

# Where am I?

- **HUL242: Fundamentals of Language Sciences**
- **Semantics (Lecture-2)**
- Thursday, April 17<sup>th</sup>

# Semantics?

- How syntactic form is associated with meaning
- To discover a small finite set of rules that underlie our semantic competence.
- Using these rules to explain people's intuitions about meaning, entailment, synonym and logically independent relationships etc.

# Entailment

- When we say one sentence  $S_1$  **entails** another sentence  $S_2$ , we mean:
  - Whenever  $S_1$  is true,  $S_2$  **must** also be true.
  - This is often written as  $S_1 \vDash S_2$ .
  - If  $S_1$  doesn't entail  $S_2$ , we write  $S_1 \not\vDash S_2$ .

# Quantifiers and Entailment

- *a* is **upward-entailing** for both N and VP.
- *every* is **downward-entailing** for N and **upward-entailing** for VP.
- *no* is **downward-entailing** for both N and VP.

	Noun	VP
a		
every		
no		

- Note: Based on the subset and superset relation

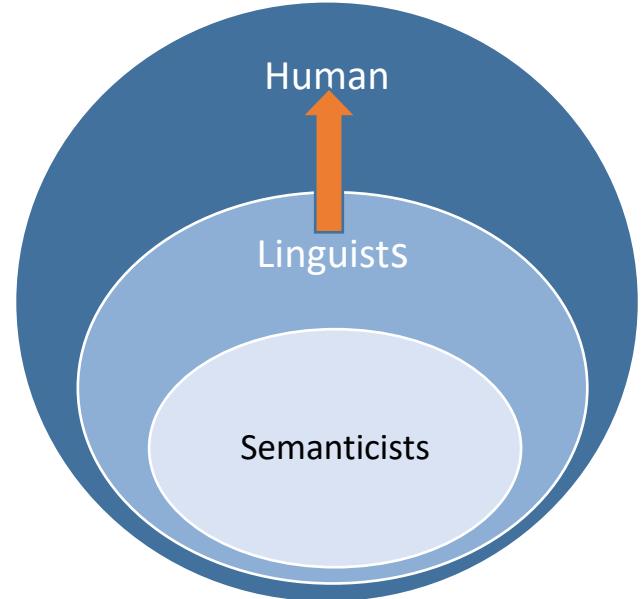
# The determiner ‘a’: NP

(1). A linguist ate berries.

➤ Make the noun less specific (2) and more specific (3):

(2). A human ate berries.      (1)  $\vDash$  (2)

(3). A semanticist ate berries.    (1)  $\not\vDash$  (3)



○ We say *a* is **upward-entailing** on the **noun**:

➤ you can replace the N with something more general, and the new sentence will be entailed by the first sentence

○ Upward-entailing = **subset to superset relation**

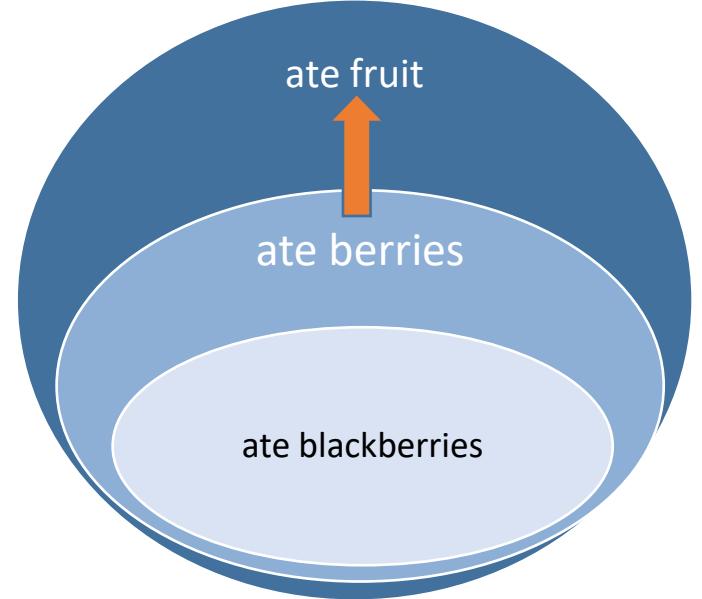
# The determiner ‘a’: VP

(1). A linguist ate berries.

