



## Data Structures & Algorithms

↓  
 how data is organised & stored

### Data Structures (D.S.)

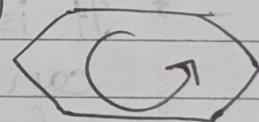
#### Linear D.S.

- Arrays
- linked lists
- Stack
- Queue

#### Non-linear D.S.

- ~~cyclic~~
- Trees
- Graphs

Always form cyclic structure



### Operations on D.S.

- ① Traversing (Accessing all the data inside D.S. ~~at least~~ once) (Updation)
- ② Insertion (start, end, specific position)
- ③ Deletion
- ④ Searching
- ⑤ Sorting

Stu. Name = 'Prakhar'

SEM = 3<sup>rd</sup>

D.O.B = 18/8/2003

Branch = CSE-AIML

Database → data structure  
(D.S.)

- A data structure is a particular way of organising data in the system so that we can use it efficiently.
- It is a set of algorithms that we can use in any programming language to structure the data in the memory.

D.S.

↓

Linear

→ Arrays

→ linked list

→ Queues

→ stacks

↓

Non-Linear

→ Trees

→ graphs

## # Applications of Data Structures

1) Operating Systems

2) DBMS

3) Compiler design

4) AI (Knowledge - Base)

5) Analysis

## # Linear D.S.

① Arrays

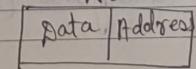
→ It is a collection of elements. It is used in mathematical problems like matrix, algebra; etc.

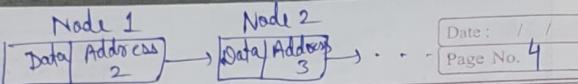
→ Each element of an array is referenced by a subscripted variable or value of index enclosed in parenthesis.

② linked list

→ It is a collection of data elements.

→ It consists of 2 parts → <sup>(data)</sup> information & <sup>(address)</sup> link(address).





Date: / /  
Page No. 4

Date: / /  
Page No. 5

- Info gives information & link is an address of next node.
- linked list can be implemented by using pointers

H.W. Applications of linked list

### ③ Stack

- It is a list of elements.
- In stack, an element may be inserted or deleted at one end which is known as top of the stack.
- It performs 2 operations → push & pop.

- (i) Push → Adding an element in stack
- (ii) Pop → Removing an element from stack.

- It is also called LIFO.

### Implementation of stack

- Push → overflow (जब जारी नहीं हो)
- Pop → underflow (खाली जब नहीं हो)

### ④ Queue

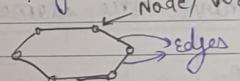
- Queue is a linear list of elements.
- In queue, elements are added at one end called Rear end & are deleted from another end called front end.
- It is also called FIFO.
- # Non-linear D.S.

### ① Trees



- It is a Non-linear D.S.
- flexible, versatile & powerful
- used to represent data items processing hierarchical relationship b/w the root & its children.
- It is an ideal data structure for representing any hierarchical data.

### ② Graph



- It is a non-linear D.S. which consists of a finite set of ordered pairs called edges.
- graph is a set of elements connected by edges. Each element is called vertex or node.

## # D.S. Operations

### ① Traversing

- Accessing each element of D.S. atleast once.

### ② Searching

- Search for any element in a D.S.

### ③ Sorting

- Sort the elements of a D.S. either in an ascending or descending order.

### ④ Insertion

- Insert any element in a D.S.

### ⑤ Deletion

- To remove the element from the D.S.

### ⑥ Updation

- By performing any modification in a D.S. either by,
  - swapping the elements
  - inserting or deleting the elements
  - sorting elements
  - replacing element with another element

## # Algorithm

→ Algo. is a finite sequence of instructions each of which is very elementary that must be followed to solve a problem.

→ An algo. is a well-defined computational procedure that transforms inputs into outputs by achieving the desired I/P - O/P relationship.

→ All algo.'s must satisfy the following criteria -

- I/P's are well-specified
- O/P
- finiteness
- effectiveness
- definiteness

→ Algo.

