

## \* Fermi Energy Formula for an Intrinsic Semiconductor :

In intrinsic semiconductor the conduction is due to the intrinsic characteristics of the crystal without impurity. The electrons are excited from the top of the valence band to the bottom of the conduction band by thermal energy. The no. of electrons excited across the gap can be calculated by Fermi-Dirac Distribution function

$$f(E) = \frac{1}{1 + \exp((E - E_F)/k_B T)} \quad \text{--- (1)}$$

The Fermi level  $E_F$  for intrinsic semiconductor lies midway in the forbidden gap as shown in fig. The probability of finding an electron here is 50%. Then  $(E - E_F)$  in eqn. (1) is equal to  $E_g/2$ , where  $E_g$  is magnitude of energy gap.

For exp. Silicon has  $E_g = 1.1 \text{ eV}$ , so  $(E - E_F) = 0.55 \text{ eV}$ , which is twice times higher than thermal energy  $k_B T = 0.026 \text{ eV}$ .

The factor unity in denominator can be ignored, so the probability  $f(E)$  of an electron occupying energy level  $E$

$$f(E) = \exp(-E_g/2k_B T) \quad \text{--- (2)}$$

So for the number of electron ( $n$ ) promoted across gap

$$n = N \cdot \exp(-E_g/2k_B T) \quad \text{--- (3)}$$

where  $N$  = no. of electrons available for excitation for top of valence band.

The electron across the gap leaves some vacant electron site in valence band. These are called holes. An intrinsic semiconductor have equal no. of holes in valence band and electrons in conduction band,  $n_e = n_h$ .

Under externally applied field the excited electrons can accelerate using the vacant states available in conduction band.



At the same time holes in valence band also move but in opposite direction of electrons. Conductivity of intrinsic semiconductor depends upon charge carriers  $n_e$  and  $n_h$ .

Like drift velocity in case of metal we have mobility of conduction electron and holes  $\mu_e$  and  $\mu_h$  as drift velocity. So the conductivity  $\sigma$  of intrinsic semiconductor as:

$$\sigma_i = n_e e \mu_e + n_h e \mu_h \quad \text{--- (4)}$$

where  $e$  = electronic charge and  $n_e$  and  $n_h$  are concentration of electrons & holes.

Fermi Level  $\Rightarrow$  The no. of free electrons per unit volume in an intrinsic semiconductor is

$$n = 2 \left( \frac{2\pi m_e kT}{h^2} \right)^{3/2} \exp \left( \frac{E_F - E_c}{kT} \right)$$

The no. of holes per unit volume in an intrinsic semiconductor is

$$p = 2 \left[ \frac{2\pi m_h kT}{h^2} \right]^{3/2} \exp \left( \frac{E_v - E_F}{kT} \right)$$

Since  $n = p$  in intrinsic semiconductor

$$2 \left( \frac{2\pi m_e kT}{h^2} \right)^{3/2} \exp \left( \frac{E_F - E_c}{kT} \right) = 2 \left( \frac{2\pi m_h kT}{h^2} \right)^{3/2} \exp \left( \frac{E_v - E_F}{kT} \right)$$

$$(m_e)^{3/2} \exp \left( \frac{E_F - E_c}{kT} \right) = (m_h)^{3/2} \exp \left( \frac{E_v - E_F}{kT} \right)$$

$$e^{2E_F/kT} = \left( \frac{m_h}{m_e} \right)^{3/2} \exp \left( \frac{E_v + E_c}{kT} \right)$$

Taking log on both sides

$$\frac{2E_F}{kT} = \frac{3}{2} \log_e \left( \frac{m_h}{m_e} \right) + \log_e \left[ \exp \left( \frac{E_v + E_c}{kT} \right) \right]$$

