



Sunbeam Institute of Information Technology
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Algorithms and Data structures

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- organising data inside memory for efficient processing along with operations like add, delete, search, etc which can be performed on data.
- eg stack - push/pop/peek

- data structures are used to achieve
 - Abstraction
Abstract Data Types (ADT)
 - Reusability
 - Efficiency
time
space

Types of data structures

Linear data structures (Basic)

- data is organised sequentially/ linearly



- data can be accessed sequentially
e.g. Array, structure/class, stack, queue,
lined list

Hash table

Non linear data structures (Advanced)

- data is organised in multiple levels (hierarchy)

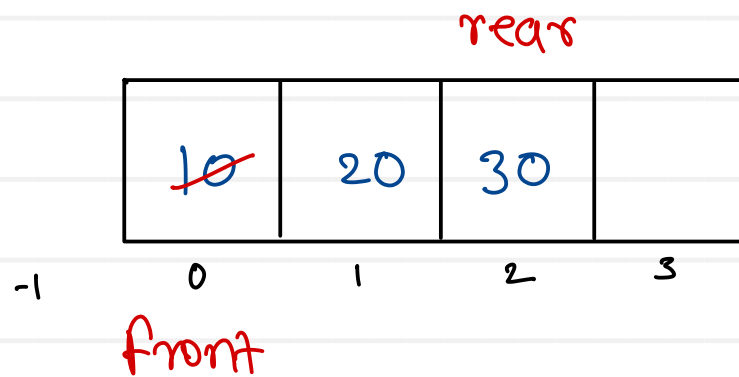


- data can not be accessed sequentially
e.g. Tree, Graph

Linear queue

- linear data structure which has two ends - front and rear
- Data is inserted from rear end and removed from front end
- Queue works on the principle of “First In First Out” / “FIFO”

capacity = 4

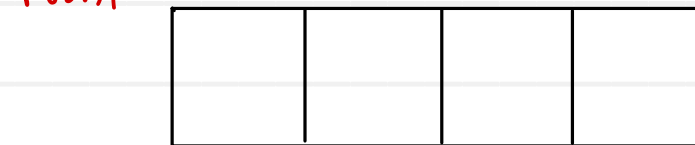


Operations :

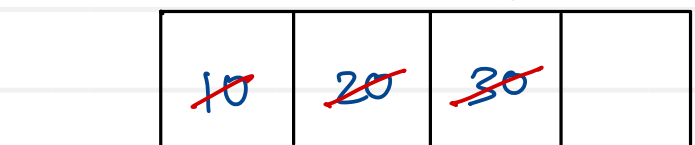
1. Push / enqueue / add / insert :
 - a. reposition rear (inc)
 - b. add value at rear index
2. Pop / dequeue / delete / remove :
 - a. reposition front (inc)
3. Peek :
 - a. read / return data at front + 1 index

Linear queue - Conditions

Empty
front



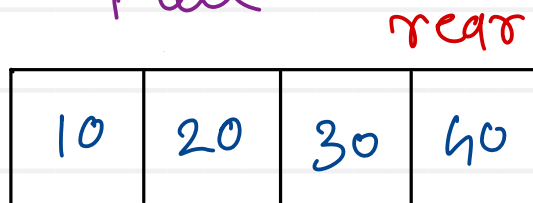
-1 rear 0 1 2 3



-1 0 1 2 3 front

front == rear

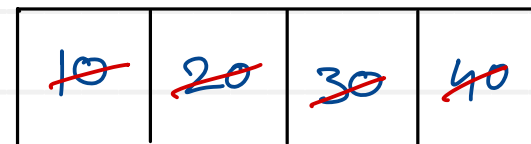
Full



-1 front

rear == size - 1

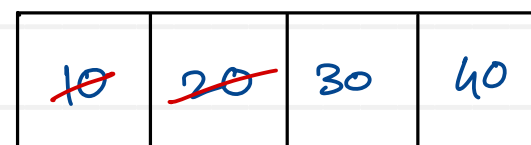
rear



-1 0 1 2 3 front

pop():
if(front == rear)
front = rear = -1;

