Foundation of Data Science & Analytics (FDSA)

Model Evaluation

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Materials Adaptation:

Classification: Basic Concepts

- Classification: Basic Concepts
- Decision Tree Induction
- Bayes Classification Methods
- Rule-Based Classification
- Model Evaluation and Selection



- Techniques to Improve Classification Accuracy:
 Ensemble Methods
- Summary

Model Evaluation and Selection

- Evaluation metrics: How can we measure accuracy? Other metrics to consider?
- Use validation test set of class-labeled tuples instead of training set when assessing accuracy
- Methods for estimating a classifier's accuracy:
 - Holdout method, random subsampling
 - Cross-validation
 - Bootstrap
- Comparing classifiers:
 - Confidence intervals
 - Cost-benefit analysis and ROC Curves

Classifier Evaluation Metrics: Confusion Matrix

Confusion Matrix:

Actual class\Predicted class	C ₁	¬ C ₁
C_{1}	True Positives (TP)	False Negatives (FN)
¬ C ₁	False Positives (FP)	True Negatives (TN)

Example of Confusion Matrix:

Actual class\Predicted	buy_computer	buy_computer	Total
class	= yes	= no	
buy_computer = yes	6954	46	7000
buy_computer = no	412	2588	3000
Total	7366	2634	10000

- Given m classes, an entry, $CM_{i,j}$ in a confusion matrix indicates # of tuples in class i that were labeled by the classifier as class j
- May have extra rows/columns to provide totals

Multi-class Problem: Confusion Matrix

	C1	C2	C3
C1	TP	Other	Other
C2	Other	TP	Other
C3	Other	Other	TP

Classifier Evaluation Metrics: Accuracy, Error Rate, Sensitivity and Specificity

A\P	С	¬С	
С	TP	FN	Р
¬C	FP	TN	N
	P'	N'	All

- Classifier Accuracy, or Recognition Rate
- Percentage of test set tuples that are correctly classified

$$Accuracy = (TP + TN)/AII$$

Error rate: 1 - accuracy, or

Classifier Evaluation Metrics: Accuracy, Error Rate, Sensitivity and Specificity

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 Classifier Accuracy, or recognition rate: percentage of test set tuples that are correctly classified

Accuracy = (TP + TN)/AII

Error rate: 1 – accuracy, or Error rate = (FP + FN)/All

Class Imbalance Problem:

- One class may be rare, e.g. fraud, or HIV-positive
- Significant majority of the negative class and minority of the positive class
- Sensitivity: True Positive recognition rate
 - Sensitivity = TP/P
- Specificity: True Negative recognition rate
 - Specificity = TN/N

Classifier Evaluation Metrics: Precision and Recall, and F-measures

- Precision: exactness what % of tuples that the classifier labeled as positive are actually positive precision
- **Recall:** completeness what % of positive tuples did the classifier label as positive? $recall = \frac{TP}{TP + FN}$
- Perfect score is 1.0
- Inverse relationship between precision & recall
- **F measure** (F_1 or F-score): harmonic mean of precision and recall, $= \frac{2 \times precision \times recall}{precision + recall}$
- \mathbf{F}_{β} : weighted measure of precision and recall
 - assigns ß times as much weight to recall as to precision

$$F_{\beta} = \frac{(1+\beta^2) \times precision \times recall}{\beta^2 \times precision + recall}$$

Actual Class\Predicted class	cancer = yes	cancer = no	Total	Recognition(%)
cancer = yes	90	210	300	
cancer = no	140	9560	9700	
Total	230	9770	10000	96.50 (accuracy)

Actual Class\Predicted class	cancer = yes	cancer = no	Total	Recognition(%)
cancer = yes	90	210	300	
cancer = no	140	9560	9700	
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$$precision = \frac{TP}{TP + FP}$$

$$recall = \frac{TP}{TP + FN}$$

$$F = \frac{2 \times precision \times recall}{precision + recall}$$

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$$Recall = 90/300 = 30.00\%$$

