

# Introduction to Statistics with Randomization and Simulation

*Mine Çetinkaya-Rundel, Johanna Hardin, others...*

*2020-01-09*



# Contents

<b>Preamble</b>	<b>5</b>
<b>1 Introduction to data</b>	<b>7</b>
1.1 Case Study (capable of extending to MLR or 2 by 2 table) . . . .	7
1.2 Taxonomy of Data . . . . .	7
1.3 Overview of data collection principles . . . . .	7
1.4 Observational studies and sampling strategies . . . . .	7
1.5 Experimental design and causality . . . . .	7
1.6 Revisit case study with new terminology we learned . . . . .	7
<b>2 Exploratory Data Analysis</b>	<b>9</b>
2.1 Cat vs. cat - segmented plots / contingency tables . . . . .	9
2.2 Num vs. cat - side-by-side box plots / comparing distributions .	9
<b>3 Correlation and Regression</b>	<b>11</b>
3.1 Visual summaries of data: scatterplot, side-by-side boxplots, histogram, density plot, box plot (lead out with multivariate, follow with univariate) . . . . .	11
3.2 Describing distributions: correlation, central tendency, variability, skew, modality . . . . .	11
3.3 Num vs. num - SLR . . . . .	11
<b>4 Multiple Regression</b>	<b>13</b>
4.1 Num vs. whatever - MLR . . . . .	13
4.2 Parallel slopes . . . . .	13
4.3 Hint at interaction, planes, and parallel planes but not quantify .	13
4.4 Logistic regression . . . . .	13
<b>5 Foundations of inference</b>	<b>15</b>
5.1 Understanding inference through simulation . . . . .	15
5.2 Randomization case study: gender discrimination . . . . .	15
5.3 Randomization case study: opportunity cost . . . . .	15
5.4 Hypothesis testing . . . . .	15
5.5 Confidence intervals . . . . .	15

5.6	Simulation case studies . . . . .	15
<b>6</b>	<b>Inference for categorical data</b>	<b>17</b>
6.1	Inference for a single proportion . . . . .	17
6.2	Difference of two proportions . . . . .	17
6.3	Testing for goodness of fit using chi-square (special topic, include simulation version) . . . . .	17
6.4	Testing for independence in two-way tables (special topic) . . . .	17
<b>7</b>	<b>Inference for numerical data</b>	<b>19</b>
7.1	One-sample means . . . . .	19
7.2	Paired data . . . . .	19
7.3	Difference of two means . . . . .	19
7.4	Comparing many means with ANOVA (special topic, include simulation version) . . . . .	19
<b>8</b>	<b>Inference for regression</b>	<b>21</b>
8.1	Inference for linear regression . . . . .	21
8.2	Checking model assumptions using graphs . . . . .	21
8.3	Inference for multiple regression . . . . .	21
8.4	Inference for logistic regression . . . . .	21
<b>9</b>	<b>Appendix: Probability</b>	<b>23</b>

# Preamble

Need to move preamble here.



# Chapter 1

## Introduction to data

- 1.1 Case Study (capable of extending to MLR or 2 by 2 table)
- 1.2 Taxonomy of Data
- 1.3 Overview of data collection principles
- 1.4 Observational studies and sampling strategies
- 1.5 Experimental design and causality
- 1.6 Revisit case study with new terminology we learned





## Chapter 2

# Exploratory Data Analysis

### 2.1 Cat vs. cat - segmented plots / contingency tables

- Conditional probability from contingency tables
- Bayes Theorem (law of total probability?)

### 2.2 Num vs. cat - side-by-side box plots / comparing distributions

- Mention univariate - center, skew, shape, spread
- Mention conditional probabilities as well



## Chapter 3

# Correlation and Regression

**3.1 Visual summaries of data:** scatterplot, side-by-side boxplots, histogram, density plot, box plot (lead out with multivariate, follow with univariate)

**3.2 Describing distributions:** correlation, central tendency, variability, skew, modality

**3.3 Num vs. num - SLR**

- correlation
- Line fitting, residuals, and correlation
- Fitting a line by least squares regression
- Types of outliers in linear regression



## Chapter 4

# Multiple Regression

### 4.1 Num vs. whatever - MLR

- Introduction to multiple regression

### 4.2 Parallel slopes

### 4.3 Hint at interaction, planes, and parallel planes but not quantify

- Visualization of higher-dimensional models (rgl demo)

### 4.4 Logistic regression

- Binary vs. num/whatever
- Three scales interpretation (e.g. probability, odds, log-odds)
- “parallel” logistic curves?



## Chapter 5

# Foundations of inference

5.1 Understanding inference through simulation

5.2 Randomization case study: gender discrimination

5.3 Randomization case study: opportunity cost

5.4 Hypothesis testing

5.5 Confidence intervals

5.6 Simulation case studies





## Chapter 6

# Inference for categorical data

### 6.1 Inference for a single proportion

- Simulation
- Exact (if we include course on probability)
- CLT and Normal approximation

### 6.2 Difference of two proportions

### 6.3 Testing for goodness of fit using chi-square (special topic, include simulation version)

### 6.4 Testing for independence in two-way tables (special topic)



## Chapter 7

# Inference for numerical data

### 7.1 One-sample means

- Bootstrap (for means, medians)
- t-distribution

### 7.2 Paired data

### 7.3 Difference of two means

### 7.4 Comparing many means with ANOVA (special topic, include simulation version)



## Chapter 8

# Inference for regression

### 8.1 Inference for linear regression

- Bootstrap for regression coefficients
- t-distribution for regression coefficients
- Model Comparison: Occam's Razor and  $R^2 > R^2_{\text{adj}}$

### 8.2 Checking model assumptions using graphs

- L-I-N-E

### 8.3 Inference for multiple regression

- residuals vs. fitted instead of residuals vs. x

### 8.4 Inference for logistic regression



## Chapter 9

# Appendix: Probability

(Keep same content as before, minus the bit of probability that got moved to categorical EDA)