\* Algorithm Development Life cycle,

→ In the life cycle of an algo. [for the development of algo.] following phases are involved;

- Design Phase (Algo Design)
- Writing Phase

- (3) Testing or Experiment Phase
- (4) Analysing Phase (Time & Space complexity)

Apriori Analysis

Posteriori Analysis

- Apriori Analysis; It is system dependent

→ analysis of an algo. running on a specific system.

- Posteriori Analysis; Actual amount of time & space taken by the algo's are recorded during the execution.

### Time and Space Complexity

- Space complexity → amount of space needed for algo to solve the problem.
- An efficient algo takes space as small as possible.
- Space needed by a program is the sum of the following components:-

### (a) Instruction Space

→ space needed to store the executable version of a program & it is fixed.

### (b) Data Space

(i) → space needed to store all elements - all constant, variables & the following components  
 (ii) → space needed by constant & simple variable. The space is fixed!

### Space

(iii) → space needed by fixed size structured variables such as arrays & structures.

### (c) Dynamically-allocated space from memory pool.

→ This space usually varies

### (d) Inbuilt stack space

→ space needed to store the info.

→ space needed to resume the suspended function.

Questions

Q1 W.A.P to swap 2 elements without using 3<sup>rd</sup> variable.

Ans-1)  $\begin{aligned} \text{int } a = 3; \\ \text{int } b = 4; \\ \cancel{b = (a+b)-a}. \end{aligned}$

$$\begin{aligned} b &= (a+b) - (a=b); \\ \text{cout} &\ll a \ll b; \end{aligned}$$

Q2 W.A.P. to access each element of an array {2, 9, 10, 3, 4, 6}.

Ans-2)  $\begin{aligned} \text{int arr}[] = \{2, 9, 10, 3, 4, 6\}; \\ \text{for (int } i=0; i < \text{arr.length}; i++) \\ \{ \\ \text{cout} \ll \text{arr}[i] \ll \text{endl}; \\ \} \end{aligned}$

Q3 Insert an element in stack

→ Insert = 8

→ Delete last element from stack.

3
1
4
2

~~int~~

~~import stack  
stack<int>s = {2, 4, 1, 3};  
s.push(8);~~

int s = [2, 4, 1, 3];

Ans-3) ~~import stack  
stack<int>s = {2, 4, 1, 3};~~

$\begin{aligned} \text{int size} = 7; \\ \text{if (s.length} < \text{size}) \{ \\ \quad \text{s.push(8)}; \\ \} \end{aligned}$

$\begin{aligned} \text{else if} \\ \quad \text{cout} \ll \text{"size overflow"} \ll \text{endl}; \end{aligned}$

$\begin{aligned} \text{while (!s.empty)} \\ \{ \\ \quad \text{s.pop}(); \\ \} \end{aligned}$

# Time Complexity

Linear Search A = {3, 2, 0, 40, 6, 15, 1}

Key element = 3 → Best case  $\Rightarrow O(1)$

Key element = 1 → Worst case  $\Rightarrow O(n)$

Best Case

O

Average Case

w

Worst Case

Big-oh (O)

→ The time complexity of an algo. is the no. of computer amount of time needed by computer to execute the complete code.

## \* Rules for computing running time complexity

### ① Sequence

Add the time of the individual statements.

### ② Loops

Execution time of a loop is atmost the execution time of the statements of the body multiplied by the no. of iterations.

### ③ Nested loops

Analyse them inside-out.

### ④ Alternative Structures

Time for testing the condition

+

Max. time taken by any of the alternative paths.

### ⑤ Sub-programs

Analyse them as separate algos & substitute the time wherever necessary.

