

1. Points (-2,2),(1,1).

$$\begin{aligned} 1 + \lambda < (-2, 2), (1, 1) > -\lambda < (-2, 2), (-2, 2) > -\gamma &= 0 \\ 1 + \lambda < (-2, 2), (1, 1) > -\lambda < (1, 1), (1, 1) > -\gamma &= 0 \end{aligned} \quad (1)$$

The above equation simplifies to:

$$\begin{aligned} 1 - 8\lambda - \gamma &= 0 \\ 1 - 2\lambda + \gamma &= 0 \end{aligned} \quad (2)$$

Solving above we get: $\lambda = 1/5$, $\gamma = -3/5 = b$

$$\begin{aligned} \bar{w} &= \lambda_1 \bar{x}_1 - \lambda_2 \bar{x}_2 \\ \bar{w} &= 1/5(-2, 2), -1/5(1, 1) = \left(\frac{-3}{5}, \frac{1}{5} \right) \end{aligned} \quad (3)$$

we can confirm the value of b

$$\begin{aligned} b &= 1 - \left(\frac{-3}{5}, \frac{1}{5} \right) \cdot (-2, 2) = 1 - \frac{8}{5} = -3/5 = \gamma \\ b &= -1 - \left(\frac{-3}{5}, \frac{1}{5} \right) \cdot (1, 1) = -1 - \frac{-2}{5} = -3/5 = \gamma \end{aligned} \quad (4)$$

2. Points (1,1),(4,3).

$$\begin{aligned} 1 + \lambda < (1, 1), (4, 3) > -\lambda < (1, 1), (1, 1) > -\gamma &= 0 \\ 1 + \lambda < (1, 1), (4, 3) > -\lambda < (4, 3), (4, 3) > -\gamma &= 0 \end{aligned} \quad (5)$$

The above equation simplifies to:

$$\begin{aligned} 1 + 5\lambda - \gamma &= 0 \\ 1 - 18\lambda + \gamma &= 0 \end{aligned} \quad (6)$$

Solving above we get: $\lambda = 2/13$, $\gamma = 23/13 = b$

$$\begin{aligned}\bar{w} &= \lambda_1 \bar{x}_1 - \lambda_2 \bar{x}_2 \\ \bar{w} &= 2/13(1, 1) - 2/13(4/3) = \left(\frac{-6}{13}, \frac{-4}{13}\right)\end{aligned}\tag{7}$$

we can confirm the value of b

$$\begin{aligned}b &= 1 - \left\langle \left(\frac{-6}{13}, \frac{-4}{13}\right), (1, 1) \right\rangle = 1 - \frac{-10}{13} = 23/13 = \gamma \\ b &= -1 - \left\langle \left(\frac{-6}{13}, \frac{-4}{13}\right), (4, 3) \right\rangle = -1 - \frac{-36}{13} = 23/13 = \gamma\end{aligned}\tag{8}$$

3. Points $(2, -2), (-1, 1)$.

$$\begin{aligned}1 + \lambda < (2, -2), (-1, 1) > -\lambda < (2, -2), (2, -2) > -\gamma &= 0 \\ 1 + \lambda < (2, -2), (-1, 1) > -\lambda < (-1, 1), (-1, 1) > -\gamma &= 0\end{aligned}\tag{9}$$

The above equation simplifies to:

$$\begin{aligned}1 - 12\lambda - \gamma &= 0 \\ 1 - 4\lambda + \gamma &= 0\end{aligned}\tag{10}$$

Solving above we get: $\lambda = 1/9$, $\gamma = -1/3 = b$

$$\begin{aligned}\bar{w} &= \lambda_1 \bar{x}_1 - \lambda_2 \bar{x}_2 \\ \bar{w} &= 1/9(2, -2) - 1/9(-1, 1) = \left(\frac{1}{3}, \frac{-1}{3}\right)\end{aligned}\tag{11}$$

we can confirm the value of b

$$\begin{aligned}b &= 1 - \left\langle \left(\frac{1}{3}, \frac{-1}{3}\right), (2, -2) \right\rangle = 1 - \frac{4}{3} = -1/3 = \gamma \\ b &= -1 - \left\langle \left(\frac{1}{3}, \frac{-1}{3}\right), (-1, 1) \right\rangle = -1 - \frac{-2}{3} = -1/3 = \gamma\end{aligned}\tag{12}$$

$(-2, 2)$

$(1, 1)$





