

Where am I?

- **HUL242: Fundamentals of Language Sciences**
- **Semantics (Lecture-2)**
- Thursday, April 17th

Semantics?

- How syntactic form is associated with meaning
- To discover a small finite set of rules that underlie our semantic competence.
- Using these rules to explain people's intuitions about meaning, entailment, synonym and logically independent relationships etc.

Entailment

- When we say one sentence $S1$ **entails** another sentence $S2$, we mean:
 - Whenever $S1$ is true, $S2$ **must** also be true.
 - This is often written as $S1 \models S2$.
 - If $S1$ doesn't entail $S2$, we write $S1 \not\models S2$.

Quantifiers and Entailment

- *a* is **upward-entailing** for both N and VP.
- *every* is **downward-entailing** for N and **upward-entailing** for VP.
- *no* is **downward-entailing** for both N and VP.

	Noun	VP
<i>a</i>		
<i>every</i>		
<i>no</i>		

- Note: Based on the subset and superset relation

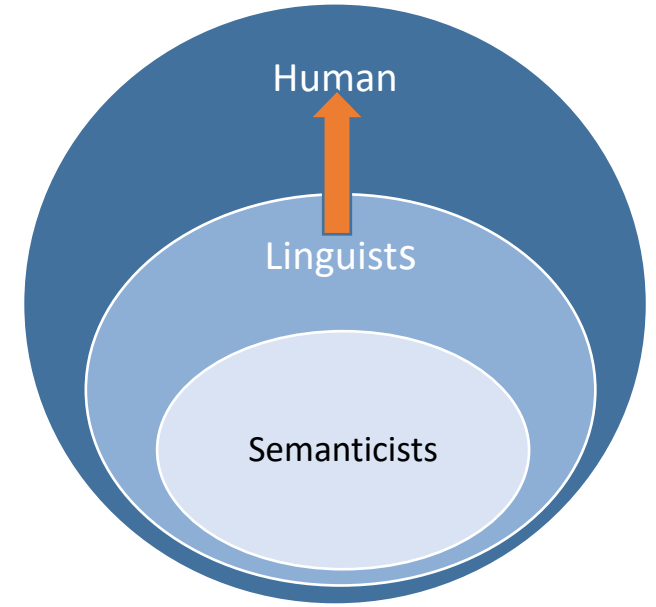
The determiner 'a': NP

(1). A linguist ate berries.

➤ Make the noun less specific (2) and more specific (3):

(2). A human ate berries. (1) \models (2)

(3). A semanticist ate berries. (1) $\not\models$ (3)



○ We say a is **upward-entailing** on the **noun**:

➤ you can replace the N with something more general, and the new sentence will be entailed by the first sentence

○ Upward-entailing = **subset to superset relation**

The determiner 'a': VP

(1). A linguist ate berries.

➤ Make the VP less specific (4) and more specific (5):

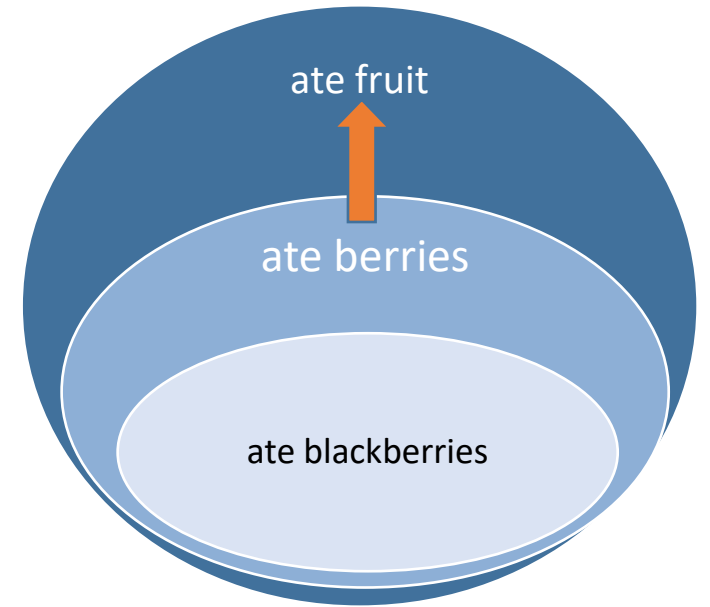
(4). A linguist ate fruit. $(1) \models (4)$

(5). A linguist ate blackberries. $(1) \not\models (5)$

○ We say 'a' is **upward-entailing** on its **VP**:

➤ you can replace the VP with something more general, and the new sentence will be entailed by the first sentence

○ So, 'a' is **upward-entailing on both its N and VP**.



