



## Informatics Institute of Technology

# Formal Methods 6SENG005C.1

Course Work Report

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### 1 Machine Structure Diagram

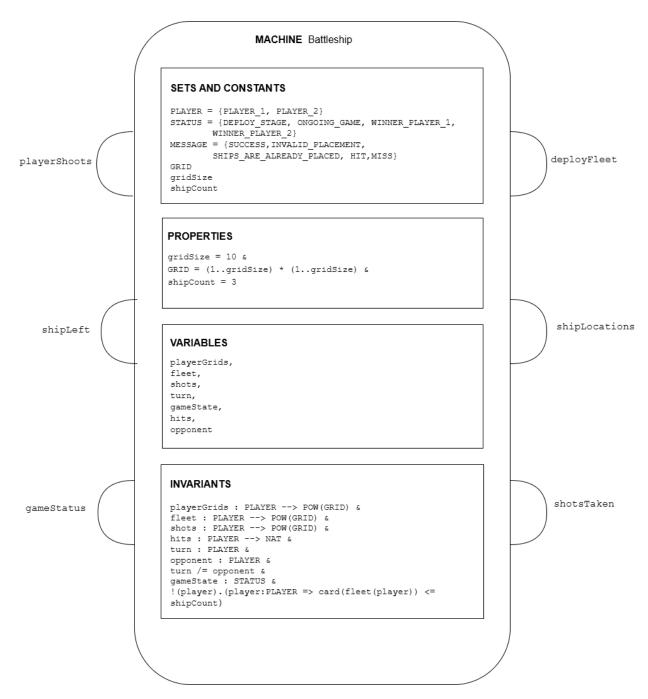


Figure 1: Machine Structure Diagram

#### 2 Justifications:

Detailed explanations for the assigned and utilized SETS, VARIABLES and INVARIENTS are provided below.

Figure 2: SETS, VARIABLES and INVARIENTS

#### 2.1 SETS & CONSTANTS

SET & CONSTANTS	Explanation
PLAYER = {PLAYER_1, PLAYER_2}	This Represents the two participants in the game. Battleship game involves two players, requiring this set to distinguish between them.
<pre>STATUS = {DEPLOY_STAGE, ONGOING_GAME, WINNER_PLAYER_1, WINNER_PLAYER_2}</pre>	This Represents different game status. This is requires to keep track the game progression throughout the different stages of the game.
<pre>MESSAGE = {SUCCESS,   INVALID_PLACEMENT,   SHIPS_ARE_ALREADY_PLACED, HIT, MISS,   YOU_TRIED_THIS_TARGET_BEFORE}</pre>	This Represents the feedback messages. This Requires to provide relevant game notifications during the play.
GRID	This is the game board coordinates which defines the playable area for ship placement and targeting.

gridSize	This constant used for set the grid dimensions. As for this specification it uses 10 x 10 grid, hence the grid size would be 10.
shipCount	This is the number of ships that each player can deploy. This fixes ship count for balanced gameplay.

#### 2.2 VARIABLES & INVARIENTS

VARIABLES & INVARIENTS	Explanation
<pre>playerGrids playerGrids : PLAYER&gt; POW(GRID)</pre>	playerGrids uses to map players to their own grids and this keeps track of each player's board setup. Each player must have a grid of valid coordinates. This ensures proper grid assignment.
<pre>Fleet fleet : PLAYER&gt; POW(GRID) !(player).(player:PLAYER =&gt; card(fleet(player)) &lt;= shipCount)</pre>	Stores ships' positions of each player for ship placement validation and hit detection. Each player's fleet must consist of valid coordinates within the grid. A player's fleet cannot exceed the allowed ship count.
Shots shots: PLAYER> POW(GRID)	Tracks all shots fired by each player for prevent duplicate shots and helps determine game progress.  All the shots must be valid grid coordinates.
Hits hits: PLAYER> NAT	Tracks successful hits per player. This requires for determine when a player wins the game. Since negative hits are logically impossible and there can be an event that a player don't have any successful hit. Hence this tracks natural numbers including 0.
Turn turn : PLAYER	The game is alternates between player's turn, hence the turn variable tracks the current player who's attacking at the moment. The current turn must belong to a valid player and it must be always assigned.
opponent : PLAYER turn /= opponent	This is the opposing player during the current turn. This requires for determine whose ships are targeted.