81

int a = 0, b = 0;  
for (int i = 0; i < n; i++)  $\rightarrow O(n)$

{  
    a = a + rand();  
}

for (j = 0; j < m; j++)  $\rightarrow O(m)$   
{  
    b = b + rand();  
}

$\Rightarrow O(n+m)$

82

int a = 0;  
for (i = 0; i < n; i++)  $\rightarrow O(n)$

{  
    for (j = n; j > i; j--)  $\rightarrow O(n)$   
    {  
        a = a + i + j;  
    }  
}

$\Rightarrow O(n \cdot n) \Rightarrow O(n^2)$

83

int i, j, k = 0;  
for (i = n/2; i <= n; i++)

{  
    for (j = 2; j <= n; j++)

{  
        k = k + n/2;  
    }

$\Rightarrow O(n \log n) = O(n \log_2 n)$

base 3, 4, 5 etc  
st 10  
mention para  
gears 2  
para 2  
etc  
base 2  
para 2  
etc

Date: 19/7/23

## Questions on Time Complexity No. 14

Q1

```

int k=1;
while(k<=n)
{
    cout << k << endl;
    k = k * 2;
}
 $O(\log_2 n)$ 

```

Q2

```

for (int i=0; i<n; i++)
{
    for (int j=i; j>0; j--)
        cout << i << j;
}
 $O(n^2)$ 

```

Q3

```

import random
def fun(N):
    counter = 0
    for i in range(N):
        count += random.randint(0, 100)
    print(counter)
 $O(N)$ 

```

Q4

```

def function(N, M):
    counter = 0
    for i in range(N):
        for j in range(M):
            counter += 1
    print(counter)
 $O(NM)$ 

```

Q5

```

def fun(n, m):
    arr = [[0] * m for i in range(n)]
    for i in range(n):
        for j in range(m):
            k = 1
            while k < n * m:
                arr[i][j] = k
                k *= 2
arr  $O(nm \log(nm))$ 

```

Q6

```

def recursion(N):
    if (N == 0):
        return
    print(N)
    recursion(N-1)
 $O(N)$ 

```

Q7

```

if (i > j)
{
    (Conditional statement)
}
 $O(1)$ 

```

Q8 def fun(N):

    counter = 10

    for i in range(1, N+1): → N

        for j in range(1, i+1):

            counter += 1

    print(counter)

$O(N^2)$

Q9 def fun(N)

    for i in range(1, N+1):

        j = N

        while j > 0

            j // 2

$O(N \log_2 N)$

(★ O, Ω, Θ → Asymptotic Notations)

## Searching

# Linear Search

0	1	2	3	4	5	6	7
1	2	3	8	0	14	10	6

$n = 8$

Key = 3 (returns index = 2)

If Key = 11 (This key is NOT present)  
 $\therefore i = n$

(Time complexity)

Best Case →  $O(1)$

Worst Case →  $O(n)$

Code → for (i = 0; i < n; i++)

    if (a[i] == key)

        printf ("Element found at index: /d", i);  
 break;

    if (i == n)

        printf ("Element not found");

B) i) Explain linear search

ii) Explain algo

iii) Explain time complexity → all 3 with examples

(i) Time best → then avg worst → complexity

## # Binary Search

0	1	2	3	4	5	6	7
2	4	6	8	10	12	14	16
l	mid	mid	mid	r	(Key=12)	(Key=12)	

\* Array should be "sorted" then ONLY we can apply Binary search

$$\text{mid} = \frac{l+r}{2} = \frac{0+7}{2} = 3.5$$

case-1: if key == a[mid]

case-2: if key < a[mid]

case-3: if key > a[mid]

$$\text{mid} = \frac{l+r}{2} = \frac{4+7}{2} = 5.5$$

(element is found here)

0	1	2	3	4	5	6	7	8	9	10	11	12	13
3	6	10	12	13	16	21	30	63	70	85	95	100	101

i) Key = 13

ii) Key = 101

l	r	mid	mid [data]
0	13	6	21 > key
0	5	2	10 < key
3	5	4	[13 = key]

l	r	mid	mid [data]
(Key=101)	0	13	21 < key
7	13	10	85 < key
11	13	12	100 < key
13	13	13	[101 = key]

\* code → Binary search (a, n, data)

```
l = 0 ; r = n - 1;
```

```
while (l <= r)
```

```
{ mid = (l + r) / 2;
```

```
if (data == a[mid])
    return mid;
```

```
else if (data < a[mid])
    r = mid - 1;
```

```
else
    l = mid + 1;
```

```
}
```

```
return -1;
```

