

$$T(n) = 2T(n-1) + 1 - 0$$

$$T(n) = 2T(n-2) + 1$$

$$T(n) = 2T(n-2) + 1$$

$$T(n) = 2T(n-2) + 1 + 1$$

$$T(n) = 4T(n-2) + C1 + 2 - 2$$

$$T(n) = 4T(n-3) + 1 + 1 + 2$$

$$T(n) = 8T(n-3) + (1+2+4) - 3$$

$$T(n) = 8T(n-3) + (1+2+4) - 3$$

$$T(n) = 16T(n-4) + (1+2+4) + 9$$

$$T(n) = 2^{K}T(n-K) + (1+2+4+8) - 9$$

$$T(n) = 2^{K}T(n-K) + (1+2+4+8+-1) + (1+2+4+8+-1)$$

$$(Kdmes)$$

$$T(n) = 2^{n-1}T(1) + (1+2+4+8+-1)$$

$$S_{n} = \frac{\alpha(3^{n}-1)}{3^{n}-1} \qquad \alpha = 1, \ \beta = 2, \ n = n-1$$

$$T(n) = 2^{n} + \left(2^{n-1}-1\right) \qquad T(n) = 2^{n}-1 + \left(4^{n}-1\right)$$

$$T(n) = 2^{n} + 2^{n}-1 \qquad T(n) = 2(2^{n}-1)-1$$

$$T(n) = 2^{n}-1$$

$$T(n) = 0(2^{n})$$

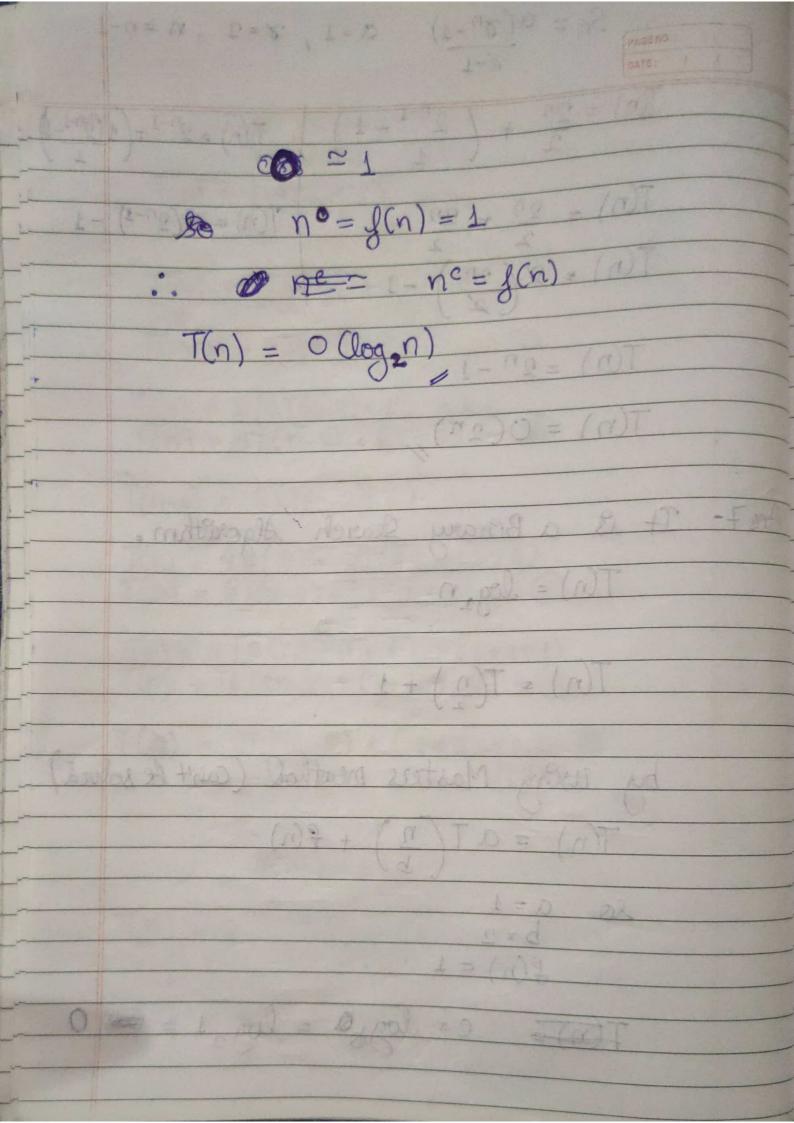
$$T(n) = \log_{2} n$$

$$T(n) = T(\frac{n}{2}) + 1$$

$$\log_{2} n \qquad \log_{2} n$$

$$T(n) = \alpha T(\frac{n}{b}) + \beta(n)$$

$$\log_{2} n = 1$$



Ans8- T(1) = 1 1. T(n) = T(n-1) +1 - 0 T(n) = T(n-2) + 2 - (2)T(n) = T(n-3) + 3 - 3 T(n) = T(n-R) + PR - (9)N-R=1 R=N-1T(n) = T(1) + n-1 T(n) = n $T(n) = O(n)_{ij}$ 2. T(n) = T(n-1) + n - 0 T(n-1) = T(n-2) + (n-1) - 8 + (n-1)T(n) = T(n-2) + (n + (n-1)) - 2T(n) = T(n-3) + (n+(n-1)+(n-2)) - 3T(n) = T(n-k) + (n + (n-1) + (n-2) - (n-k)T(n-k) = T(1)n = k+1k = n-1 T(n) = T(1) + (n+(n-1)+(n-2)---- (n-max-s) T(n) = 1 + (n + (n-1) + (n-2) + --- 1) $T(n) = 1 + h(n+3) = n^2 + 1 + 1$

$$T(n) = n^2 + 2$$

$$T(n) = O(n^2)$$

$$(4n88)$$
 $(4n83)$ $(7n) = T(n) + 1 - 0$

$$T(\underline{n}) = T(\underline{n}) + 1$$

$$T(\frac{n}{4}) = T(\frac{n}{8}) + 1$$

$$T(n) = T(\frac{n}{8}) + 8 - 3) + (2-n)T = (n)T$$

$$T(n) = T\left(\frac{n}{2K}\right) + K - \frac{1}{9}$$

$$\frac{9}{2^{k}} = \frac{1}{2}(10) + (1-0) + (1) + (1-0) + (1) + (1-0$$

$$QK = n$$

$$K = log_2 n$$

$$T(n) = T(1) + \log_2 n$$