➤ Make the VP less specific (4) and more specific (5):

(4). A linguist ate fruit.      (1)  $\vDash$  (4)

(5). A linguist ate blackberries. (1)  $\not\vDash$  (5)



○ We say ‘a’ is **upward-entailing** on its **VP**:

➤ you can replace the VP with something more general, and the new sentence will be entailed by the first sentence

○ So, ‘a’ is **upward-entailing on both its N and VP**.

# The determiner ‘every’: NP

(1). Every linguist ate berries.

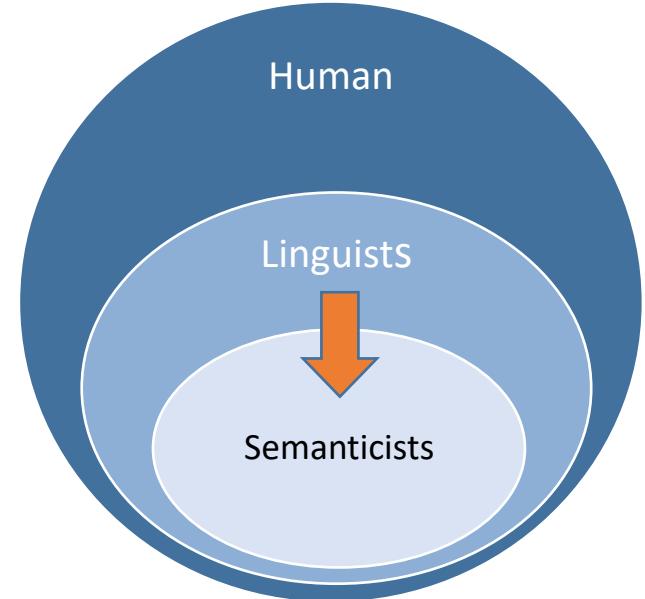
➤ Make the noun less specific (2) and more specific (3):

- (2). Every human ate berries. (1)  $\not\models$  (2)  
(3). Every semanticist ate berries. (1)  $\models$  (3)

○ Every is **downward-entailing on its Noun**:

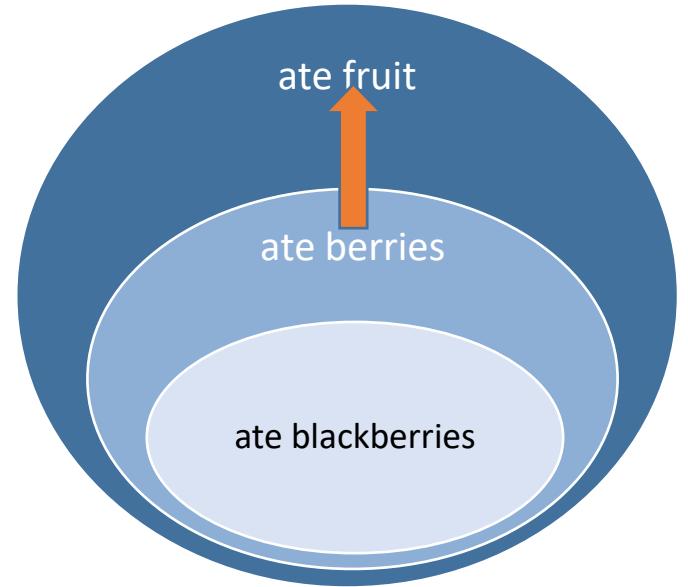
➤ You can replace the N with something more specific, and the new sentence is entailed by the first sentence

