

Confidence Interval.

1. Population = 1,000,000 men

Sample = 1000 men

$$\mu = 180$$

$$\sigma = 30$$

$$C.I = \mu \pm Z \times \sigma$$

$$= 180 \pm 2 \times SE \text{ (at 95\%)}$$

$$= 180 \pm 2 \times \frac{30}{\sqrt{1000}}$$

$$= 180 \pm 1.89 \Rightarrow (178.11, 181.89)$$

$$2. \sigma = 3.6$$

$$n = 120$$

$$\mu = 16.2$$

$$a) CI \text{ (at 92\%)} = \mu \pm 1.75 SE$$

$$= 16.2 \pm 1.75 \times \frac{3.6}{\sqrt{120}}$$

$$= 16.2 \pm 0.576 \Rightarrow (15.624, 16.776)$$

$$b) Z \times SE = 15 \text{ seconds.}$$

$$= 0.25 \text{ min}$$

$$1.75 \times \frac{3.6}{\sqrt{n}} = 0.25$$

$$\boxed{n = 635}$$

3. a) 2% margin of error and 90% confidence interval.

$$ME = Z \times SE$$

$$0.02 = 1.64 \times \sqrt{\frac{pq}{n}}$$

$$\text{assume } p = 0.5; \quad \sqrt{n} = \frac{1.64 \times \sqrt{(0.5)(0.5)}}{0.02} = 1681$$

b) 95% C.I for P, when out of 1000 sample 400 are happy.

$$\Rightarrow \frac{400}{1000} \pm 2 \sqrt{\frac{0.4 \times 0.6}{1000}}$$

$$\Rightarrow 0.40 \pm 0.030 \Rightarrow (0.37, 0.43)$$

4. Mean for 0.95, 1.02, 1.01, 0.98

$$\text{Mean for } \bar{x} = 0.99$$

$$S.D = \sqrt{\frac{\sum (x - \bar{x})^2}{n}} = 0.027$$

a) C.I at 95% $\Rightarrow 0.99 \pm 2 \times \frac{0.027}{\sqrt{4}}$

$$= (0.963, 1.017)$$

b) Consider hypothesis testing.

$$\text{Null hypothesis } \mu = 0.99 \quad H_0$$

$$\text{Alternate hypothesis } \mu \neq 0.99 \quad H_1$$

Since μ lies between C.I, we fail to reject null hypothesis.

5. Null hypothesis; $\mu = 45 \quad H_0$

Alternate hypothesis; $\mu \neq 45 \quad H_1$

$$n = 9$$

$$\text{Standard Error} = \frac{3.5}{\sqrt{9}}; \text{d.f} = 8$$

$$\text{at 5\% Significance; } T = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}} = \frac{49.2 - 45}{\frac{3.5}{\sqrt{9}}} = 3.6$$

$$t\text{-score at df 8 and 5\% significance} \Rightarrow 2.306$$

Hence it is evident that mean time has changed after exercise, hence accept alternate hypothesis.

6. Standard Deviation = 5 min

$$\mu = 42 \text{ mins}$$

$$95\% \text{ CI} \Rightarrow \mu \pm 2SE$$

$$n = 64$$

$$\Rightarrow 42 \pm 2 \frac{5}{\sqrt{64}}$$

$$\Rightarrow 42 \pm 1.25 \Rightarrow (40.75, 43.25)$$

7. Sum of value = -3.50

$$n = 17$$

$$\therefore \mu = \frac{-3.50}{17} = -0.205$$

$$\sigma^2 = \frac{\text{Sum squared}}{17} - (\mu)^2$$

$$= \frac{19.13}{17} - (-0.205)^2$$

$$= 1.125 - 0.0420$$

$$\sigma^2 = 1.083$$

$$\therefore \sigma = \sqrt{1.083} = 1.040$$

$$\text{at } 90\% \text{ CI, } \Rightarrow -0.205 \pm \frac{1.040 \times 1.64}{\sqrt{17}}$$

$$\text{C.I} = -0.205 \pm 0.413$$

$$\Rightarrow (-0.618, 0.208)$$

8. ME = 1 cm

$$\sigma^2 = 9 \text{ cm}^2$$

$$\sigma = 3 \text{ cm}$$

$$n = \left(\frac{Z}{ME} \right)^2 = \left(\frac{2 \times 3}{1} \right)^2$$

$$\boxed{n = 36}$$

$$\boxed{n = 36}$$

9. $\mu = 141$ 95% C.I $\Rightarrow \mu \pm 2 SE$

$$n = 16$$

$$s = 4$$

$$= 141 \pm 2 \frac{4}{\sqrt{16}}$$

$$\boxed{C.I = 141 \pm 2}$$

10. $n = 17,096$

need to determine proportion of binge-drinkers.

\therefore there are known 3314 Binge-drinkers.

$$\therefore p = \frac{3314}{17,096} = 0.1938$$

$$q = 0.806$$

$$\therefore \text{at } 90\% \text{ C.I ; } \hat{p} \pm 1.64 SE \Rightarrow \sqrt{\frac{pq}{n}}$$

$$\Rightarrow \frac{3314}{17096} \pm 1.64 \sqrt{\frac{(0.1938)(0.806)}{17096}}$$

$$\Rightarrow 0.1938 \pm 0.0049$$

11. $n = 100$ S.D = 4.49

$$\mu = 49 \quad \text{C.I at } 90\%$$

$$\Rightarrow \cancel{49 \pm 1.84} \quad 49 \pm 1.64 \left(\frac{4.49}{\sqrt{100}} \right)$$

$$\Rightarrow 49 \pm 0.736$$

12. 95% C.I proportion of fraudulent clicks.

$$p = \frac{175}{1200} = 0.145 ; q = 0.855$$

$$\Rightarrow 0.145 \pm 2 \sqrt{\frac{0.145 \times 0.855}{1200}}$$

$$\Rightarrow 0.145 \pm 0.064$$

13. $n = 59$

proportion of left-hand players at 95% CI

$$p = \frac{15}{59} = 0.254 \quad ; \quad q = 0.746$$

$$\Rightarrow 0.254 \pm 2 \sqrt{\frac{0.254 \times 0.746}{59}}$$

$$\Rightarrow 0.254 \pm 0.1133$$

14. $n = \left(\frac{Z_{\alpha}}{ME} \right)^2$

at 90%. $z = 1.64$

$$n = \left(\frac{1.64 \times 475}{100} \right)^2$$

$$\boxed{n = 61}$$

15. $\mu = 55.3 \quad n = 10$

$$\sigma^2 = 227.61$$

$$\sigma = 15.08$$

C.I at 95%.

$$\Rightarrow 55.3 \pm 2 \frac{15.08}{\sqrt{10}}$$

$$\Rightarrow 55.3 \pm 9.53$$