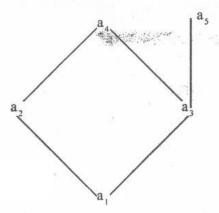
- 9. a) Solve the difference equation  $a_r 4a_{r-1} + 4a_{r-2} = 0$  and find the particular solution, given that  $a_0 = 1$  and  $a_1 = 6$ . 7
  - b) Define the following:
    - i) Complete lattice
- ii) Distributive lattice
- iii) Complemented lattice iv) Bounded lattice. 7

OR

- 10. a) Find the total solution of the recurrence relation:  $a_r-5a_{r-1}+6a_{r-2}=2^r+r$ ,  $r \ge 2$  with boundary condition  $a_0=1$  and  $a_1=1$ .
  - b) Consider the Hasse diagram of the Poset as shown in fig.



- i) Determine the least and greatest element of Poset, if they exist.
- ii) Determine L.V.B. of all pair of elements.
- iii) Determine G.L.B. of all pair of elements.

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## CS/IT - 302

## **B.E. III Semester**

Examination, December 2013

## Discrete Structure

Time: Three Hours

Maximum Marks: 70

Note: 1. Attempt all questions.

2. All questions carry equal marks.

1. a) Prove that:

i)  $A \times (B \cap C) = (A \times B) \cap (A \times C)$ 

ii) 
$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$
 7

b) Prove by mathematical induction:

$$1^{2}-2^{2}+3^{2}-\ldots + (-1)^{n+1}n^{2} = \frac{(-1)^{n+1}n(n+1)}{2}$$

OR

- a) Among 100 students, 32 study Maths, 20 study Physics, 45 study Biology, 15 study Maths and Biology, 7 study Maths and Physics, 10 study Physics and Biology and 30 do not study any of the three subjects.
  - i) Find the number of students studying all the three subjects.
  - ii) Find the number of students studying exactly one of the three subjects.

b) Show that the relation

 $R = \{(a,b) \mid a,b \in z \text{ and } a-b \text{ is divisible by 3}\}$ 

is on equivalence relation where z is set of all integer. 7

- 3. a) Define the following:
  - i) Semi group ii) Monoids iii) Sub group 7
  - b) Consider an algebraic system  $(\theta, *)$ , where  $\theta$  is the set of rational numbers and \* is a binary operation defined by  $a*b=a+b-ab \ \forall \ a,b \in \theta$

Determine whether  $(\theta, +)$  is a group.

a group.

OR

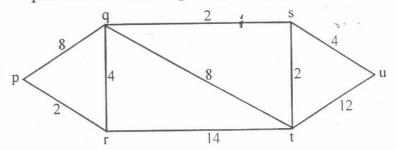
- 4. a) Consider a ring (R,+,\*) defined by a\*a = a. Determine whether the ring is commutative or not.
  - b) Define normal subgroup and show that the intersection of two normal subgroups of a group is a normal subgroup.
- 5. a) Show that the following propositions are tautologies.
  - i)  $(P \wedge Q) \vee (P \wedge \sim Q) \vee (\sim P \wedge Q) \vee (\sim P \wedge \sim Q)$
  - ii)  $\{(P \lor \sim Q) \land (\sim P \lor \sim P)\} \lor Q$
  - b) Show that the following language is not a finite state language:

$$L = \left\{ 1^{i} \ 0^{j} \ 1^{i+j} / i \ge 1, j \ge 1 \right\}$$

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OR

- 6. a) Prove that the following statement is logically equivalent  $(p \lor q) \lor r \equiv (p \lor r) \Rightarrow (q \lor r)$ .
  - b) Determine the negation of the following statements.
    - i)  $\exists_x \forall_y (p(x) \lor q(y))$
    - ii)  $\forall_x \exists_y (p(x,y) \rightarrow q(x,y))$
    - iii)  $\forall_x \forall_y (p(x) \land q(y))$
- 7. a) Using Dijkstra's algorithm find the shortest path between p to u in the following weighted graph:



- b) Define the following:
  - i) Eulerian path ii) Hamiltonian circuit.
    OR
- 8. a) Show that the maximum number of edges in a simple graph with n vertices is n(n-1)/2.
  - b) Draw the undirected graph for its incidence matrix given below.