

Algorithms and Data Structures Using Java

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Recursion

- In Java, a method that calls itself is known as a recursive method. And, this process is known as recursion.
- A physical world example would be to place two parallel mirrors facing each other.
- Any object in between them would be reflected recursively.

Recursion

Any function which calls itself directly or indirectly is called Recursion and the corresponding function is call as recursive function.

- A recursive method solves a problem by calling a copy of itself to work on a smaller problem.
- It is important to ensure that the recursion terminates.
- Each time the function call itself with a slightly simple version of the original problem.
- Using recursion, certain problems can be solved quite easily.

E.g: Tower of Hanoi (TOH), Tree traversals, DFS of Graph etc.,

How it works?

```
public static void main(String[] args) {  
    ... ... ...  
    recurse() .....  
    ... ... ...  
}  
  
static void recurse() {  
    ... ... ...  
    recurse()<.....  
    ... ... ...  
}
```

The diagram illustrates the execution flow between the `main` method and the `recurse` method. A dashed box encloses the `main` method's body. An arrow points from the `recurse()` call in `main` to the `recurse()` method definition, labeled "Normal Method Call". Another arrow points from the `recurse()` method definition back to its own `recurse()` call, labeled "Recursive Call".

What is base condition in recursion?

- In the recursive program, the solution to the base case is provided and the solution of the bigger problem is expressed in terms of smaller problems.

```
int fact(int n)
{
    if (n <= 1) // base case
        return 1;
    else
        return n*fact(n-1);}
```

What is base condition in recursion?

- In the above example, base case for $n = 1$ is defined and larger value of number can be solved by converting to smaller one till base case is reached.

Why base condition ?

```
class A {  
    abc() {  
        abc(); // Recursive call to itself  
    }  
  
    main() {  
        abc(); // First call to abc() from main  
    }  
}
```

Direct Recursion

- Direct and indirect recursion in Java are two types of recursion where a function calls itself.
- Direct recursion occurs when a function directly calls itself.

Example: calculate the factorial of a number uses direct recursion:

```
public static int factorial(int n) {  
    if (n == 0) {  
        return 1;  
    } else {  
        return n * factorial(n - 1);  
    }  
}
```

Indirect Recursion

- Indirect recursion occurs when a function calls another function, which then calls the original function directly or indirectly.
- For example, the following two functions use indirect recursion to reverse a string:

Indirect Recursion

```
public static String reverse(String str)

{
    if (str.length() == 0) {
        return "";
    } else {
        return reverse(str.substring(1))+str.charAt(0);
    }
}

public static String reverseHelper(String str) {
    return reverse(str);
}
```

Memory Allocation

- When a function is called in Java, a stack frame is allocated on the stack.
- The stack frame is a region of memory that stores the local variables and parameters of the function. When the function returns, the stack frame is deallocated.
- In recursive functions, a new stack frame is allocated for each recursive call.
- This means that the memory usage of a recursive function can grow exponentially with the number of recursive calls.

Memory Allocation

To avoid this, it is important to design recursive functions carefully.

- One way to do this is to use a base case to stop the recursion as soon as possible. Another way to reduce memory usage is to use tail recursion.
- Tail recursion is a type of recursion where the recursive call is the last thing the function does.
- This means that the stack frame for the current recursive call can be deallocated before the stack frame for the previous recursive call is returned.

Memory Allocation:Recursive Functions

There are two types of recursive functions:

1. tail recursive function : recursive function in which recursive function call is the last executable statement.

```
void fun( int n ){
    if( n == 0 )
        return;
    printf("%4d", n);
    fun(n--);//rec function call
```

Memory Allocation:Recursive Functions

2.non-tail recursive function : recursive function in which recursive function call is not the last executable statement.

Example:

```
void fun( int n ){  
    if( n == 0 )  
        return;  
    fun(n--);//rec function call  
    printf("%4d", n);  
}
```

Memory Allocation: Recursive Functions

Here is an example of a recursive function that is

non-tail recursive:

```
public static int factorial(int n) {  
    if (n == 0) {  
        return 1;  
    } else {  
        return n * factorial(n - 1);  
    }  
}
```

Memory Allocation

- This function will allocate a new stack frame for each recursive call.
- Here is an example of a tail recursive function to calculate the factorial of a number:

```
public static int factorialTailRecursive(int n, int accumulator) {  
    if (n == 0) {  
        return accumulator;  
    } else {  
        return factorialTailRecursive(n - 1, n * accumulator);  
    }  
}
```

Memory Allocation

- Here are some tips for reducing memory usage in recursive functions:
 - Use a base case to stop the recursion as soon as possible.
 - Use tail recursion whenever possible.
 - Avoid using global variables in recursive functions.
 - Pass as few arguments to recursive functions as possible.
 - Use tail call optimization (TCO), if available on your compiler.

Pros: Recursion

- Elegance: Recursive functions can be very concise and elegant, especially for problems that can be naturally divided into subproblems.
- Expressiveness: Recursion can be used to express complex algorithms in a clear and concise way.
- Modularity: Recursive functions can be used to implement complex algorithms in a modular way, making them easier to understand and maintain.
- Efficiency: Tail recursive functions can be very efficient, and some compilers can optimize them to use the same stack frame for all recursive calls.

Cons: Recursion

- **Memory usage:** Recursive functions can use a lot of memory, especially if they are not tail recursive.
- **Complexity:** Recursive functions can be difficult to understand and debug, especially for complex problems.
- **Stack overflows:** Recursive functions can cause stack overflows if the recursion depth is too large.

Function complexity

- The function complexity during recursion depends on the following factors:
 - The number of recursive calls: The more times the function calls itself, the more complex the function will be.
 - The complexity of the recursive calls: The complexity of the recursive calls also contributes to the overall complexity of the function.
 - The complexity of the base case: The complexity of the base case is the complexity of the simplest form of the problem that can be solved directly.