Ans 8 $T(n) = 2T\left(\frac{n}{2}\right) + 1.$ (Ans 4) c = 1nc = n $n^{e} > J(n)$ T(n) = O(n)Ans 8 T(n) = 2T(n-1) + 1 $T(n) = O(2^n)$ Ans 8 (Ans 6)- T(n) = ST(n-1), T(0) = 1 T(n) = 3(T(n-1) - D) T(n-1) = 3T(n-2) T(n) = 9T(n-2) $T(n) = 3^3 T(n-3)$ $T(n) = 3^{\kappa}T(n-k)$ T(n) = 3nT(0)T(n) = 3n $T(n) = O(3^n)_{n}$

Ans 8

(Ans 7) -
$$T(n) = T(\sqrt{n}) + 1$$
 $T(n) = T(n^{1/2}) + 1$
 $T(n)$

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(8)- T(n)= T(VT)+n
Ans 8-
      T(Jn) = T (n/4) + Jn
      T(n) = T (n/4) + (n+vn)
     T(n) = T(n/8) + (n+vn+n/4)
     T(n) = T (n = R) + (n+n1/2+n1/4+--
          for n= 2
               \frac{1}{2R} = \frac{1}{2} \log(n)
                2K = \log(n)
            K = log (log (n))
         = 1 + (n + m + m)
                   GP a=n
v=In
                       No of terms = K
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 $J(n) = 1 + n \left(\left(\sqrt{n} \right)^{\log \log (n)} - 1 \right)$ $\log \log (n) - 1$ T(n) = n.loglog(n) & by neglecting T(n) = O(n log(log(n))) Int sum = 0, l;

for (l=0; i<n; l++)

sum += l; Ans 9 -0,1,2,-. n So T(n) = O(n), , & pace O(1) -O(N*(N,N-1, ---, 1)) O(N* (N+1)) (4.) O (N*N) $O\left(\frac{n}{2}*\left(\log_2 N\right)\right)$ O(nlogn),

Ans 12-(2) X will always be a better chorce for Ans 13- (4) O(log N) Ans 19- $T(n) = 7\left(\frac{T(n)}{(2)}\right) + (3n^2 + 2)$ $f(n) = 3n^2 + 2$ $C = \log_{b} \alpha = \log_{2} 7 = 2.807$ $10^{\circ} = 30^{2.8} \approx 0.3.8$ 30 $T(n) = O(n^{2})$ or (c) $O(n^{2} \cdot 8)$ (d) $O(n^{3})$ Ans $15 - f(n) = n^{\sqrt{n}}$ $f(n) = 2^n$ $f_3(n) = (1.000001)^n$ $f_4(n) = n (10 * 2)^n$ a) f2(n) > f4(n) > f3(n) > f3(n)

Ans $16 - f(n) = 2^{2n}$

 $\log J(n) = 2n \log_2 2$

log f(n) = 2n

J(n) = 2n.2n

N(2n)=

Ans $17 - T(n) = 2T(\frac{n}{2}) + n^2$

C = 1 $n^{c} = n$

 $n^2 > n$ $f(n) > n^c$

T(n) = 0 (n2) = (n) 02

Ansio- OCilog N)

Lite a G.C.D function
where n keeps on do ordaning
by 1/2]

Ans 19 -T(n)= O(N2+N)

T(n)= O(N2)