

# Telecommunication Networks

## 15B11EC611



# Time Division Switching

Till now, we discussed time division switches where an inlet or outlet corresponded to a single subscriber line with one speech sample appearing every 125  $\mu$ s on the line. Such switches are used in local exchanges.

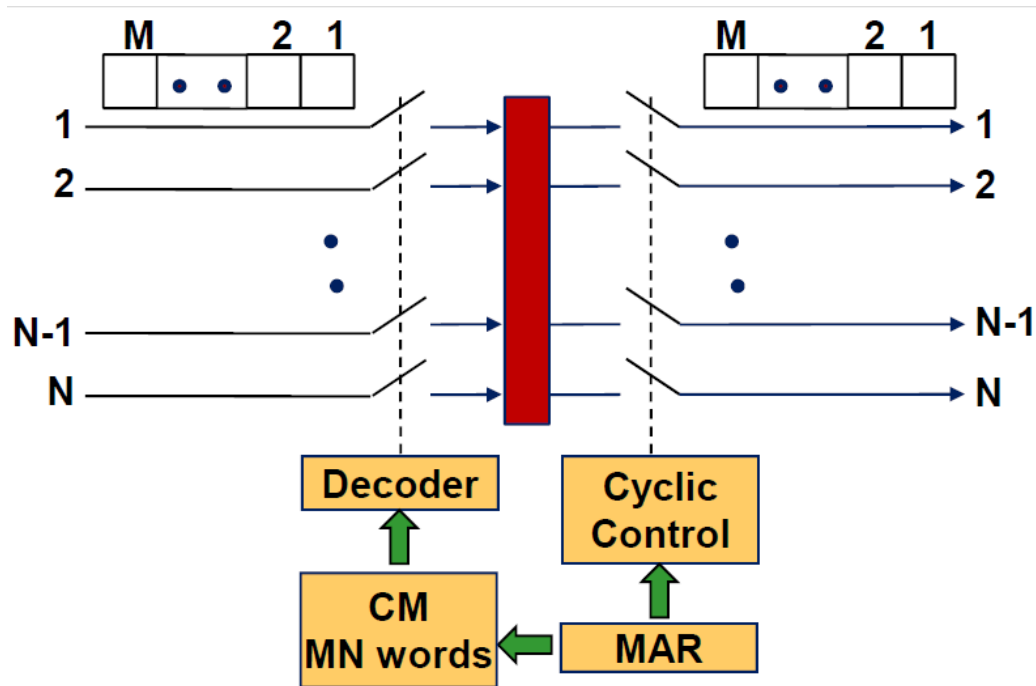
## ❖ Time multiplexed switches →

- Switches required in transit exchanges.
- Inlets and outlets are trunks which carry time division multiplexed data

## ❖ Time multiplexed switches:

1. Time multiplexed space switching
2. Time multiplexed time switching

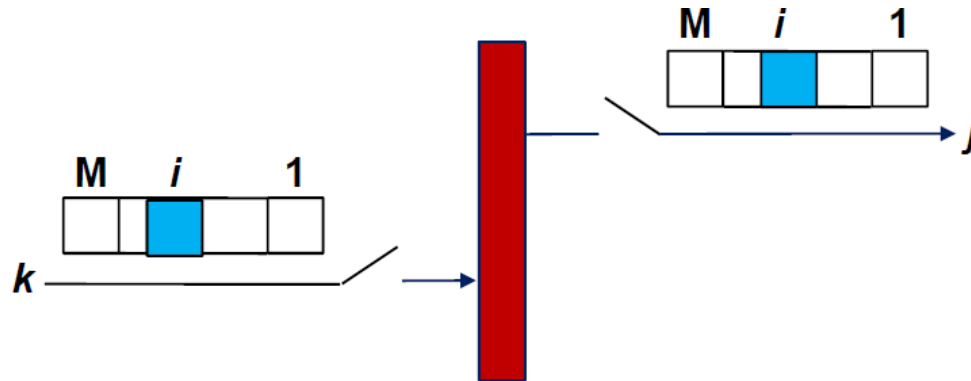
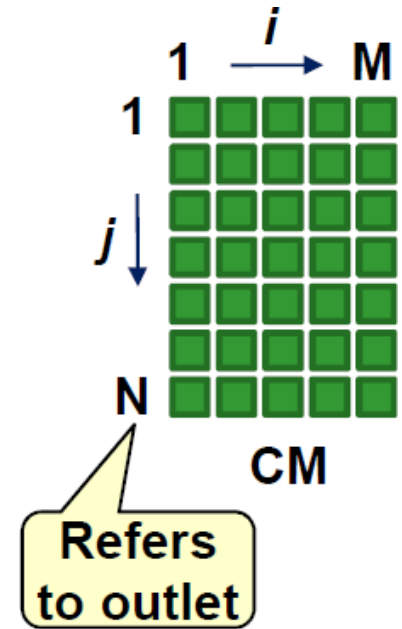
# Time Multiplexed Space Switching



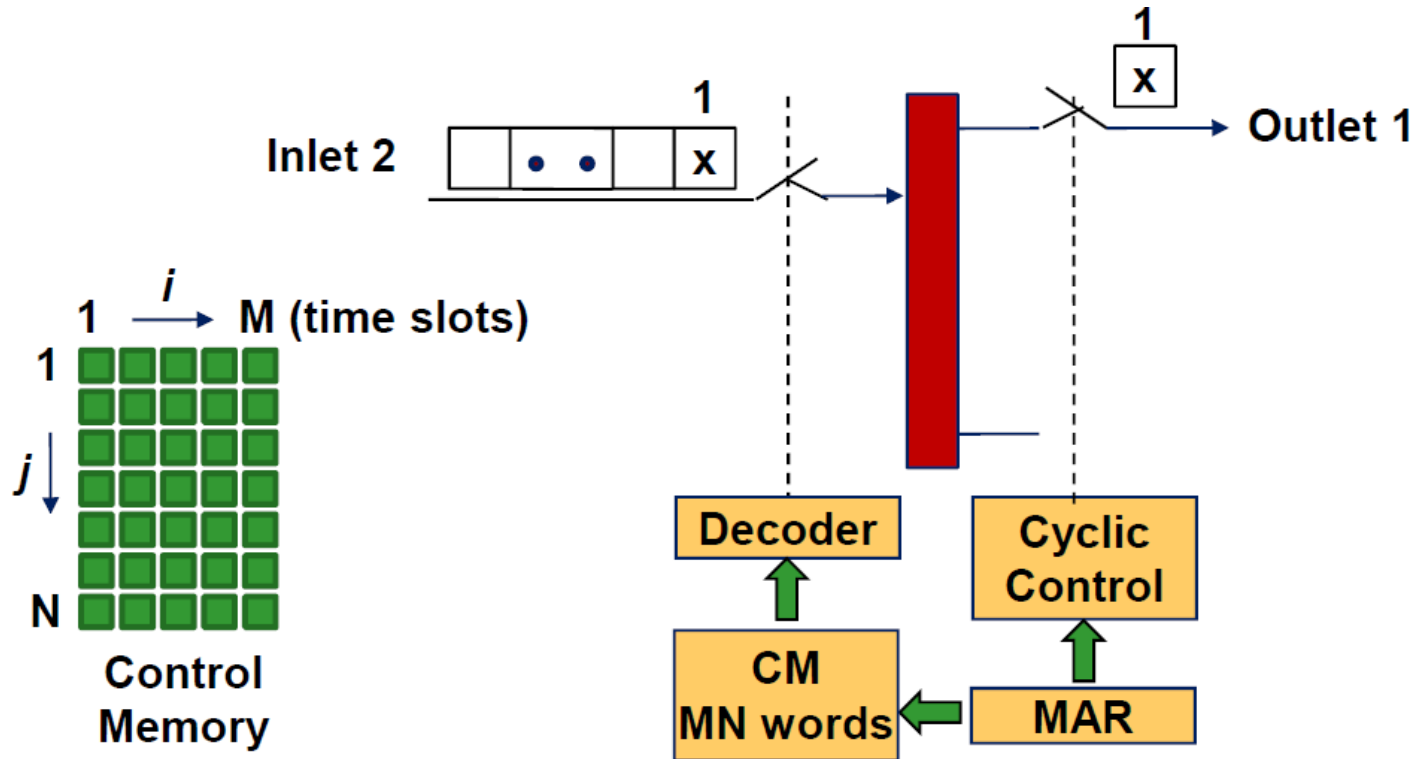
- Time multiplexed space switch has
  - N time-multiplexed trunks as inlets and outlets.
  - There are M time slots in a frame carrying PCM voice samples.
- Being a space switch, there is no time shift of voice samples.

