

ML:

# Hypothesis Testing:-

To test a claim about the value of a Parameter

## ① Null Hypothesis

- \* always contains the equal sign.

e.g greater than or equal to K

~~$H_0: \mu \geq K$~~

$$H_0: \mu \geq K$$

## ② Alternative Hypothesis

- \* alternative of  $H_0$
- \* contains only inequality

e.g company admission mean of its furnace is more than 18 yrs

$$H_0: \mu \leq 18$$

$$H_a: \mu > 18$$

## # Types of error:

|              | $H_0$ is True | $H_0$ is false |
|--------------|---------------|----------------|
| Accept $H_0$ | CORR decision | Type 2 error   |
| Reject $H_0$ | Type 1 error  | CORR decision  |

$\alpha$  = Prob of committing Type 1 error  
= significance level.

$\beta$  = Prob of comm of Type 2 error..

## # Steps for Testing a Hypothesis: using P-value for Z-Test

① Find out Z.

$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

cond: normal distr  
or  $n \geq 30$ .

② state the Null & Alternative hypothesis mathematically.

$H_a:$

$H_0:$



③ specify level of significance  
identify  $\alpha$

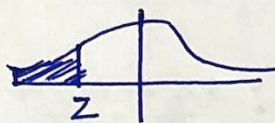
④ Find out the standardised test statistic: find  $Z$

$$Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$$

⑤ Draw the distribution and mark  $Z$ .

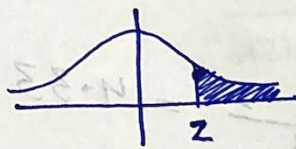
⑥ Find the P-value.

(1) For left tailed test



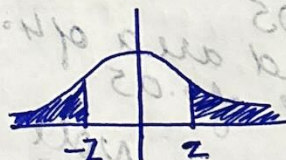
$P = \text{Area in left Tail}$   
 $= \text{value at } Z \text{ from Normal Table}$

(2) For Right Tailed:



$P = \text{Area in right Tail}$   
 $= 1 - N(Z)$

(3) Two Tailed Test



$P = \text{Area of shaded region.}$

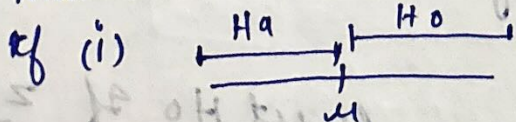
⑦ Make a decision:

if  $P \leq \alpha$  Reject  $H_0$

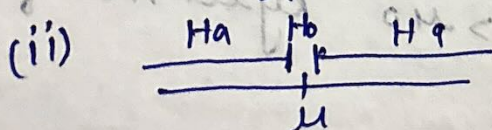
if  $P > \alpha$  Fail to Reject  $H_0$ .

⑧ Interpret the decision.

IMP: Map  $H_0$  &  $H_a$  on a line



left tailed



Two-tailed  
[when equality is given]



# Finding Critical Values (z values) [6 - in knowers]

- ① specify the  $\alpha$  value
- ② determine whether the test is left, right or 2 tailed
- ③ For:
  - (i) left tailed = z value corresponding to  $\alpha$
  - (ii) Right tailed = z value corr to  $1 - \alpha$ .
  - (iii) Two-tailed = z values corr to  $\frac{1}{2}\alpha$  &  $1 - \frac{1}{2}\alpha$
- ④ sketch the distribution.

Question: claim:  $\mu = 22$ .

$$H_0: \mu = 22$$

$$H_a: \mu \neq 22$$

$$N = 121$$

$$\bar{x} = 23.3$$

$$s = 3.3$$

$$Z = \frac{23.3 - 22}{\frac{3.3}{\sqrt{121}}} = 4.33$$

Note: Here  $\alpha = 0.05$   
 so I couldn't find area of 4.33  
 so I find z value of 0.05  
 = 1.65

$$\text{Now } Z > 1.65$$

Reject  $H_0$ .

