf{i},  \operatorname{forall}  \mathbf{i}) \\ & \to \{a_n\}, \Big\{a_i \Big  \forall i \Big\} \\ & \operatorname{Set}(\operatorname{vec}(1, \mathbf{n}),  \operatorname{forall}  \mathbf{n}) \\ & \to \left\{ \binom{1}{n} \middle  \forall n \right\} \end{split}$	math set, use Set not set since the latter is a Typst keyword
evaluated(content)	eval	$\begin{array}{l} \operatorname{eval}(f(x))\_0^{\smallfrown} \inf \inf \\ \to f(x)\big _0^{\infty} \\ \operatorname{eval}(f(x)/g(x))\_0^{\smallfrown} 1 \\ \to \frac{f(x)}{g(x)}\Big _0^1 \end{array}$	attach a vertical bar on the right to denote evaluation boundaries
expectationvalue	expval	$\begin{array}{l} \operatorname{expval}(\mathbf{u}) \longrightarrow \left\langle u \right\rangle \\ \operatorname{expval}(\mathbf{f/N}) \longrightarrow \left\langle \frac{f}{N} \right\rangle \end{array}$	expectation value

# 3.2. Vector notations

Symbol	Abbr.	Example	Notes
typst vec ()		$\operatorname{vec}(1,2) \to \binom{1}{2}$	column vector
vecrow()		$\mathrm{vecrow(1,2)} \longrightarrow (1,2)$	row vector
		vecrow(sum_0^n a_i, b) $(\sum_{i=1}^{n} a_i)$	
		$\rightarrow \left(\sum_{0}^{n} a_{i}, b\right)$	
TT		$v^TT$ , $A^TT \to v^T, A^T$	transpose
<pre>vectorbold(content)</pre>	vb	vb(a),vb(mu_1) $ ightarrow a, \mu_1$	vector, bold
<pre>vectorunit(content)</pre>	vu	vu(a),vu(mu_1) $ ightarrow \hat{a},\hat{\mu}_1$	unit vector
<pre>vectorarrow(content)</pre>	va	va(a),va(mu_1) $ ightarrow ec{a},ec{\mu}_1$	vector, arrow
			(not bold: see ISO 80000-2:2019)
gradient	grad	grad f $ ightarrow oldsymbol{ abla} f$	gradient
divergence	div	div vb(E) $ ightarrow oldsymbol{ abla} \cdot oldsymbol{E}$	divergence
curl		curl vb(B) $ ightarrow oldsymbol{ abla} imes B$	curl
laplacian		diaer(u) = c^2 laplacian u	Laplacian, different from
		$\to \ddot{u} = c^2 \nabla^2 u$	$^{ m typst}$ laplace $\Delta$
dotproduct	dprod	a dprod b $ ightarrow a \cdot b$	dot product
crossproduct	cprod	a cprod b $\longrightarrow a \times b$	cross product

# 3.3. Matrix notations

Symbol	Abbr.	Example	Notes
TT		$\mathbf{v} \mathbf{^{TT}}, \ \mathbf{A} \mathbf{^{TT}} \to v^{T}, A^{T}$	transpose
typst mat()			matrix
<pre>matrixdet()</pre>	mdet	$mdet(1,x;1,y) \to \begin{bmatrix} 1 & x \\ 1 & y \end{bmatrix}$	matrix determinant
diagonalmatrix()	dmat	$dmat(1,2) \rightarrow \begin{pmatrix} 1 \\ 2 \end{pmatrix}$	diagonal matrix
		dmat(1,a,xi,delim:"[",fill	:
		$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
antidiagonalmatrix()	admat	$\operatorname{admat}(1,2) \to \binom{1}{2}$	anti-diagonal matrix
			l:dot)
<pre>identitymatrix()</pre>	imat	$imat(2) \rightarrow \begin{pmatrix} 1 \\ 1 \end{pmatrix}$	identity matrix
		<pre>imat(3,delim:"[",fill:*)</pre>	
		1 * * * 1 * * * 1	