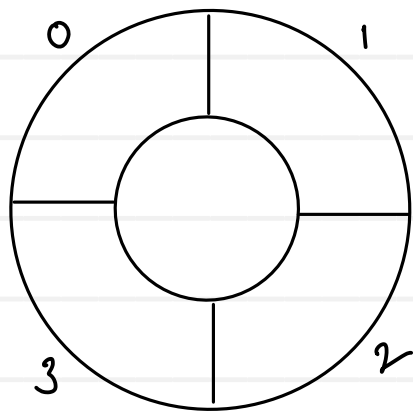
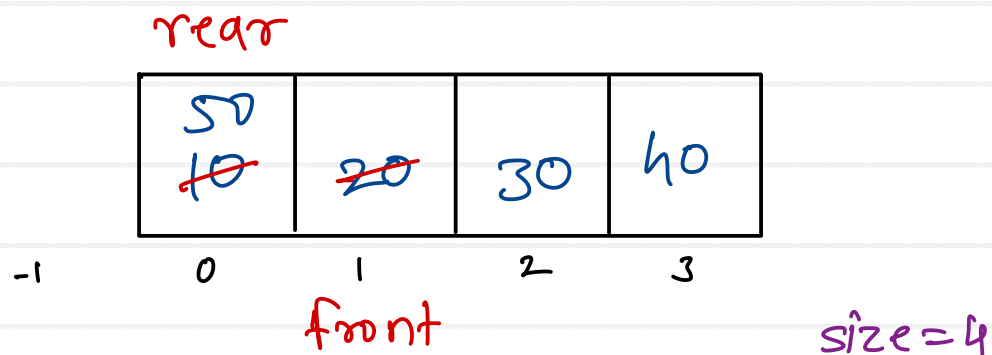
rear



-1 0 1 2 3 front

if few initial locations of queue are vacant, we can not reuse them till queue is not empty, this leads to poor memory utilization

Circular queue



$$\text{front} = (\text{front} + 1) \% \text{size}$$

$$\text{rear} = (\text{rear} + 1) \% \text{size}$$

$$\text{front} = \text{rear} = -1$$

$$= (-1 + 1) \% 4 = 0$$

$$= (0 + 1) \% 4 = 1$$

$$= (1 + 1) \% 4 = 2$$

$$= (2 + 1) \% 4 = 3$$

$$= (3 + 1) \% 4 = 0$$

Operations :

1. Push / enqueue / add / insert :

- reposition rear (inc)
- add value at rear index

2. Pop / dequeue / delete / remove :

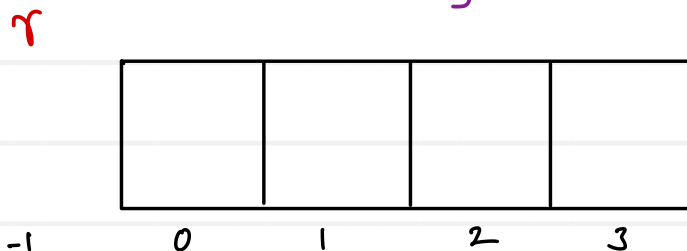
- reposition front (inc)

3. Peek :

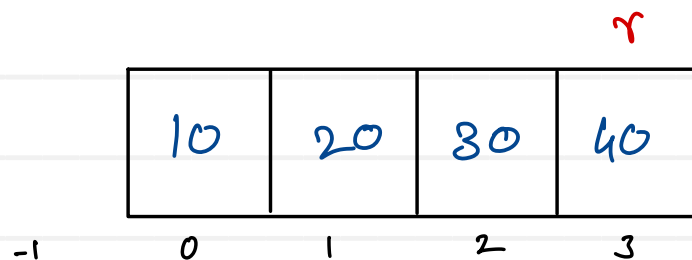
- read / return data at front + 1 index

Circular queue - Conditions

Empty

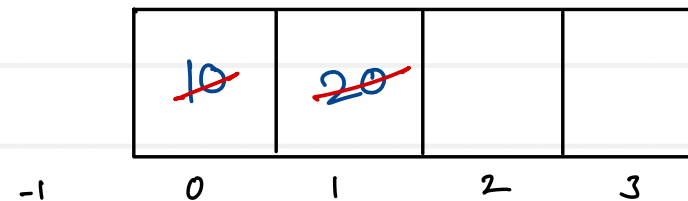


$front == rear \ \&\& \ rear == -1$



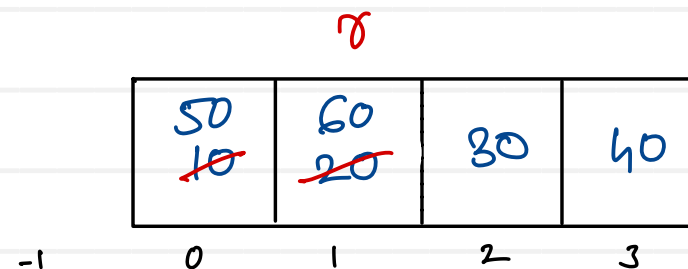
$front == -1 \ \&\& \ rear == size - 1$

r



pop() : if (front == rear)
front = rear = -1

Full



$front == rear \ \&\& \ rear != -1$

- Stack is a linear data structure which has only one end - top
- Data is inserted and removed from top end only.
- Stack works on principle of "Last In First Out" / "LIFO"

capacity = 4

Operations :

