

In greedy technique most of problem are having n inputs and our object is to find the subset of given input which will satisfy our requirement.

n - input	condition	max profit
	or	or
	constraint	min cost

- Problem Definition
understanding the problem clearly
- Find solution space
all possible solution for a given n inputs
- It is one of the solution from solution space, which will satisfy the condition
- Optimal solution
It is the solution from solution which will give max. profit or min cost.

Application of greedy technique

- greedy Knapsack
- job sequencing / scheduling problem with deadline
- optimal merge pattern
- Huffman coding
- min cost spanning tree

• signal source shortest path

$$\text{Problem} = \sum_{i=1}^n w_i > M$$

$$\text{Feasible} = \sum_{i=1}^n w_i \times x_i \leq M$$

$$\text{Optimal} = x_i \times p_i$$

Eg:- $n = 3$, $M = 20$

obj	obj-1	obj-2	obj-3
Profit	25	24	15
weight	18	15	10

greedy about profit $\rightarrow m - 18 = 2$

	obj-1	obj-2	obj-3
Profit	1	$2/15$	0
Weight	1×25	$2/15 \times 24$	0
	$= 25 + 3.2$	$= 28.2$	

greedy about weight $\rightarrow m - 10 = 10$

	obj-1	obj-2	obj-3
Weight	0	$10/15$	1
Profit	0	$\frac{10}{15} \times 24$	$+ 1 \times 15$
	$= 16 + 15$	$= 31$	

greedy about both

$$\text{obj} - 1 \quad P/W = 25/18 = 1.4$$

$$\text{obj} - 2 \quad P/W = 24/15 = 1.6$$

$$\text{obj} - 3 \quad P/W = 15/10 = 1.5$$

$$\text{obj} - 2 > \text{obj} - 3 > \text{obj} - 1$$

$$1.6 > 1.5 > 1.4 \quad M - 15 = 5$$

$$1 \quad 5/10 \quad 0$$

$$24 \times 1 + 5/10 \times 15 + 0 = 31.5$$

Eg:- $n = 5, M = 12$

object	obj-1	obj-2	obj-3	obj-4	obj-5
Profit	5	2	2	4	5
weight	5	4	6	2	1

greedy about profit

	obj-1	obj-2	obj-3	obj-4	obj-5	$M - 6 = 6$
profit	1	1	0	1	1	$6 - 2 = 4$
weight	1×5	1×4	0	1×2	1×1	$4 - 4 = 0$
	$= 5 + 4 + 2 + 1 = 12$					

greedy about weight

	obj-1	obj-2	obj-3	obj-4	obj-5	$M - 1 = 11$
weight	1	1	0	1	1	$11 - 2 = 9$
profit	1×5	1×2		1×4	1×5	$9 - 4 = 5$
	$= 5 + 2 + 4 + 5$					
	$= 16$					

greedy about both

obj-1	P/W	=	5/5	=	1
obj-2	P/W	=	2/4	=	0.5
obj-3	P/W	=	2/6	=	0.3
obj-4	P/W	=	4/2	=	2
obj-5	P/W	=	5/1	=	5

$$M-1=11 \quad 11-2=9 \quad 9-5=4 \quad 4-4=0$$

obj-5 > obj-4 > obj-1 > obj-2 > obj-3

5 > 2 > 1 > 0.5 > 0.3

1 1 1 1 0

$$1 \times 5 + 1 \times 4 + 1 \times 5 + 1 \times 2 + 0$$

$$5 + 4 + 5 + 2 = 16$$

g:

$$n = 7$$

$$M = 15$$

object	0-1	0-2	0-3	0-4	0-5	0-6	0-7
Profit	10	5	15	7	6	18	3
weight	2	3	5	7	1	4	1

greedy about profit

$$6-2=4$$

$$11-5=6$$

$$M-4=11$$

	0-1	0-2	0-3	0-4	0-5	0-6	0-7
profit	1	0	1	4/7	0	1	0
weight	1x2	0	1x5	4/7x7	0	1x4	0
	2	5	4	4	15		

18
15
16
49

greedy about weight

	greedy	about	weight				
	$13-2=11$	$11-3=8$		$14-1=13$	$8-4=4$	$11-1=10$	
	0-1	0-2	0-3	0-4	0-5	0-6	0-7
Profit	1	1	$\frac{4}{5}$	0	1	1	1
weight	1×20	1×5	$\frac{4}{5} \times 15$	0	1×6	1×18	1×3
	$20 + 5 + 12 + 6 + 18 + 3$						
	$= 54$						

greedy about both

obj-1 $P/W = 10/2 = 5$

obj-2 $P/W = 5/3 = 1.6$

obj-3 $P/W = 15/5 = 3$

obj-4 $P/W = 7/7 = 1$

obj-5 $P/W = 6/1 = 6$

obj-6 $P/W = 18/4 = 4.5$

obj-7 $P/W = 3/1 = 3$

$M-1=11 \quad 11-2=9 \quad 9-4=5 \quad 5-5=0$

obj-5 > obj-1 > obj-6 > obj-3 > obj-7 > obj-2 > obj-4

$6 > 5 > 4.5 > 3 > 3 > 1.6 > 1$

$1 > 1 > 1 > 1 \quad 0 \quad 0 \quad 0$

$1 \times 6 + 1 \times 10 + 1 \times 18 + 1 \times 15 + 0$

$= 6 + 10 + 18 + 15 = 49$

$M-1=11 \quad 11-2=9 \quad 9-4=5 \quad 5-1=4$

obj-5 > obj-1 > obj-6 > obj-7 > obj-3 > obj-2 > obj-4

$6 > 5 > 4.5 > 3 > 3 > 1.6 > 1$

$1 \quad 1 \quad 1 > 1 \quad 4/5 > 0 > 0$

$1 \times 6 + 1 \times 10 + 1 \times 18 + 1 \times 3 + 4/5 \times 15$

$= 6 + 10 + 18 + 3 + 12 = 49$

Algorithm of greedy technique

i) Calculate the Profit/Weight (P/w) ratio for each object.

for ($i=1$ to n)

$$a[i] = P_i/W_i \Rightarrow O(n)$$

ii) Arrange the P/w ratio in descending order $\Rightarrow O(n \log n)$

iii) Take the object one by one from the descending array until capacity of Knapsack becomes 0.

while ($m \neq 0$)
{

$$M = M - W_i X_i$$

$$P = P + P_i X_i \Rightarrow O(n)$$

$$\begin{aligned} \therefore \text{Time Complexity} &= O(n) + O(n \log n) + O(n) \\ &= 2O(n) + O(n \log n) \\ &= O(n \log n) \end{aligned}$$

Minimum Cost Spanning Tree

Spanning Tree

$$G(V, E) = S(V, |V| - 1)$$

A connected sub graph (S) of a graph $G(V, E)$ is called as a spanning tree if and only if

- i) It should consist V vertex
- ii) It should consist $|V| - 1$ edges

Complete graph \Rightarrow no. of vertices = n^{n-2}