Time complexity →  $O(\log n)$

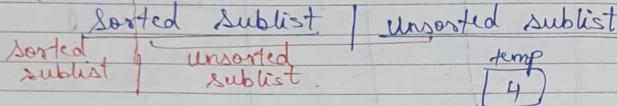
## Sorting

Date: 24/7/23

Page No. 20

### # Insertion Sort

A:	5	4	10	1	6	2
----	---	---	----	---	---	---



①	5	10	1	6	2
---	---	----	---	---	---

sorted | unsorted

temp  
10

②	4	5	10	1	6	2
---	---	---	----	---	---	---

sorted | unsorted

temp  
1

4	5	10	6	2
---	---	----	---	---

4	5	10	6	2
---	---	----	---	---

4	5	10	6	2
---	---	----	---	---

4	5	10	6	2
---	---	----	---	---

sorted | unsorted

1	4	5	10	1	2
---	---	---	----	---	---

~~left to right~~

1	4	5	10	1	2
---	---	---	----	---	---

1	4	5	6	10	2
---	---	---	---	----	---

sorted | unsorted

1	4	5	6	10	
---	---	---	---	----	--

1	4	5	6	10	
---	---	---	---	----	--

temp  
2

1	4	5	6	10	
---	---	---	---	----	--

1	4	5	6	10	
---	---	---	---	----	--

1	4	5	6	10	
---	---	---	---	----	--

1	4	5	6	10	
---	---	---	---	----	--

sorted! (through insertion sort)

## \* Code of Insertion Sort

```

for (i=1; i<n; i++)
{
    temp = a[i];
    j = i-1;
    while (j >= 0 && a[j] > temp)
    {
        a[j+1] = a[j];
        j--;
    }
    a[j+1] = temp;
}

```

## # Bubble Sort

A : [40 | 50 | 6 | 15 | 10 ]

Pass-1 [40 | 50 | 6 | 15 | 10 ]

[40 | 6 | 50 | 15 | 10 ]

[40 | 6 | 15 | 50 | 10 ]

[40 | 6 | 15 | 10 | 50 ]

Pass-2

[40 | 6 | 15 | 10 | 50 ]

[6 | 40 | 15 | 10 | 50 ]

[6 | 15 | 40 | 10 | 50 ]

[6 | 15 | 10 | 40 | 50 ]

Pass-3

[6 | 15 | 10 | 40 | 50 ]

(Repetitive)

[6 | 15 | 10 | 40 | 50 ]

[6 | 10 | 15 | 40 | 50 ]

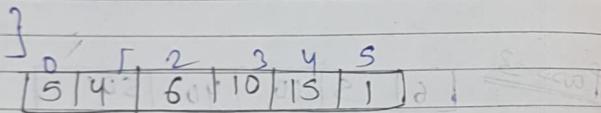
Pass-4

[6 | 10 | 15 | 40 | 50 ]

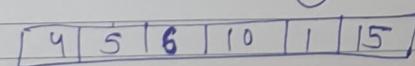
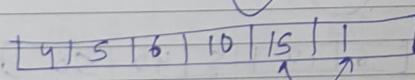
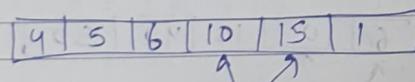
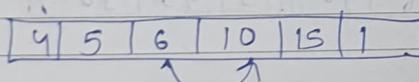
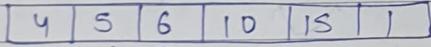
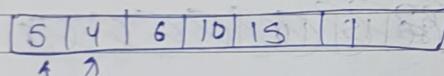
[6 | 10 | 15 | 40 | 50 ]