$$F = \frac{2 \times precision \times recall}{precision + recall}$$

$$F = (2*39.13*30)/(39.13+30)$$

Evaluating Classifier Accuracy: 1. Holdout Method

Holdout method

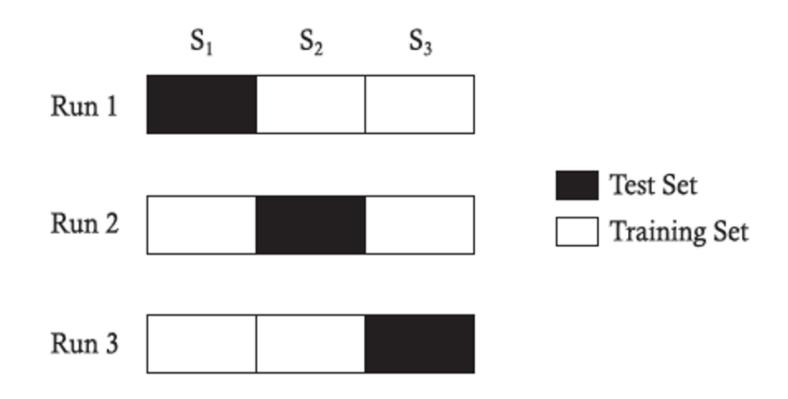
- Given data is randomly partitioned into two independent sets
 - Training set (e.g., 2/3) for model construction
 - Test set (e.g., 1/3) for accuracy estimation
- Random sampling: a variation of holdout
 - Repeat holdout k times, accuracy = avg. of the accuracies obtained

Evaluating Classifier Accuracy: 2. Cross-Validation Methods

- Cross-validation (k-fold, where k = 10 is most popular)
 - Randomly partition the data into k mutually exclusive subsets, each approximately equal size
 - At i-th iteration, use D_i as test set and others as training set
 - Leave-one-out: k folds where k = # of tuples, for small sized data
 - *Stratified cross-validation*: folds are stratified so that class dist. in each fold is approx. the same as that in the initial data

K-fold Cross-Validation

3-fold cross-validation



Evaluating Classifier Accuracy: 3. Bootstrap

Bootstrap

- Works well with small data sets
- Samples the given training tuples uniformly with replacement
 - i.e., each time a tuple is selected, it is equally likely to be selected again and re-added to the training set
- Repeat the sampling procedure k times, overall accuracy of the model:

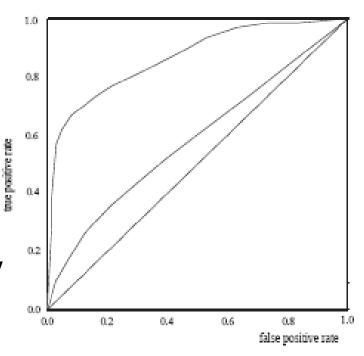
Evaluating Classifier Accuracy: 3. Bootstrap

- Bootstrap : Works well with small data sets
- Several bootstrap methods, and a common one is .632 boostrap
 - A data set with d tuples is sampled d times, with replacement, resulting in a training set of d samples. The data tuples that did not make it into the training set end up forming the test set. About 63.2% of the original data end up in the bootstrap, and the remaining 36.8% form the test set (since $(1 1/d)^d \approx e^{-1} = 0.368$)
 - Repeating sampling procedure k times, overall accuracy of model:

$$Acc(M) = \frac{1}{k} \sum_{i=1}^{k} (0.632 \times Acc(M_i)_{test_set} + 0.368 \times Acc(M_i)_{train_set})$$

Model Selection: ROC Curves

- ROC (Receiver Operating Characteristics) curves: for visual comparison of classification models
- Originated from signal detection theory
- Shows the trade-off between the true positive rate and the false positive rate
- The area under the ROC curve is a measure of the accuracy of the model
- Rank the test tuples in decreasing order: the one that is most likely to belong to the positive class appears at the top of the list
- The closer to the diagonal line (i.e., the closer the area is to 0.5), the less accurate is the model



- Vertical axis represents the true positive rate
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 the false positive rate
- The plot also shows a diagonal line
- A model with perfect accuracy will have an area of 1.0

Issues Affecting Model Selection

Accuracy

classifier accuracy: predicting class label

Speed

- time to construct the model (training time)
- time to use the model (classification/prediction time)
- Robustness: handling noise and missing values
- Scalability: efficiency in disk-resident databases

Interpretability

- understanding and insight provided by the model
- Other measures, e.g., goodness of rules, such as decision tree size or compactness of classification rules

Estimating Confidence Intervals: Classifier Models M₁ vs. M₂

- Suppose we have 2 classifiers, M_1 and M_2 , which one is better?
- Use 10-fold cross-validation to obtain $\overline{err}(M_1)$ and $\overline{err}(M_2)$
- These mean error rates are just estimates of error on the true population of future data cases
- What if the difference between the 2 error rates is just attributed to chance?
 - Use a test of statistical significance
 - Obtain confidence limits for our error estimates

