

**Unit - V**

Roll No .....

**CS - 505****B.E. V Semester**

Examination, December 2013

**Theory of Computation****Time : Three Hours****Maximum Marks : 70**

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9. a) Show that travelling salesman problem is NP-complete.

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b) Write short notes on following (any two)

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i) NP hard Vs NP complete

ii) Vertex cover problem

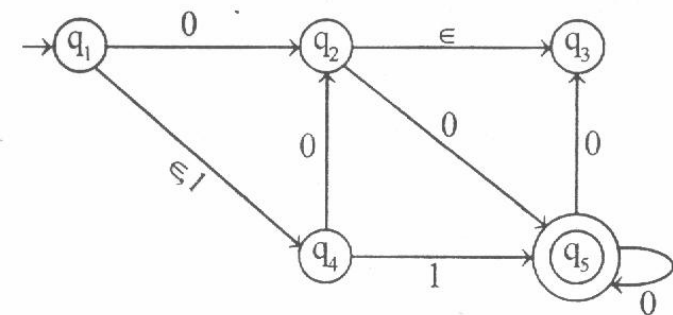
iii) Hamiltonian path problem

**Note:** Attempt one question from each unit. All questions carry equal marks.

**Unit - I**

1. a) Consider the FA below and construct the, smallest DFA which accepts the same language.

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b) Give mealy and Moore machines for the input from  $(0+1)^*$ , if the inputs ends in '000', output A; if the input ends in '111', output B; otherwise output C.

7

OR

2. a) Explain pumping lemma for regular sets. Prove by pumping lemma the following set is not regular.

$$L = \{W \in W^R / W \in (0+1)^*\} \quad 7$$

- b) Design a DFA that accepts the string such that number of zero divisible by five and number of one divisible by three.

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### Unit - II

3. a) Write the CFG for the following language 7

i)  $L = \{0^i 1^j 2^k / i = j \text{ or } j = k\}$

ii)  $L = \{0^n 1^n / n \geq 1\}$

- b) Convert the following grammar G into chomsky Normal Form. 7

$$S \rightarrow ABAC$$

$$A \rightarrow aA / \epsilon$$

$$B \rightarrow bB / \epsilon$$

$$C \rightarrow c$$

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OR

4. a) Convert the following grammar into GNF. 7

$$A_1 \rightarrow A_2 A_3$$

$$A_2 \rightarrow A_3 A_1 / b$$

$$A_3 \rightarrow A_1 A_2 / a$$

- b) Find regular grammars for the following languages on  $\{a, b\}$ . 7

i)  $L = \{w: n_a(w) \text{ and } n_b(w) \text{ are both even}\}$

ii)  $L = \{w: (n_a(w) - n_b(w)) \bmod 3 = 1\}$

### Unit - III

5. a) Design a PDA which accepts the language  $L = \{W \in (a, b)^* / W \text{ has the equal number of } a\text{'s and } b\text{'s}\}$ . 7

- b) Explain closure properties of CFL's. 7

OR

6. a) Design PDA corresponding to given CFG 7

$$S \rightarrow aSa$$

$$S \rightarrow bSb$$

$$S \rightarrow c$$

- b) Explain pumping lemma for CFL. Prove that following language is CFL or not? 7

$$L = \{a^n b^n c^n / n \geq 1\}$$

### Unit - IV

7. a) What do you mean by recursive language. Prove that complement of a recursive language is recursive. 7

- b) Build a Turing machine that accepts the language: 7

$$L = \{a^n b^{2^n}\}$$

OR

8. a) Design a turing machine to compute the function  $f(m, n) = m + n$  where  $m$  and  $n$  are non negative numbers. 7

- b) What do you mean by Turing machine. Explain multiple tapes Turing machine. 7