	Opponent also should be a valid player and since players cannot play against themselves, opponent cannot be the turn at the same time.
gameState gameState: STATUS	This Represents the current state of the game. This is requires to manage game flow from deployment to conclusion. gameState should be always a valid STATUS.

# 3 Machine Testing results:

#### 3.1 Type Check Result

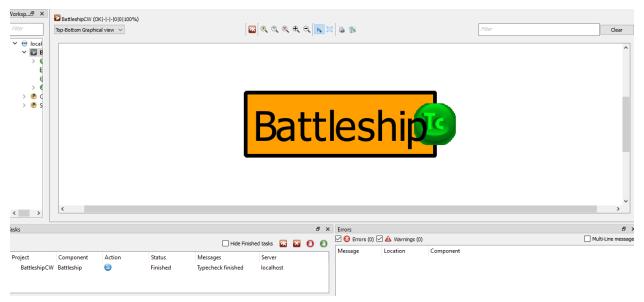
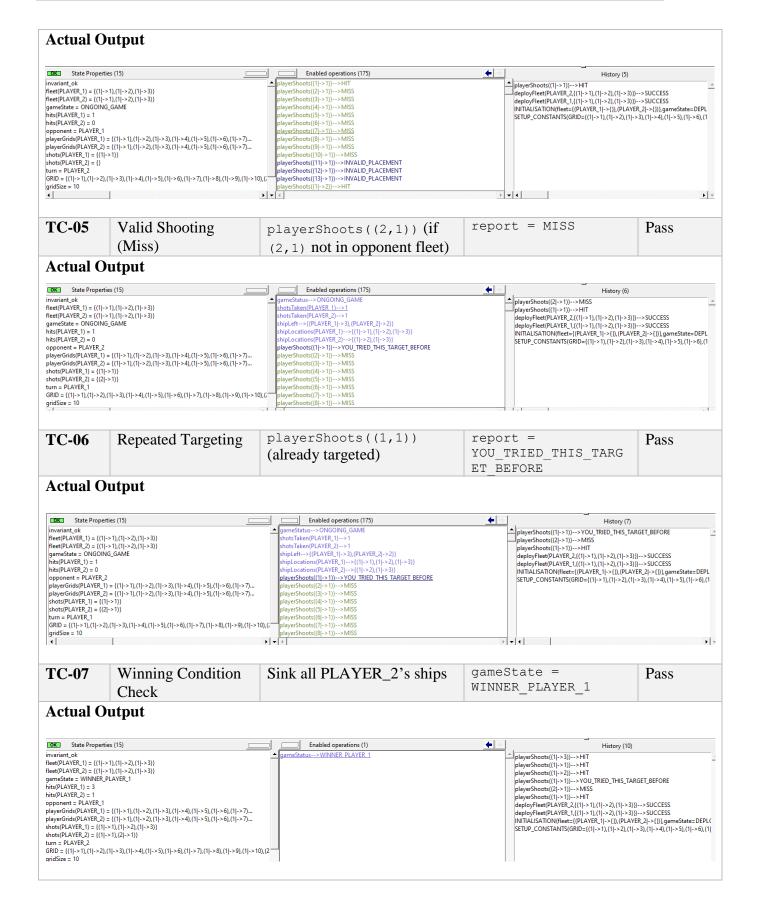
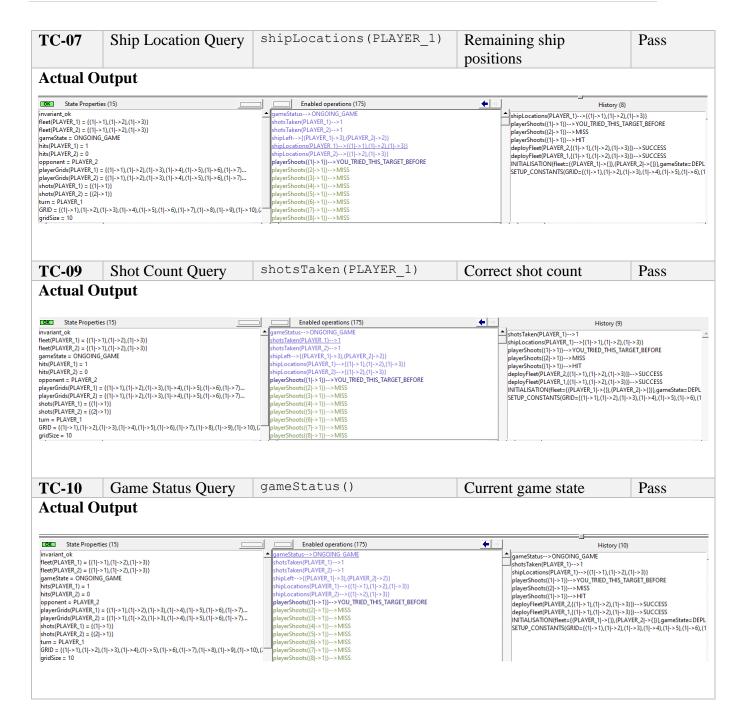


