# Partitioning matrix and modifying min sum algorithm

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## Min sum decoding algorithm

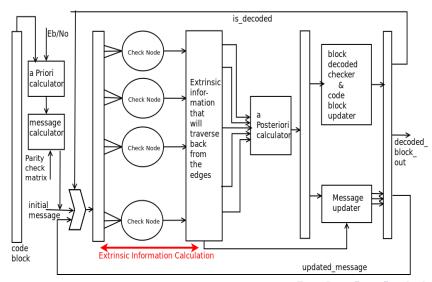


#### main.c

```
readMatrix() // reads the parity check matrix
readCodeBlock() // reads the input code block
minSumDecode() // decode the code block
findAccuracy() // check accuracy of decoded block
```

#### minSumDecode() :

```
initialize_aPriori()
initializeMessage()
while nitr > Max_nitr do
  initialize\_aPosteriori() \Leftarrow aPriori
  initializeExtrinsicInfo() \Leftarrow 0
  checkNodeComputeEngine()
  is\_decoded = checkIsDecode()
  if is decoded = 1 then
     break
  else
     updateMessage()
  end if nitr + +
end while
```



## Algorithmic complexity at each stage

- A priori calculation : O(m)
- Message calculation :  $O(m \times p)$
- Extrinsic information calculation :  $O(m \times p \times (p-1))$  $\approx O(mp^2)$
- A posteriori calculation :  $O(m \times p)$
- Message updation :  $O(m \times p)$
- block decoded calculation & code block updation : O(m)

## Partitioning matrix



After partitioning the matrix we get four matrices as follows :

$$H = \begin{bmatrix} H11 & H12 \\ \hline H21 & H22 \end{bmatrix}$$

example :

$$\begin{bmatrix} c1 & c2 & c3 & c4 & c5 & c6 & c7 & c8 \\ \hline r1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ r2 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 \\ r3 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 0 \\ r4 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 \end{bmatrix} \Rightarrow \begin{bmatrix} c4 & c6 & c7 & c1 & c2 & c3 & c8 & c5 \\ \hline r2 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 \\ \hline r3 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ \hline r1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 \\ \hline r4 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

■ H12 and H21 are highly sparse.

## Modified min sum algorithm



#### main.c

```
Require: Parity check matrix in row compressed form.
readMatrixH11()
readMatrixH12()
readMatrixH21()
readMatrixH22()
readCodeBlock1()
readCodeBlock2()
modifiedMinSumDecode()
findAccuracy()
```

### modifiedMinSumDecode() :

```
initialize_aPriori(aPriori1)
initialize_aPriori(aPriori2)
initializeMessage(message11)
initializeMessage(message12)
initializeMessage(message21)
initializeMessage(message22)
while nitr > Max_nitr do
  initialize_aPosteriori(aPosteriori1) \Leftarrow aPriori1
  initialize_aPosteriori(aPosteriori2) \Leftarrow aPriori2
  initializeExtrinsicInfo(ext\_info11) \leftarrow 0
  initializeExtrinsicInfo(ext\_info12) \leftarrow 0
  initializeExtrinsicInfo(ext\_info21) \leftarrow 0
  initializeExtrinsicInfo(ext_info22) \leftarrow 0
```

#### modifiedMinSumDecode() :

#### while ... do

. . .

```
computeEngine(H11, message11, ext_info11, trans_info11_12)
computeEngine(H22, message22, ext_info22, trans_info22_12)
computeEngine(H12, message12, ext_info12, trans_info12_11)
computeEngine(H21, message21, ext_info21, trans_info21_22)
transverseCorrection(H11, transverse_info12_11, ext_info11)
transverseCorrection(H22, transverse_info21_22, ext_info22)
transverseCorrection(H21, transverse_info22_21, ext_info21)
transverseCorrection(H12, transverse_info11_12, ext_info12)
update_aPosteriori(H11, ext_info11, aPosteriori1)
update_aPosteriori(H22, ext_info22, aPosteriori2)
update_aPosteriori(H12, ext_info12, aPosteriori1)
update_aPosteriori(H21, ext_info21, aPosteriori2)
```

#### modifiedMinSumDecode() :

```
while ... do
  is\_decoded1 = checklsdecoded(code\_block1, aPosteriori1)
  is\_decoded2 = checklsdecoded(code\_block2, aPosteriori2)
  if (is\_decoded1\&\&is\_decoded2) == 1 then
    break
  else
     updateMessage(ext_info11, aPosteriori1, message11)
     updateMessage(ext_info22, aPosteriori2, message22)
     updateMessage(ext_info12, aPosteriori1, message12)
     updateMessage(ext_info21, aPosteriori2, message21)
  end if
  nitr + +
end while
```