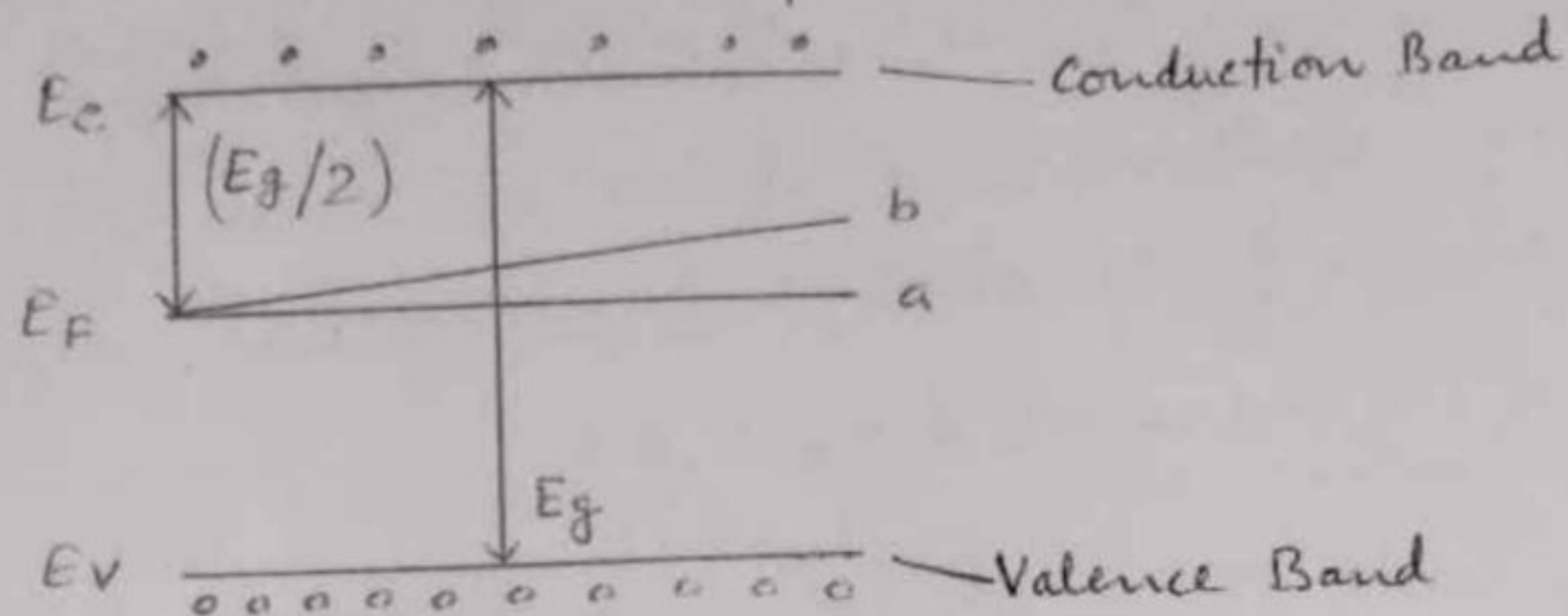
$$\frac{2E_F}{kT} = \frac{3}{2} \log_e \left( \frac{m_h}{m_e} \right) + \left( \frac{E_v + E_c}{kT} \right)$$

$$E_F = \frac{3kT}{4} \log_e \left( \frac{m_h}{m_e} \right) + \left( \frac{E_v + E_c}{2} \right)$$

If we assume  $m_e = m_h$   $E_F = \left( \frac{E_v + E_c}{2} \right)$  ( $\log_e 1 = 0$ )