## \* code of BUBBLE SORT |

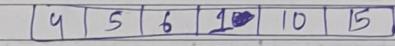
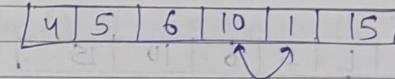
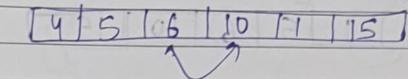
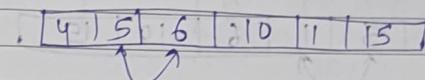
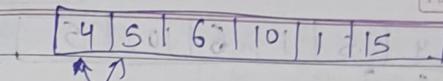
```
for (i = 0; i < n-1; i++) {
    for (j = 0; j < n-i-1; j++) {
        if (A[j] > A[j+1])
            temp = A[j];
            A[j] = A[j+1];
            A[j+1] = temp;
    }
}
```



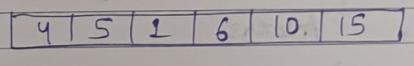
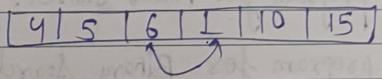
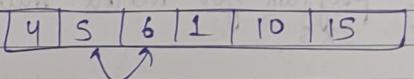
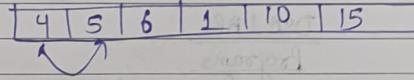
Pass-1



Pass-2



Pass-3



~~Pass-4~~

P.T.O. →

Page-4

[ 4 | 5 | 1 | 6 | 10 | 15 ]

[ 4 | 5 | 1 | 6 | 10 | 15 ]

[ 4 | 1 | 5 | 6 | 10 | 15 ]

Page-5

[ 4 | 5 | 1 | 6 | 10 | 15 ]

[ 1 | 4 | 5 | 6 | 10 | 15 ] sorted

25/9/23

DSA LAB  
Programs

Q1 Write a program for matrix multiplication  
of size 3x3.

Q2 Write a program for linear search.

Q3 Write a program for Binary Search.

Answers:

A-1

$$\begin{pmatrix} 2 & 1 & 0 \\ 3 & 4 & 2 \\ 5 & 1 & 0 \end{pmatrix} \begin{pmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 3 & 0 & 4 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$A = \begin{bmatrix} 2 & 5 & 8 \\ 9 & 10 & 15 \\ 5 & 11 & 17 \end{bmatrix}$$

( ), ( ) ( ) ( ) ;

for (i=0; i< arr.length; i++)

{ for (j=0; j<3; j++)

arr3[i][j] =

arr1[i][j]

0 2 4

1 \* 0, 0, 0

0 1 2 3 4 5 6 7 8 9

(P.T.O.) →

```
#include <iostream>
using namespace std;
int main()
{
    int arr1[3][3] = {{2, 1, 0}, {3, 4, 2}, {5, 1, 0}};
    int arr2[3][3] = {{1, 0, 3}, {2, 1, 0}, {3, 2, 4}};
    int arr3[3][3];
    for (int i = 0; i < 3; i++)
    {
        for (int x = 0; x < 3; x++)
        {
            int sum = 0;
            for (int j = 0; j < 3; j++)
            {
                sum += arr1[i][j] * arr2[x][j];
            }
            arr3[i][x] = sum;
        }
    }
    for (int i = 0; i < 3; i++)
    {
        for (int j = 0; j < 3; j++)
        {
            cout << arr3[i][j] << " ";
        }
        cout << endl;
    }
    return 0;
}
```

~~tmp~~

while ~~initialising~~ a 2-D (n-dimensional array), we can skip the length of first parameter BUT it is necessary to give the length of other parameters.

✓) int arr1[ ][3] = {{1, 2, 3}, {4, 5, 6}, {7, 8, 9}};

→ BUT while ~~declaring~~ a 2-D (n-dimensional array) it's necessary to give the first parameter also. We cannot skip it. If we skip the first parameter while DECLARING, then it will give error.

✗) int arr1[ ][3]; //error

it's imp. to give the first parameter also while DECLARING.