The determiner 'every': NP

(1). Every linguist ate berries.

- Make the noun less specific (2) and more specific (3):

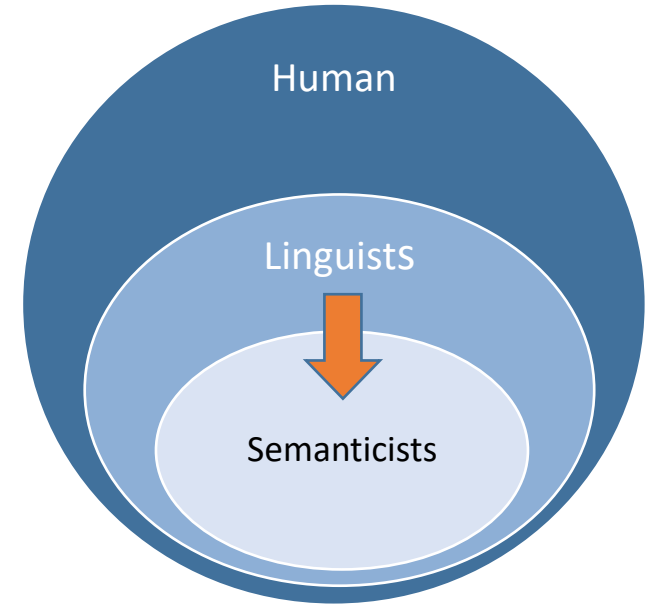
(2). Every human ate berries. $(1) \not\models (2)$

(3). Every semanticist ate berries. $(1) \models (3)$

- Every is **downward-entailing on its Noun**:

- You can replace the N with something more specific, and the new sentence is entailed by the first sentence

- Downward-entailing = **superset to subset relation**



The determiner 'every': VP

(1). Every linguist ate berries.

➤ Making the VP less specific (4) and more specific (5):

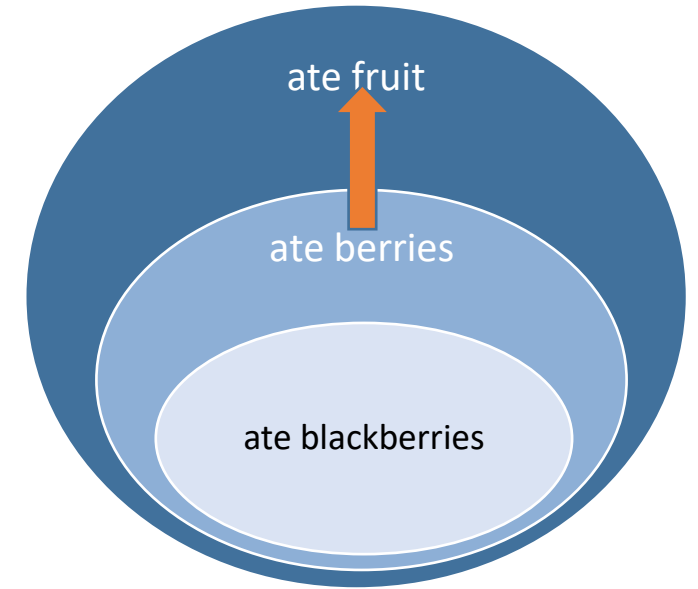
(4). Every linguist ate fruit. $(1) \models (4)$

(5). Every linguist ate blackberries. $(1) \not\models (5)$

○ Every is **upward-entailing** on its VP

➤ you can replace the VP with something more general, and the new sentence will be entailed by the first sentence

○ Every is **downward-entailing on its N** and **upward-entailing on its VP**



The determiner 'No': NP

(1). No linguist ate berries.