Estimating Confidence Intervals: Null Hypothesis

- Perform 10-fold cross-validation
- Assume samples follow a t distribution with k-1 degrees of freedom (here, k=10)
- Use t-test (or Student's t-test)
- Null Hypothesis: $M_1 \& M_2$ are the same
- If we can reject null hypothesis, then
 - we conclude that the difference between M₁ & M₂ is
 statistically significant
 - Chose model with lower error rate

Estimating Confidence Intervals: t-test

- If only 1 test set available: pairwise comparison
 - For ith round of 10-fold cross-validation, the same cross partitioning is used to obtain $err(M_1)_i$ and $err(M_2)_i$
 - Average over 10 rounds to get $\overline{err}(M_1)$ and $\overline{err}(M_2)$
 - t-test computes t-statistic with k-1 degrees of freedom:

reedom:
$$t = \frac{\overline{err}(M_1) - \overline{err}(M_2)}{\sqrt{var(M_1 - M_2)/k}} \quad \text{where}$$

$$var(M_1 - M_2) = \frac{1}{k} \sum_{i=1}^k \left[err(M_1)_i - err(M_2)_i - (\overline{err}(M_1) - \overline{err}(M_2)) \right]^2$$

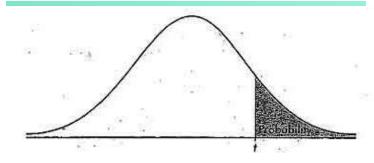
If two test sets available: use non-paired t-test

where
$$var(M_1 - M_2) = \sqrt{\frac{var(M_1)}{k_1} + \frac{var(M_2)}{k_2}},$$

where $k_1 \& k_2$ are # of cross-validation samples used for $M_1 \& M_2$, resp.

Estimating Confidence Intervals:

Table for t-distribution



- Symmetric
- Significance level, e.g., sig = 0.05 or 5% means M₁ & M₂ are *significantly* different for 95% of population
- Confidence limit, z = siq/2

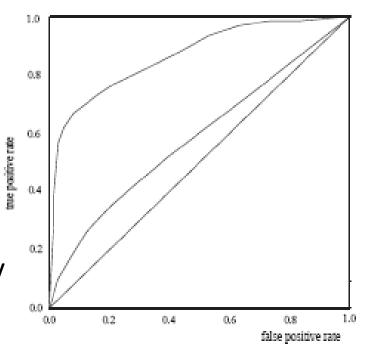
-	. Tail probability p											
df	,25	.20	.15	,10	.05	.025	.02	.01	.005	.0025	.001	.0005
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.6
2	.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.60
3	.765	.978	1.250	1.638	2.353	3,182	3,482	4.541	5.841	7.453	10.21	12.92
4	.741	.941	1.190	1.533	2.132	2.776	2.999	3.747	G 200 E B 200 E	5.598	7.173	8.610
5	.727	.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6.869
6	.718	.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317		5.959
7	.711	.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5,408
8	.706	.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5:041
9	.703	.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.781
10	.700	.879	1.093	1.372	1.812	2.228	2,359	2.764	3.169	3.581	4.144	4.587
11	.697	.876	1.088	1.363	1.796	2,201	2.328	2.718	3.106	3,497	4.025	4.437
12	.695	.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.318
13	.694	.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4.221
14	.692	.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	4.140
15	.691	.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3,733	4.073
16	.690	.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252-	3.686	4.015
17	.689	.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.965
18	.688	.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.922
19	.688	.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.883
20	.687	.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.850
21	.686	.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.819
22	.686	.858	1.061	1.321	1.717	2.074	2,183	2.508	2.819	3.119	3.505	3.792
23	.685	.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768
24	685	.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467.	3.745
25	.684	.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3,450	3.725
26	.684	.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	3.067	3,435	3.707
27	.684	.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.690
28	.683	.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	3.047	3.408	3.674
29	.683	.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.659
30	.683	.854	1.055	1.310	1.697	2.042	2.147	2:457	2.750	3.030	3.385	3.646
40	.681	.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.551
50	.679	.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.496
50	.679	.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3,460
80	.678	.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.416
00	.677	.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.390
00	.675	.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.300
00	.674	.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.291
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.9%

