good jole

## **Submitted by: Anushka Menon and Yashasvee Goel**

## **Answer 1**

For any two sites i,j the interaction is termed as J.

The role of I is as follows:

J>0 → Interaction is ferromagnetic

J<0 → Interaction is anti-ferromagnetic

import matplotlib.pyplot as plt

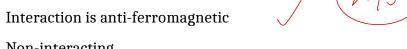
for x in range  $(\hat{N})$ :

return s

s.append(choice((+1,-1)))

 $J=0 \rightarrow Non-interacting$ 

import numpy as np



## **Answer 2**

When we consider periodic boundary conditions, the last spins are considered to be their nearest neighbour of each other.

```
1 -D chain becomes a rung
                                  112/1
                                           How did you apply it in code?)
Answer 3
# Defining the necessary modules
```

from numpy.random import random from random import choice # The 1-D Ising Model def H(J,h,s): # Hamiltonian ret\_value = 0.0 n = len(s)for x in range(n): We start by iterating over all spin states ret value += -J\*(s[(x-1)%n]\*s[x])-h\*s[x] # for periodicboundary condition return ret value def S random(n): Defining array of length n filled with +1 or -1 random spin so that it doesn't needa states and appending it to S it should be

# We have considered J = 1 and k B = 1 as suggested in the question J=1

giolal variable to run.

# After differentiating the expression for <m> analytically, we get

```
the following expression:
                                                        ( paints deduced only for over analysis
def m exact(n,h,T):
    \# ret m = (np.tanh(h/T))/n
                                                       evact in and calculating standard deviation would
    # return float(ret m)
                           n here its supposed to
    sin = np.sinh(h)
                              be hIT and JIT
    cos = np.cosh(h)
    exp = np.exp(-4*J)
    ratio = (cos-np.sqrt(sin**2+exp))/(cos+np.sqrt(sin**2+exp))
                                              There isn't any temperature

Dependence in your exact function

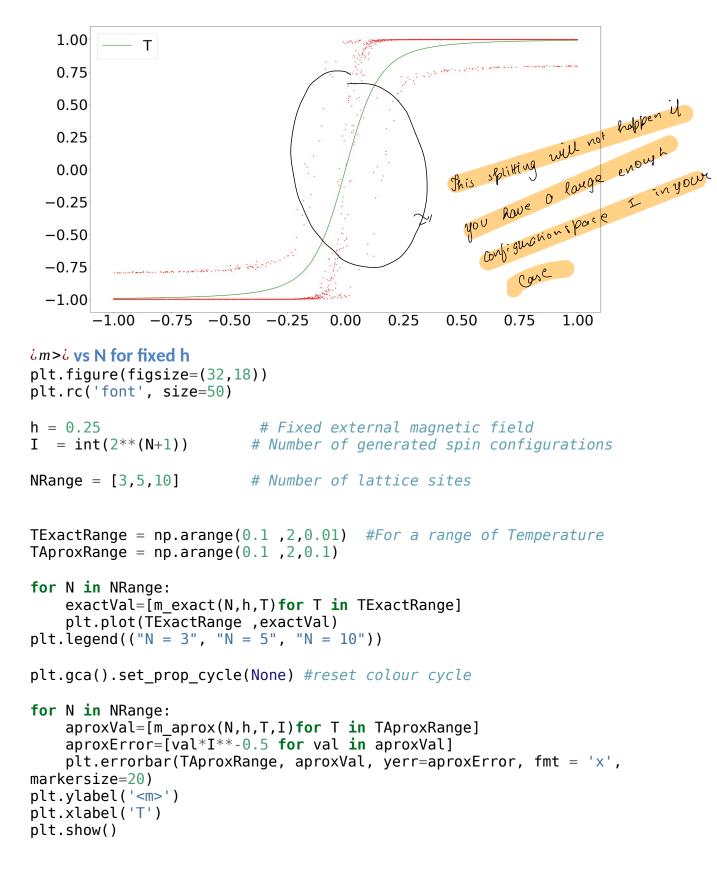
Bhats why your plots don't
    ret value = (1-ratio**N)/(1+ratio**N)
    ret value *= sin/np.sqrt(sin**2+exp)
    return ret value
def m aprox(n,h,T,I):
                                                    agree.
    num = 0.0
    den = 0.0
    for i in range(I):
         S = S random(N)
                                                      # create random
configuration
         num += (sum(S)/N)*np.exp(-H(J,h,S)/T) # use the observable
sum(spin) / #of spins
         den += np.exp(-H(J,h,S)/T)
    return num/den
```