○ Downward-entailing = **superset to subset relation**



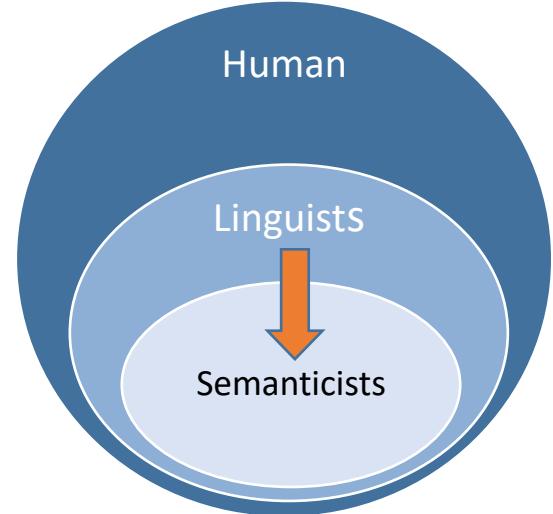
# The determiner ‘every’: VP

- (1). Every linguist ate berries.
- Making the VP less specific (4) and more specific (5):
  - (4). Every linguist ate fruit. (1)  $\vDash$  (4)
  - (5). Every linguist ate blackberries. (1)  $\not\vDash$  (5)
- Every is **upward-entailing** on its VP
  - you can replace the VP with something more general, and the new sentence will be entailed by the first sentence
- Every is **downward-entailing on its N** and **upward-entailing on its VP**



# The determiner ‘No’: NP

- (1). No linguist ate berries.
- Make the noun less specific (2) and more specific (3):
  - (2). No human ate berries.                    (1)  $\not\models$  (2)
  - (3). No semanticist ate berries.                    (1)  $\models$  (3)
- No is **downward-entailing** to its N
- You can replace the N with something more specific, and the new sentence is entailed by the first sentence.



# The determiner ‘No’: VP

(1). No linguist ate berries.

➤ Making the VP less specific (4) and more specific (5):

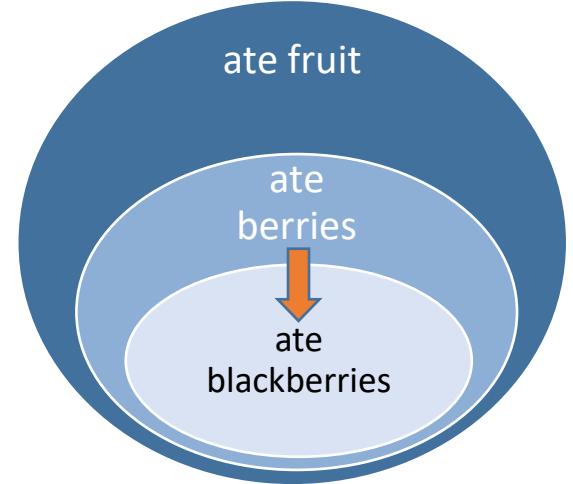
(4). No linguist ate fruit. (1)  $\not\models$  (4)

(5). No linguist ate blackberries. (1)  $\models$  (5)

○ No is also **downward-entailing** to its VP

➤ You can replace the N with something more specific, and the new sentence is entailed by the first sentence.

○ So, ‘no’ is **downward-entailing on both its N and VP**.



# Summary

	Noun	VP
a	↑	↑
every	↓	↑
no	↓	↓

- ↑, the up arrow, stands for **upward entailing** (*from subset to superset*).
- ↓, the down arrow, stands for **downward-entailing** (*form superset to subset*).

## More determiners: In tutorial

- Fill in the chart for the quantifiers *not every*, *at least three*, *exactly five*. Give sentence pair (and the entailment relation to them!) to justify your answer.

	Noun	Verb phrase
at least three		
not every		
exactly five		

- Use ↑ to show upward-entailing and ↓ to show downward-entailing

# More determiners: In tutorial

- Fill in the chart for the quantifiers *not every*, *at least three*, *exactly five*. Give sentence pair (and the entailment relation to them!) to justify your answer.

	Noun	Verb phrase
at least three	↑	↑
not every	↑	↓
exactly five	✗	✗

# Meaning of ‘names’, ‘nouns’ and ‘VPs’

- The meanings of names? **Individuals.**

『Deepak』 = DEEPAK  
= d

- The meanings of nouns? **Set of Individuals.**

『TA』 = {JOYNAL, TANVI, SIDDHARTH}  
= {j, t, s}

- The meanings of VP? **Set of Individuals.**

『teach linguistics』 = {DEEPAK, JOYNAL, TANVI, SIDDHARTH}  
= {d, j, t, s}

# Sentence meaning

- Sentences express a proposition that has a “**truth value**”.
- The meaning of a sentence is its truth value i.e., **true or false**.
- This is called **truth-conditional semantics**. It takes speakers’ knowledge of truth conditions as basic. That is, if you know the meaning of a sentence, you know its **truth conditions**.
- We calculate the truth value of the above sentences via compositional interpretation.

