

# GP Write Up 7

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October 15, 2018

Experimental results

## 1. Results comparison Naive vs Convolutions with Conjugate gradient loss

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All the experiments are performed using the squared exponential kernel:

$$k(x, y) = \sigma_f^2 \exp\left(\frac{(x - y)^T (x - y)}{2l^2}\right) \quad (1)$$

In the naive way we maximize the marginal log likelihood wrt to  $\sigma_f$  and  $l$ :

$$\log p(y|X) = -0.5y^T (K + \sigma_n^2 I)y - 0.5 \log |K + \sigma_n^2 I| - 0.5n \log(2\pi) \quad (2)$$

For the training data we used three different smooth functions on a grid of size  $50 \times 50$ , with 5% of the observations missing and are filled with  $\mathcal{N}(0, 10^{100})$ .

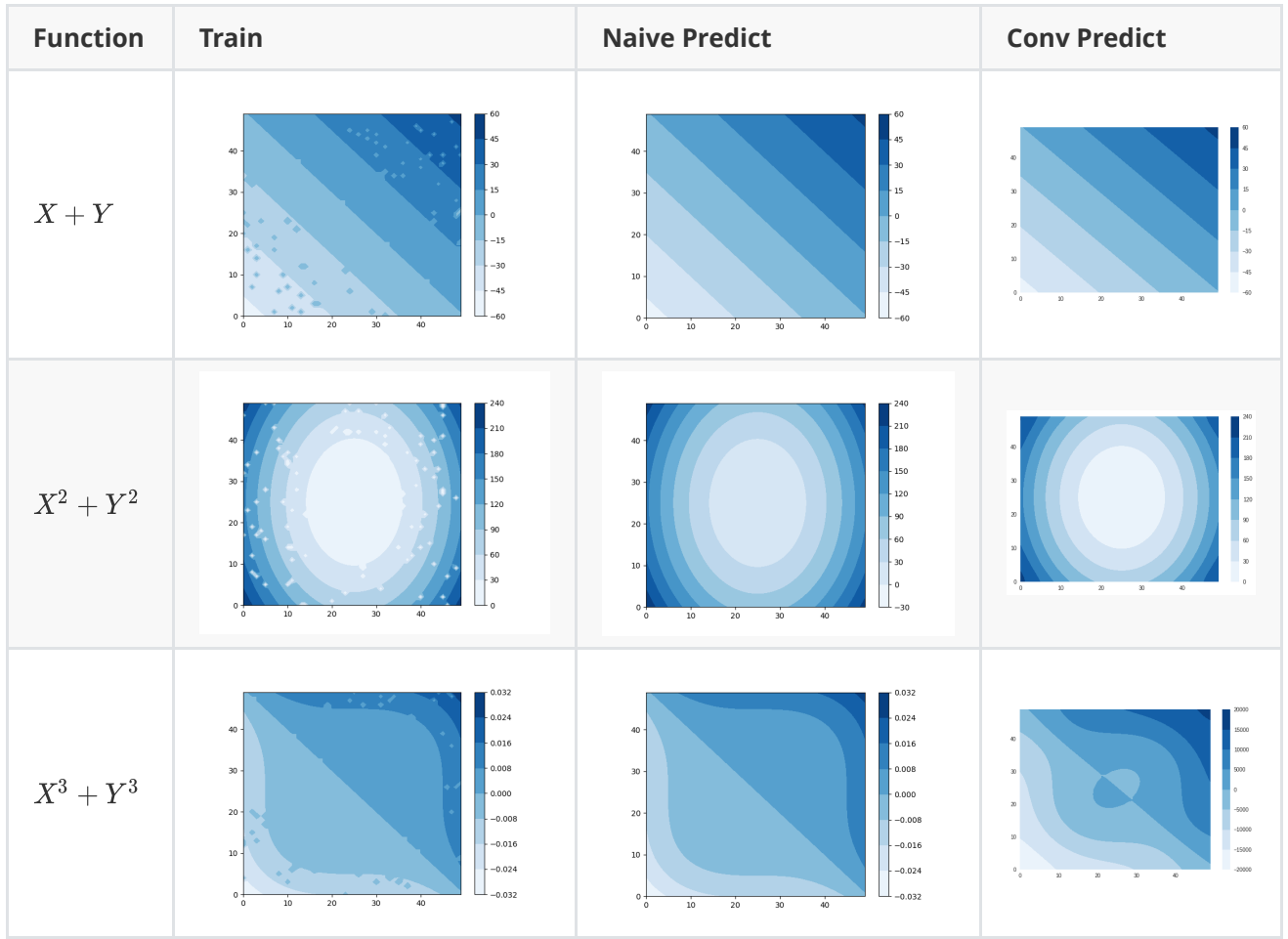
The convolution implementation uses the conjugate gradient loss and the network is run for 10k iterations, with  $\sigma_f, l$  set to 0.1 and 10 respectively.

We compare the performance between the methods by taking the predicted mean for the naive and convolution methods and obtaining the squared l2 norm between the predicted mean and the training data without the imaginary observations:

$$L(y_{pred}, y_{train}) = ((y_{pred} - y_{train}) * mask)^2 \quad (3)$$

For the functions described below:

$$X \in [-25, 25], Y \in [-25, 25] \quad (4)$$



**Table 1:** Predictions for naive gp and conjugate gradient methods against the training data with missing observations. Each of the above images are contour plots.

Function	Naive , $\sigma_f, l$	Naive loss	Conv Loss
$X + Y$	5.6,10.7	$1.8 \times 10^{-5}$	464.6
$X^2 + Y^2$	5.9,9.8	0.0014	4k
$X^3 + Y^3$	4.7,10.9	$9.6 \times 10^{-11}$	$10^{10}$

**Table 2:** Hyper parameters learned in naive gp, loss incurred according to equation (3) for naive and conjugate gradient implementation.