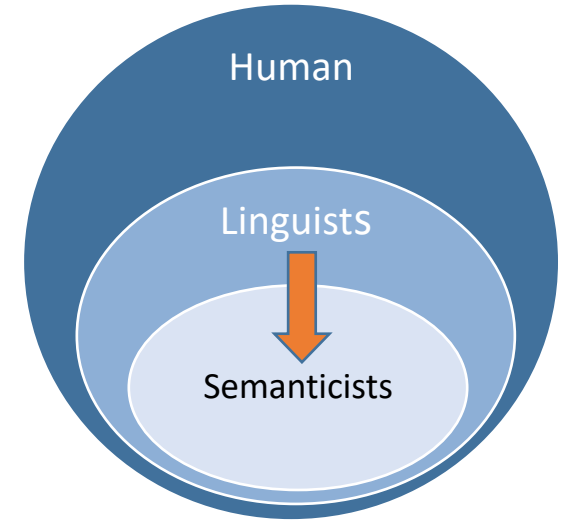
➤ Make the noun less specific (2) and more specific (3):

(2). No human ate berries. (1) $\not\models$ (2)

(3). No semanticist ate berries. (1) \models (3)

○ No is **downward-entailing** to its N

➤ You can replace the N with something more specific, and the new sentence is entailed by the first sentence.



The determiner 'No': VP

(1). No linguist ate berries.

➤ Making the VP less specific (4) and more specific (5):

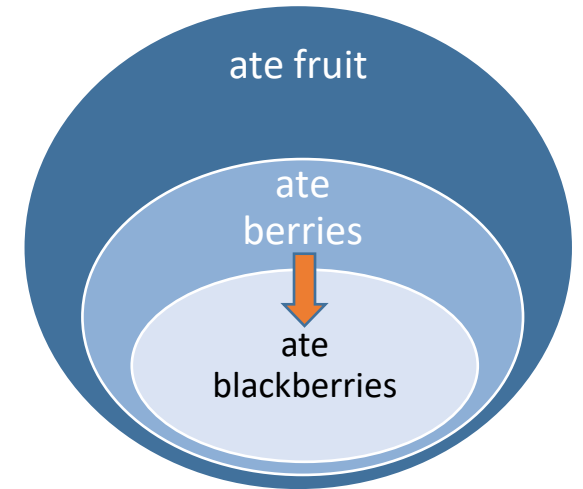
(4). No linguist ate fruit. (1) $\not\models$ (4)

(5). No linguist ate blackberries. (1) \models (5)

○ No is also **downward-entailing** to its VP

➤ You can replace the N with something more specific, and the new sentence is entailed by the first sentence.

○ So, 'no' is **downward-entailing on both its N and VP**.



Summary

	Noun	VP
a	↑	↑
every	↓	↑
no	↓	↓

- ↑, the up arrow, stands for **upward entailing** (*from subset to superset*).
- ↓, the down arrow, stands for **downward-entailing** (*from superset to subset*).

More determiners: In tutorial

- Fill in the chart for the quantifiers *not every*, *at least three*, *exactly five*. Give sentence pair (and the entailment relation to them!) to justify your answer.

	Noun	Verb phrase
at least three		
not every		
exactly five		

- Use ↑ to show upward-entailing and ↓ to show downward-entailing

More determiners: In tutorial

- Fill in the chart for the quantifiers *not every*, *at least three*, *exactly five*. Give sentence pair (and the entailment relation to them!) to justify your answer.

	Noun	Verb phrase
at least three	↑	↑
not every	↑	↓
exactly five	x	x

Meaning of ‘names’, ‘nouns’ and ‘VPs’

- The meanings of names? **Individuals.**

$\llbracket \text{Deepak} \rrbracket = \text{DEEPAK}$
 $= d$

- The meanings of nouns? **Set of Individuals.**

$\llbracket \text{TA} \rrbracket = \{JOYNAL, TANVI, SIDDHARTH\}$
 $= \{j, t, s\}$

- The meanings of VP? **Set of Individuals.**

$\llbracket \text{teach linguistics} \rrbracket = \{DEEPAK, JOYNAL, TANVI, SIDDHARTH\}$
 $= \{d, j, t, s\}$

Sentence meaning

- Sentences express a proposition that has a “**truth value**”.
- The meaning of a sentence is its truth value i.e., **true or false**.
- This is called **truth-conditional semantics**. It takes speakers’ knowledge of truth conditions as basic. That is, if you know the meaning of a sentence, you know its **truth conditions**.
- We calculate the truth value of the above sentences via compositional interpretation.

