

Purpose of Program-

So basically, the branch- “Combinatorics” revolves around four fundamental concepts. They are listed as below-

- 1) *Combinations without repetitions/replacements.*
- 2) *Combinations with repetitions/replacements.*
- 3) *Permutations without repetitions/replacements.*
- 4) *Permutations with repetitions/replacements.*

Suppose we have a string of length- **n** and we want to generate all **combinations/permutations** taken **r** at a time **with/without repetitions.**

Below is a summary table depicting the fundamental concepts in Combinatorics Theory.

Summary Table

	<u>Replacements/Repetitions allowed</u>	<u>Replacements/Repetitions not allowed</u>
<u>Permutations/Order Important</u>	n^r possibilities See this- http://www.geeksforgeeks.org/print-all-combinations-of-given-length/ See the special case when $r=n$ below http://www.geeksforgeeks.org/print-all-permutations-with-repetition-of-characters/	nP_r possibilities See this- http://www.geeksforgeeks.org/write-a-c-program-to-print-all-permutations-of-a-given-string/ Here $r=n$, as we are permuting all the characters of the string.
<u>Combinations/Order Not Important</u>	${}^{n+r-1}C_r$ possibilities	nC_r possibilities See this- http://www.geeksforgeeks.org/print-all-possible-combinations-of-r-elements-in-a-given-array-of-size-n/

Motivation behind the article-

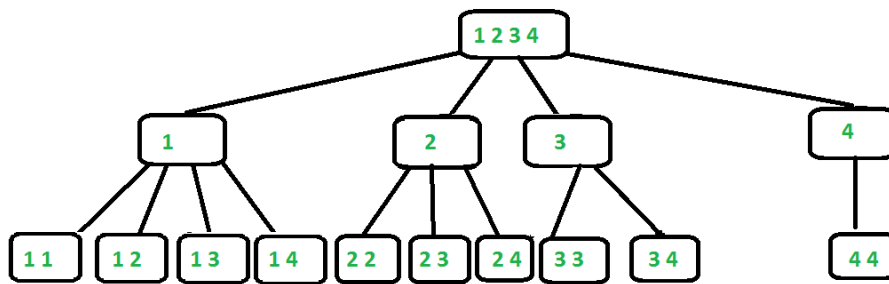
As, I felt that there is no good article/code for the third case(**Order Not important and Repetitions allowed**) on the web (including-<http://www.geeksforgeeks.org>) , hence this article came to my mind.

Explanation-

We will recur for all the possibilities of the string, even if the characters are repeating.

The base case of the recursion is when there is a total of 'r' characters and the combination is ready to be printed.

For clarity, see the recursion tree for the string- " 1 2 3 4" and r=2



Recursion Tree for the string= " 1 2 3 4 "

Time Complexity-

For a string of length- **n** and combinations taken **r** at a time with repetitions, it takes a total of $O(n^{r-1}C_r)$ time.

Space Complexity-

Since, we have created another array- chosen[] of size- '**r**', hence we need an extra **O(r)** space.

References- <https://en.wikipedia.org/wiki/Combination>