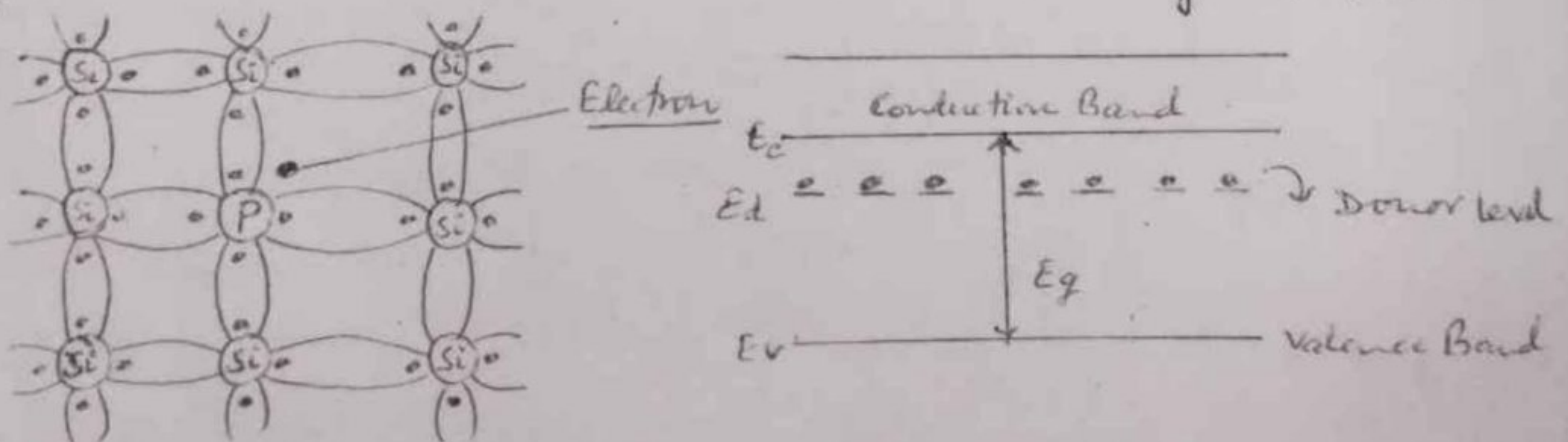
Thus the Fermi level is located <sup>6</sup>half way between valence and conduction band and is independent of temperature. Since  $m_h > m_e$ ,  $E_F$  is just above the middle and rise slightly with increase in temperature.



Position of Fermi level in an intrinsic Semiconductor at various temperature, (a) At  $T=0$ , (b) As temp increases  $E_F$  shift

N-type of Semiconductor  $\Rightarrow$  When <sup>small amount of</sup> pentavalent impurity such as P, As, Sb is added to the intrinsic semiconductor, n-type semiconductor is formed.

When fifth column element phosphorus substitute for a Silicon atom, four of the five electrons in the outermost orbit of Phosphorus atom take part in tetrahedral bonding with four Silicon atoms. The fifth electron cannot take part and it is loosely bound. It revolves around the +ve charged P ion.



The electron of phosphorus atom is moving in the electric field of Silicon crystal and not in free space.

This brings in dielectric constant of crystal into orbit calculation and the radius of electron orbit here turns out to be very