Figure 3: Type Check result

## 3.2 Machine Testing

Case ID	Description	Input	<b>Expected Output</b>	Pass/Fail
TC-01	Verify Initial State	-	<pre>gameState = DEPLOY_STAGE, turn = PLAYER_1</pre>	Pass
Actual O	utput			
OK State Propert fleet(PLAYER_2) = {}	ies (15)	Enabled operations (21)  AgameStatus> DEPLOY_STAGE	History	
gameState = DEPLOY_1 hits(PLAYER_1) = 0 hits(PLAYER_2) = 0 opponent = PLAYER_2 playerGrids(PLAYER_1) playerGrids(PLAYER_2) shots(PLAYER_1) = {} shots(PLAYER_2) = {} turn = PLAYER_1	STAGE  = {(1 -> 1),(1 -> 2),(1 -> 3),(1 -> 4),(1 -> 5),(1 -> 6),(1 -> 7)  = ((1 -> 1),(1 -> 2),(1 -> 3),(1 -> 4),(1 -> 5),(1 -> 6),(1 -> 7)  (1 -> 3),(1 -> 4),(1 -> 5),(1 -> 6),(1 -> 7),(1 -> 8),(1 -> 9),(1 -> 6),(1 -> 7),(1 -> 8),	deployFleet(PLAYER_1,((2)-3),(2)-3),(3)-3)))-> SUCCESS deployFleet(PLAYER_1,((2)-2),(2)-3),(3)-3)))-> SUCCESS deployFleet(PLAYER_1,((1)-3),(2)-3),(3)-3)))-> SUCCESS deployFleet(PLAYER_1,((1)-3),(2)-3),(3)-3)))-> SUCCESS deployFleet(PLAYER_1,((1)-2),(2)-3),(3)-3)))-> SUCCESS deployFleet(PLAYER_1,((1)-2),(2)-3),(3)-3)))-> SUCCESS deployFleet(PLAYER_1,((1)-3),(2)-3),(3)-3)))-> SUCCESS deployFleet(PLAYER_1,((1)-3),(2)-1),(3)-3)))-> SUCCESS deployFleet(PLAYER_1,(1)-3),(3)-3))-> SUCCESS deployFleet(PLAYER_1,(1)-3),(3)-3))-> SUCCESS deployFleet(PLAYER_1,(1)-3),(3)-3))-> SUCCESS deployFleet(PLAYER_1,(1)-3),(3)-3))-> SUCCESS deployFleet(PLAYER_1,(1)-3),(3)-3))-> SUCCESS deployFleet(PLAYER_1,(1)-3),(3)-3))-> SUCCESS deployFleet(PLAYER_1,(1)-3),(3)-3)) SUCCESS deployFleet(PLAYER_1,(1)-3),(3)-3)	INITIALISATION(fleet=((PLAYER_I)=-X[)), SETUP_CONSTANTS(GRID=((TI=>1)),(TI=>	
TC-02	Valid Fleet	deployFleet(PLAYER_1,	report = SUCCESS	Pass
	Deployment	{(1,1), (2,3), (3,3)})		
Actual O	utput			
OK State Propert	ies (15)	Enabled operations (21)  deployFleet(PLAYER 2.{11-> 1).{11-> 2}.{11-> 3})}> SUCCESS	History (   deployFleet(PLAYER_1,{(1 ->1),(2 ->3),(3 -	
invariant_ok fleet(PLAYER_1) = {(1 -	>1),(2 ->3),(3 ->3)}	deployFleet(PLAYER_2,{(1 ->1),(2 ->1),(3 ->1)})>SUCCESS		LAYER_2 ->{})},gameState=DEPL
fleet(PLAYER_1) = {(1]- fleet(PLAYER_2) = {} gameState = DEPLOY_ hits(PLAYER_1) = 0 hits(PLAYER_2) = 0 opponent = PLAYER_2 playerGrids(PLAYER_1) playerGrids(PLAYER_1) = {} shots(PLAYER_2) = {} turn = PLAYER_1	STAGE	deployFleet(PLAYER_2((1)-3),(2)-3),(3)-3)))> SUCCESS deployFleet(PLAYER_2((1)-3),(2)-3),(3)-3)))> SUCCESS deployFleet(PLAYER_2((1)-1),(2)-2),(3)-3)))> SUCCESS deployFleet(PLAYER_2((1)-1),(2)-3),(3)-3)))> SUCCESS deployFleet(PLAYER_2((2)-1),(2)-3),(3)-3)))> SUCCESS deployFleet(PLAYER_2((2)-1),(2)-3),(3)-3)))> SUCCESS