# Time Multiplexed Space Switching

- CM has  $MN$  locations, one for each time slot.
  - A memory location is specified as  $(i, j)$ .
  - **Location  $(i, j)$  corresponds to time slot  $i$  of outlet  $j$ .**
  - Location  $(i, j)$  contains **address  $k$**  which corresponds to **inlet  $k$** .
- ✓ It implies that voice sample in  **$i$  th time slot** of inlet  $k$  will be switched to  **$i$  th time slot** of outlet  $j$ .



# Time Multiplexed Space Switching



- CM is read column-wise and from top to bottom.
- If (1, 1) location in CM contains 2,
  - 2<sup>nd</sup> inlet is connected to outlet 1 and 8-bit data (x) of time slot 1 of inlet 2 is switched to outlet 1 at the output.

# Time Multiplexed Space Switching

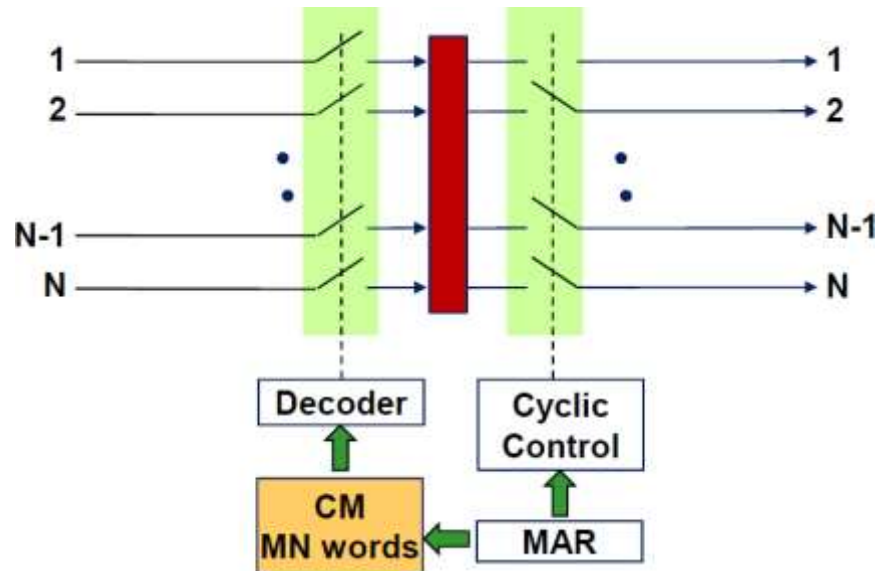
If  $t_s$  is the switching time,

**The number of trunks (N)** that can be supported by the switch is

$$N = 125 / (M t_s), \quad M = \text{time slots}$$

**The Switch cost C** can be estimated as

- $C = \text{Number of switches} + \text{Number of memory words}$
- $C = 2N + MN$



# Time Multiplexed Space Switching

## Example

Calculate the number of trunks that can be supported on a time multiplexed space switch, given that

- a) 32 channels are multiplexed in each stream,
- b) Control memory access time is 100 ns,
- c) Bus switching and data transfer time is 100 ns per transfer.

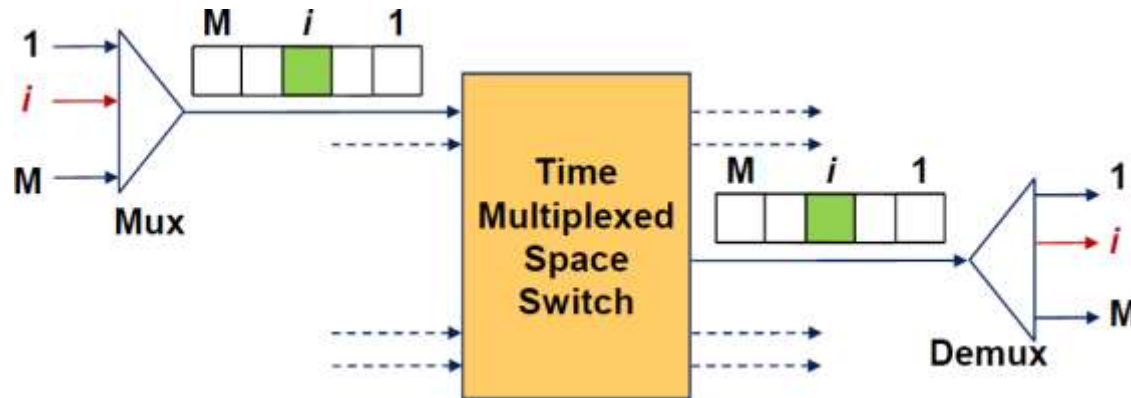
## Solution:

The total switching time  $t_s = 100 \text{ ns} + 100 \text{ ns} = 200 \text{ ns}$

$$N = 125 / (32 \times 200 \times 10^{-3}) = 19.53 \approx 20$$

# Time Multiplexed Space Switching

- Time multiplexed space switch **does not provide full availability** as it does not permit time-slot interchange (TSI).
- ***i* th** time slot of input trunk can only be switched as ***i* th** time slot of any output trunk.

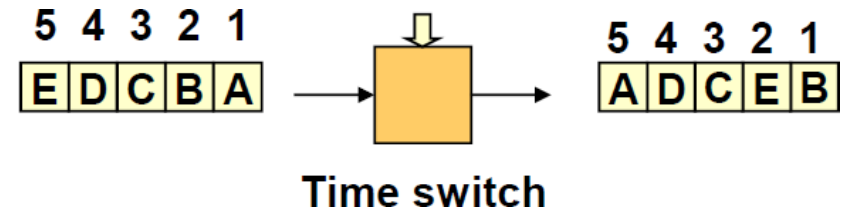


- Thus for any voice channel, there are only N possible time slots out of total MN time slots at the outlets.
- Rest  $MN - N = N(M - 1)$  outlets cannot be reached.



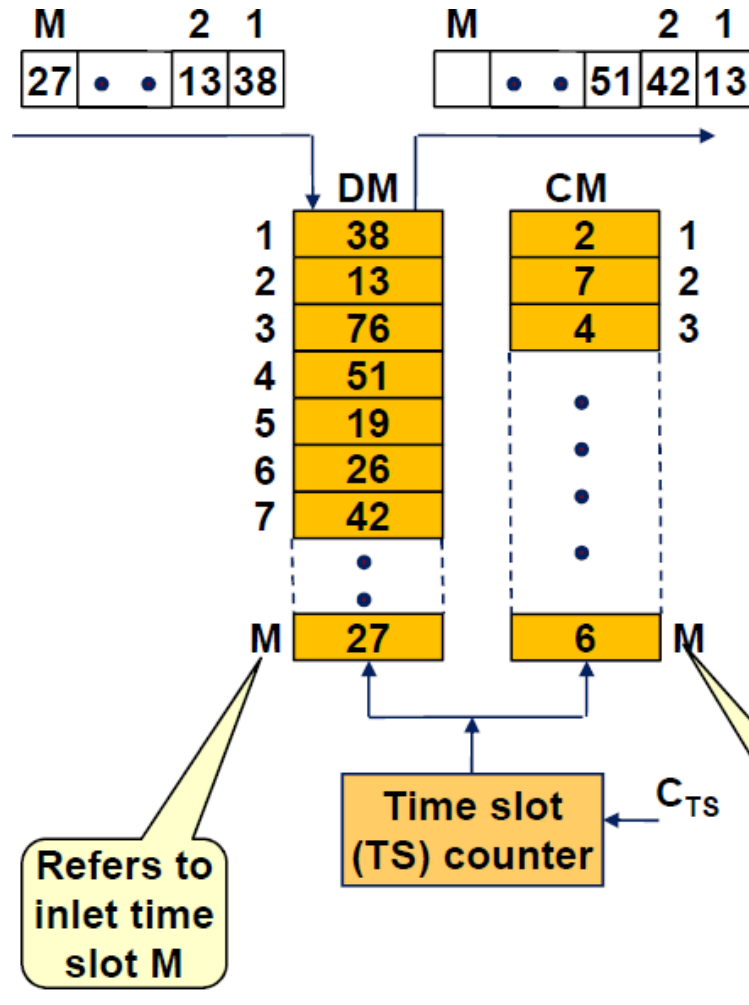
# Time Multiplexed Time Switching

- Time multiplex time switch is based on time slot interchange (TSI).
  - Speech sample of a time slot is switched to different time slot .