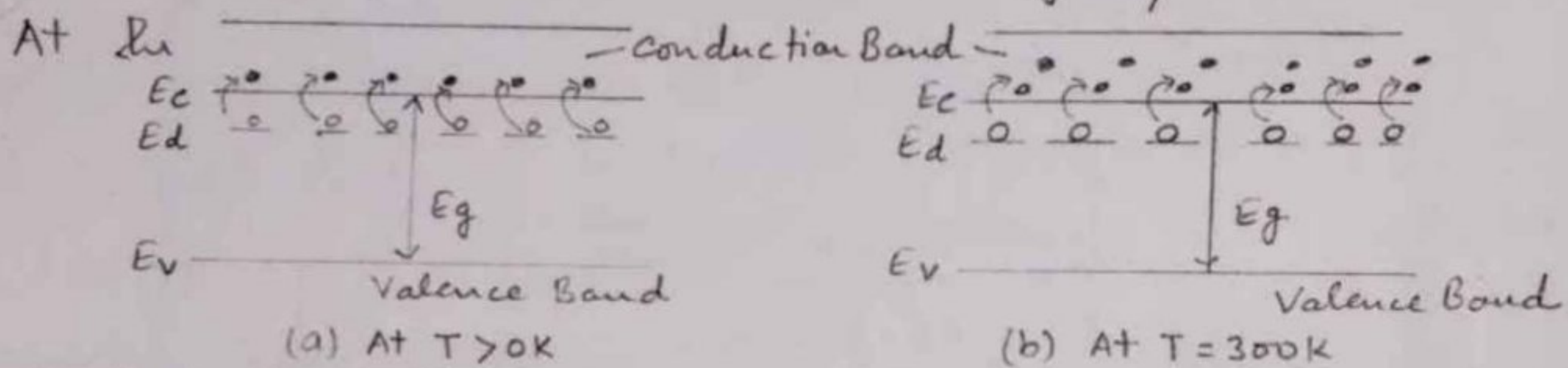


large about  $80\text{\AA}$ . Such large orbit means fifth electron free and is at energy level close to conduction band.

At 0K the electronic system is in its lowest state, all the valence electron will be in valence band and all phosphorus atom will be unionised.

In energy level diagram the energy level of fifth electron is called donor level. The energy level of donor atoms are very close to bottom of conduction band.

Most of donor level electrons are excited into conduction band at room temperature & become majority carriers.



At high thermal energy, in addition to ionization of donor impurity atom, breaking of covalent bond give rise to electron hole pair.