Jacobian matrix: jacobianmatrix(...), i.e. jmat(...).

$$\begin{aligned} & \text{jmat}(\textbf{f}_{1},\textbf{f}_{2};~\textbf{x},\textbf{y}) & \text{jmat}(\textbf{f}_{1},\textbf{f}_{2};~\textbf{x},\textbf{y},\textbf{z};~\text{delim}:"["]) \\ & \begin{pmatrix} \frac{\partial f_{1}}{\partial x} & \frac{\partial f_{1}}{\partial y} \\ \frac{\partial f_{2}}{\partial x} & \frac{\partial f_{2}}{\partial y} \end{pmatrix} & & \\ & \begin{bmatrix} \frac{\partial f_{1}}{\partial x} & \frac{\partial f_{1}}{\partial y} & \frac{\partial f_{1}}{\partial z} \\ \frac{\partial f_{2}}{\partial x} & \frac{\partial f_{2}}{\partial y} & \frac{\partial f_{2}}{\partial z} \end{bmatrix} \end{aligned}$$

Hessian matrix: hessianmatrix(...), i.e. hmat(...).

Matrix built with an element building function: xmatrix(m, n, func), i.e. xmat(...). The element building function func takes two integers which are the row and column numbers starting from 1.

#### 3.4. Dirac braket notations

Symbol	Abbr. Example	Notes
bra(content)	$bra(u)  o \langle u  $	bra
	$bra(vec(1,2)) \rightarrow \left\langle \begin{pmatrix} 1 \\ 2 \end{pmatrix} \right $	
ket(content)	$ket(u) \to  u\rangle$	ket
	$ket(u)  o \ket{u}$ $ket(vec(1,2))  o \ket{\binom{1}{2}}$	
expval(content)	$\operatorname{expval}(u)  o \langle u \rangle$	expectation
	expval(u) $ ightarrow \langle u  angle$ expval(vec(1,2)) $ ightarrow \left\langle egin{pmatrix} 1 \\ 2 \end{pmatrix}  ight angle$	

## 3.5. Math functions

Typst built-in math operators: <a href="math.op">math.op</a>.

Expressions	Results
sin(x), $sinh(x)$ , $arcsin(x)$ , $asin(x)$	$\sin(x), \sinh(x), \arcsin(x), \sin(x)$
cos(x), $cosh(x)$ , $arccos(x)$ , $acos(x)$	$\cos(x), \cosh(x), \arccos(x), \cos(x)$
tan(x), $tanh(x)$ , $arctan(x)$ , $atan(x)$	$\tan(x), \tanh(x), \arctan(x), \tan(x)$
sec(x), $sech(x)$ , $arcsec(x)$ , $asec(x)$	$\sec(x), \operatorname{sech}(x), \operatorname{arcsec}(x), \operatorname{asec}(x)$
csc(x), $csch(x)$ , $arccsc(x)$ , $acsc(x)$	$\csc(x), \operatorname{csch}(x), \operatorname{arccsc}(x), \operatorname{acsc}(x)$
<pre>cot(x), coth(x), arccot(x), acot(x)</pre>	$\cot(x), \coth(x), \operatorname{arccot}(x), \operatorname{acot}(x)$

Expressions	Results	Notes
typst Pr(x)	$\Pr(x)$	probability
<sup>typst</sup> exp x	$\exp x$	exponential
<sup>typst</sup> log x, lg x, ln x	$\log x, \lg x, \ln x$	logarithmic
<sup>typst</sup> det A	$\det A$	matrix determinant
diag(-1,1,1,1)	$\mathrm{diag}(-1,1,1,1)$	diagonal matrix, compact form (use dmat for the "real" matrix form)
trace A, tr A	$\operatorname{trace} A,\operatorname{tr} A$	matrix trace
Trace A, Tr A	$\operatorname{Trace} A, \operatorname{Tr} A$	matrix trace, alt.
rank A	$\operatorname{rank} A$	matrix rank
erf(x)	$\operatorname{erf}(x)$	Gauss error function