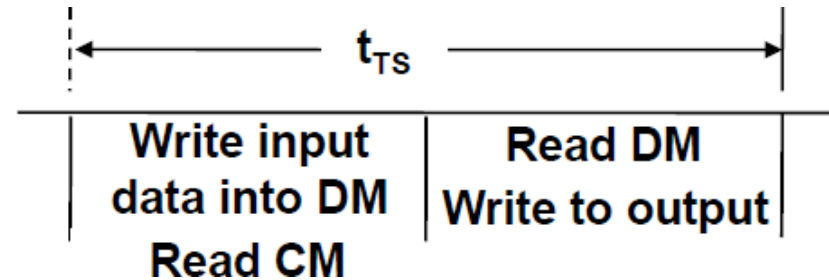
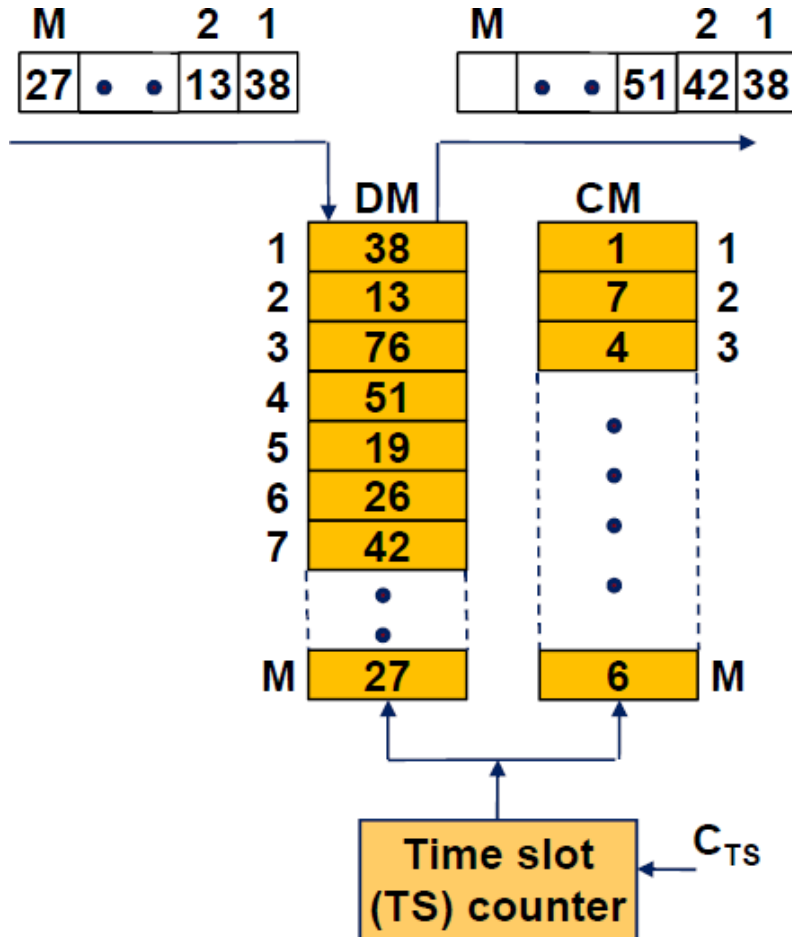
- Time switching necessarily involves **delay**.
  - A time multiplexed **frame must first be stored**.
  - Contents of its time slots can then be switched and transmitted.

# Time Multiplexed Time Switching



- Time slot counter runs at  $1/t_{TS}$  rate, where time slot  $t_{TS} = 125/M$
- DM contains voice data of time slots of the input in locations 1 to M.
- **CM contains addresses of the DM locations.** CM addresses 1 to M pertain to output time slots.
- DM and CM are simultaneously accessed on each Time Slot counter pulse.

# Time Multiplexed Time Switching



## Example

### • At time slot instance 2

1. Content (13) of time slot 2 of input is written into DM at location 2.
2. Location 2 of CM is read simultaneously. It gives the DM address 7.
3. DM location 7 is read and its content (42) is sent as output in TS 2.

There two sequential memory accesses per time slot.

$$t_{TS} = 2t_m$$

$$125 = 2Mt_m$$

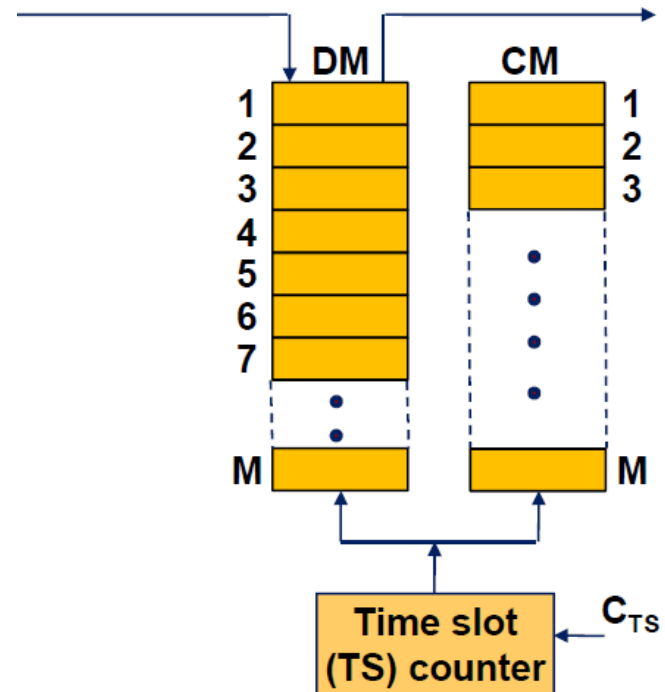
where  $t_m$  is memory access time in  $\mu s$ .

# Time Multiplexed Time Switching

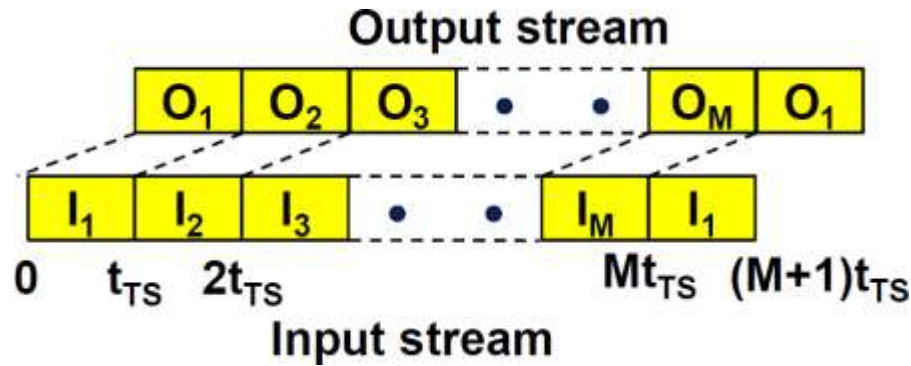
- Since there are no switching elements, switch cost  $C$  is based on memory locations.