Fermi Energy :  $\Rightarrow$

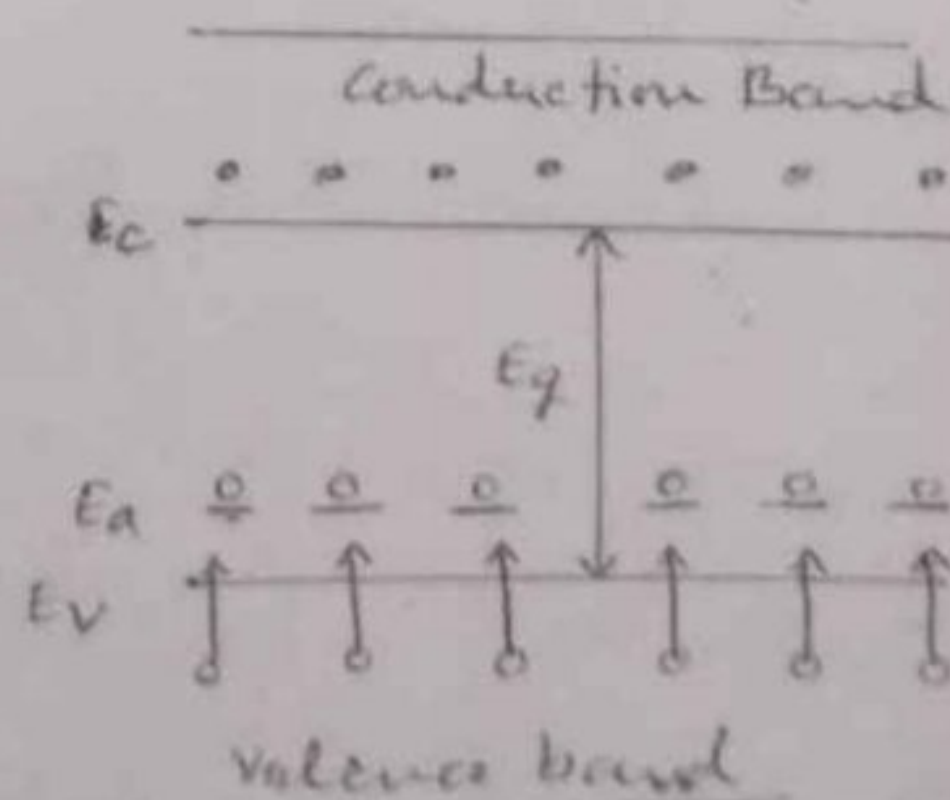
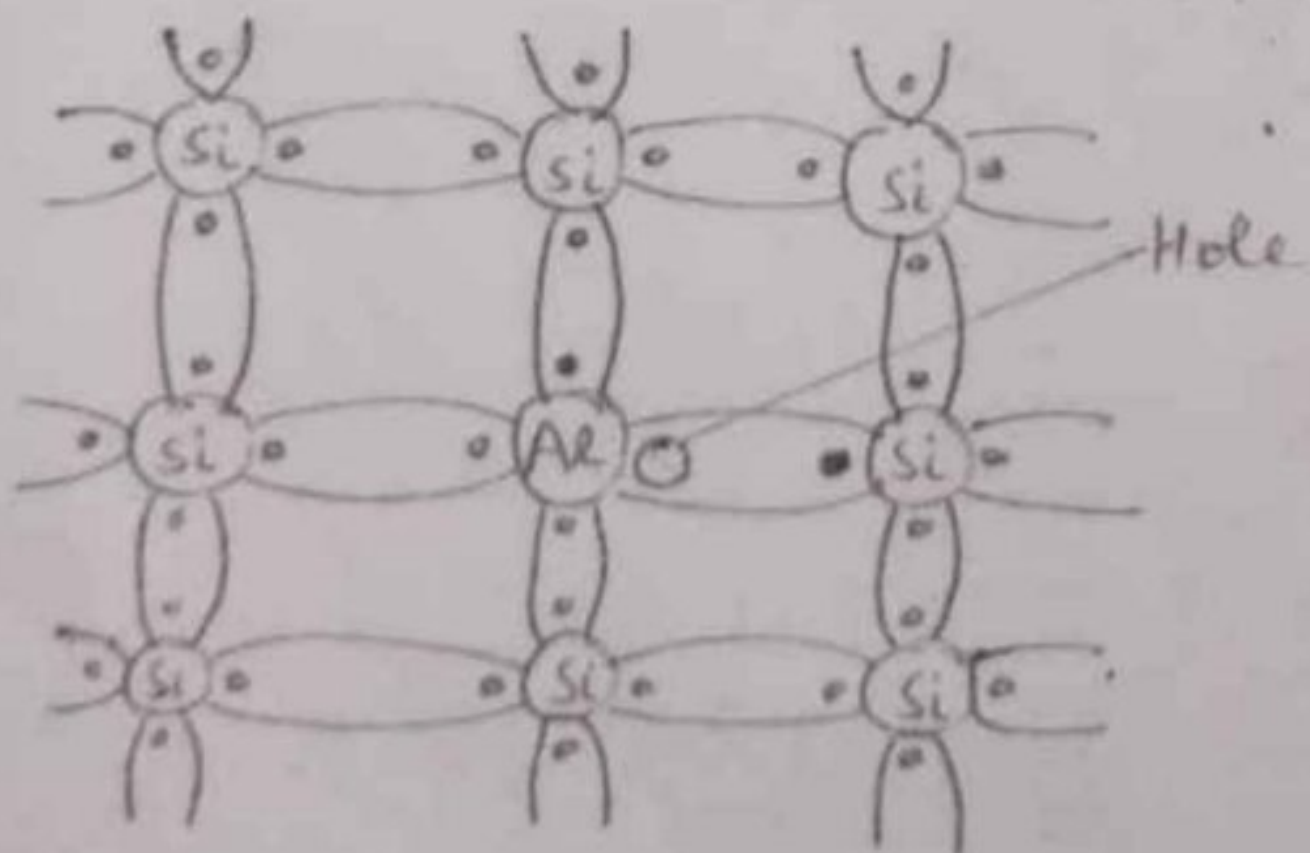
The fermi energy for n-type semiconductor is

$$E_F = \frac{(E_c + E_d)}{2} + \frac{kT}{2} \log \left[ \frac{N_d}{2 \left( \frac{2\pi m_e kT}{h^2} \right)^{3/2}} \right] ; \text{ At } 0\text{K}, E_F = \frac{E_c + E_d}{2}$$



P-type Semiconductor :  $\Rightarrow$  When trivalent impurity like Al is added to the intrinsic semiconductor, P-type semiconductor is formed. Aluminium has three electrons, while substituting for Silicon in the crystal it needs an extra electron to complete the tetrahedral bonds. The extra electron can come out only from one of the neighbouring Si atom, thereby creating a vacant electron site (hole). The Al atom with extra-electron becomes a negative charge and the holes with positive charge can be considered to revolve around Aluminium atoms.