Res A	$\operatorname{Res} A$	residue (complex analysis)
Re z, Im z	${\rm Re}z, {\rm Im}z$	real, imaginary (complex analysis)
sgn x	$\operatorname{sgn} x$	sign function

#### 3.6. Differentials and derivatives

Symbol	Abb	r.Example	Notes
<pre>differential()</pre>	dd	e.g. $df$ , $dxdy$ , $d^3x$ , $dx \wedge dy$ See Section 3.6.1	differential
variation()	var	${ m var(f)}  ightarrow \delta f$ ${ m var(x,y)}  ightarrow \delta x \delta y$	<pre>variation, shorthand of dd(, d: delta)</pre>
difference()		$\begin{array}{l} \text{difference(f)} \rightarrow \Delta f \\ \text{difference(x,y)} \rightarrow \Delta x \Delta y \end{array}$	<pre>difference, shorthand of dd(, d: Delta)</pre>
derivative()	dv	e.g. $\frac{\mathrm{d}}{\mathrm{d}x}, \frac{\mathrm{d}f}{\mathrm{d}x}, \frac{\Delta^k f}{\Delta x^k}, \mathrm{d}f/\mathrm{d}x$ See Section 3.6.2	derivative
partialderivative()	pdv	e.g. $\frac{\partial}{\partial x}, \frac{\partial f}{\partial x}, \frac{\partial^4 f}{\partial x^2 \partial y^2}, \frac{\partial^5 f}{\partial x^2 \partial y^3}, \partial f/\partial x$ See Section 3.6.3	partial derivative, could be mixed order

#### 3.6.1. Differentials

Functions: differential(\*args, \*\*kwargs), abbreviated as dd(...).

- positional *args*: the variable names, then at the last **optionally** followed by an order number e.g. 2, or an order array e.g. [2,3], [k], [m n, lambda+1].
- named *kwargs*:
  - d: the differential symbol [default: upright(d)].
  - p: the product symbol connecting the components [default: none].

#### Order assignment algorithm:

- If there is no order number or order array, all variables has order 1.
- If there is an order number (not an array), then this order number is assigned to *every* variable, e.g. dd(x,y,2) assigns  $x \leftarrow 2, y \leftarrow 2$ .
- If there is an order array, then the orders therein are assigned to the variables in order, e.g. dd(f,x,y,[2,3]) assigns  $x \leftarrow 2, y \leftarrow 3$ .
- If the order array holds fewer elements than the number of variables, then the orders of the remaining variables are 1, e.g. dd(x,y,z,[2,3]) assigns  $x \leftarrow 2, y \leftarrow 3, z \leftarrow 1$ .
- If a variable x has order 1, it is rendered as dx not  $d^{1}x$ .

#### **Examples**

(1) 
$$dd(f)$$
,  $dd(x,y)$  (2)  $dd(x,3)$ ,  $dd(f,[k])$ ,  $dd(f,[k],d:delta)$  
$$d^3x, d^kf, \delta^kf$$
 (3)  $dd(f,2)$ ,  $dd(vb(x),t,[3,])$  (4)  $dd(x,y,[2,3])$ ,  $dd(x,y,z,[2,3])$  
$$d^2f, d^3xdt$$
 (4)  $dd(x,y,[2,3])$ ,  $dd(x,y,z,[2,3])$  
$$d^2xd^3y, d^2xd^3ydz$$
 (5)  $dd(x,y,z,[2,3])$  (6)  $dd(x,y,z,[2,3])$  
$$d^2xd^3y dz$$
 (6)  $dd(x,y,z,[2,3])$  
$$d^2xd^3y dz$$
 (7)  $dd(x,y,z,[2,3])$  
$$d^2xd^3y dz$$
 (8)  $dd(x,y,z,[2,3])$  
$$d^2xd^3y dz$$
 (9)  $dd(x,y,z,[2,3])$  
$$d^2xd^3y dz$$
 (1)  $dd(x,y,z,[2,3])$  (2)  $dd(x,y,z,[2,3])$ 