$C = \text{Data memory locations} + \text{Control memory locations}$

$$C = M + M = 2M$$

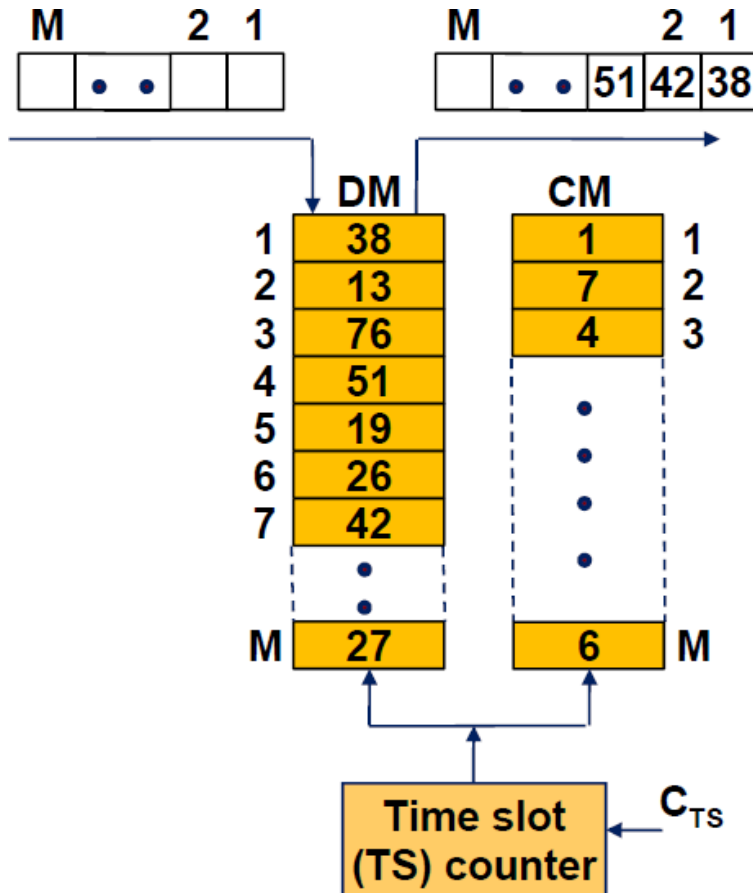


# Time Multiplexed Time Switching



- ❑ Time switch has inherent delay of one time slot.
  - All the 8 bits of a time slot become available at the end of the time slot.
  - Then these 8 bits are written into DM.
- ❑ The voice channels may have delay ranging from 1 to M time slots.
  - Delay depends on output time slot to which an input time slot content is switched.

# Time Multiplexed Time Switching



## Example

- ❑ 2nd location of CM contains 7.
- ❑ 7th location of DM has data 42 that was written during previous frame during 7th time slot.
- ❑ Delay =  $[M - 7 + 2 + 1]t_{TS}$   
= (M-4) Time slots
  - 2 is added as 42 is being read in 2nd timeslot of current frame.
  - 1 is added as there is delay of one TS between input and output streams.

In general, Delay = M - Inlet + Outlet + 1

**Example:** For a TSI switch with 1 trunk and 24 slots, working in sequential write/random read mode. Find out the delay in getting sample at outlet for following connections:

2 ----- 7 ,                      3 ----- 4 ,                      1 ----- 1

**Solution:**

Trunk , N = 1

Channel / Slots , M = 32

Time slot duration,  $t_{TS} = 125 \mu s / M =$

→ Inherent delay = 1  $t_{TS}$

→ For 2 - 7, Delay =  $[M - 2 + 7 + 1] t_{TS}$

→ For 3 - 4, Delay =  $[M - 3 + 4 + 1] t_{TS}$

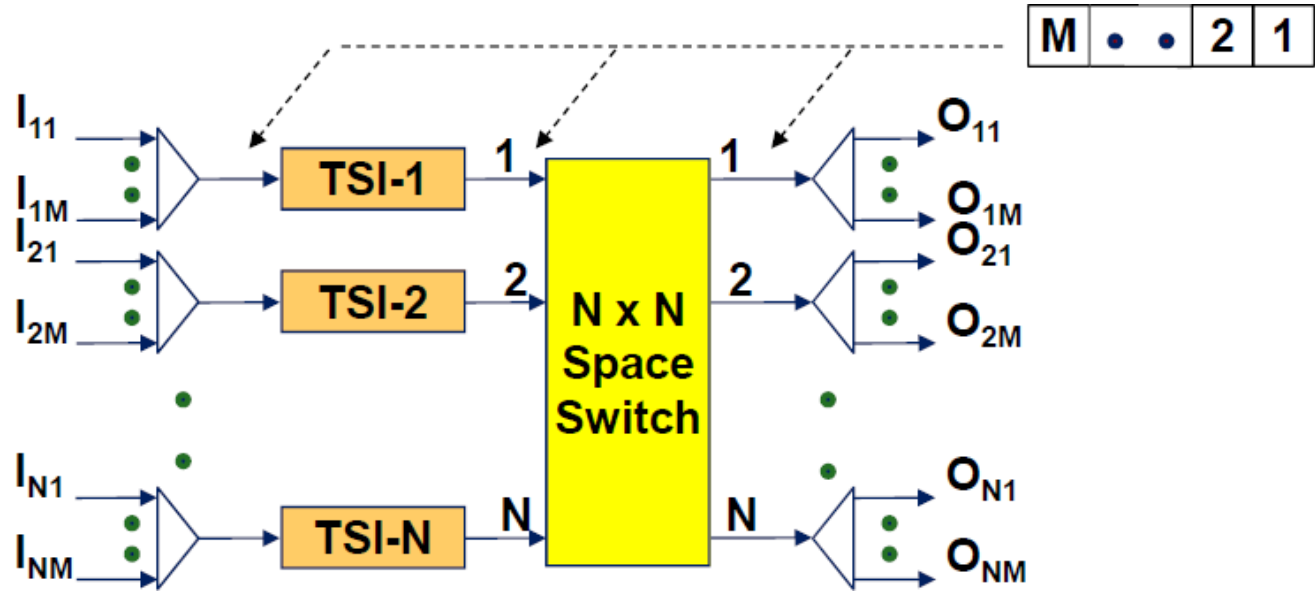
→ For 1 - 1, Delay = 1  $t_{TS}$

# Combination Switching

- ❑ Time multiplexed time division space switch does not provide full availability as it cannot do time slot interchange.
- ❑ Time multiplexed time division Time switch cannot switch time slot data across different trunks.
- ❖ A combination of time and space switches can achieve both time switching (i.e. time slot interchange) & space switching (i.e. Sample switching across trunks).
- A combination switch can be build using several stages of time and space switching.
  - 2 stage switch: TS (Time-Space)  
ST (Space-Time)
  - 3 stage switch: TST (Time-Space-Time)  
STS (Space-Time-Space)



# Time-Space Switch



- ❖ 1<sup>st</sup> Stage consists  $\rightarrow$  1 time slot interchanger per inlet
- ❖ 2<sup>nd</sup> Stage consists  $\rightarrow$  a  $N \times N$  space switch

□ Each time-multiplexed inlet/outlet carries M channels.

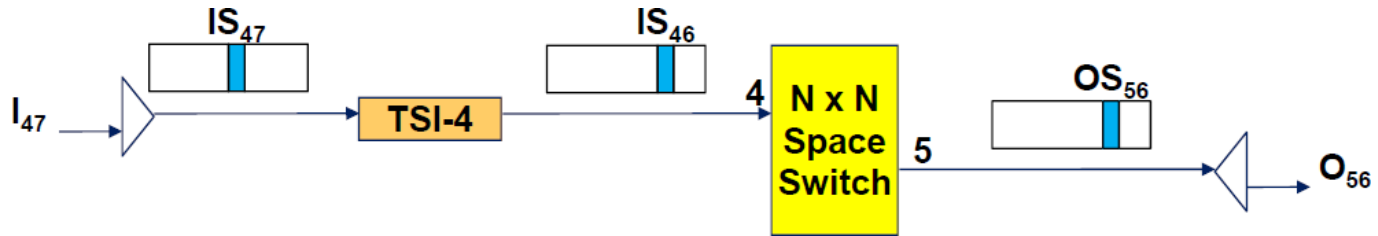
Notation for subscribers for input and output side

- $I_{47} \rightarrow$  A input subscriber assigned to line 4 (TSI-4) at time slot 7.
- $O_{56} \rightarrow$  A subscriber connected to the outlet 5 and time slot 6.

- ❖ The respective time slots are identified as  $IS_{47}$  and  $OS_{56}$ .

# Time-Space Switch

Suppose  $I_{47}$  is to be connected to  $O_{56}$ .



1. Data of time slot  $IS_{47}$  is moved to  $IS_{46}$  by  $TSI-4$ .
2. Data of time slot  $IS_{46}$  of inlet 4 is moved to  $OS_{56}$  of outlet 5 by the space switch.