# Compositional interpretation of a sentence

- The meaning of simple sentences (where the subject NP is a ‘name’) is a claim about **set membership**.
- The meaning of  $[NP\ VP]$  is the following **truth condition**:
  - If the meaning of NP (an individual) is a member of the meaning of VP (a set of individuals), then S is TRUE; otherwise, it is FALSE.
- A general rule for interpretation:

$$[\![ NP\ VP ]\!] = [\![ NP ]\!] \in [\![ VP ]\!]$$

**Notation:** We write  $[\![ X ]\!]$  for meaning of X

We write  $\in$  for ‘member of’

# Working with sets

# Union

The **union** of two sets A and B, written as  $A \cup B$ , means the set containing all the elements that are at least in A or in B.

$$A = \{\text{DEEPAK, SIDDHARTH}\}$$

$$B = \{\text{DEEPAK, JOYNAL, TANVI}\}$$

$$A \cup B = \{\text{DEEPAK, SIDDHARTH}\} \cup \{\text{DEEPAK, JOYNAL, TANVI}\}$$

$$= \{\text{DEEPAK, SIDDHARTH, JOYNAL, TANVI}\}$$

**Note: No need to mention the same member twice.**

# Union: Practise

$$A = \{a, b, c, d\}$$

$$B = \{1, 2, 3\}$$

$$A \cup B = ?$$

$$A \cup B = \{a, b, c, d, 1, 2, 3\}$$

.....

$$C = \{2, 4, 6, 8\}$$

$$D = \{1, 3, 5, 7\}$$

$$C \cup D = ?$$

$$C \cup D = \{1, 2, 3, 4, 5, 6, 7, 8\}$$

## Intersection

The **intersection** of  $A$  and  $B$ , written ' $A \cap B$ ', means the set consisting only of things that are in **both**  $A$  and  $B$ .

$$A = \{\text{DEEPAK, SIDDHARTH}\}$$

$$B = \{\text{DEEPAK, JOYNAL, TANVI}\}$$

$$\begin{aligned} A \cap B &= \{\text{DEEPAK, SIDDHARTH}\} \cap \{\text{DEEPAK, JOYNAL, TANVI}\} \\ &= \{\text{DEEPAK}\} \end{aligned}$$

## Intersection: Practise

$$A = \{ 2, 3, 4, 5, 6\}$$

$$B = \{4, 6\}$$

$$A \cap B = ?$$

$$A \cap B = \{4, 6\}$$

.....

$$A = \{ 2, 3\}$$

$$B = \{4\}$$

$$A \cap B = ?$$

$$A \cap B = \{ \}$$

## Set subtraction

**Subtracting  $B$  from  $A$ ,** written ' $A - B$ ', means removing every member of  $B$  from  $A$ .

$$A = \{\text{DEEPAK, JOYNAL, SIDDHARTH, TANVI}\}$$

$$B = \{\text{DEEPAK, SIDDHARTH}\}$$

$$\begin{aligned} A - B &= \{\text{DEEPAK, JOYNAL, SIDDHARTH, TANVI}\} - \{\text{DEEPAK, SIDDHARTH}\} \\ &= \{\text{JOYNAL, TANVI}\} \end{aligned}$$

## Set subtraction: Practise

$$A = \{2, 3, 4\}$$

$$B = \{4\}$$

$$A - B = ?$$

$$A - B = \{2, 3\}$$

.....

$$A = \{2, 3, 4\}$$

$$B = \{5, 6\}$$

$$A - B = ?$$

$$A - B = \{2, 3, 4\}$$

## Subsets and Supersets

If every element of  $A$  is also in  $B$ , we say that  $A$  is a **subset** of  $B$ , and we say that  $B$  is a **superset of  $A$** .