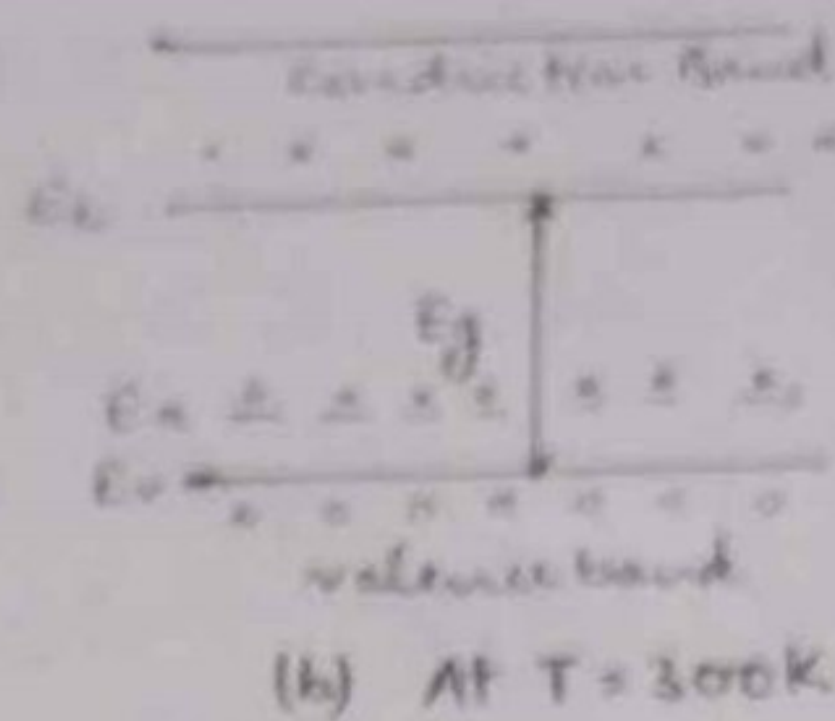
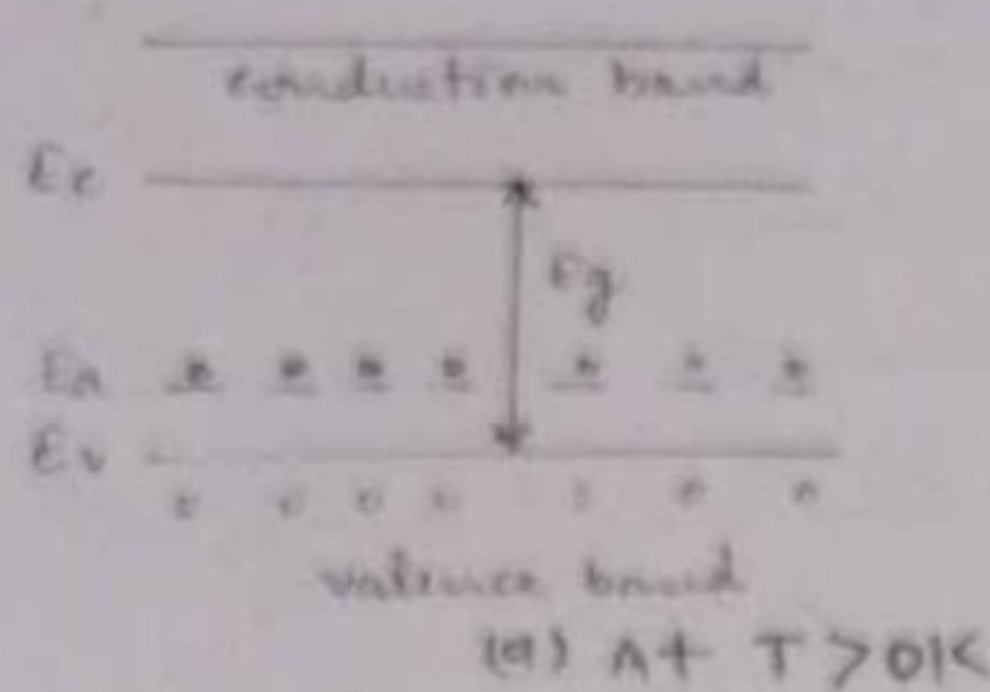
- $\rightarrow$  Since the trivalent impurity accepts an electron, the energy level of this impurity atom is called acceptor level. This acceptor level lies just above the valence band.
- $\rightarrow$  Even at relatively low temperature, these acceptor atoms get ionized taking electrons from the valence band and thus giving rise to holes in the valence band for conduction.
- $\rightarrow$  Due to ionization of acceptor atoms, only holes and no electrons are created. If the temperature is sufficiently high, in addition to the above process electron and hole pairs are generated due to breaking of covalent bonds. Thus holes are majority carriers and electrons are minority carriers for p-type semiconductor.



