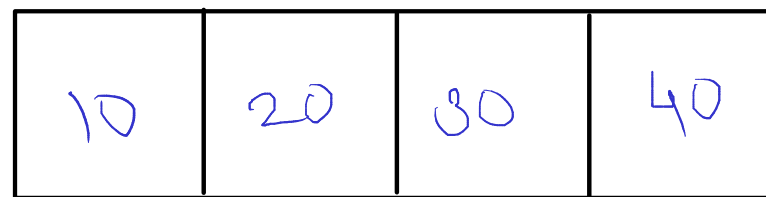


## Linear Queue

Full →



—| 0 1 2 3

~~f~~

r

$r = \text{size} - 1$

Empty →

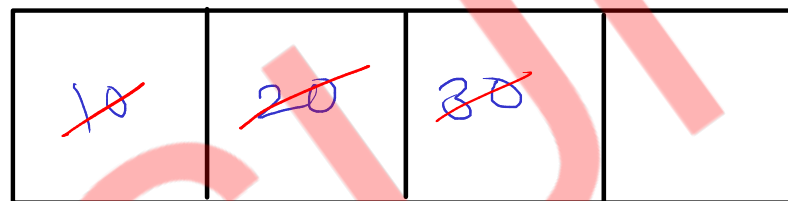


—| 0 1 2 3

~~f~~

$r == f$

Empty →



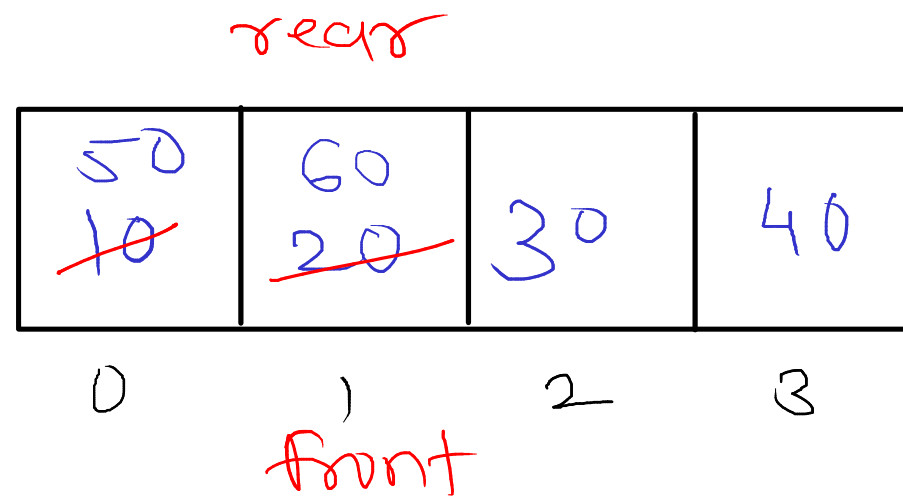
—| 0 1 2 3

~~f~~

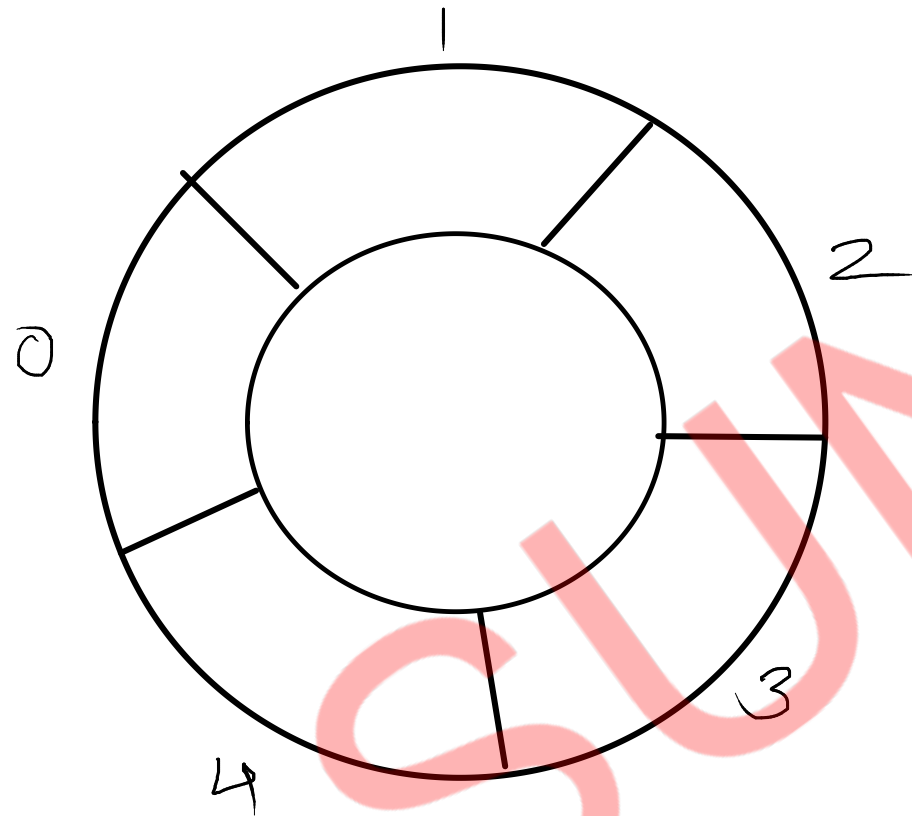
$r == f$

— once rear is reached to last index of array & few initial locations are empty, still we are not able to utilise them, this will lead to poor memory utilization