(7) 
$$dd(t,x_1,x_2,x_3,p:and)$$
 (7)  $dd(t,x_1,x_2,x_3,d:upright(D))$  
$$dt \wedge dx_1 \wedge dx_2 \wedge dx_3$$
 
$$DtDx_1Dx_2Dx_3$$

### 3.6.2. Ordinary derivatives

Function: derivative(f, \*args, \*\*kwargs), abbreviated as dv(...).

- *f*: the function, which can be #none or omitted,
- positional args: the variable name, then at the last **optionally** followed by an order number e.g. 2,
- named kwargs:
  - d: the differential symbol [default: upright(d)].
  - s: the "slash" separating the numerator and denominator [default: none], by default it produces the normal fraction form  $\frac{df}{dx}$ . The most common non-default is slash or simply \/, so as to create a flat form df/dx that fits inline.

**Order assignment algorithm:** there is just one variable, so the assignment is trivial: simply assign the order number (default to 1) to the variable. If a variable x has order 1, it is rendered as x not  $x^1$ .

## **Examples**

(1) 
$$\text{dv}(,x)$$
,  $\text{dv}(,x,2)$ ,  $\text{dv}(f,x,k+1)$  (2)  $\text{dv}(,\text{vb}(r))$ ,  $\text{dv}(f,\text{vb}(r)_e, 2)$  
$$\frac{\text{d}}{\text{d}x}, \frac{\text{d}^2}{\text{d}x^2}, \frac{\text{d}^{k+1}f}{\text{d}x^{k+1}}$$
 
$$\frac{\text{d}}{\text{d}r}, \frac{\text{d}^2}{\text{d}r_e^2}$$
 (3)  $\text{dv}(f,x,2,s:\/)$ ,  $\text{dv}(f,xi,k+1,s:slash)$  (4)  $\text{dv}(,x,d:delta)$ ,  $\text{dv}(,x,2,d:Delta)$  
$$\frac{\text{d}^2f/\text{d}x^2}{\text{d}x^2}, \frac{\text{d}^{k+1}f/\text{d}\xi^{k+1}}{\text{d}x^2}$$
 
$$\frac{\delta}{\delta x}, \frac{\Delta^2}{\Delta x^2}$$
 (5)  $\text{dv}(\text{vb}(u),t,2,d:upright(D),s:slash)$  
$$\frac{D^2u}{Dt^2}$$

## 3.6.3. Partial derivatives (incl. mixed orders)

Function: partialderivative (f, \*args, \*\*kwargs), abbreviated as pdv (...).

- f: the function, which can be #none or omitted,
- positional *args*: the variable names, then at last **optionally** followed by an order number e.g. 2, or an order array e.g. [2,3], [k], [m n, lambda+1].
- named *kwargs*:
  - s: the "slash" separating the numerator and denominator [default: none], by default it produces the normal fraction form  $\frac{\partial f}{\partial x}$ . The most common non-default is slash or simply \/, so as to create a flat form  $\partial f/\partial x$  that fits inline.
  - total: the user-specified total order.
    - If it is absent, then (1) if the orders assigned to all variables are numeric, the total order number will be **automatically computed**; (2) if non-number symbols are present, computation will be attempted with minimum effort, and a user override with argument total may be necessary.

### Order assignment algorithm:

- If there is no order number or order array, all variables has order 1.
- If there is an order number (not an array), then this order number is assigned to *every* variable, e.g. pdv(f,x,y,2) assigns  $x \leftarrow 2, y \leftarrow 2$ .