We represent it as  $A \subseteq B$  ( $A$  is a subset of  $B$ )

$B \supseteq A$  ( $B$  is a superset of  $A$ )

$$A = \{\text{DEEPAK, JOYNAL}\}$$

$$B = \{\text{DEEPAK, JOYNAL, SIDDHARTH, TANVI}\}$$

- $A$  is a subset and  $B$  is a superset

## Subsets and Superset: Practise

$A = \{\text{DEEPAK, JOYNAL, SIDDHARTH, TANVI}\}$

$B = \{\text{DEEPAK, JOYNAL}\}$

$A \subseteq B = ?$

**No**

What about this?

$\{\} \subseteq \{\text{DEEPAK, JOYNAL}\} = ?$

**Yes**

Note: An **empty set** is a member of **every set**.

Sentence meaning: compositional interpretation

# Simple Sentences

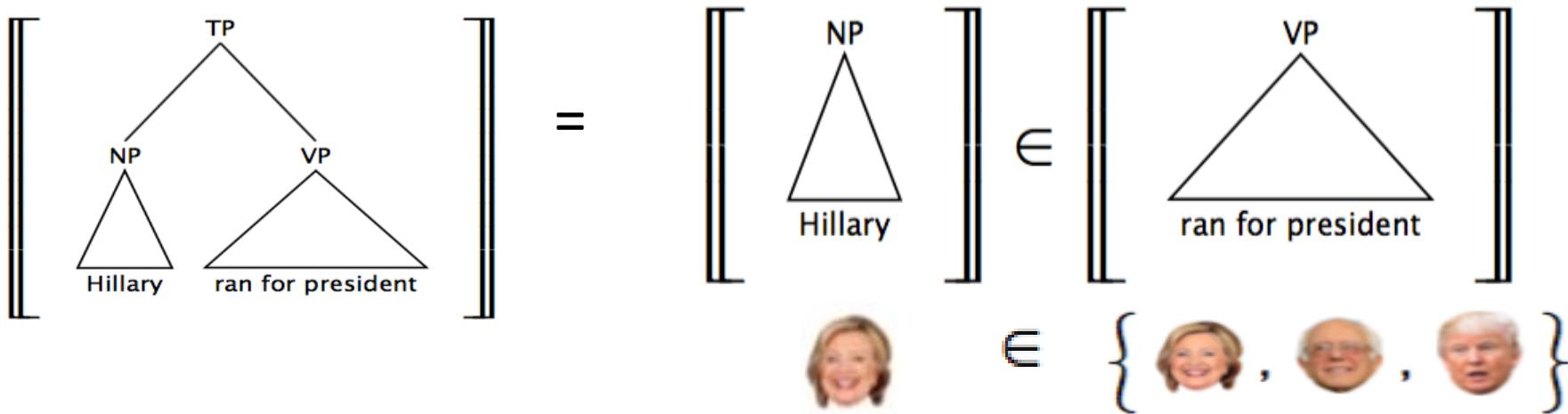
- The meaning of simple sentences (where the subject NP is a ‘name’) is a claim about **set membership**.
- A general rule for interpretation:  $\llbracket \text{NP VP} \rrbracket = \llbracket \text{NP} \rrbracket \in \llbracket \text{VP} \rrbracket$
- What is the meaning of ‘Hillary ran for president.’  
(Situation: presidential election in the USA for 2017-2021)

$$\llbracket \text{Hillary ran for president} \rrbracket = \llbracket \text{Hillary} \rrbracket \in \llbracket \text{ran for president} \rrbracket$$
$$\quad \quad \quad \in \quad \{ \text{Hillary Clinton}, \text{Bernie Sanders}, \text{Donald Trump} \}$$

- This sentence makes a **true** claim. You can find Hillary inside the set of people who ran for president.