✓) int arr1[3][3]; //correct

## # Asymptotic Notations

### \* Types of fns

$O(1)$  → constant

$O(\log n)$  → logarithmic

$O(n)$  → linear

$O(n^2)$  → quadratic

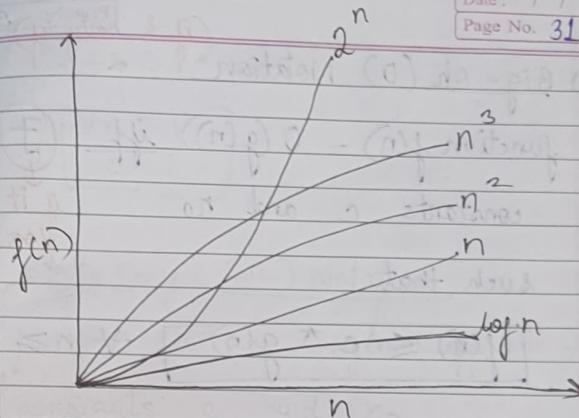
$O(n^3)$  → cubic

$O(2^n)$  → exponential

### \* Orders of function

$$1 < \log n < \sqrt{n} < n < n \log n < n^2 < n^3 < \dots < 2^n < 3^n < \dots < n^n$$

	$\log n$	$n$	$n^2$	$n^3$	$2^n$
$n=1$	0	1	1	1	2
$n=2$	1	2	4	8	4
$n=4$	2	4	16	64	16
$n=8$	3	8	64	512	256



→ Asymptotic Notations are mathematical tools to represent time complexity of an algorithm.

→ They are used to express the rate of growth of an algo's running time in terms of I/P size.

### \* Types of Asymptotic Notations

- ① Big Oh ( $O$ ) Notation [Upper-bound]
- ② Omega ( $\Omega$ ) Notation [Lower-bound]
- ③ Theta ( $\Theta$ ) Notation [Average-bound]

## ① Big-oh ( $O$ ) Notation (if & only if)

function  $f(n) = O(g(n))$  iff f +ve  
 constants  $c$  and  $n_0$  such that  
 if it exists for all

$$[f(n) \leq c * g(n)] \quad \forall n \geq n_0$$

$\therefore f(n) = 2n+3$

②  $f(n) \leq c * g(n)$  (considering  $g(n) = n$  here)

$$\Rightarrow 2n+3 \leq c * n$$

$$c = 10, n = 1$$

$$\Rightarrow [2+3 \leq 10] \quad \boxed{\begin{array}{l} \forall n \\ \text{&} c=10 \end{array}}$$

③  $2n+3 \leq c * (2n^2 + 3n^2)$  (Considering  $g(n) = 2n^2 + 3n^2$  here)

$\rightarrow$  Agar (Big-oh) satisfy karna hai at  $g(n)$  aur  $c$  get like satisfy karo.

$\rightarrow$  Agar agar check karna hoga for  $f(n)$  (big-oh)  $\not\in O(n^2)$  at  $f(n) = 2n+3$  given range.

$$\Rightarrow 2n+3 \leq c * 5n^2$$

$$\boxed{\begin{array}{l} \forall n \geq 1 \\ \text{&} c=1 \end{array}}$$

## ② Big-Omega ( $\Omega$ ) Notation

function  $f(n) = \Omega(g(n))$  iff f +ve  
 constants  $c$  and  $n_0$  such that

$$[f(n) \geq c * g(n)] \quad \forall n \geq n_0$$

$\therefore f(n) = 2n+3$

④  $2n+3 \geq c * n$

$$5 \geq 1$$

$$\boxed{\begin{array}{l} \forall n \geq 1 \\ \text{&} c=1 \end{array}}$$

⑤  $2n+3 \geq f * \log_2 n$

$$\begin{array}{rcl} 5 & \geq & 0 \\ 7 & \geq & 1 \\ 11 & \geq & 2 \end{array}$$

(3) Theta ( $\Theta$ ) Notation.

function  $f(n) = \Theta(g(n))$  iff  $\exists$

+ve constants  $c_1, c_2$  &  $n_0$

such that

$$c_1 * g(n) \leq f(n) \leq c_2 * g(n)$$

Q  $f(n) = 2n+3$

consider  $g(n) = n$

$$1^*(n) \leq 2n+3 \leq 5^*(n)$$

for  $c_1 = 1$

$c_2 = 5$

$n \geq 1$

$\Theta(n)$  is satisfied.