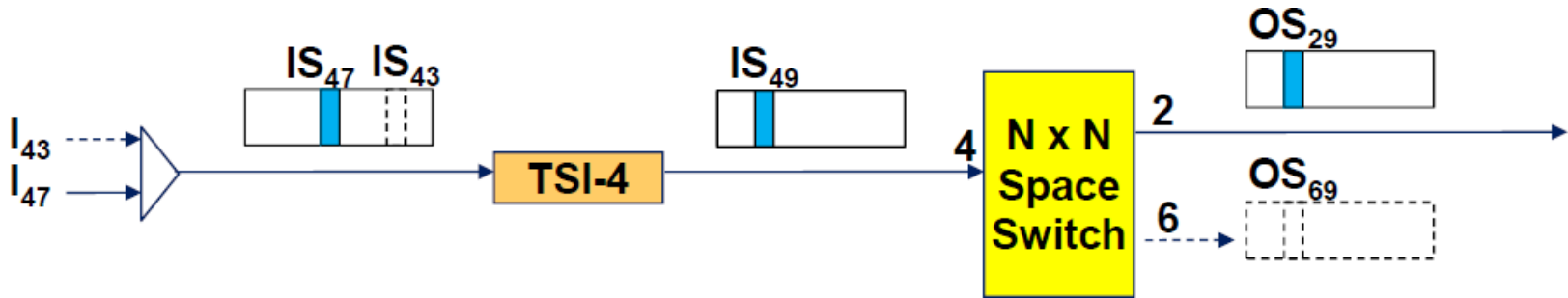
✓ Note that time slot location remains same '6' in space switch.

❖ Connection between  $I_{47}$  and  $O_{56}$  established.

**Note** that any inlet  $I_{xy}$  can be connected any outlet  $O_{mn}$ . Thus, 2-stage TS switch provides Full Availability.

# Time-Space Switch

- Consider that connection  $IS_{47} \rightarrow OS_{29}$  is already established.
  - Note that time slot location is '9' in outlet 2.

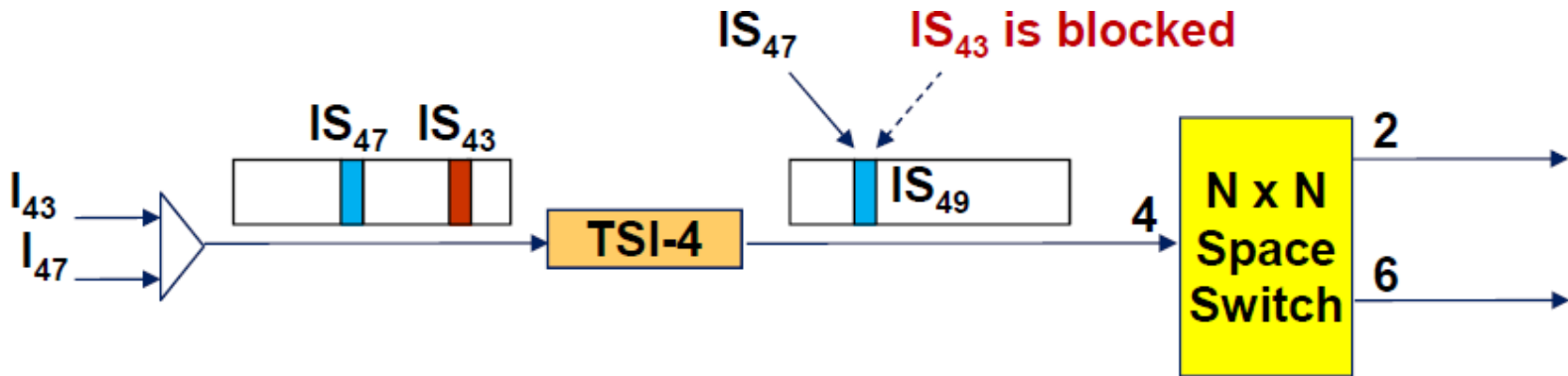


- ❑ There is request for another connection  $IS_{43} \rightarrow OS_{69}$ .

Note that time slot location required is '9' in outlet 6, a different outlet.

# Time-Space Switch

- ✓ For the new connection, TSI-4 needs to switch data of time slot  $IS_{43}$  to time slot  $IS_{49}$ .
- As  $IS_{49}$  is already engaged for  $IS_{47}$ , the new connection request  $IS_{43} \rightarrow OS_{69}$  will be blocked by the switch.

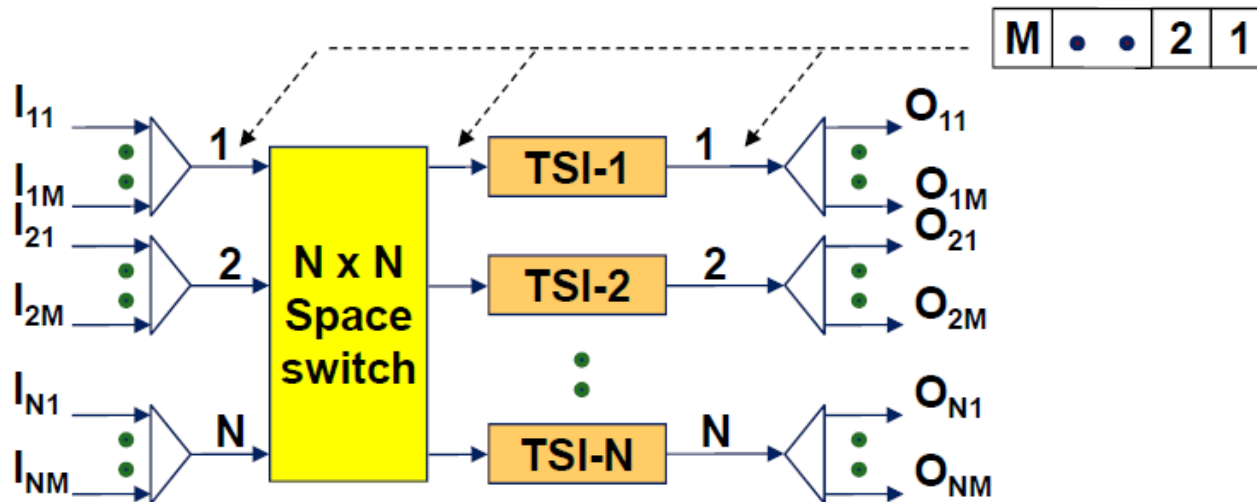


- This situation always occurs when two or more inlets of a time frame are to be connected to the same timeslot in different outlets.
- 2-stage TS switch provides Full availability but it is Blocking switch.

# **Space-Time Switch**

# Space-Time Switch

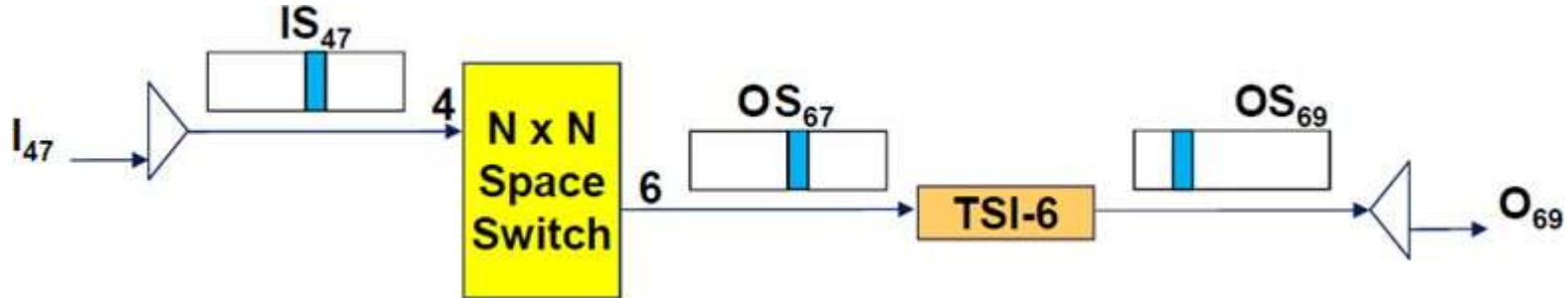
- Space switch has  $N$ -inlets/outlets each carrying time-multiplexed  $M$  channels.
- Each outlet of the space switch has TSI switch that interchanges the time-slot data.
- **Notation for inputs, outputs & time-slots is same as before.**