# Cautionary note

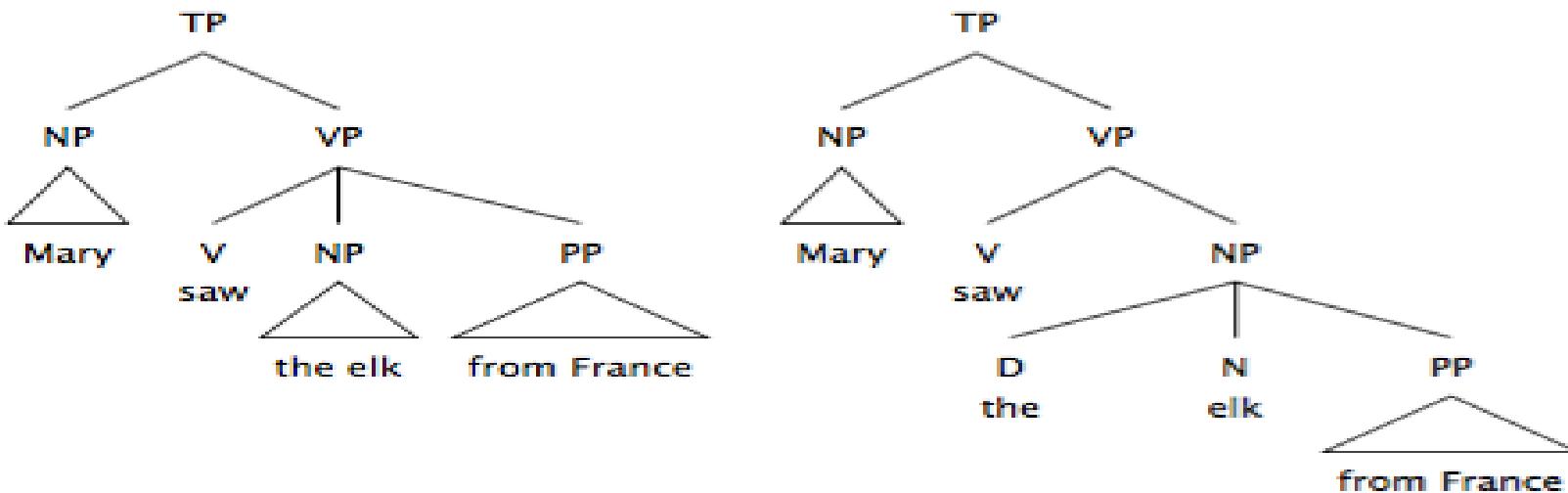
- We interpret the structure of the sentence



- Why?

# Cautionary note

- **Mary saw the elk from France.** Mary is in France or The elk is from France



- The same words but putting them in different ways gives you different meanings.
- **Note: we will use sentences (not structures) for the sake of simplicity.**

# Simple sentences with VP conjunction

1. Deepak teaches Linguistics and likes semantics.
2. Deepak teaches Linguistics and speaks Farsi.

VP conjunction

$$[\![\text{VP1 and VP2}]\!] = [\![\text{V1}]\!] \cap [\![\text{V2}]\!]$$

## Situation/world

$U = \{DEEPAK, JOYNAL, TANVI, SIDDHARTH, ISHAN, SUMITASH\}$

『teach linguistics』 =  $\{DEEPAK, JYONAL, TANVI, SIDDHARTH\}$

『teach lecture classes』 =  $\{DEEPAK\}$

『teach tut classes』 =  $\{JOYNAL, TANVI, SIDDHARTH\}$

『like semantics』 =  $\{DEEPAK\}$

『speaks Farsi』 = { }

# Simple sentences with VP conjunction

Deepak teaches Linguistics and likes semantics.

『Deepak teaches Linguistics and likes semantics』

『Deepak』 ∈ 『teaches Linguistics and likes semantics』

『Deepak』 ∈ 『 teaches Linguistics』 ∩ 『 likes semantics』

DEEPAK ∈ {*DEEPAK, JOYNAL, TANVI, SIDDHARTH*} ∩ {DEEPAK}

DEEPAK ∈ {DEEPAK}

The sentence makes a **true** claim.

# Simple sentences with VP conjunction

Deepak teaches Linguistics and speaks Farsi.

『 Deepak teaches Linguistics and speaks Farsi』

『Deepak』 ∈ 『teaches Linguistics and speaks Farsi』

『Deepak』 ∈ 『 teaches Linguistics』 ∩ 『 speaks Farsi』

DEEPAK ∈ {*DEEPAK, JOYNAL, TANVI, SIDDHARTH*} ∩ {}

DEEPAK ∈ {}

The sentence makes a **False** claim.

## Semantics of negation

- We saw how to interpret sentences like (1). How about (2)?
  1. Deepak [teaches linguistics].
  2. Deepak [**doesn't** teach linguistics].
- The meaning of a sentence is its compositional interpretation.
- Because of this **compositionality**, ‘doesn’t teach linguistics’ should have something to do with ‘teach linguistics’.
- How do we get this?