Compositional interpretation of a sentence

- The meaning of simple sentences (where the subject NP is a ‘name’) is a claim about **set membership**.
- The meaning of [NP VP] is the following **truth condition**:
 - If the meaning of NP (an individual) is a member of the meaning of VP (a set of individuals), then S is TRUE; otherwise, it is FALSE.
- A general rule for interpretation:

$$\llbracket \text{NP VP} \rrbracket = \llbracket \text{NP} \rrbracket \in \llbracket \text{VP} \rrbracket$$

Notation: We write $\llbracket X \rrbracket$ for meaning of X

We write \in for ‘member of’

Working with sets

Union

The **union** of two sets A and B, written as $A \cup B$, means the set containing all the elements that are at least in A or in B.

$$A = \{\text{DEEPAK, SIDDHARTH}\}$$

$$B = \{\text{DEEPAK, JOYNAL, TANVI}\}$$

$$\begin{aligned} A \cup B &= \{\text{DEEPAK, SIDDHARTH}\} \cup \{\text{DEEPAK, JOYNAL, TANVI}\} \\ &= \{\text{DEEPAK, SIDDHARTH, JOYNAL, TANVI}\} \end{aligned}$$

Note: No need to mention the same member twice.

Union: Practise

$$A = \{a, b, c, d\}$$

$$B = \{1, 2, 3\}$$

$$A \cup B = ?$$

$$A \cup B = \{a, b, c, d, 1, 2, 3\}$$

.....

$$C = \{2, 4, 6, 8\}$$

$$D = \{1, 3, 5, 7\}$$

$$C \cup D = ?$$

$$C \cup D = \{1, 2, 3, 4, 5, 6, 7, 8\}$$

Intersection

The **intersection** of A and B , written ' $A \cap B$ ', means the set consisting only of things that are in **both** A and B .

$$A = \{\text{DEEPAK, SIDDHARTH}\}$$

$$B = \{\text{DEEPAK, JOYNAL, TANVI}\}$$

$$\begin{aligned} A \cap B &= \{\text{DEEPAK, SIDDHARTH}\} \cap \{\text{DEEPAK, JOYNAL, TANVI}\} \\ &= \{\text{DEEPAK}\} \end{aligned}$$

Intersection: Practise

$$A = \{ 2, 3, 4, 5, 6 \}$$

$$B = \{ 4, 6 \}$$

$$A \cap B = ?$$

$$A \cap B = \{ 4, 6 \}$$

.....

$$A = \{ 2, 3 \}$$

$$B = \{ 4 \}$$

$$A \cap B = ?$$

$$A \cap B = \{ \}$$

Set subtraction

Subtracting B from A , written ' $A - B$ ', means removing every member of B from A .

$$A = \{\text{DEEPAK, JOYNAL, SIDDHARTH, TANVI}\}$$

$$B = \{\text{DEEPAK, SIDDHARTH}\}$$

$$\begin{aligned} A - B &= \{\text{DEEPAK, JOYNAL, SIDDHARTH, TANVI}\} - \{\text{DEEPAK, SIDDHARTH}\} \\ &= \{\text{JOYNAL, TANVI}\} \end{aligned}$$

Set subtraction: Practise

$$A = \{2, 3, 4\}$$

$$B = \{4\}$$

$$A - B = ?$$

$$A - B = \{2, 3\}$$

.....

$$A = \{2, 3, 4\}$$

$$B = \{5, 6\}$$

$$A - B = ?$$

$$A - B = \{2, 3, 4\}$$

Subsets and Supersets

If every element of A is also in B , we say that A is a **subset** of B , and we say that B is a **superset** of A .

We represent it as $A \subseteq B$ (A is a subset of B)

$B \supseteq A$ (B is a superset of A)

$A = \{\text{DEEPAK, JOYNAL}\}$

$B = \{\text{DEEPAK, JOYNAL, SIDDHARTH, TANVI}\}$

- A is a subset and B is a superset

Subsets and Superset: Practise

$A = \{\text{DEEPAK, JOYNAL, SIDDHARTH, TANVI}\}$

$B = \{\text{DEEPAK, JOYNAL}\}$

$A \subseteq B = ?$

No

What about this?