At  $T = 0\text{ K}$

P-type Semiconductor





Fermi Energy :  $\Rightarrow$  The Fermi energy for p-type semiconductor is

$$E_F = \left( \frac{E_v + E_a}{2} \right) + \frac{kT}{2} \log \left[ \frac{N_a}{2 \left( \frac{2\pi m_e kT}{h^2} \right)^{3/2}} \right]$$

At 0K,  $E_F = \frac{E_v + E_a}{2}$

i.e., at 0K, Fermi level is exactly at the middle of the acceptor level on the top of valence band.

Q<sub>3</sub> :  $\Rightarrow$  Explain with sketch the variation of Fermi level and carrier concentration with temperature in case of P and N type semiconductor for high and low doping levels.

Ans : Variation of Fermi level with temperature (N-type) :  $\Rightarrow$

The Fermi Energy is given by

$$E_F = \left( \frac{E_d + E_c}{2} \right) + \frac{kT}{2} \log \frac{N_d}{2 \left[ \frac{2\pi m_e kT}{h^2} \right]^{3/2}}$$

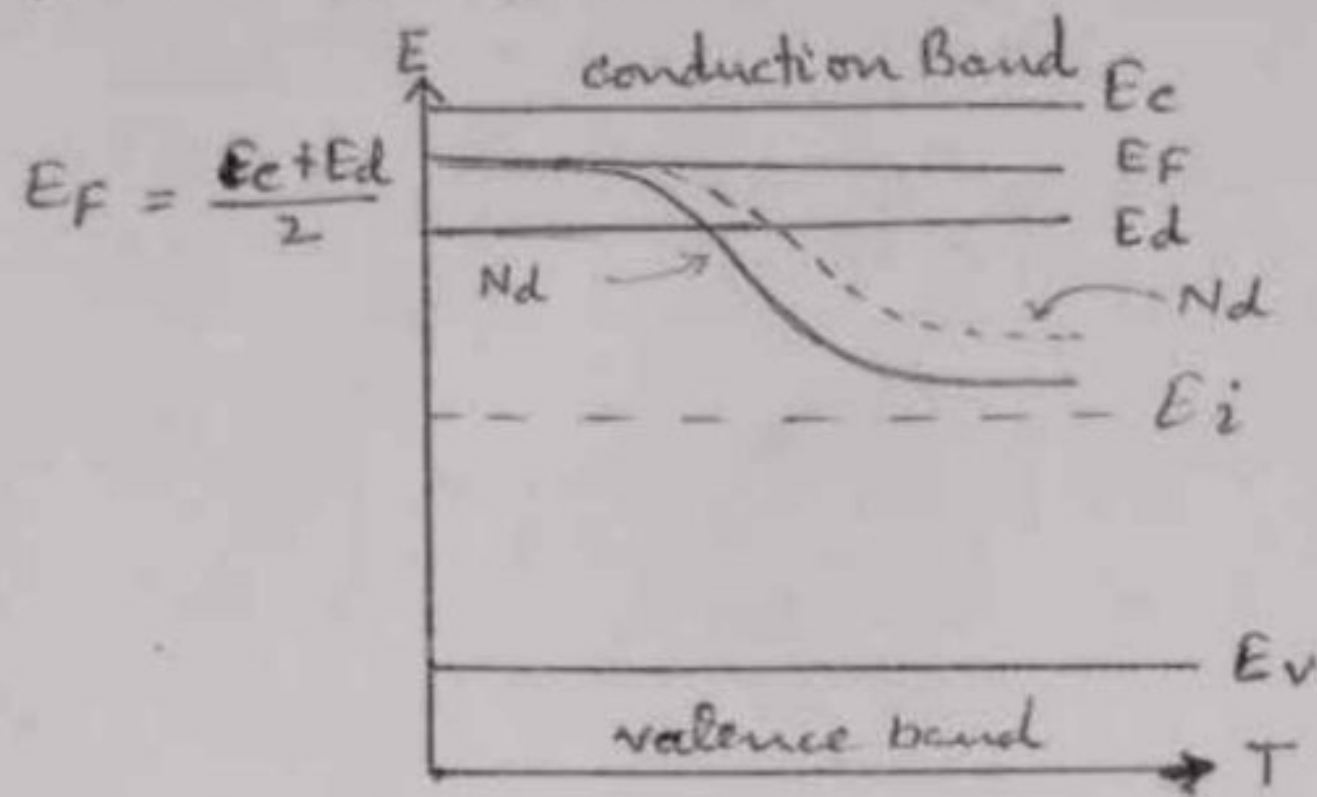
Let  $2 \left[ \frac{2\pi m_e kT}{h^2} \right]^{3/2} = N_x$

$$\begin{aligned} \therefore E_F &= \left( \frac{E_d + E_c}{2} \right) + \frac{kT}{2} \log \left( \frac{N_d}{N_x} \right) = \left( \frac{E_d + E_c}{2} \right) - \frac{kT}{2} \log \left( \frac{N_x}{N_d} \right)^{-1} \\ &= \left( \frac{E_d + E_c}{2} \right) - \frac{kT}{2} \log \left( \frac{N_x}{N_d} \right) \end{aligned}$$

$\rightarrow$  As  $T$  increases, Fermi level drops. For a given temperature the Fermi level shift upward as concentration increases.



- Above eqn. show that  $E_F$  decreases with increases as temp.
- As the temperature increased, more donor atom are ionized.
- For a particular temperature all donor atom are ionized.
- Further increase in temperature generate electron-hole pair due to breaking of covalent bond, & material behave as intrinsic semiconductor.



Variation of Fermi level with donor concentration with temperature.

Variation of Fermi level with temperature (P-type) : ⇒

The fermi energy is given by

$$E_F = \left( \frac{E_v + E_a}{2} \right) - \frac{kT}{2} \log \left[ \frac{N_a}{2 \left( \frac{2\pi m_e kT}{h^2} \right)^{3/2}} \right] = \left( \frac{E_v + E_a}{2} \right) - \frac{kT}{2} \log \left( \frac{N_a}{N_y} \right)$$

where  $N_y = 2 \left( \frac{2\pi m_e kT}{h^2} \right)^{3/2}$

$$E_F = \left( \frac{E_v + E_a}{2} \right) + \frac{kT}{2} \log \left( \frac{N_a}{N_y} \right)$$

- The above eqn. shows that  $E_F$  increases as the temperature increases.
- As the temp. increases more & more acceptor atom are ionized.
- For a particular temperature all the acceptor atoms are ionized.
- Further increases in temperature generates the electron-hole pair due to breaking of covalent bond and the material behave as intrinsic semi-conductor.