Tutorial-4

T(n) =
$$3T(h/2) + h^2$$
 $a = 3, b = 2$ $f(n) = h^2$
 $n\log_b^a = n\log_2^3$

comparing $n\log_2^3$ and n^2
 $n\log_2^3 < n^2$ (case 3)

... cue. for mostor's Theorem

 $T(n) = O(h^2)$

(2)
$$T(n) = 4T(n/2) + n^2$$

 $\alpha = 4$, $b = 2$
 $n \log_{h}^{2} = n \log_{2}^{4} = n^2 = f(n)$ (case 2)
 $\alpha = 4$, $\alpha = 4$ master's theorem $T(n) = O(n^2 \log n)$

(3)
$$T(n) = T(n/2) + 2^n$$
 $\alpha = 1, b = 2$
 $h \log_2 1 = n^0 = 1$
 $1 < 2^n \text{ (asi3)}$
 $\therefore \text{ Acc. to master's theorem } T(n) = O(2^n)$

(9) Ten = 2" T(n/2) + n"

... Mastor's theorem is not applicable as a w of n

$$\begin{array}{lll}
\boxed{3} & Ten = (6T(n/u) + n \\
a = 16, b = 4, f(n) = n \\
n \log_0^9 = n \log_0^{16} = n^2 \\
n^2 > f(n) & (auxel)
\end{array}$$

$$T(n) = O(n^2)$$

(a)
$$T(n) = 2T(n/2) + n \log n$$

 $a = 2$, $b = 2$, $f(n) = n \log n$
 $n \log_b^a = n \log_2^2 = n$
Now $f(n) > n$
 \therefore Acc. to master's $T(n) = 0$ ($n \log n$)

T(n) =
$$2T(N_2) + \frac{n}{\log n}$$

$$a = 2, b = 2, f_{n} = \frac{n}{\log n}$$

$$n \log_b^9 = n \log_2^2 = n$$

$$n > f(n)$$

$$\therefore Au \cdot fo \text{ master's Theorem } T(n) = o(n)$$

B
$$T(n) = 2T(n/4) + n^{0.51}$$

$$a = 2, b = 4, f(n) = n^{0.51}$$

$$n = n \log^2 n = n^{0.5}$$

$$n^{0.5} < f(n)$$

$$\therefore Acc - to master's theorem $T(n) = O(n^{0.5})$$$

- (1) T(n) = 0.5 T (n/2) + in

 ... Master's Net applicable as a < 1
- (18) $Tun_1 = 16T(n/u) + n1$ u = 16, b = 4, f(n) = n! $n \log_b^a = n \log_u^{16} = n^2 \quad n^2 \times n!$ $\therefore Acc. \text{ for master's}, T(n) = O(n!)$
- (f) $T(n) = 4T(\frac{\pi}{4}) + \log n$ $a = 4, b = 2, f(n) = \log n$ $h \log_{b}^{9} = n \log_{2}^{4} = n^{2}$ $h^{2} > f(n)$ $\therefore Au. \text{ for master's }, T(n) = O(n^{2})$
- (3) T(n) = 8T(n/2) + n $\alpha = 3, b = 3, f(n) = \sqrt{n}$ $n \log_{3}^{\alpha} = n \log_{3}^{3} = n$ $n > \sqrt{n}$ $\therefore Ae to master theorem, T(n) = Q(n)$

(I) T(n) = -3T(n/3) + Jn $\alpha = 3, b = 3, f(n) = Jn$ $n \log_3^{\alpha} = n \log_3^{23} = n$ n > Jn $\therefore Acc. +o master theorem, <math>T(n) = O(n)$

(15) $T(n) = 4T(N_2) + Cn$ A = 4, b = 2, f(n) = C + n $h \cdot \log_{2}^{a} = n \cdot \log_{2}^{u} = n^{2}$ $h^{2} > C + n$ $\vdots \quad Au. \quad to \quad master's \quad theorem, \quad T(n) = O(n^{2})$

(a) $T(n) = 3T(n/4) + n\log n$ a = 3, b = 4, $f(m) = n\log n$ a = 3, $f(m) = n\log n$ a

(F)
$$T(n) = 3T(n/3) + n/2$$

$$a = 3, b = 3, f(n) = n/2$$

$$n \log_b^a = n \log_3^3 = n$$

$$O(n) = O(n/2)$$

$$Acc. to master's theorem $T(n) = O(n^2 \log n)$$$

(8)
$$T(n) = 6T(n/3) + n^2 \log n$$

$$Q = 6, b = 3; f(n) = n^2 \log n$$

$$h \log_6 6 = n \log_3 6 = n^{1.63}$$

$$h^{1.63} < h^2 \log n$$

$$h^{1.63} < h^2 \log n$$

$$\therefore \text{ But to master s. Hewsen } To 1 = O(h^2 \log n)$$

T(n) = 4T (n/2) + n fleg n.

$$\alpha = \mu$$
, $b = 2$, $f(n) = n/\log n$
 $h \log_{10}^{10} = n \log_{10}^{10} = n^{2}$
 $n^{2} > n/\log n$
i. And Acc. He master's theorem T(n) = $O(n^{2})$

(20) $T(n) = 64T(n/8) - n^2 \log n$ Master's theorem is not applicable as S(n) is not increasing function. $\begin{array}{lll}
\boxed{2} & T(n) = £ 77 (n/3) + n^2 \\
\alpha = 7, b = 3, f(n) = n^2 \\
h \log_3 \alpha = n \log_3 7 = n^{1.7} \\
n^{1.7} < n^2
\end{array}$ i. But to master's, $T(n) = O(n^2)$

T(n) = T(n/2) + n(2-cos n)

Master's theorem isn't applicable since sugularity

condition is isolated in case 3.