$\{ \} \subseteq \{\text{DEEPAK, JOYNAL}\} = ?$

Yes

Note: An **empty set** is a member of **every set**.

Sentence meaning: compositional interpretation

Simple Sentences

- The meaning of simple sentences (where the subject NP is a ‘name’) is a claim about **set membership**.

- A general rule for interpretation: $\llbracket \text{NP VP} \rrbracket = \llbracket \text{NP} \rrbracket \in \llbracket \text{VP} \rrbracket$

- What is the meaning of ‘Hillary ran for president.’

(Situation: presidential election in the USA for 2017-2021)

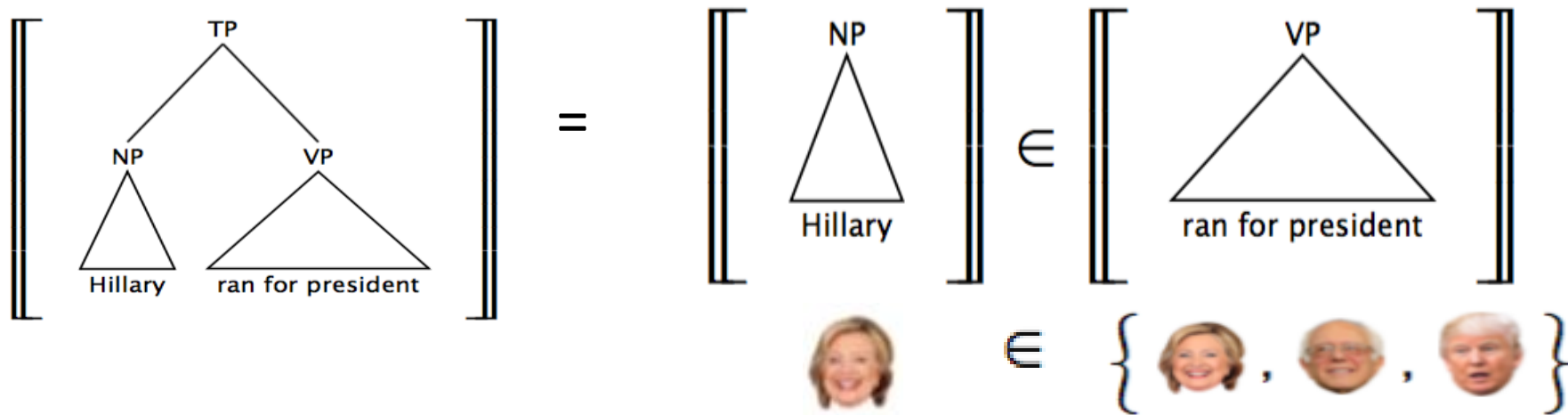
$\llbracket \text{Hillary ran for president} \rrbracket = \llbracket \text{Hillary} \rrbracket \in \llbracket \text{ran for president} \rrbracket$

 \in $\{ \text{Hillary Clinton emoji}, \text{Joe Biden emoji}, \text{Donald Trump emoji} \}$

- This sentence makes a **true** claim. You can find Hillary inside the set of people who ran for president.