# Semantics of negation

$$U = \{DEEPAK, JOYNAL, TANVI, SIDDHARTH, ISHAN, SUMITASH\}$$

( **U** stands for the **universe** of individuals. In the present scenario, that's just six people.)

$$\llbracket \text{teach linguistics} \rrbracket = \{DEEPAK, JOYNAL, TANVI, SIDDHARTH\}$$

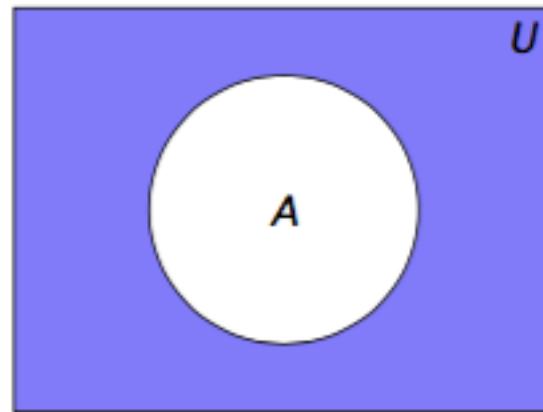
$$\llbracket \text{doesn't teach linguistics} \rrbracket = ?$$

- We get ‘doesn’t teach linguistics’ after subtracting the people who ‘teach linguistics’ from the set of all the people in the given universe (U).
- The rule for interpretation of negated VP:

$$\llbracket \text{not VP} \rrbracket = U - \llbracket \text{VP} \rrbracket$$

## Complementation: Van diagram

- In the diagram below, the circle is the set  $A$ , the rectangle is the universe  $U$ , and the shaded blue area is  $U - A$ .



- This rule of subtraction i.e.,  $U - A$  is called **complementation** and the result of this subtraction is called **complement** (of  $A$ ).

# Semantics of negation

Deepak [doesn't teach linguistics].

$\llbracket \text{NP} \rrbracket \in \llbracket \text{not VP} \rrbracket$

$\llbracket \text{NP} \rrbracket \in U - \llbracket \text{VP} \rrbracket$

$\llbracket \text{NP} \rrbracket \in U - \llbracket \text{teach linguistics} \rrbracket$

$\text{DEEPAK} \in \{ \text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH}, \text{ISHAN}, \text{SUMITASH} \} - \{ \text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH} \}$

$\text{DEEPAK} \in \{ \text{ISHAN}, \text{SUMITASH} \}$

The sentence makes a **False** claim.

# Semantics of negation

Deepak doesn't speak Farsi.

$$[\![\text{NP}]\!] \in [\![\text{not VP}]\!]$$

$$[\![\text{NP}]\!] \in U - [\![\text{VP}]\!]$$

$$[\![\text{NP}]\!] \in U - [\![\text{SPEAK Farsi}]\!]$$

$$\text{DEEPAK} \in \{\text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH}, \text{ISHAN}, \text{SUMITASH}\} - \{ \}$$

$$\text{DEEPAK} \in \{\text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH}, \text{ISHAN}, \text{SUMITASH}\}$$

The sentence makes a **True** claim.

# Interim Summary

- A simple sentence with a simple VP:

Deepak teaches linguistics.

$$[\![ \text{NP VP} ]\!] = [\![ \text{NP} ]\!] \in [\![ \text{VP} ]\!]$$

- A simple sentence with VP conjunction:

Deepak teaches linguistics and likes semantics.

$$[\![ \text{NP VP}_1 \text{ and VP}_2 ]\!] = [\![ \text{NP} ]\!] \in [\![ \text{V}_1 ]\!] \cap [\![ \text{V}_2 ]\!]$$

- A simple sentence with negated VP

Deepak doesn't speak Farsi.

$$[\![ \text{NP not VP} ]\!] = [\![ \text{NP} ]\!] \in U - [\![ \text{VP} ]\!]$$

## Next class

We will discuss how to derive the meaning of different kinds of sentences.

Reading:

Chapter 7, **section 7.4** (Fromkin et. al)

Chapter 8, **ONLY section 8.3: Relative scope** (Fromkin et. al)