

**INPUT:** Formula  $F$  of the form  $G_1 \wedge \dots \wedge G_n$ , where each  $G_i$  can be of the form:

- $t_1 \diamond t_2$ . Possible forms of  $t_1, t_2$  and  $\diamond$  are presented in the table:

$t_1$	$t_2$	$\diamond$
arithmetic term <sup>a</sup>	arithmetic term	$\{<, <, \leq, \geq, =, \neq\}$
<i>record</i>	<i>record</i>	$\{=, \neq\}$
<i>record</i>	<i>symbolic constant</i>	$\{\neq\}$
<i>record</i>	<i>arithmetic term</i>	$\{\neq\}$
<i>variable</i>	<i>record</i>	$\{=, \neq\}$
<i>variable</i>	<i>symbolic constant</i>	$\{<, <, \leq, \geq, =, \neq\}$
<i>variable</i>	<i>arithmetic term</i>	$\{<, <, \leq, \geq, =, \neq\}$

<sup>a</sup>for definition of arithmetic term, see algorithms.pdf

- $t \in D$ . Possible forms of  $t$  and  $D$  are presented in the table :

$t$	$D$
<i>arithmetic term</i>	$n_1..n_2, \{n_1, \dots, n_k\}$ , where $n_1, \dots, n_k$ are numbers
<i>non-arithmetic variable</i> <sup>a</sup>	$\{t_1, \dots, t_n\}$ , where all $t_i$ are arbitrary ground terms.

<sup>a</sup>for definition of arithmetic variable, see algorithms.pdf

- $\neg(t \in D)$  the possible forms of  $t$  and  $D$  are the same as in  $(t \in D)$ .

**OUTPUT:** True if  $F$  is satisfiable and false otherwise.

**BEGIN.**  $BODY := \text{true}; \Pi_{prolog} := \emptyset$

**For each**  $G_i$  in  $G_1 \wedge \dots \wedge G_n$

1.  $G_i$  of the form  $t_1 \diamond t_2$  or  $\neg(t_1 \diamond t_2)$   
 $BODY := BODY \wedge G_i$
2.  $G_i$  of the form  $(t \in D)$ 
  - (a) **t is an arithmetic term, and D is of the form  $n1..n2$**   
 $BODY := BODY \wedge t \text{ in } n1..n2$
  - (b) **t is an arbitrary term, D is of the form  $\{t1, t2, \dots, tn\}$**   
 $\Pi_{prolog} := \Pi_{prolog} \cup \text{set\_d}(X) : \neg \text{member}(X, [t1, t2, \dots, tn]).$ <sup>1</sup>  
 $BODY := BODY \wedge \text{set\_d}(t)$
3.  $G_i$  of the form  $\neg(t \in D)$ ,
  - (a) **t is an arithmetic term and D is of the form  $n1..n2$**   
 Let  $g_i$  is an unique label for  $G_i$   
 $\Pi_{prolog} := \Pi_{prolog} \cup g_i(t) : \neg n\# > n_2. \cup g_i(t) : \neg n\# < n_2.$   
 $BODY := BODY \wedge g_i(t)$
  - (b) **t is an arbitrary term, D is of the form  $\{t1, t2, \dots, tn\}$**   
 $\Pi_{prolog} := \Pi_{prolog} \cup \text{set\_d}(X) : \neg \text{member}(X, [t1, t2, \dots, tn]).$ <sup>2</sup>  
 $BODY := BODY \wedge \neg \text{set\_d}(t)$

<sup>1</sup>if  $t$  is arithmetic, we preprocess  $D$  and remove all non-numbers to avoid errors

<sup>2</sup>same as above

**End for**

Let  $V_1, \dots, V_n$  be all arithmetic variables in  $G_1, \dots, G_n$

$BODY : -REORDER(BODY) \cap labeling([], [V_1, \dots, V_n])$ .

$\Pi_{prolog} := \Pi_{prolog} \cap p : -BODY$ .

If the answer to query  $?-p$  to program  $\Pi_{prolog}$  is 'yes',  
return true; else return false.

**END**