Cautionary note

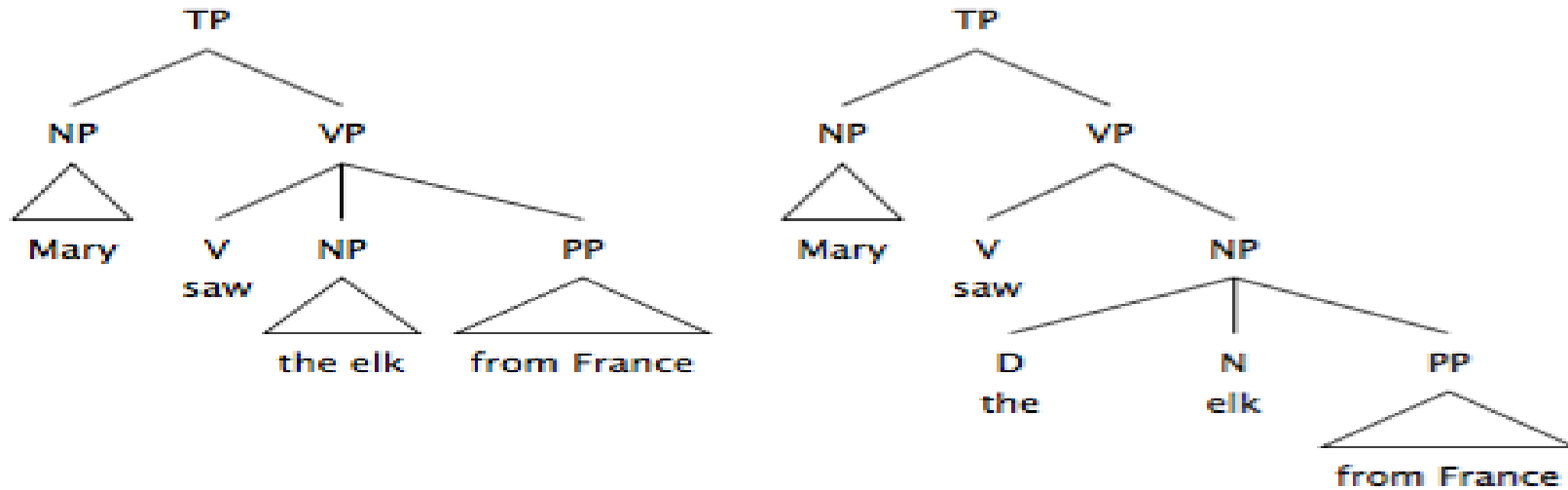
- We interpret the structure of the sentence



- Why?

Cautionary note

- **Mary saw the elk from France.** Mary is in France or The elk is from France



- The same words but putting them in different ways gives you different meanings.
- **Note: we will use sentences (not structures) for the sake of simplicity.**

Simple sentences with VP conjunction

1. Deepak teaches Linguistics and likes semantics.
2. Deepak teaches Linguistics and speaks Farsi.

VP conjunction

$$[[VP1 \text{ and } VP2]] = [[V1]] \cap [[V2]]$$

Situation/world

$U = \{DEEPAK, JOYNAL, TANVI, SIDDHARTH, ISHAN, SUMITASH\}$

$\llbracket \text{teach linguistics} \rrbracket = \{DEEPAK, JOYNAL, TANVI, SIDDHARTH\}$

$\llbracket \text{teach lecture classes} \rrbracket = \{DEEPAK\}$

$\llbracket \text{teach tut classes} \rrbracket = \{JOYNAL, TANVI, SIDDHARTH\}$

$\llbracket \text{like semantics} \rrbracket = \{DEEPAK\}$

$\llbracket \text{speaks Farsi} \rrbracket = \{ \}$

Simple sentences with VP conjunction

Deepak teaches Linguistics and likes semantics.

$\llbracket \text{Deepak teaches Linguistics and likes semantics} \rrbracket$

$\llbracket \text{Deepak} \rrbracket \in \llbracket \text{teaches Linguistics and likes semantics} \rrbracket$

$\llbracket \text{Deepak} \rrbracket \in \llbracket \text{teaches Linguistics} \rrbracket \cap \llbracket \text{likes semantics} \rrbracket$

$\text{DEEPAK} \in \{ \text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH} \} \cap \{ \text{DEEPAK} \}$

$\text{DEEPAK} \in \{ \text{DEEPAK} \}$

The sentence makes a **true** claim.

Simple sentences with VP conjunction

Deepak teaches Linguistics and speaks Farsi.

$\llbracket \text{Deepak teaches Linguistics and speaks Farsi} \rrbracket$

$\llbracket \text{Deepak} \rrbracket \in \llbracket \text{teaches Linguistics and speaks Farsi} \rrbracket$

$\llbracket \text{Deepak} \rrbracket \in \llbracket \text{teaches Linguistics} \rrbracket \cap \llbracket \text{speaks Farsi} \rrbracket$

$\text{DEEPAK} \in \{ \text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH} \} \cap \{ \}$

$\text{DEEPAK} \in \{ \}$

The sentence makes a **False** claim.

Semantics of negation

- We saw how to interpret sentences like (1). How about (2)?
 1. Deepak [teaches linguistics].
 2. Deepak [**doesn't** teach linguistics].
- The meaning of a sentence is its compositional interpretation.
- Because of this **compositionality**, 'doesn't teach linguistics' should have something to do with 'teach linguistics'.
- How do we get this?