Q1  $f(n) = 2n^2 + 3n + 4$

find  $O, \Theta, \Omega$

for such type of  
ques take 1

$g(n)$  & satisfy

$0, \Theta, \Omega$  for that

$g(n)$

(1)  $O$  (Big Oh)

consider  $g(n) = n^2$

$$2n^2 + 3n + 4 \leq 10^* n^2$$

for  $c = 10$

$n \geq 1$

$O(n^2)$  is satisfied.

Aux  $g(n) \leq f(n)$

if  $g(n) \leq f(n)$

then  $\Theta$  consider  $\Theta$ .

(2)  $\Omega$  (Omega)

consider  $g(n) = n$

$$2n^2 + 3n + 4 \geq 1^* n$$

for  $c = 1$   
 $n \geq 1$

$\Omega(n)$  is satisfied.

(3)  $\Theta$  (Theta)

consider  $g(n) = n^2$

$$1^*(n^2) \leq 2n^2 + 3n + 4 \leq 10^*(n^2)$$

for  $c_1 = 1$

$c_2 = 10$

$n \geq 1$

$\Theta(n^2)$  is satisfied.

Q2  $f(n) = n^2 \log n + n$

(1)  $O$  (Big Oh)

consider  $g(n) = n^3$

~~$2n^2 + n^2 \log n + n \leq 10^* n^3$~~

for  $c = 10$

$n \geq 1$

$O(n^3)$  is satisfied.

(2)  $\Omega(\text{Omega})$

Consider  $g(n) = n$

$$n^2 \log n + n \geq n^2$$

$$\text{for } c=1 \quad 1 = 1 \text{ true}$$

$$n \geq 1$$

$\Omega(n)$  is satisfied

(3)  $\Theta(\text{Theta})$

Consider  $g(n) = n^2$

$$1^*(n^2) \leq n^2 \log n + n \leq 10^*(n^2)$$

$$\text{For } c_1 = 1$$

$$c_2 = 10$$

$$n \geq 1$$

$\Theta(n)$  is satisfied

81  $f(n) = 2n^2 + 3n + 4$ . Satisfy.  $\Omega$ ,  $\Omega$ ,  $\Omega$ .

Ans Consider  $g(n) = n^2$

(i)  $\Omega(n^2)$

$$f(n) \leq c * g(n)$$

$$2n^2 + 3n + 4 \leq 10^*(n^2)$$

① For  $(c=10)$

$\Omega(n^2)$  is satisfied.

(ii)  $\Omega(n^2)$

$$f(n) \geq c * g(n)$$

$$2n^2 + 3n + 4 \geq 1^*(n^2)$$

② For  $(c=1)$

$\Omega(n^2)$  is satisfied.

(iii)  $\Theta(n^2)$

$$1^*(n^2) \leq 2n^2 + 3n + 4 \leq 10^*(n^2)$$

For  $(c_1 = 1)$   
 $c_2 = 10$   
 $g(n) = n^2$

$\Theta(n^2)$  is satisfied.

Q2  $f(n) = n^2 \log n + n$

Ans Consider  $g(n) = n^2 \log n$

(i)  $\Theta(n^2 \log n)$

$$f(n) \leq c^* g(n)$$

$$n^2 \log n + n \leq 10^* n^2 \log n.$$

for  $c=10$   
 $n \geq 2$

$\Theta(n^2 \log n)$  is satisfied.

(ii)  $\Omega(n^2 \log n)$

$$f(n) \geq c^* g(n)$$

$$n^2 \log n + n \geq 1^* n^2 \log n.$$

for  $c=1$   
 $n \geq 1$

$\Omega(n^2 \log n)$  is satisfied.

(iii)  $\Theta(n^2 \log n)$

$$c_1^* g(n) \leq f(n) \leq c_2^* g(n)$$

$$1^* (n^2 \log n) \leq n^2 \log n + n \leq 10^* (n^2 \log n)$$

for  $c_1 = 10$   
 $c_2 = 10$   
 $n \geq 2$

$\Theta(n^2 \log n)$  is satisfied.

