

**15B11EC611**



# PERFORMANCE ISSUES

- **APPENDIX 7A PERFORMANCE ISSUES**
- **Kindly refer page numbers: 216 to 222 of the Book\_2\_Data-and-Computer-Communications-by-WilliamStallings (8<sup>th</sup> Edition) for detailed discussion.**

## Performance analysis over noisy channel

- Frame transmitted over a noisy channel may get corrupted/lost. Therefore it may require several retransmissions.

### Average number of transmissions of a frame

Probability that a bit is in error =  $p$

Probability that a bit is not in error =  $1-p$

Probability that all the  $L$  bits are not in error =  $(1-p)^L$

Probability ( $P_f$ ) of one/more errors in a frame =  $1 - (1-p)^L$

Probability that  $(i-1)$  frames are received with one/more errors  
 $= P_f^{i-1}$

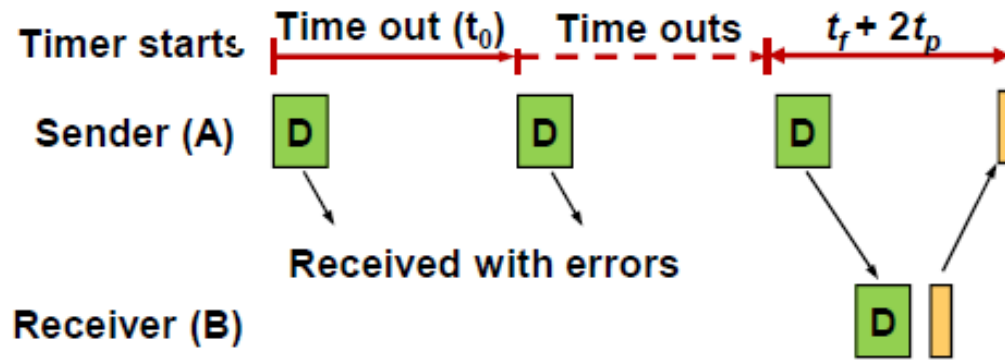
Probability that  $i^{\text{th}}$  frame is without errors =  $P_f^{i-1}(1 - P_f)$

**Average number of transmissions of a frame**

$$N_r = \sum_{i=1}^{\infty} i P_f^{i-1} (1 - P_f) = \frac{1}{1 - P_f} = \frac{1}{(1 - p)^L}$$

$$\text{Note } \sum_{i=1}^{\infty} (iX^{i-1}) = \frac{1}{(1-X)^2} \text{ where } -1 < X < 1$$

# Link Utilization in Stop-and-Wait protocol



Number of transmissions required for a frame  $= N_r$

Time out interval  $= t_0$

Time required for sending a frame correctly  $= (N_r - 1) t_0 + t_f + 2t_p$

Minimum value of  $t_0$   $= (t_f + 2t_p)$

Min. time for transmission of a frame correctly  $= N_r (t_f + 2t_p)$

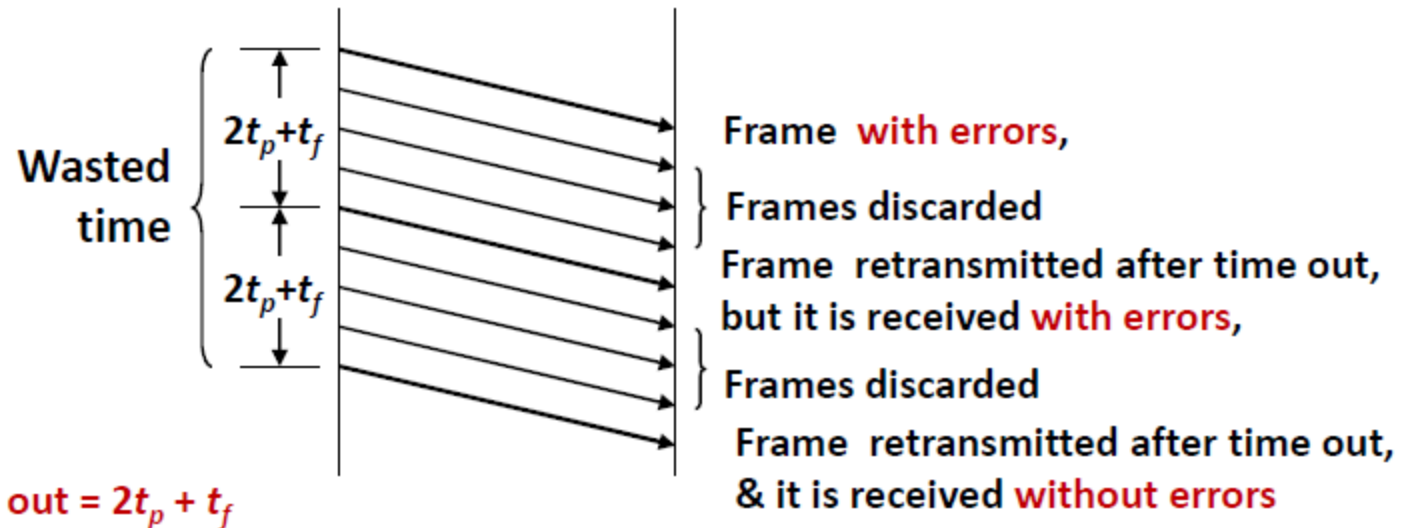
Link utilization

$$U = \frac{t_f}{N_r (t_f + 2t_p)} = \frac{1 - P_f}{1 + 2A}$$

$$N_r = \sum_0^{\infty} i P_f^{i-1} (1 - P_f) = \frac{1}{1 - P_f} = \frac{1}{(1 - p)^L}$$