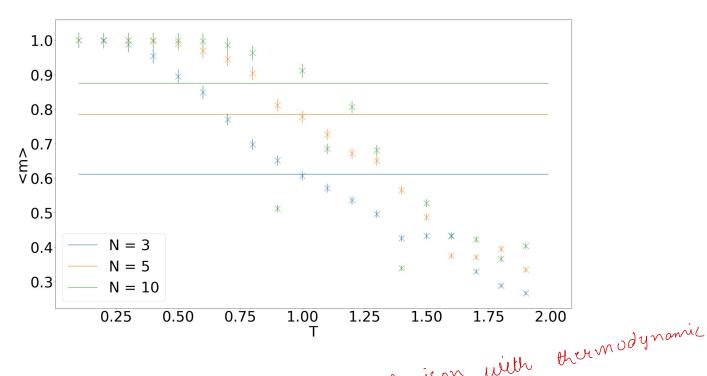
The relevant dimensionless ratios are as follows:

```
aproxError=[val*I**-0.5 for val in aproxVal]
plt.plot(hRange ,exactVal ,'r',color="green")
# We have chosen the value of T as 0.5
plt.legend(("T = 0.5"))
plt.errorbar(hRange, aproxVal, yerr=aproxError, fmt='ro',
markersize=2)
plt.vlabel('<m>')
plt.xlabel('h')
plt.title("Graph for <m> vs h for fixed N")
plt.show()
/tmp/ipvkernel 7392/3058133422.pv:16: UserWarning: color is
redundantly defined by the 'color' keyword argument and the fmt string "r" (-> color=(1.0,\ 0.0,\ 0.0,\ 1)). The keyword argument will take
precedence.
  plt.plot(hRange ,exactVal ,'r',color="green")
ValueError
                                            Traceback (most recent call
last)
Cell In [6], line 20
     17 # We have chosen the value of T as 0.5
     18 plt.legend(("T = 0.5"))
---> 20 plt.errorbar(hRange, aproxVal, yerr=aproxError, fmt='ro',
markersize=2)
     22 plt.ylabel('<m>')
     23 plt.xlabel('h')
File ~/.local/lib/python3.8/site-packages/matplotlib/pyplot.py:2482,
in errorbar(x, y, yerr, xerr, fmt, ecolor, elinewidth, capsize,
barsabove, lolims, uplims, xlolims, xuplims, errorevery, capthick,
data, **kwargs)
   2476 @ copy docstring and deprecators(Axes.errorbar)
   2477 def errorbar(
   2478
                 x, y, yerr=None, xerr=None, fmt='', ecolor=None,
   2479
                 elinewidth=None, capsize=None, barsabove=False,
lolims=False,
                 uplims=False, xlolims=False, xuplims=False,
   2480
errorevery=1,
   2481
                 capthick=None, *, data=None, **kwargs):
-> 2482
            return gca().errorbar(
                 x, y, yerr=yerr, xerr=xerr, fmt=fmt, ecolor=ecolor,
   2483
   2484
                 elinewidth=elinewidth, capsize=capsize,
barsabove=barsabove,
```

```
2485
                lolims=lolims, uplims=uplims, xlolims=xlolims,
   2486
                xuplims=xuplims, errorevery=errorevery,
capthick=capthick,
                **({"data": data} if data is not None else {}),
   2487
**kwargs)
File ~/.local/lib/python3.8/site-packages/matplotlib/ init .py:1423,
in preprocess data.<locals>.inner(ax, data, *args, **kwargs)
   1420 @functools.wraps(func)
   1421 def inner(ax, *args, data=None, **kwargs):
   1422
            if data is None:
-> 1423
                return func(ax, *map(sanitize sequence, args),
**kwarqs)
            bound = new sig.bind(ax, *args, **kwargs)
   1425
   1426
            auto label = (bound.arguments.get(label namer)
   1427
                          or bound.kwarqs.qet(label namer))
File
~/.local/lib/python3.8/site-packages/matplotlib/axes/ axes.py:3587, in
Axes.errorbar(self, x, y, yerr, xerr, fmt, ecolor, elinewidth,
capsize, barsabove, lolims, uplims, xlolims, xuplims, errorevery,
capthick, **kwarqs)
   3584 res = np.zeros(err.shape, dtype=bool) # Default in case of
nan
   3585 if np.any(np.less(err, -err, out=res, where=(err == err))):
            # like err<0, but also works for timedelta and nan.
   3586
-> 3587
            raise ValueError(
                f"'{dep axis}err' must not contain negative values")
   3588
   3589 # This is like
              elow, ehigh = np.broadcast to(...)
   3590 #
   3591 #
              return dep - elow * ~lolims, dep + ehigh * ~uplims
   3592 # except that broadcast to would strip units.
   3593 low, high = dep + np.row stack([-(1 - lolims), 1 - uplims]) *
err
```

ValueError: 'yerr' must not contain negative values





(Not done comparison with love morphism is flow for morphism is have toep)

wind brown because doesn't have toep)

for thermodynamic limit: Take the limit of the theoretical expression in case N-00 you should get

$$\langle m \rangle = -\frac{\sinh(h)}{\int \sinh^2(h) + e^{-4\tilde{J}}}$$
 where  $h = \frac{h}{T}$   $J = \frac{J}{T}$ 