Estimating Confidence Intervals: Statistical Significance

- Are M₁ & M₂ significantly different?
 - Compute t. Select significance level (e.g. sig = 5%)
 - Consult table for t-distribution: Find t value corresponding to k-1 degrees of freedom (here, 9)
 - t-distribution is symmetric: typically upper % points of distribution shown \rightarrow look up value for **confidence limit** z=sig/2 (here, 0.025)
 - If t > z or t < -z, then t value lies in rejection region:</p>
 - Reject null hypothesis that mean error rates of M₁ & M₂ are same
 - Conclude: <u>statistically significant</u> difference between M₁
 & M₂
 - Otherwise, conclude that any difference is chance

Model Selection: ROC Curves

- ROC (Receiver Operating Characteristics) curves: for visual comparison of classification models
- Originated from signal detection theory
- Shows the trade-off between the true positive rate and the false positive rate
- The area under the ROC curve is a measure of the accuracy of the model
- Rank the test tuples in decreasing order: the one that is most likely to belong to the positive class appears at the top of the list
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Issues Affecting Model Selection

Accuracy

classifier accuracy: predicting class label

Speed

- time to construct the model (training time)
- time to use the model (classification/prediction time)
- Robustness: handling noise and missing values
- Scalability: efficiency in disk-resident databases

Interpretability

- understanding and insight provided by the model
- Other measures, e.g., goodness of rules, such as decision tree size or compactness of classification rules

Classification of Class-Imbalanced Data Sets

- Class-imbalance problem: Rare positive example but numerous negative ones, e.g., medical diagnosis, fraud, oil-spill, fault, etc.
- Traditional methods assume a balanced distribution of classes and equal error costs: not suitable for class-imbalanced data
- Typical methods for imbalance data in 2-class classification:
 - Oversampling: re-sampling of data from positive class
 - Under-sampling: randomly eliminate tuples from negative class
 - Threshold-moving: moves the decision threshold, t, so that the rare class tuples are easier to classify, and hence, less chance of costly false negative errors
 - Ensemble techniques: Ensemble multiple classifiers introduced above
- Still difficult for class imbalance problem on multiclass tasks

Issues: Evaluating Classification Methods

- Accuracy
 - classifier accuracy: predicting class label
 - predictor accuracy: guessing value of predicted attributes
- Speed
 - time to construct the model (training time)
 - time to use the model (classification/prediction time)
- Robustness: handling noise and missing values
- Scalability: efficiency in disk-resident databases
- Interpretability
 - understanding and insight provided by the model
- Other measures, e.g., goodness of rules, such as decision tree size or compactness of classification rules

Predictor Error Measures

- Measure predictor accuracy: measure how far off the predicted value is from the actual known value
- **Loss function**: measures the error betw. y_i and the predicted value y_i'
 - Absolute error: | y_i y_i' |
 - Squared error: $(y_i y_i')^2$
- Test error (generalization error): the average loss over the test set

 - Mean absolute error: $\frac{\sum_{i=1}^{d} |y_i y_i'|}{d}$ Mean squared error: $\frac{\sum_{i=1}^{d} (y_i y_i')^2}{\sum_{i=1}^{d} |y_i y_i'|}$ Relative squared error: $\frac{\sum_{i=1}^{d} (y_i y_i')^2}{\sum_{i=1}^{d} |y_i \overline{y}|}$

The mean squared-error exaggerates the presence of outliers

Popularly use (square) root mean-square error, similarly, root relative squared error

Cluster Validation

- For supervised classification we have a variety of measures to evaluate how good our model is
 - Accuracy, precision, recall
- For cluster analysis, the analogous question is how to evaluate the "goodness" of the resulting clusters?
- But "clusters are in the eye of the beholder"!
- Then why do we want to evaluate them?
 - To avoid finding patterns in noise
 - To compare clustering algorithms
 - To compare two sets of clusters
 - To compare two clusters

Internal Measures: Cohesion and Separation

- Cluster Cohesion: Measures how closely related are objects in a cluster
 - Example: SSE
- Cluster Separation: Measure how distinct or wellseparated a cluster is from other clusters
- Example: Squared Error
 - Cohesion is measured by the within cluster sum of squares (SSE)