# Link Utilization in Sliding Window: Go-back-N

## Case (1) $W \geq 1+2A$



Transmissions required for one frame =  $N_r = 1/(1 - P_f)$

Time wasted in retransmissions =  $(N_r - 1)(t_f + 2t_p)$

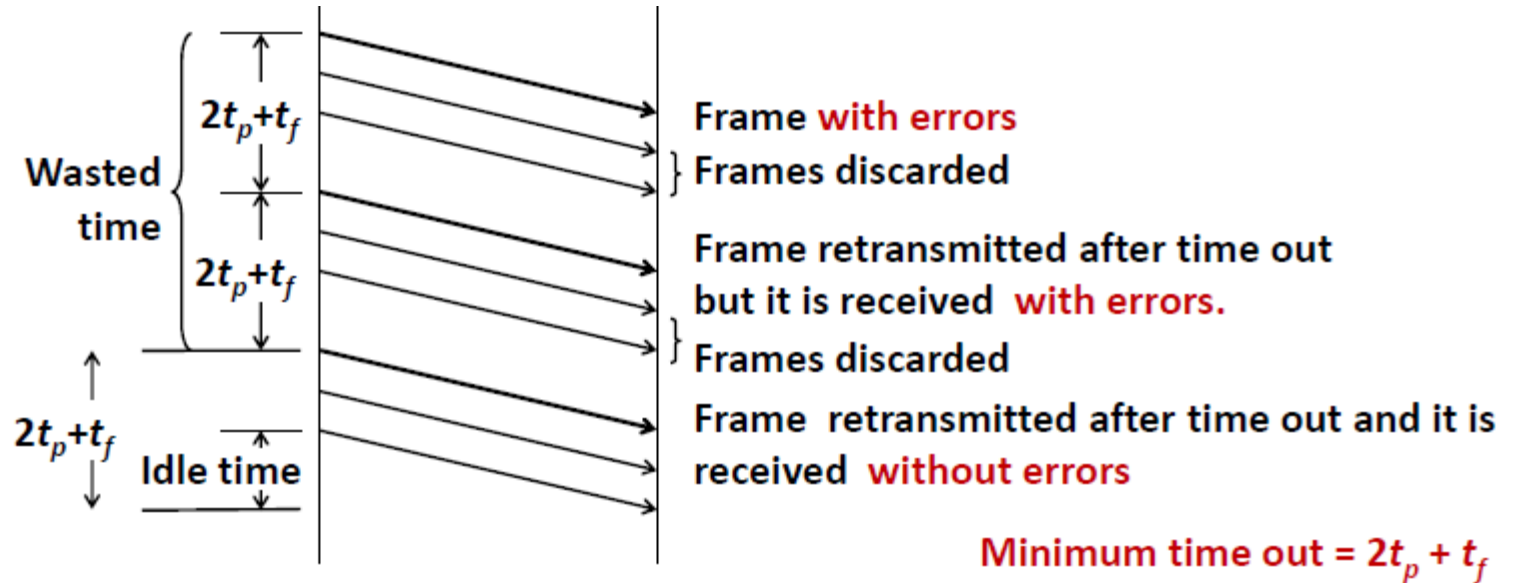
Link time effectively utilized =  $t_f$

Link utilization efficiency

$$\begin{aligned}
 U &= t_f / [t_f + (N_r - 1)(t_f + 2t_p)] \\
 &= 1 / [1 + (N_r - 1)(2A + 1)] \\
 &= (1 - P_f) / [(1 - P_f) + P_f(2A + 1)] \\
 &= (1 - P_f) / (1 + 2P_f A)
 \end{aligned}$$

# Link Utilization in Sliding Window: Go-back-N

## Case (2) $W < 1+2A$



When a frame is received correctly, frames sent in  $(t_f + 2t_p) = W$

Average link engagement time per frame  $= (t_f + 2t_p) / W$

Time wasted in retransmissions  $= (N_r - 1)(t_f + 2t_p)$

Link utilization efficiency  $= t_f / [(N_r - 1)(t_f + 2t_p) + (t_f + 2t_p) / W]$   
 $= W / [(2A + 1)(1 + W(N_r - 1))]$   
 $= W(1 - P_f) / [(2A + 1)(1 - P_f + WP_f)]$

# Link Utilization in Sliding Window: Selective-reject

## Case (1) $W \geq 1+2A$

- Sender receives acknowledgement before it exhausts its window i.e. when  $W \geq 1+2A$ .
  - Channel is continuously occupied before arrival of acknowledgement.