# Space-Time Switch

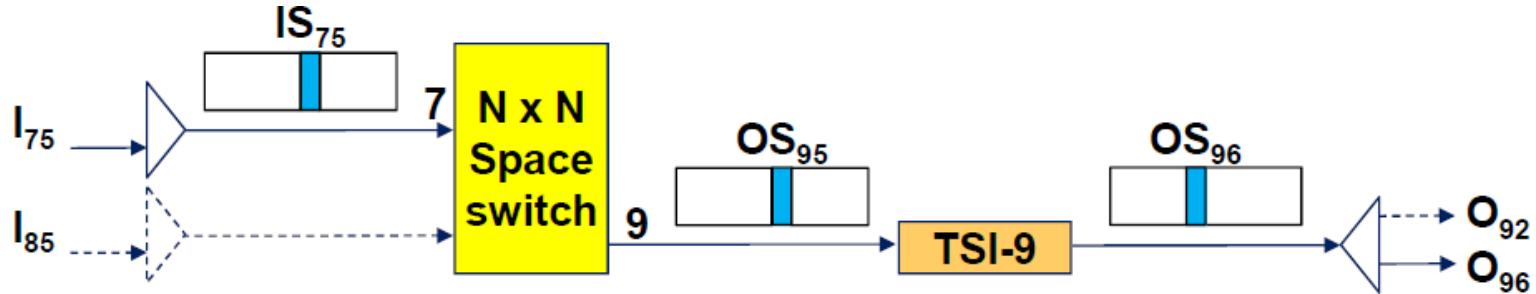
❖ Suppose  $I_{47}$  is to be connected to  $O_{69}$ .

1. Data of time slot  $IS_{47}$  is switched from inlet 4 to outlet 6.
  2. It is then switched to time slot 9 by TSI-6 and the connection is established.
- ✓ As in case of TS switch, this switch has Full Availability.

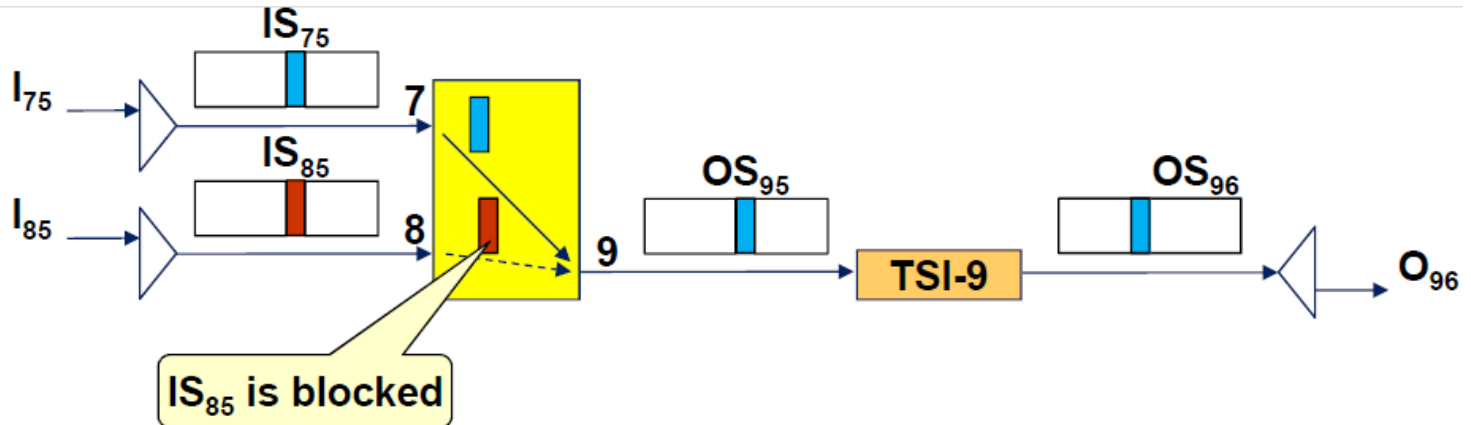


# Space-Time Switch

- Consider that connection  $IS_{75} \rightarrow OS_{96}$  is already established.
  - $IS_{75}$  is space switched as  $OS_{95}$ .
  - $OS_{95}$  is time switched as  $OS_{96}$ .
- There is request for another connection  $IS_{85} \rightarrow OS_{92}$ .



- $IS_{85}$  is to be space switched as  $OS_{95}$ .
- But  $OS_{95}$  is already engaged by the connection  $IS_{75} \rightarrow OS_{96}$ .
- The new connection request  $IS_{85} \rightarrow OS_{92}$  is blocked.



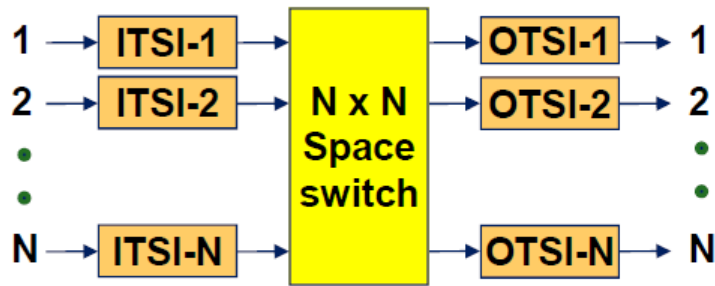
- ✓ ST switch has Full Availability but it is a Blocking switch.



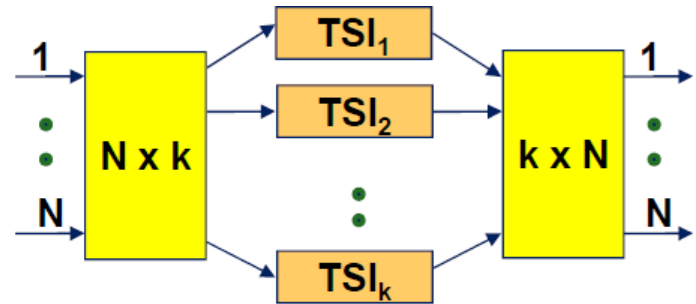
# **Three-Stage Combination Switching**

# Three-Stage Combination Switching

❖ 3-stage time and space combination switches are more flexible than 2-stage



Time-Space-Time (TST) Switch



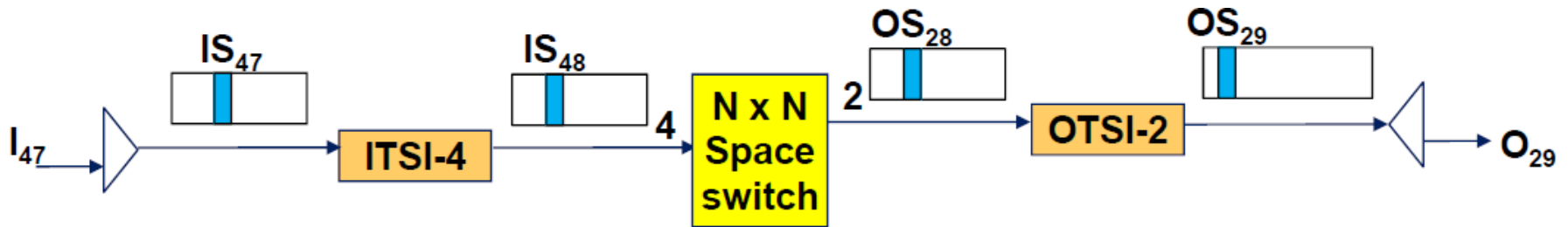
Space-Time-Space (STS) Switch

- 3-stage combination switch architecture has the two configurations:
  - Time-Space-Time (TST) switch.
  - Space-Time-Space (STS) switch.
- The middle switch introduces the flexibility of switching a incoming channel to
  - a free intermediate time slot (in case of TST)
  - A free intermediate outlet (in case of STS).
- Subsequently, the intermediate time slot/outlet is switched to the desired time slot/outlet.