- If there is an order array, then the orders therein are assigned to the variables in order, e.g. pdv(f,x,y,[2,3]) assigns  $x \leftarrow 2, y \leftarrow 3$ .
- If the order array holds fewer elements than the number of variables, then the orders of the remaining variables are 1, e.g. pdv(f,x,y,z,[2,3]) assigns  $x \leftarrow 2, y \leftarrow 3, z \leftarrow 1$ .
- If a variable x has order 1, it is rendered as x, not  $x^1$ .

### **Examples**

$$\frac{\partial}{\partial x}, \frac{\partial^2}{\partial x^2}, \frac{\partial^k}{\partial x^k}$$

$$rac{\partial arphi}{\partial m{r}}, rac{\partial^2 arphi}{\partial m{r}_e^2}$$

(3) 
$$pdv(,x,y)$$
,  $pdv(,x,y,2)$ 

(4) 
$$pdv(f,x,y,2)$$
,  $pdv(f,x,y,3)$ 

$$\frac{\partial^2}{\partial x \partial y}, \frac{\partial^4}{\partial x^2 \partial y^2}$$

$$\frac{\partial^4 \varphi}{\partial x^2 \partial y^2}, \frac{\partial^6 \varphi}{\partial x^3 \partial y^3}$$

(6) 
$$pdv(,t,2,s:\/)$$
,  $pdv(f,x,y,s:slash)$ 

$$\frac{\partial^3}{\partial x^2 \partial y}, \frac{\partial^3}{\partial x \partial y^2}$$

$$\partial^2/\partial t^2$$
,  $\partial^2 f/\partial x \partial y$ 

$$(7) \text{ pdv}(, (x^1), (x^2), (x^3), [1,3])$$

$$\frac{\partial^5}{\partial(x^1)\partial(x^2)^3\partial(x^3)}$$

$$\frac{\partial^7 \varphi}{\partial x^2 \partial u^2 \partial z^2 \partial \tau}$$

$$\frac{\partial^{\eta+\xi+5}}{\partial x \partial y^{\xi} \partial z^2 \partial t^{\eta+2}}$$

$$\frac{\partial^{(\xi+1)n}}{\partial x^{\xi n}\partial y^{n-1}\partial z}$$

(11) integral\_V dd(V) (pdv(cal(L), phi) - diff\_mu (pdv(cal(L), (diff\_mu phi)))) = 0

$$\int_V \mathrm{d}V \! \left( \frac{\partial \mathcal{L}}{\partial \varphi} - \partial_\mu \! \left( \frac{\partial \mathcal{L}}{\partial \left( \partial_\mu \varphi \right)} \right) \right) = 0$$

## 3.7. Miscellaneous

#### 3.7.1. Reduced Planck constant (hbar)

In the default font, the Typst built-in symbol planck. reduce  $\hbar$  looks a bit off: on letter "h" there is a slash instead of a horizontal bar, contrary to the symbol's colloquial name "h-bar". This package offers hbar to render the symbol in the familiar form:  $\hbar$ . Contrast:

Typst's planck.reduce 
$$E=\hbar\omega$$
  $\frac{\pi G^2}{\hbar c^4}$   $Ae^{\frac{i(px-Et)}{\hbar}}$   $i\hbar\frac{\partial}{\partial t}\psi=-\frac{\hbar^2}{2m}\nabla^2\psi$  this package's hbar  $E=\hbar\omega$   $\frac{\pi G^2}{\hbar c^4}$   $Ae^{\frac{i(px-Et)}{\hbar}}$   $i\hbar\frac{\partial}{\partial t}\psi=-\frac{\hbar^2}{2m}\nabla^2\psi$ 

#### **3.7.2. Tensors**

Tensors are often expressed using the <u>abstract index notation</u>, which makes the contravariant and covariant "slots" explicit. The intuitive solution of using superscripts and subscripts do not suffice if both upper (contravariant) and lower (covariant) indices exist, because the notation rules require the indices be vertically separated: e.g.  $T^a_b$  and  $T^b_a$ , which are of different shapes. " $T^a_b$ " is flatly wrong, and T^(space w)\_(i space j) produces a weird-looking " $T^w_i$ " (note w,j vertically overlap).