$$SSE = WSS = \sum_{i} \sum_{x \in C_i} (x - m_i)^2$$

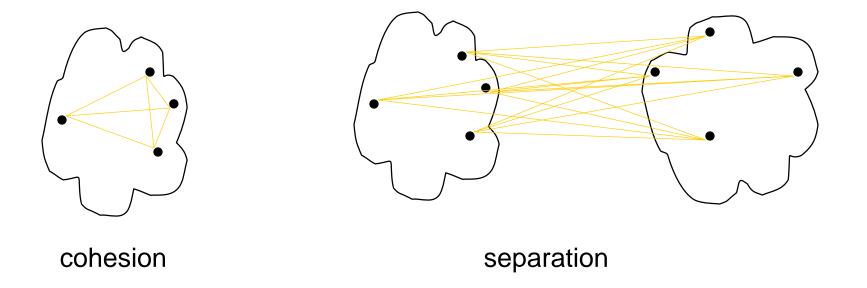
Separation is measured by the between cluster sum of squares

$$BSS = \sum |C_i| (m - m_i)^2$$

• Where ${}^{i}C_{i}$ is the size of cluster i

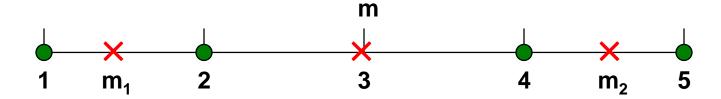
Internal Measures: Cohesion and Separation

- A proximity graph based approach can also be used for cohesion and separation.
 - Cluster cohesion is the sum of the weight of all links within a cluster.
 - Cluster separation is the sum of the weights between nodes in the cluster and nodes outside the cluster.



Internal Measures: Cohesion and Separation

- Example: SSE
 - BSS + WSS = constant



$$SSE = WSS = (1-3)^{2} + (2-3)^{2} + (4-3)^{2} + (5-3)^{2} = 10$$

$$BSS = 4 \times (3-3)^{2} = 0$$

$$Total = 10 + 0 = 10$$

$$SSE = WSS = (1-1.5)^{2} + (2-1.5)^{2} + (4-4.5)^{2} + (5-4.5)^{2} = 1$$

$$BSS = 2 \times (3-1.5)^{2} + 2 \times (4.5-3)^{2} = 9$$

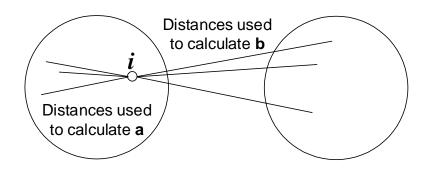
$$Total = 1 + 9 = 10$$

Internal Measures: Silhouette Coefficient

- Silhouette coefficient combines ideas of both cohesion and separation, but for individual points, as well as clusters and clusterings
- For an individual point, i
 - Calculate a = average distance of i to the points in its cluster
 - Calculate $b = \min$ (average distance of i to points in another cluster)
 - The silhouette coefficient for a point is then given by

$$s = (b - a) / max(a,b)$$

- Typically between 0 and 1.
- The closer to 1 the better.



Can calculate the average silhouette coefficient for a cluster or a clustering

External Measures of Cluster Validity: Entropy and Purity

Table 5.9. K-means Clustering Results for LA Document Data Set

Cluster	Entertainment	Financial	Foreign	Metro	National	Sports	Entropy	Purity
1	3	5	40	506	96	27	1.2270	0.7474
2	4	7	280	29	39	2	1.1472	0.7756
3	1	1	1	7	4	671	0.1813	0.9796
4	10	162	3	119	73	2	1.7487	0.4390
5	331	22	5	70	13	23	1.3976	0.7134
6	5	358	12	212	48	13	1.5523	0.5525
Total	354	555	341	943	273	738	1.1450	0.7203

entropy For each cluster, the class distribution of the data is calculated first, i.e., for cluster j we compute p_{ij} , the 'probability' that a member of cluster j belongs to class i as follows: $p_{ij} = m_{ij}/m_j$, where m_j is the number of values in cluster j and m_{ij} is the number of values of class i in cluster j. Then using this class distribution, the entropy of each cluster j is calculated using the standard formula $e_j = \sum_{i=1}^{L} p_{ij} \log_2 p_{ij}$, where the L is the number of classes. The total entropy for a set of clusters is calculated as the sum of the entropies of each cluster weighted by the size of each cluster, i.e., $e = \sum_{i=1}^{K} \frac{m_i}{m} e_j$, where m_j is the size of cluster j, K is the number of clusters, and m is the total number of data points.

purity Using the terminology derived for entropy, the purity of cluster j, is given by $purity_j = \max p_{ij}$ and the overall purity of a clustering by $purity = \sum_{i=1}^{K} \frac{m_i}{m} purity_j$.

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