# Circular Queue



$f=r=-1$



$front = (front + 1) \% size$   
 $rear = (rear + 1) \% size$

Operation:

1) Push

- i) reposition rear
- ii) add value at rear index

2) Pop

- i) reposition front

3) peek

- i) read from front read

- All operations can be performed in  $O(1)$  time complexity

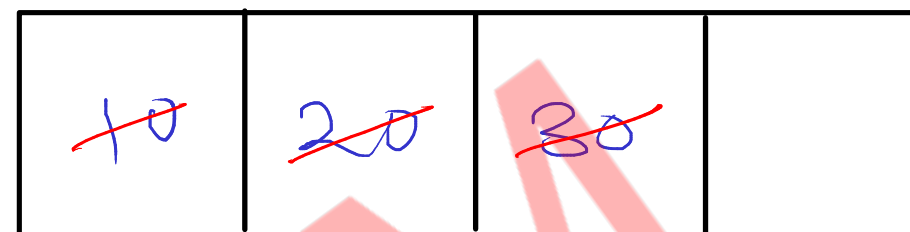
rear



-1 0 1 2 3

front

rear



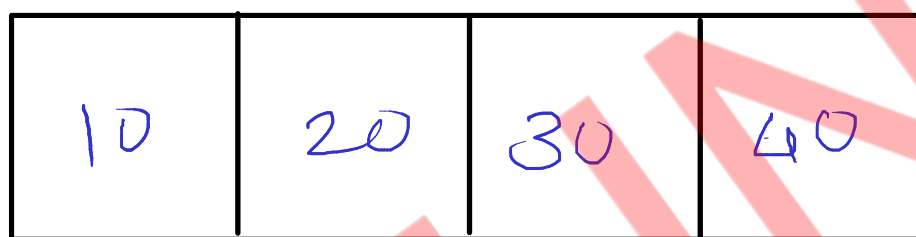
-1 0 1 2 3

front

Empty:  $\text{rear} == \text{front} \ \&\& \ \text{rear} == -1$

```
pop() {  
    front = (front + 1) % size;  
    if (front == rear)  
        front = rear = -1;  
}
```

rear



-1 0 1 2 3

front

rear



-1 0 1 2 3

front

$\text{front} == -1 \ \&\& \ \text{rear} == \text{size} - 1$

$\text{rear} == \text{front} \ \&\& \ \text{rear} != -1$

Full:  $(\text{front} == -1 \ \&\& \ \text{rear} == \text{size} - 1) \ || \ (\text{rear} == \text{front} \ \&\& \ \text{rear} != -1)$

# Stack

- linear data structure which stores similar data
- insertion and removal of data is allowed only from **one** end (top)
- works on principle of "Last In First Out" (LIFO)
- top always points to the last inserted data



## Operations

### 1. Push

- i. reposition top (inc)
- ii. add value at top index

### 2. Pop

- i. reposition top (dec)

### 3. Peek

- i. read data of top index

## Conditions

### 1. isEmpty

$\text{top} == -1$

### 2. isFull

$\text{top} == \text{size} - 1$

- All operations are performed in  $O(1)$  time complexity

# Stack and Queue Time Complexity Analysis (Array Implementation)

	Stack	Linear Queue	Circular Queue
Push	O(1)	O(1)	O(1)
Pop	O(1)	O(1)	O(1)
Peek	O(1)	O(1)	O(1)

# Stack Application

## Expression Evaluation and Conversion

1. Postfix Evaluation
2. Prefix Evaluation
3. Infix to Postfix Conversion
4. Infix to Prefix Conversion

### Expression:

- set/combination of operands and operators

operands - values/variables

operators - mathematical symbols (+, -, /, \*, %)

e.g.  $a + b$ ,  $4 * 2 - 3$

### Types:

- |            |         |          |
|------------|---------|----------|
| 1. Infix   | $a + b$ | human    |
| 2. Prefix  | $+ a b$ | computer |
| 3. Postfix | $a b +$ | computer |