Function: tensor(symbol, \*args).

- *symbol*: the tensor symbol,
- positional *args*: each argument takes the form of +... or -..., where a + prefix denotes an upper index and a prefix denotes a lower index.

### **Examples**

$$T^a_{\phantom{a}b}, T_a^{\phantom{a}b}$$

(5) tensor((dd(x^lambda)),-a)   
 (6) tensor(AA,+a,+b,-c,-d,+e,-f,+g,-h) 
$$\begin{pmatrix} \mathrm{d} x^{\lambda} \end{pmatrix}_{a}$$
 
$$\mathbb{A}^{ab} \stackrel{e}{}_{cd} \stackrel{g}{}_{h}$$

(9) grad\_mu A^nu = diff\_mu A^nu + tensor(Gamma,+nu,-mu,-lambda) A^lambda

$$\boldsymbol{\nabla}_{\mu}A^{\nu}=\partial_{\mu}A^{\nu}+\boldsymbol{\Gamma}^{\nu}_{\phantom{\nu}\mu\lambda}A^{\lambda}$$

#### 3.7.3. Isotopes

Function: isotope(element, a: ..., z: ...).

- *element*: the chemical element (use ".." for multi-letter symbols)
- *a*: the mass number *A* [default: none].
- *z*: the atomic number *Z* [default: none].

Change log: Typst merged my PR, which fixed a misalignment issue with the surrounding text.

#### Examples

(3) isotope("Bi",a:211,z:83) --> isotope("Tl",a:207,z:81) + isotope("He",a:4,z:2) 
$$^{211}_{83} \text{Bi} \longrightarrow {}^{207}_{81} \text{Tl} + {}^{4}_{2} \text{He}$$

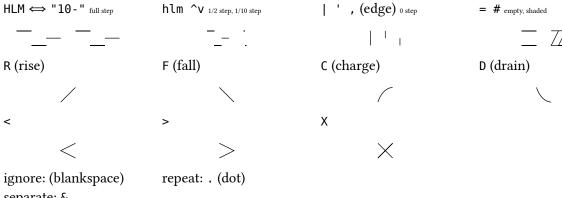
## 3.7.4. Signal sequences (digital timing diagrams)

In engineering, people often need to draw digital timing diagrams for signals, like

Function: signals(str, step::..., style:...).

- str: a string representing the signals. Each character represents an glyph (see below).
- step (optional): step width, i.e. how wide each glyph is [default: #1em].
- color (optional): the stroke color [default: #black].

### Glyph characters



separate: &

## **Examples**

(1) signals("10.1"), signals("1|0|1|0R"), signals("CD"), signals("CD", step: #2em)

(2) signals( $"M'H|L|h|l|^|v,&|H'M'H|l,m,l|"$ ) (the ampersand & serves as a separator)

(3) signals("-|=|-", step: #2em), signals("-|#|-"), signals("-<=>-<=")

(4) signals("R1..F0..", step: #.5em)signals("R1.|v|1", step: #.5em, color:#fuchsia)



**(5)** 

```
"clk:" & signals("|1....|0....|1....|0....|1....|0....|1....|0....| step: #0.5em) \
"bus:" & signals(" #.... X=... X=... X=... X#.", step: #0.5em)
                  bus: ////////
```

## 3.8. Symbolic addition

This package implements a very rudimentary, bare-minimum-effort symbolic addition function to aid the automatic computation of a partial derivative's total order in the absence of user override (see Section 3.6.3). Though rudimentary and unsophisticated, this should suffice for most use cases in partial derivatives.

Function: BMEsymadd([...]).

• ...: symbols that need to be added up e.g. [1,2], [a+1,b^2+1,2].

## **Examples**

# 4. Acknowledgement

Huge thanks to these LATEX packages, for lighting the way of physics typesetting.

- physics by Sergio C. de la Barrera,
- derivatives by Simon Jensen,
- tensor by Philip G. Ratcliffe et al.