# Time-Space-Time (TST) switch

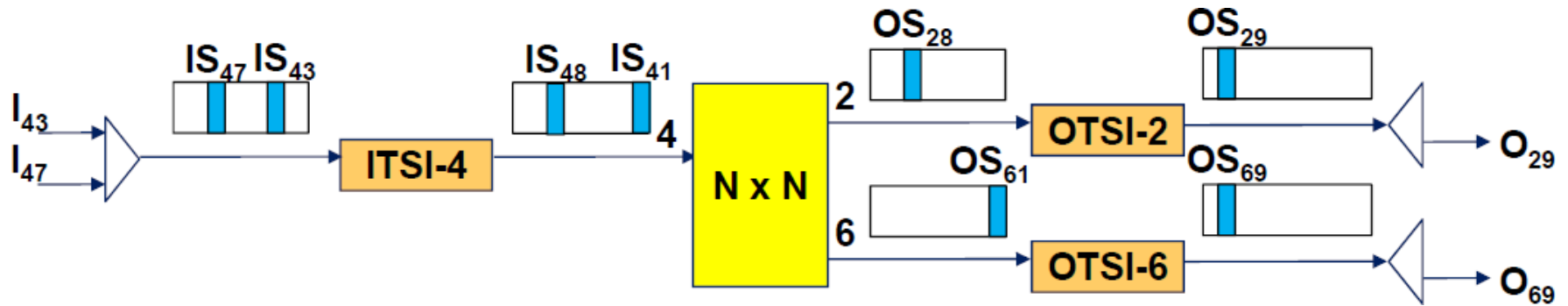
❖ Let us say there is request for connection  $I_{47} \rightarrow O_{29}$

- ITSI-4 switches the data of  $IS_{47}$  to a **free intermediate time slot**  $IS_{48}$  that has path through the space switch to outlet 2.
- Space switch switches time slot ( $IS_{48}$ ) data to outlet 2 ( $OS_{28}$ ).
- OTSI-2 switches the data of  $OS_{28}$  to the desired location  $OS_{29}$ .



- Let us say there is working connection  $I_{47} \rightarrow O_{29}$ . **There is request for another connection  $I_{43} \rightarrow O_{69}$ .**
- **2-stage TS switch will block this call** because intermediate time slot  $IS_{49}$  would be engaged by the first call.
  1.  $IS_{47} \rightarrow IS_{49} \rightarrow OS_{29}$
  2.  $IS_{43} \rightarrow IS_{49} \rightarrow OS_{69}$
- **3-stage TST does not block this call** as there are alternative intermediate time slots .

# Time-Space-Time (TST) switch



❖  $IS_{47} \rightarrow IS_{48} \rightarrow OS_{28} \rightarrow OS_{29}$

❖  $IS_{43} \rightarrow IS_{41} \rightarrow OS_{61} \rightarrow OS_{69}$

- ✓ So long as **alternative free intermediate time slot** that has path through the space switch is available, the next call will not be blocked.

# Blocking in (TST) switch

**For some specific situation, TST switch can be blocking.**

❖ Consider a situation:

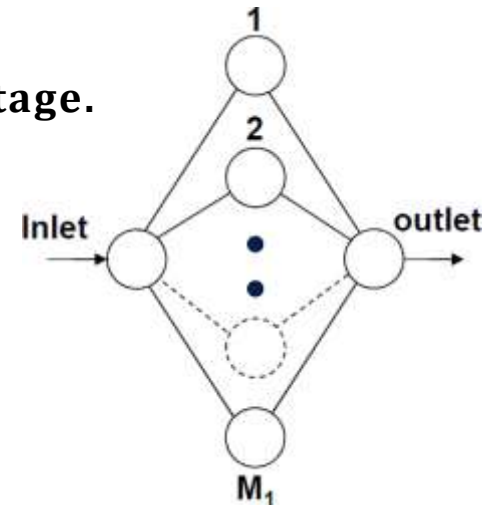
- (M-1) slots in an inlet  $I_j$  are all busy.
- Let traffic arrive in the  $M$ -th slot destined to a time slot outlet  $O_k$ .
- It is possible that during the time slot M, the outlet  $O_k$  is busy receiving some other output.
- As a result, blocking occurs.

❑ If this happens, we need one more additional slot to establish a connection.

❖ This means that we need a total of  $2M - 1$  time slots in the intermediate space stage.

# Blocking in (TST) switch

- In a functional sense, a TST switch is identical to a 3-stage space division network.
- An equivalent Lee's graph of TST switch is shown.
  - $M_1$  number of time slots of a frame in the middle stage.
- Recall that for blocking space switch blocking probability is
$$P_B = [1 - (1 - \alpha/k)^2]^s$$
- For non-blocking space switch,  $s = 2p - 1$ 
  - $p$  is number of inlets in input module.



## IN SIMILAR FASION

- The expression for the blocking probability of a TST switch is given by

$$P_B = (1 - (1 - \alpha/L)^2)^{M_1}$$

Where  $M_1$  = number of time slots on the output side of the TSI switch

$L$  = expansion or concentration factor =  $M_1 / M$

$\alpha$  = traffic intensity on an inlet

- ✓ Non blocking TST switch has frame size of  $M_1 = 2M - 1$  for the middle stage.

**Example:** A TST switch supports 32 trunks of 32 channels each. A time expansion/concentration factor of 2 and a single stage space switch are used. What is the blocking probability of the switch if the channel loading is 0.9E per channel?

**Solution:**

➤ the blocking probability of a TST switch is given by

$$P_B = (1 - (1 - \alpha/L)^2)^{M_1}$$

Where  **$M_1$  = number of time slots on the output side of the TSI switch**

**$L$  = expansion or concentration factor =  $M_1 / M$**

**$\alpha$  = traffic intensity on an inlet**

**Given,  $\alpha = 0.9$  E**

**$M = 32$**

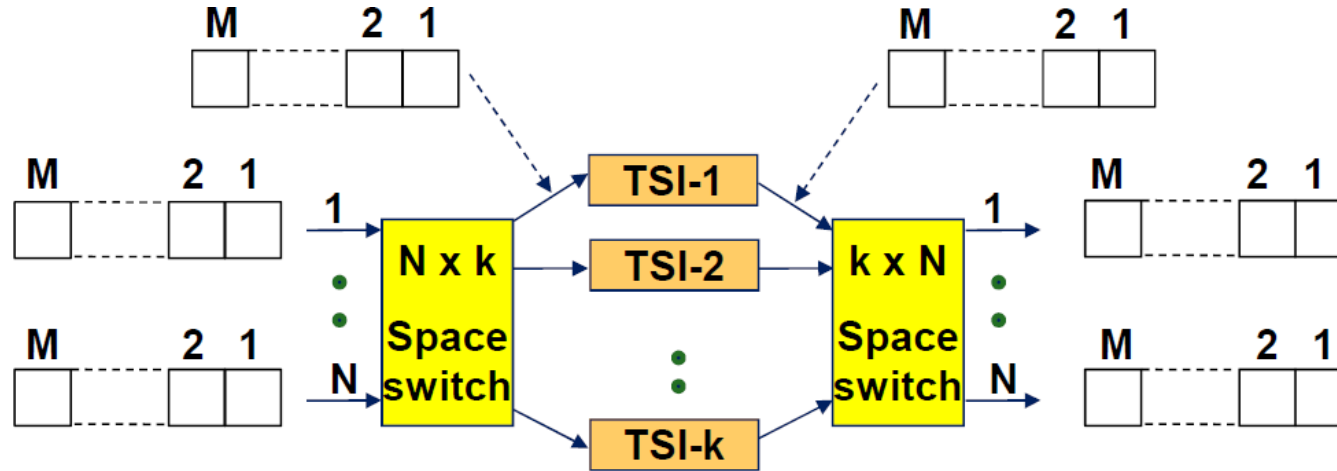
**$L = 2 = M_1 / M \rightarrow M_1 = 2 * 32 = 64$**