### Operators:

()  
power  
\* / %  
+ -



# Postfix Evaluation

Postfix : 4 5 6 \* 3 / + 9 + 7 -

left  $\longrightarrow$  right

⑤  $23 - 7$   
 $= 16$

④  $14 + 9$   
 $= 23$

③  $4 + 10$   
 $= 14$

②  $30 / 3$   
 $= 10$

①  $5 * 6$   
 $= 30$

Stack

16
<del>7</del>
<del>23</del>
<del>9</del>
<del>14</del>
<del>10</del>
<del>3</del>
<del>30</del>
<del>6</del>
<del>5</del>
<del>4</del>

result

# Prefix Evaluation

Prefix : - + + 4 / \* 5 6 3 9 7

left ← right

⑤  $23 - 7$   
 $= 16$

④  $14 + 9$   
 $= 23$

③  $4 + 10$   
 $= 14$

②  $30 / 3$   
 $= 10$

①  $5 * 6$   
 $= 30$

16
<del>23</del>
<del>14</del>
<del>4</del>
<del>10</del>
<del>30</del>
<del>5</del>
<del>6</del>
<del>8</del>
<del>9</del>
<del>7</del>

result



Example:  $1 + 3 * 4 - (6 + 8 / 2) + 7$   
 left  $\longrightarrow$  right  
 $1 + 3 * 4 - 6 + 8 / 2 + 7$   
 $1 + 3 * 4 - 6 + 4 + 7$   
 $1 + 3 * 4 - 6 + 11$   
 $1 + 12 - 6 + 11$   
 $13 - 6 + 11$   
 $7 + 11$   
 $18$

**Infix : 1 \$ 9 + 3 \* 4 - (6 + 8 / 2) + 7**

left  $\longrightarrow$  right

Postfix : 19 5 3 4 \* + 6 8 2 / + - 7 +

+ <del>/</del>
X X
+ <del>/</del>
( <del>/</del>
/ 
* <del>/</del>
+ <del>/</del>
\$ <del>/</del>

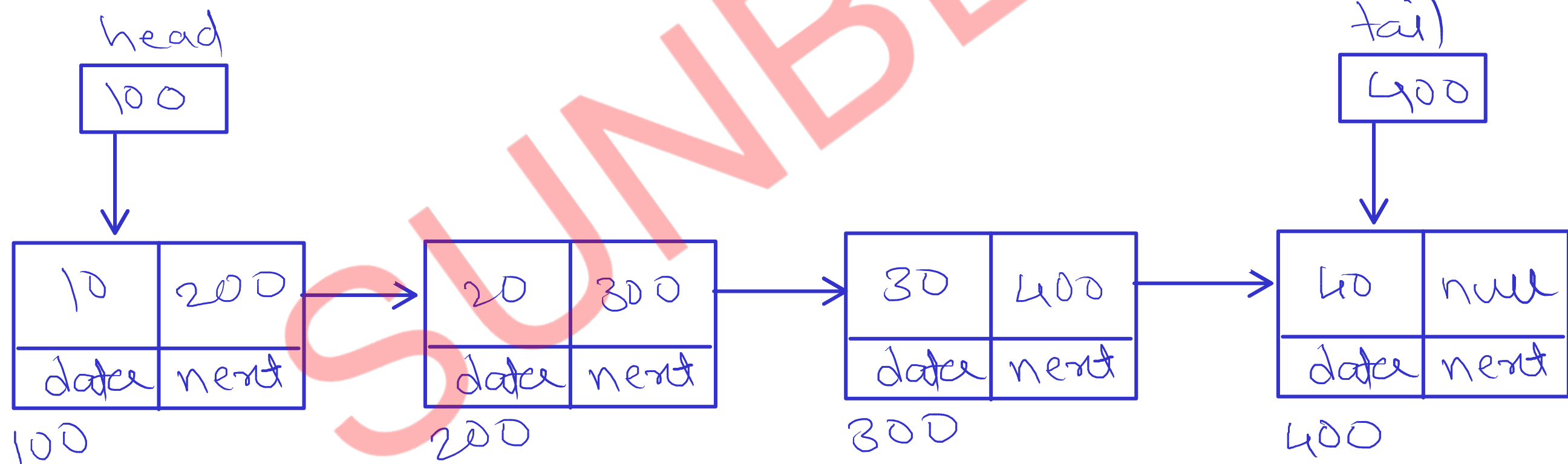
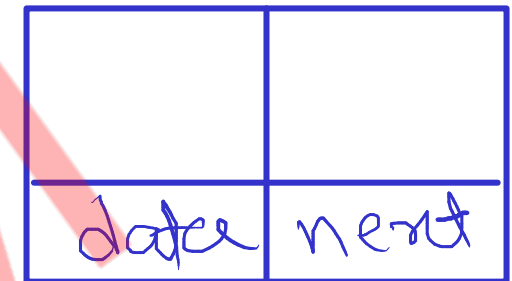
$\$1\%$

<del>\$</del>
<del>+</del>
<del>*</del>
<del>-</del>
<del>+</del>
<del>X</del>
<del>&gt;</del>
<del>+</del>

# Linked List

- linear data structure
- link of next data is kept with previous/current data
- every element is known as "node" and it consist of two part
  - data - actual data of the node
  - link - address/reference of next data/node
- address of first node is kept into head pointer/reference
- address of last node is kept into tail pointer/reference (optional)

node



## **Linked list Operations**

- 1. Add first**
- 2. Add last**
- 3. Add pos (in between)**
- 4. Delete first**
- 5. Delete last**
- 6. Delete pos (in between)**
- 7. Traverse (Display)**
- 8. reverse**
- 9. search**
- 10. sort**

## **Linked List Types:**

- 1. Singly Linear linked List**
- 2. Singly Circular linked list**
- 3. Doubly Linear linked list**
- 4. Doubly Circular linked list**