deployFleet(PLAYER_2((1)-3),(2)-3),(3)-3)))> SUCCESS deployFleet(PLAYER_2((1)-3),(2)-3),(3)-3)))> SUCCESS deployFleet(PLAYER_2((1)-3),(2)-2),(3)-3)))> SUCCESS deployFleet(PLAYER_2((1)-3),(2)-2),(3)-3)))> SUCCESS deployFleet(PLAYER_2((1)-3),(2)-2),(3)-3)))> SUCCESS	INITIALISATION(fleet=((PLAYER_1 ->(1),(P) SETUP_CONSTANTS(GRID=((1 ->1),(1 ->2)	LAYER_2 ->{})},gameState=DEPL(
fleet(PLAYER_1) = {(1)- fleet(PLAYER_2) = {} gameState = DPELOY_ hits(PLAYER_1) = 0 hits(PLAYER_2) = 0 opponent = PLAYER_2 playerGrids(PLAYER_2) shots(PLAYER_1) = {} thots(PLAYER_2) = {} turn PLAYER_1 GRID = {(11)-1},(11)-22	STAGE $ = \{(1 -51), (1 -52), (1 -53), (1 -54), (1 -55), (1 -56), (1 -57) \\ = \{(1 -51), (1 -52), (1 -53), (1 -54), (1 -55), (1 -56), (1 -57) \\ \} = \{(1 -51), (1 -52), (1 -53), (1 -54), (1 -55), (1 -56), (1 -57) \\ \} = \{(1 -51), (1 -52), (1 -53), (1 -54), (1 -55), (1 -56), (1 -57) \\ \} = \{(1 -51), (1 -52), (1 -53), (1 -54), (1 -55), (1 -56), (1 -57) \\ \} = \{(1 -51), (1 -52), (1 -53), (1 -54), (1 -55), (1 -56), (1 -57), (1 -56), (1 -57), (1 -56), (1 -57), (1 -56), (1 -57), (1 -56), (1 -57), (1 -56), (1 -57), (1 -56), (1$	deployFleet(PLAYER_2((11-3),(11-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-3),(11-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-1),(21-2),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-3),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((21-3),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((21-3),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-3),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-2),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-2),(21-3),(31-3))> SUCCESS deployFleet(PLAYER_2((11-2),(21-3),(31-3))		LAYER_2 ->{})},gameState=DEPL
fleet(PLAYER.1) = ((1) fleet(PLAYER.2) = {} garmeState = DEPLOY_ hits(PLAYER.1) = 0 opponent = PLAYER.2 = 0 opponent = PLAYER.2 = playerGrids(PLAYER.1) playerGrids(PLAYER.1) bhots(PLAYER.2) = {} turn = PLAYER.1 GRID = ((11)-1),(11)-2) aridSize = 10	STAGE $ = \{(1 ->1), (1 ->2), (1 ->3), (1 ->4), (1 ->5), (1 ->6), (1 ->7), \dots \\ = \{(1 ->1), (1 ->2), (1 ->3), (1 ->4), (1 ->5), (1 ->6), (1 ->7), \dots \\ , (1 ->3), (1 ->4), (1 ->5), (1 ->6), (1 ->7), (1 ->8), (1 ->9), (1 ->9), (1 ->$	deployFleet(PLAYER_2,((11->1),(11->3),(3)->1))> SUCCESS deployFleet(PLAYER_2,((11->1),(21->3),(3)->1))> SUCCESS