$$P_B = (1 - (1 - \alpha/L)^2)^{M_1}$$

$$P_B = (1 - (1 - 0.9/2)^2)^{64}$$

$$P_B = 9.7 \times 10^{-11}$$

# Space-Time-Space (STS) switch

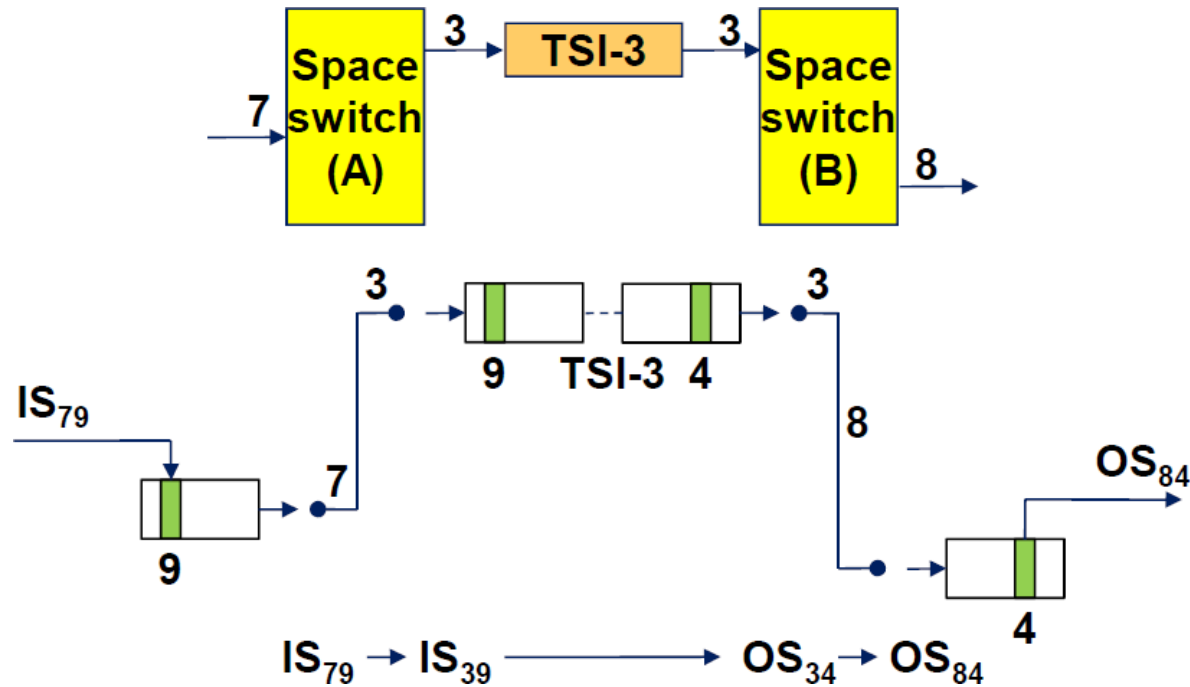


- A Space-Time-Space (STS) switch consists of-
- An  $N \times k$  space matrix at the input
  - $k$  TSI switches in middle
  - A  $k \times N$  space matrix at the output



# Space-Time-Space (STS) switch

For example, consider a connection  $I_{79} \rightarrow O_{84}$



- Space switch (A) switches data (x) of  $IS_{79}$  from 7th inlet to 3<sup>rd</sup> outlet. Time slot location within frame remains same (9).
- Time switch TSI-3 switches data (x) from time slot 9 to time slot 4.
- Space switch (B) switches data (x) from its 3<sup>rd</sup> inlet to its 8<sup>th</sup> outlet. Time slot location within frame remains same (4).

# Blocking in STS Switch

- For some specific situation, STS switch can be blocking.
- Blocking can be overcome by having expansion / compression (concentration) space switches.

✓ Blocking probability

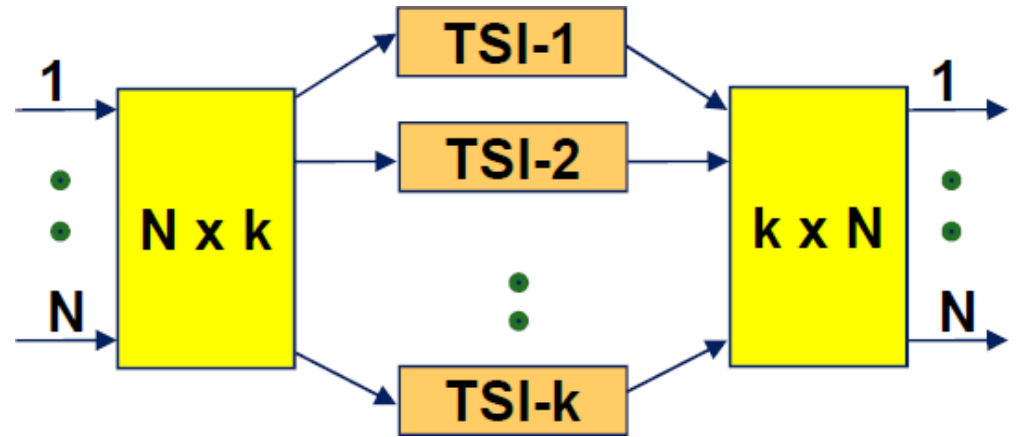
$$P_B = [1 - (1 - \alpha / L)^2]^k$$

where expansion factor  $L = k/N$

- ✓ It can be reasoned out that the **STS switch is non-blocking when**  
 **$k \geq (2N - 1)$ .**

# Cost Analysis

## Cost of STS switch



- Cost of a  $N \times k$  **space-switch** with  $MN$  memory locations

$$C_s = Nk + MN$$

Cost of 2 space-switches

$$2C_s = 2Nk + 2MN$$

- Cost of  $k$  **time-switches** is determined by memory required for  $MN$  data elements and  $MN$  addresses.

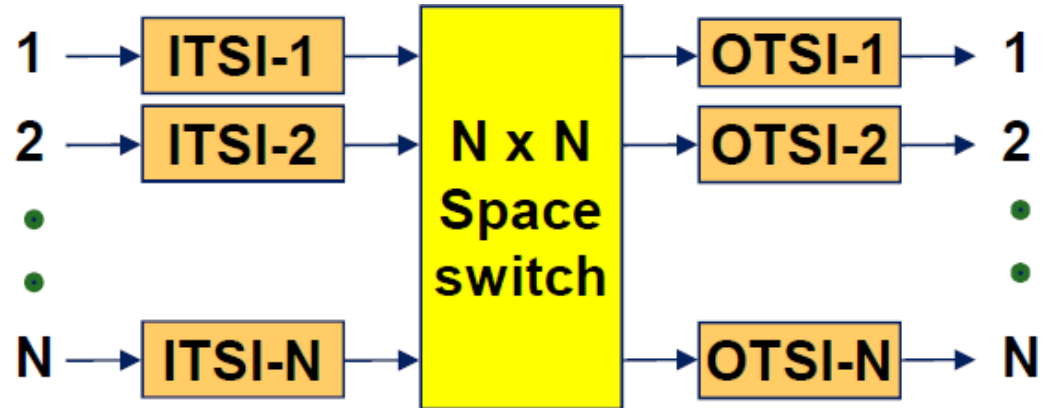
$$C_T = 2MN$$

- **Cost of STS switch**

$$C_{STS} = 2Nk + 4MN$$

# Cost Analysis

## Cost of TST switch



➤ Cost of  $N \times N$  space-switch with  $MN$  memory locations

- $C_s = N \times N + MN$

➤ Cost of  $2N$  time-switches

- $2CT = 2N \times 2M = 4MN$

➤ Cost of TST switch

- $C_{TST} = N^2 + 5MN$

# Cost Analysis

## □ For concentrating switches,

- $TST \rightarrow M_1 < M$
- $STS \rightarrow k < N$

- For  $M = k = N/2$ , we have

$$C_{STS} = 3N^2, \quad C_{TST} = 3.5N^2$$

- For symmetric switches,  $M = k = N$

$$C_{STS} = 6N^2, \quad C_{TST} = 6N^2$$

## □ For expanding switches,

- $TST \rightarrow M_1 > M$
- $STS \rightarrow k > N$ ,
- $M_1 = k = 2N$

$$C_{STS} = 12N^2, \quad C_{TST} = 11N^2$$

**Example:** A STS switch support 16 trunks and 16 channels each, and expansion factor of 2 is used. Calculate the blocking probability if the channel traffic intensity is 60 %.  
Also calculate the cost of switch.

**Solution:**

**Blocking probability**

$$P_B = [1 - (1 - \alpha / L)^2]^k$$

where expansion factor  $L = k/N$

**Given,  $N = 16$  trunks**

$$\alpha = 60 \% = 0.6$$

$$L = 2 = k/N \rightarrow k = L * N = 2 * 16 = 32$$

$$P_B = [1 - (1 - 0.6 / 2)^2]^{32}$$

$$P_B = 4.387 \times 10^{-10}$$

<b>Cost of STS switch,</b>	<b><math>C_{STS} = 12 * N^2</math></b>
	<b><math>C_{STS} = 12 * 16^2</math></b>
	<b><math>C_{STS} = 3072</math></b>

# **TST vs STS Switch**

- ✓ **TST switches have distinct advantages**
  - **TST switch is more cost effective than STS switch because time expansion is less costly than space expansion.**
  - **TST switch can handle larger volume of traffic.**
- ✓ **STS architecture is used for smaller switches.**

**THANK YOU**