Frames transmitted during  $(t_f + 2t_p)$   $= (t_f + 2t_p)/t_f$

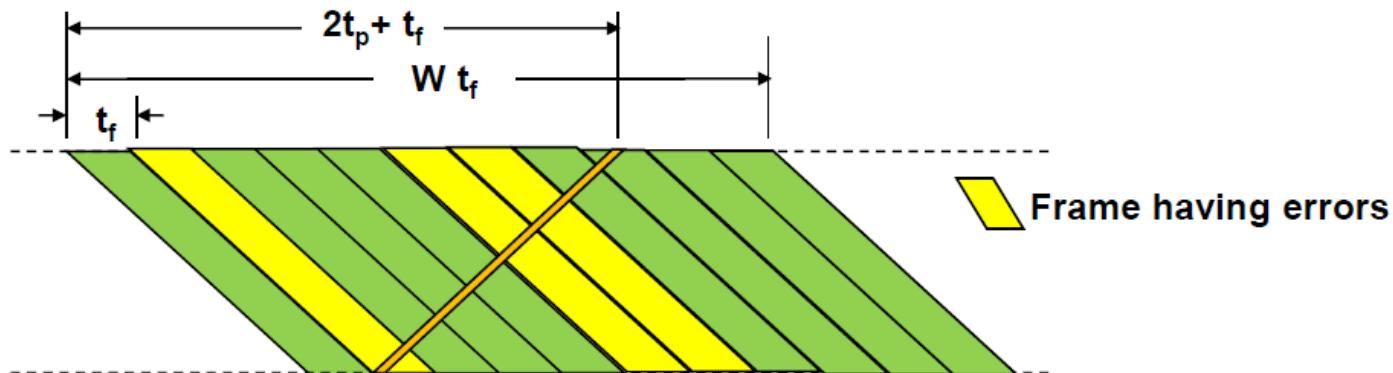
Frames received with errors  $= P_f(t_f + 2t_p)/t_f$

Link time wasted  $= t_f P_f(t_f + 2t_p)/t_f = P_f(t_f + 2t_p)$

Link time effectively utilized  $= (t_f + 2t_p) - P_f(t_f + 2t_p)$

Link utilization efficiency  $U = (t_f + 2t_p) - P_f(t_f + 2t_p)/(t_f + 2t_p)$

$$= 1 - P_f$$



# Link Utilization in Sliding Window: Selective-reject

## Case (2) $W < 1 + 2A$

- Sender exhausts its window before it receives an acknowledgement i.e.  $W < 1 + 2A$ .
  - Channel is idle after window is exhausted.

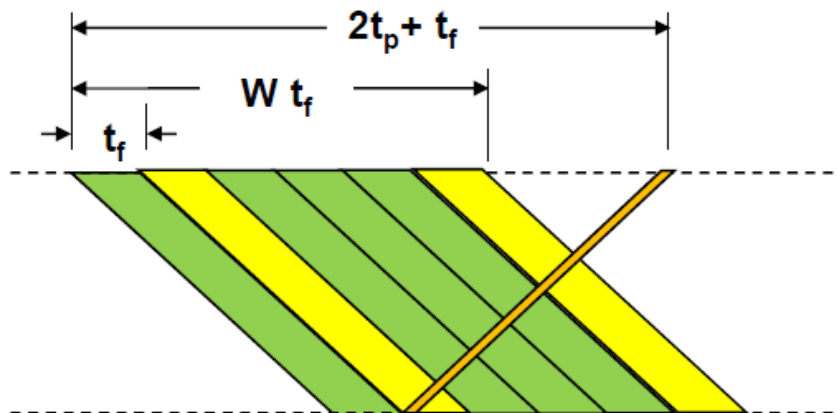
Frames transmitted during  $(t_f + 2t_p)$   $= W$


Frames received with errors  $= P_f W$

Link time wasted  $= t_f P_f W$

Link time effectively utilized  $= W t_f - t_f P_f W$

Link utilization efficiency  $U$   $= (W t_f - t_f P_f W) / (t_f + 2t_p)$   
 $= W(1 - P_f) / (1 + 2A)$



 Frame having errors



## Link utilization efficiency (U) – No errors / Noiseless channel

Stop-and- Wait,  $U = t_f / (t_f + 2t_p) = 1/(1+2A)$       where  $A = t_p / t_f$

Sliding-window      
$$U = \begin{cases} W/2A+1 & W < 2A+1 \\ 1 & W \geq 2A+1 \end{cases}$$

## Link utilization efficiency (U) – With errors / Noisy channel

Stop-and- Wait,  $U = (1-P)/(1+2A)$

Sliding-window – Selective Reject      
$$U = \begin{cases} W(1-P)/2A+1 & W < 2A+1 \\ 1-P & W \geq 2A+1 \end{cases}$$

Sliding-window – Go-back-N      
$$U = \begin{cases} W(1-P)/(2A+1)(1-P+WP) & W < 2A+1 \\ (1-P)/(1+2AP) & W \geq 2A+1 \end{cases}$$

**THANK YOU**