deployFleet(PLAYER_2,((11->1),(21->3),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((11->1),(21->2),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((21->1),(21->3),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((21->1),(21->2),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((21->1),(21->2),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((11->3),(21->1),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((11->3),(21->2),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((11->3),(21->2),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((11->2),(21->3),(3)->1)))> SUCCESS deployFleet(PLAYER_2,((11->2),(21->3),(3)->1))> SUCCESS deployFleet(PLAYER_2,((11->2),(21->3),(3)->1))	SETUP_CONSTANTS(GRID={(1 -> 1),(1 -> 2)	LAYER, 2 ->(3)), gameState=DEPL' (,1 ->3), (1 ->4), (1 ->5), (1 ->6), (1
fleet(PLAYER.1) = {(1) fleet(PLAYER.2) = {} } gameState = DEPLOY_hits(PLAYER.2) = {} } opponent = PLAYER.2 = {} ohts(PLAYER.1) = {} ohts(PLAYER.1) = {} ohts(PLAYER.2) = {} turn = PLAYER.1 = {} offile = {} f(1) = {} 1, (1) = {} 2, (	STAGE $= \{(1 +3),(1 +3),(1 +3),(1 +3),(1 +5),(1 +5),(1 +7),\\ = \{(1 +3),(1 +2),(1 +3),(1 +3),(1 +5),(1 +5),(1 +5),(1 +7),\\ ,(1 +3),(1 +3),(1 +5),(1 +5),(1 +7),(1 +8),(1 +9),(1 +7),(1 +8$	deployFleet(PLAYER_2((11-3),(11-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-3),(11-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-1),(21-2),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-3),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((21-3),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((21-3),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-3),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-2),(21-3),(31-3)))> SUCCESS deployFleet(PLAYER_2((11-2),(21-3),(31-3))> SUCCESS deployFleet(PLAYER_2((11-2),(21-3),(31-3))	report =	LAYER, 2 ->(3)), gameState=DEPL' (,1 ->3), (1 ->4), (1 ->5), (1 ->6), (1
fleet(PLAYER, 1) = ((1) - ((1) - (1)	= \( \left( \right( \right) \right)	deployFleet(PLAYER_2((1)=3),(2)=3),(3)=3)))> SUCCESS deployFleet(PLAYER_2((1)=3),(2)=3),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=1),(1)=2),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=3),(1)=2),(3)=3)))> SUCCESS deployFleet(PLAYER_2,(2)=3),(3)=3),(3)=3)))> SUCCESS deployFleet(PLAYER_2,(2)=3),(3)=3),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=3),(2)=3),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=3),(2)=3),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=3),(2)=2),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=3),(2)=2),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=3),(2)=2),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=3),(2)=2),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=3),(2)=2),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=2),(2)=2),(3)=3)))> SUCCESS deployFleet(PLAYER_2,((1)=2),(2)=2),(3)=3))> SUCCESS deployFleet(PLAYER_2,((1)=2),(2)=2),(3)=3))> SUCCESS deployFleet(PLAYER_2,((1)=2),(2)=2),(3)=3))> SUCCESS deployFleet(PLAYER_2,((1)=2),(2)=2),(3)=3))	report = INVALID_PLACEMENT  History (4)	Pass