1. Push :

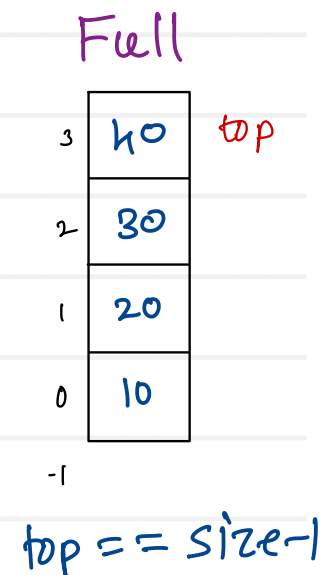
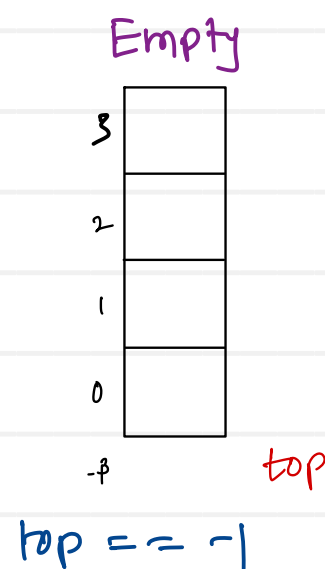
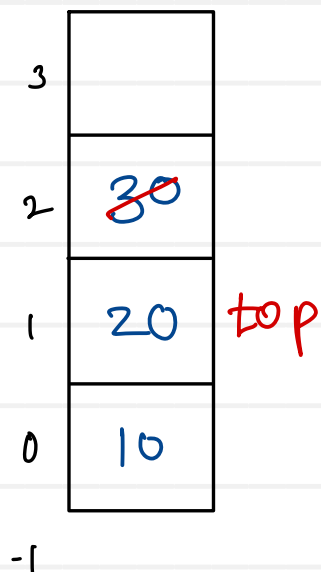
- reposition top (inc)
- add value at top index

2. Pop :

- reposition top (dec)

3. Peek :

- read/ return data of top index



Ascending stack

$top = -1$

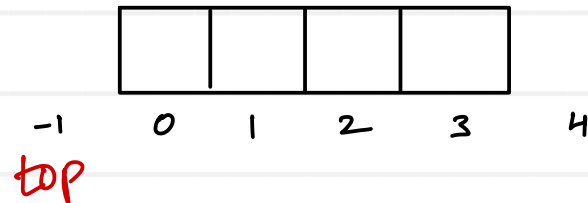
push : $top++$
 $arr[top] = value$

pop : $top--$

peek : $arr[top]$

Empty : $top == -1$

Full : $top == size-1$



Descending stack

$top = size$

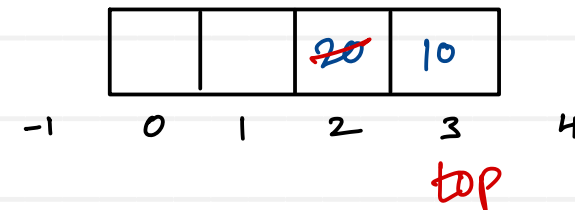
push : $top--$
 $arr[top] = value$

pop : $top++$

peek : $arr[top]$

Empty : $top == size$

Full : $top == 0$



Stack

- Parenthesis balancing — *lexical analysis*
- Expression conversion and evaluation
- Function calls
- Used in advanced data structures for traversing

- **Expression conversion and evaluation:**

- ✓ Infix to postfix
- ✓ Infix to prefix
- ✓ Postfix evaluation
- ✓ Prefix evaluation

Expression: combination of operands & operators

1. Infix : $a + b$ (human)

2. Prefix : $+ ab$

3. Postfix : $ab +$

} (computer/machine)

↓
CPU
↓
ALU

Queue

- Jobs submitted to printer [*spooler directory*]
- In Network setups – file access of file server machine is given to First come First serve basis
- Calls are placed on a queue when all operators are busy
- Used in advanced data structures to give efficiency.
- Process waiting queues in OS

Postfix Evaluation

- Process each element of postfix expression from left to right
- If element is operand
 - Push it on a stack
- If element is operator
 - Pop two elements (Operands) from stack, in such a way that
 - Op2 – first popped element
 - Op1 – second popped element
 - Perform current element (Operator) operation between Op1 and Op2
 - Again push back result onto the stack
- When single value will remain on stack, it is final result
- e.g. $4\ 5\ 6\ *\ 3\ /\ +\ 9\ +\ 7\ -$

Postfix evaluation

Postfix expression : 4 5 6 * 3 / + 9 + 7 -

left \longrightarrow right

Result = 16

- ⑤ $23 - 7 = 16$
- ④ $14 + 9 = 23$
- ③ $4 + 10 = 14$
- ② $30 / 3 = 10$
- ① $5 * 6 = 30$

