

convert 42.75 in binary and how it works for decimal explain

Let's break down **how to represent 42.75 in binary**, and **how fractional (decimal) parts are converted to binary**.

1. Convert the Integer Part (42) to Binary

- Divide by 2, write the remainder, continue with the quotient until 0.
- 42 divided by 2:

Step	Quotient	Remainder
1	21	0
2	10	1
3	5	0
4	2	1
5	1	0
6	0	1

Write remainders bottom to top:

42 = 101010₂

2. Convert the Fractional Part (0.75) to Binary

Algorithm (for base 2 fractions):

- Multiply the fraction by 2.
- The result's **integer part** is the next binary digit.
- Continue with the new fractional part until it becomes 0 or until desired precision.

Steps for 0.75:

1. $0.75 \times 2 = 1.5 \rightarrow$ integer part: **1**; new fraction: 0.5
2. $0.5 \times 2 = 1.0 \rightarrow$ integer part: **1**; new fraction: 0.0

When the fraction reaches 0, we stop.

So, **0.75₁₀ = .11₂**

3. Combine Integer and Fractional Parts

- $42 = 101010$
- $0.75 = .11$

Thus,

$$42.75_{10} = 101010.11_2$$

4. How Binary Fractions Work (How Decimals Convert)

- Place values after the point are powers of 2, just like before the point, but negative:
 - Binary point places:
1st: $1/2$ (2^{-1}), 2nd: $1/4$ (2^{-2}), 3rd: $1/8$ (2^{-3}), etc.
- So, 101010.11_2 equals:
 - $101010 = 32 + 8 + 2 = 42$
 - $.1$ (first bit after point): $1 \times 1/2 = 0.5$
 - $.1$ (second bit): $1 \times 1/4 = 0.25$
 - $.11 = 0.5 + 0.25 = 0.75$

So, total = $42 + 0.75 = 42.75$

5. Summary Table

Decimal	Binary
42	101010
0.75	.11
42.75	101010.11

In Short:

- Convert the integer part to binary as usual.
- For the fractional part, repeatedly multiply by 2, writing down the integer portion each time.
- Combine both for the binary result.

Let me know if you want more examples, or the IEEE 754 binary (machine-level) form!