fleet(PLAYER.1) = {(1) - }}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}	= {(1 ->1),(1 ->2),(1 ->3),(1 ->4),(1 ->5),(1 ->6),(1 ->7) = {(1 ->1),(1 ->2),(1 ->3),(1 ->4),(1 ->5),(1 ->6),(1 ->7) (1 ->3),(1 ->4),(1 ->6),(1 ->7),(1 ->8),(1 ->9),(1 ->7)  Invalid Fleet Deployment  utput  es (15)	deployFleet(PLAYER_2((1)→1),(1)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2((1)→1),(2)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2,((1)→1),(1)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2,((1)→1),(1)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(2)→1),(2)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(2)→1),(2)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(1)→3),(2)→3),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(1)→3),(2)→3),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(1)→3),(2)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(1)→2),(2)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(2)→2),(2)→3),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(2)→2),(2)→3),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(1)→2),(2)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_2,(1)→2),(2)→2),(3)→1)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2),(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2),(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2),(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2),(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2),(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2,(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2,(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2,(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2,(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2,(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2,(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2,(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1),(1)→2,(1)→3)))→SUCCESS deployFleet(PLAYER_1,(1)→1,(1)→2,(1)→3)))→SUCCESS	report = INVALID_PLACEMENT  deployFleet(PLAYER_1,(1 ->1),(1 ->2),(1 ->4),(1 ->1),(1 ->2),(1 ->4),(1 ->1),(1 ->2),(1 ->4),(1 ->1),(1 ->2),(1 ->4),(1 ->1),(1 ->2),(1 ->2),(1 ->1),(1 ->1),(1 ->2),(1 ->2),(1 ->1),(1 ->2),(1 ->2),(1 ->1),(1 ->2),(1 ->	Pass  Pass  Pass