16
7
23
9
14
10
3
30
6
5
4

stack

Prefix Evaluation

- Process each element of prefix expression from right to left
- If element is operand
 - Push it on a stack
- If element is operator
 - Pop two elements (Operands) from stack, in such a way that
 - Op1 – first popped element
 - Op2 – second popped element
 - Perform current element (Operator) operation between Op1 and Op2
 - Again push back result onto the stack
- When single value will remain on stack, it is final result
- e.g. - + + 4 / * 5 6 3 9 7

Prefix evaluation

Prefix expression : - + + 4 / * 5 6 3 9 7

left ← ————— right

Result = 16

$$23 - 7 = 16$$

$$14 + 9 = 23$$

$$4 + 10 = 14$$

$$30 / 3 = 10$$

$$5 * 6 = 30$$

16
23
14
4
10
30
5
6
3
9
7

infix : 11 + 22

prefix : + 11 22

postfix : "11 22 +"

String arr[]
= postfix.split(",");

arr[] = { "11", "22", "+" }

- Process each element of infix expression from left to right
- If element is Operand
 - Append it to the postfix expression
- If element is Operator
 - If priority of topmost element (Operator) of stack is greater or equal to current element (Operator), pop topmost element from stack and append it to postfix expression
 - Repeat above step if required
 - Push element on stack
- Pop all remaining elements (Operators) from stack one by one and append them into the postfix expression
- e.g. $a * b / c * d + e - f * h + i$

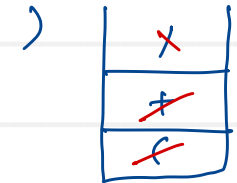
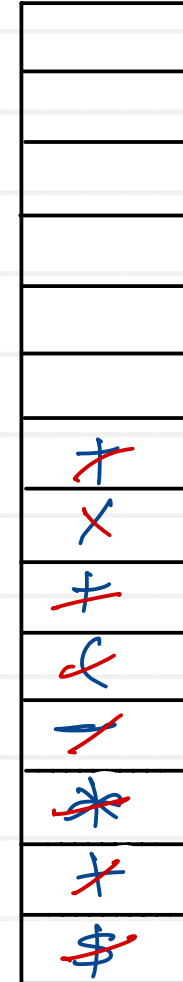


Infix to Postfix conversion

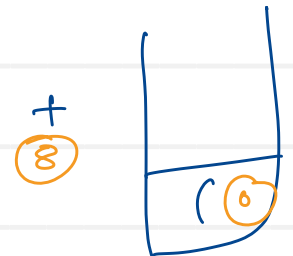
Infix expression : $1 * 9 + 3 * 4 - (6 + 8 / 2) + 7$

left \longrightarrow right

Postfix expression : $19 \$ 34 * + 682 / + - 7 +$



```
while (st.peek() != 'c')
    expr.append(st.pop());
st.pop();
```



Infix to Prefix Conversion

- Process each element of infix expression from right to left
- If element is Operand
 - Append it to the prefix expression
- If element is Operator
 - If priority of topmost element of stack is greater than current element (Operator), pop topmost element from stack and append it to prefix expression
 - Repeat above step if required
 - Push element on stack
- Pop all remaining elements (Operators) from stack one by one and append them into the prefix expression
- Reverse prefix expression
- e.g. $a * b / c * d + e - f * h + i$

Infix to Prefix conversion

Infix expression : $1 \$ 9 + 3 * 4 - (6 + 8 / 2) + 7$

left ← right

Expression : $7 2 8 / 6 + 4 3 * 9 1 \$ + - +$

Prefix expression : $+ - + \$ 1 9 * 3 4 + 6 / 8 2 7$

f

\$
+
*
-
+
7
2
+

Prefix to Postfix

- Process each element of prefix expression from right to left
- If element is an Operand
 - Push it on to the stack
- If element is an Operator
 - Pop two elements (Operands) from stack, in such a way that
 - Op1 – first popped element
 - Op2 – second popped element
 - Form a string by concatenating Op1, Op2 and Opr (element)
 - String = “Op1+Op2+Opr”, push back on to the stack
- Repeat above two steps until end of prefix expression.
- Last remaining on the stack is postfix expression
- e.g. $* + a b - c d$

Postfix to Infix

- Process each element of postfix expression from left to right
- If element is an Operand
 - Push it on to the stack
- If element is an Operator
 - Pop two elements (Operands) from stack, in such a way that
 - Op2 – first popped element
 - Op1 – second popped element
 - Form a string by concatenating Op1, Opr (element) and Op2
 - String = “Op1+Opr+Op2”, push back on to the stack
- Repeat above two steps until end of postfix expression.
- Last remaining on the stack is infix expression
- E.g. a b c - + d e – f g – h + / *



Thank you!!!

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