

Probability&RV

Assignment-05

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https://github.com/Anuradha-Uggi/Assignments-AI5002-Probability-and-Random-Variables/blob/main/Prob_ass05/rvsp_ass_5.py

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https://github.com/Anuradha-Uggi/Assignments-AI5002-Probability-and-Random-Variables/blob/main/Prob_ass05/rvsp_5.tex

I. QUESTION(PROB,4.7)

A bag consists of 10 balls each marked with one of the digits 0 to 9. If four balls are drawn successively with replacement from the bag, what is the probability that none is marked with the digit 0?

II. SOLUTION

Problem Description:

- 1) 10 Balls in an Urn marked with digits from 0 to 9
- 2) After every Draw the Ball should be replaced
- 3) 4 Balls needs to be Drawn
- 4) All Balls Drawn should be marked with non-zero digit.

Computation:

Here we Define Two Random Variables X and Y.

- X Describes whether the Ball Drawn is marked with zero or non-zero digit
- Y Describes the number of balls Drawn that are marked with non-zero digit

- $P(X=0)$ is the Probability of Drawing any ball
- $P(X=1)$ is the Probability that Ball Drawn is marked with non-zero digit.

we know that

$$P(X = 0) = \frac{1}{10} \quad (1)$$

where Sample space consists all 10 possibilities and among them the Favourable Outcome is Drawing any ball.
similarly

$$P(X = 1) = 1 - P(X = 0) = \frac{9}{10} \quad (2)$$

One ball among 10 is generally marked with 0.so now Sample Space remains same but Number of Favourable Outcomes becomes 9.

Since Trials are Bernoulli Trials Hence the Random Variable X. let

$$q = P(X = 1) \quad (3)$$

$$1 - q = P(X = 0) \quad (4)$$

then from equation 2 and 3

$$q = \frac{9}{10} \quad (5)$$

Probability that 4 balls are drawn and none of them is marked with zero-digit is

$$P(Y = 4) = \left(\frac{9}{10}\right)^4 \quad (6)$$

Generalization

Above task can be Generalized using Binomial Distribution as

$$P(Y = k) = \binom{n}{k} (q)^k (1 - q)^{n-k} \quad (7)$$

- where $n=4$
- k is a discrete variable and can take values from 0 to n
- for $n=1000, q = \frac{999}{1000}$

III. CONCLUSION

the probability that among 4 balls Drawn none is marked with the digit 0 is

$$P(Y = 4) = \left(\frac{9}{10}\right)^4 \quad (8)$$