Note: During this process for Right Tailed Test take z as +ve

Decision Criteria:

① Two Tailed: Reject  $H_0$  if  $Z > Z_{\alpha/2}$  or  $Z < -Z_{\alpha/2}$

② Left Tailed

$$H_a: \mu < \mu_0$$

Reject  $H_0$  if  $Z < Z_{\alpha}$

③ Right Tailed

$$H_a: \mu > \mu_0$$

Reject  $H_0$  if  $Z \geq Z_{\alpha}$



[ $\sigma$  is not known]

Find critical values in a t-distribution:-

- ① specify  $\alpha$
- ② calculate degrees of freedom =  $n-1$
- ③ Find the critical values at  $\text{DOF}, \alpha$ 
  - (1) left tailed: put -ve sign
  - (2) right tailed: +ve
  - (3) Two tailed: -ve & +ve

T-test for mean

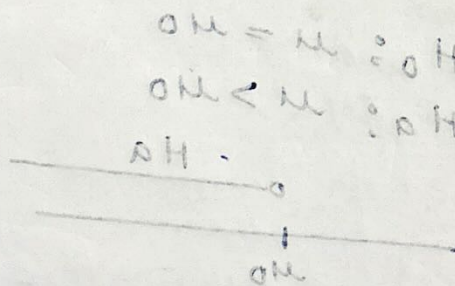
$$t = \frac{(\text{Sample mean}) - (\text{Hypothesis mean})}{\text{standard error}} = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$$

Determine the rejection region:-

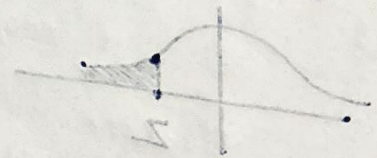
For 2 tailed:  $t < -t_0$  or  $t > +t_0$

For left tailed:  $t < -t_0$

For right tailed:  $t > +t_0$



For right tailed:  $t > +t_0$



For 2 tailed:  $t < -t_0$  or  $t > +t_0$

For left tailed:  $t < -t_0$

For right tailed:  $t > +t_0$

For 2 tailed:  $t < -t_0$  or  $t > +t_0$



## chi-square

### (1) Left Tailed Test

$$H_0: \mu = \mu_0$$

$$H_a: \mu < \mu_0$$

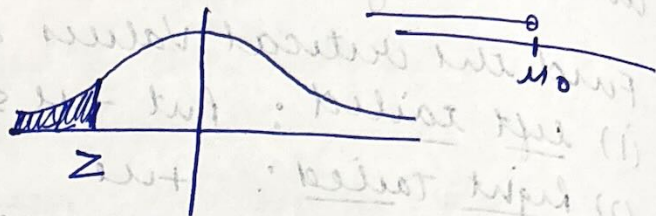
Critical Region:

① For Z-Test:

→ Z value corr to  $\alpha$

→ Take Z-value

→ Reject  $H_0$  if  $Z < Z_\alpha$



② For T-test: → t value corr to  $(n-1, \alpha)$

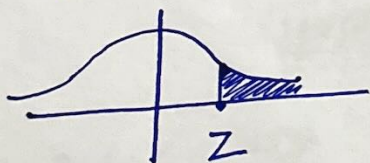
→ Put -ve sign

$$t < -t_0$$

P-Value: ① Z-Test:  $N(Z)$

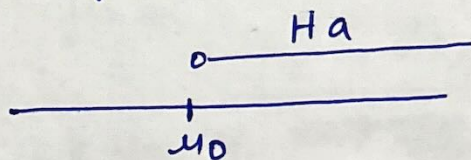
② T-test: calculate t value & test it in critical region

### (2) Right Tailed:



$$H_0: \mu = \mu_0$$

$$H_a: \mu > \mu_0$$



Critical Region:

① Z-Test: Z-value corr to  $1-\alpha$

→ Take +ve Z value

→ Reject  $H_0$  if  $Z > Z_\alpha$

② T-test: t value corr to  $(n-1, \alpha)$

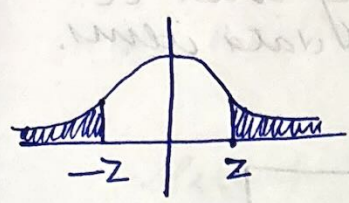
→ Put -ve sign

→ Rejection region is  $t > t_0$



P-value : ① Z-Test :  $P = 1 - N(z)$   
 ② T-test : Rejection Region :  $t > t_0$

(3) Two Tailed:



$H_0 : \mu = \mu_0$   
 $H_a : \mu \neq \mu_0$

Critical Region :

① Z-Test : Z value call to  
 → one -  $\alpha$  &  $+\alpha$

$\frac{\alpha}{2}, 1 - \frac{\alpha}{2}$

→ reject  $H_0$  if

$z > z_{\alpha/2}$

$z < -z_{\alpha/2}$

② T-test : T-value corr to  $(n-1, \alpha)$   
 $[-t_0, +t_0]$

Rejection Region :

$t < -t_0$   
 $t > +t_0$

P-value : ① Z-test

$P = 2 * N(-z)$

② T-test : Rejection Region