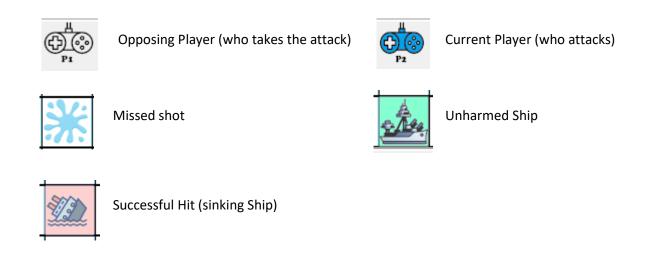




## 4 Graphical Visualization

Regarding the Battleship game B specification, Graphical visualization also implemented using an Animation Function. Following are the main Indicators and various states of the graphical visualization of the Battleship B specification.

#### 4.1 Indicators



#### 4.2 States of the Game

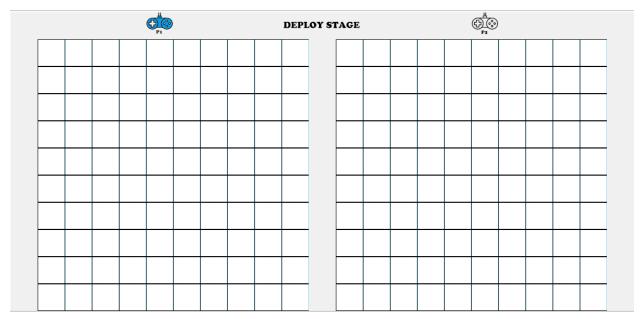


Figure 4: Deploy Game Stage (Initial Stage)

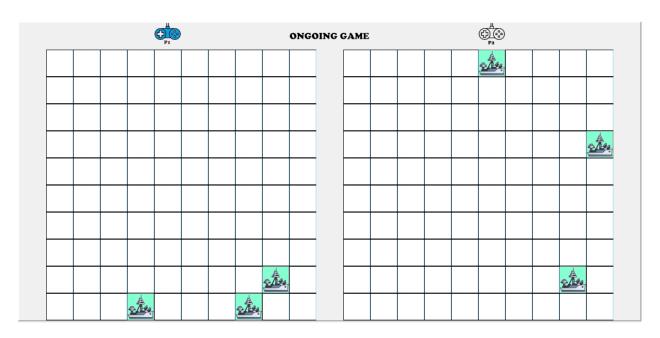


Figure 5: After the both the players placed their own fleets.

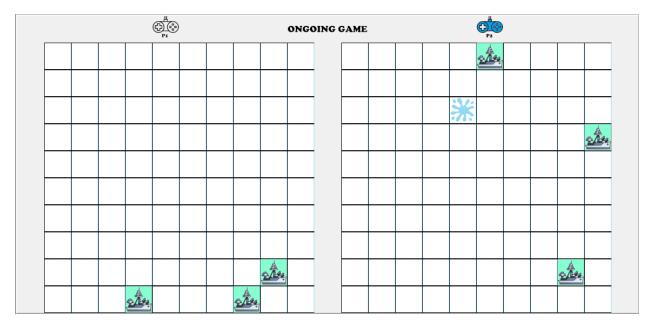


Figure 6: Player 1 fires a shot and Misses.

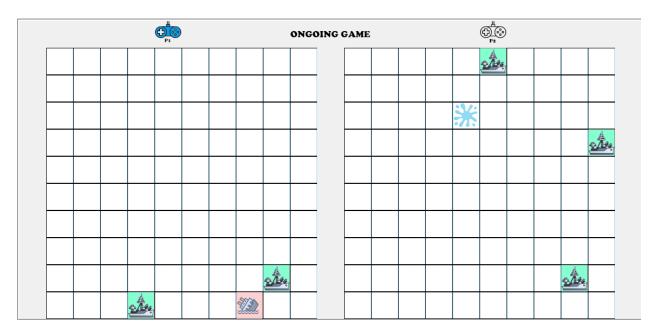


Figure 7: Player 2 Fires a shot and makes a successful hit.

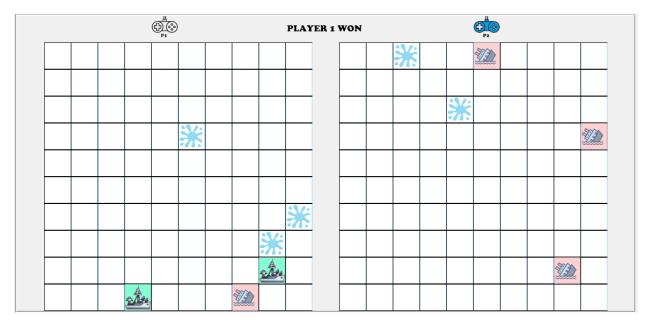


Figure 8: Player 1 sink all the ships of Player 2's Board and Win.

# 5 State Graph Visualization.

Since the State Graph visualization of the battleship B specification is too large to display inside this report it is attached as a separate PDF down below. This state graph visualization is captured during ONGOING\_GAME state after deploy fleets and fire some shots.