Semantics of negation

$U = \{DEEPAK, JOYNAL, TANVI, SIDDHARTH, ISHAN, SUMITASH\}$

(U stands for the **universe** of individuals. In the present scenario, that's just six people.)

$\llbracket \text{teach linguistics} \rrbracket = \{DEEPAK, JOYNAL, TANVI, SIDDHARTH\}$

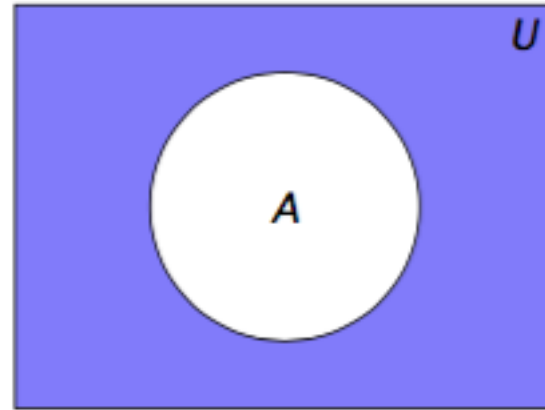
$\llbracket \text{doesn't teach linguistics} \rrbracket = ?$

- We get 'doesn't teach linguistics' after subtracting the people who 'teach linguistics' from the set of all the people in the given universe (U).
- The rule for interpretation of negated VP:

$$\llbracket \text{not VP} \rrbracket = U - \llbracket \text{VP} \rrbracket$$

Complementation: Van diagram

- In the diagram below, the circle is the set A , the rectangle is the universe U , and the shaded blue area is $U - A$.



- This rule of subtraction i.e., $U - A$ is called **complementation** and the result of this subtraction is called **complement** (of A).

Semantics of negation

Deepak [**doesn't** teach linguistics].

$\llbracket \text{NP} \rrbracket \in \llbracket \text{not VP} \rrbracket$

$\llbracket \text{NP} \rrbracket \in \text{U} - \llbracket \text{VP} \rrbracket$

$\llbracket \text{NP} \rrbracket \in \text{U} - \llbracket \text{teach linguistics} \rrbracket$

$\text{DEEPAK} \in \{ \text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH}, \text{ISHAN}, \text{SUMITASH} \} -$
 $\{ \text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH} \}$

$\text{DEEPAK} \in \{ \text{ISHAN}, \text{SUMITASH} \}$

The sentence makes a **False** claim.

Semantics of negation

Deepak doesn't speak Farsi.

$\llbracket \text{NP} \rrbracket \in \llbracket \text{not VP} \rrbracket$

$\llbracket \text{NP} \rrbracket \in \text{U} - \llbracket \text{VP} \rrbracket$

$\llbracket \text{NP} \rrbracket \in \text{U} - \llbracket \text{speaking Farsi} \rrbracket$

$\text{DEEPAK} \in \{\text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH}, \text{ISHAN}, \text{SUMITASH}\} - \{\}$

$\text{DEEPAK} \in \{\text{DEEPAK}, \text{JOYNAL}, \text{TANVI}, \text{SIDDHARTH}, \text{ISHAN}, \text{SUMITASH}\}$

The sentence makes a **True** claim.

Interim Summary

- A simple sentence with a simple VP:

Deepak teaches linguistics.

$$\llbracket \text{NP VP} \rrbracket = \llbracket \text{NP} \rrbracket \in \llbracket \text{VP} \rrbracket$$

- A simple sentence with VP conjunction:

Deepak teaches linguistics and likes semantics.

$$\llbracket \text{NP VP}_1 \text{ and VP}_2 \rrbracket = \llbracket \text{NP} \rrbracket \in \llbracket \text{V}_1 \rrbracket \cap \llbracket \text{V}_2 \rrbracket$$

- A simple sentence with negated VP

Deepak doesn't speak Farsi.

$$\llbracket \text{NP not VP} \rrbracket = \llbracket \text{NP} \rrbracket \in U - \llbracket \text{VP} \rrbracket$$

Next class

We will discuss how to drive the meaning of different kinds of sentences.

Reading:

Chapter 7, **section 7.4** (Fromkin et. al)

Chapter 8, **ONLY section 8.3: Relative scope** (Fromkin et. al)