Q1  $f(n) = 4n^2 + 5n + 3$   
 $g(n) = 5n$

Find all notations for above example.

Q2 Two Algo A<sub>1</sub> and A<sub>2</sub> run on same machine. Running time of A<sub>1</sub> is  $10n^2$  & running time of A<sub>2</sub> is  $2^n$ . for what value of n, A<sub>1</sub> runs faster than A<sub>2</sub>?

Q3 find  $c^*$  for  $f(n) = 3n^2 + 2n + 5$ .

Answers

~~A-1~~ for ①  $\Theta(5n^2)$

$$4n^2 + 5n + 3 \leq 5n^2$$

for A

$$\begin{array}{r} 36 \\ \times 3 \\ \hline 108 \\ 108 \\ \hline 108 \end{array} \quad \begin{array}{r} 81 \\ \times 4 \\ \hline 324 \\ 324 \\ \hline 324 \end{array} \quad \begin{array}{r} 64 \\ \times 5 \\ \hline 320 \\ 320 \\ \hline 320 \end{array} \quad \begin{array}{r} 81 \\ \times 5 \\ \hline 405 \\ 405 \\ \hline 405 \end{array} \quad \begin{array}{r} 36 \\ \times 9 \\ \hline 324 \\ 324 \\ \hline 324 \end{array}$$

$$\begin{array}{r} 64 \\ \times 9 \\ \hline 576 \\ 576 \\ \hline 576 \end{array} \quad \begin{array}{r} 256 \\ \times 9 \\ \hline 224 \\ 224 \\ \hline 224 \end{array} \quad \begin{array}{r} 49 \\ \times 9 \\ \hline 441 \\ 441 \\ \hline 441 \end{array}$$

$$\begin{array}{r} 108 \\ 108 \\ \hline 216 \\ 216 \\ \hline 216 \end{array} \quad \begin{array}{r} 324 \\ 324 \\ \hline 648 \\ 648 \\ \hline 648 \end{array} \quad \begin{array}{r} 320 \\ 320 \\ \hline 576 \\ 576 \\ \hline 576 \end{array}$$

### Answers

Q1  $\Theta(n^2)$

had  $g(n)$  NOT been given, we will take it to be the highest term of the expression  
 $4n^2 + 5n + 3 \leq 10n^2$   
 &  $c = (\text{coff of highest term} + 1)$

(For  $c=1$ )  
 $n \geq 6$

$\Theta(n^2)$  is satisfied  $\rightarrow$  Now for that same value of  $c$ , satisfy all 3 notations for diff. values of  $n$ .

Q2  $\Theta(n^2)$

$$4n^2 + 5n + 3 \leq 5n^2$$

(For  $c=1$ )  
 $n \geq 1$

$\Theta(n^2)$  is satisfied

don't provide constant here  
 ONLY provide the highest term.

Q3  $\Theta(n^2)$

$$\Theta(5n^2) \leq 4n^2 + 5n + 3 \leq 10(5n^2)$$

(For  $c_1=1$ )  
 $c_2=10$   
 $n \geq 1$

$\Theta(n^2)$  is satisfied.

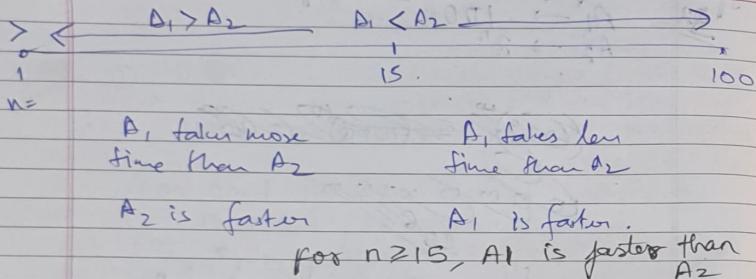
If time is there, draw graph for otherwise show in tabular form!

$$\begin{aligned} A_1 &\rightarrow 100n \\ A_2 &\rightarrow 2^n \end{aligned}$$

$$(100x)^2 \approx 10000 \approx 10^4$$

$$(100x)^4 \approx 100000000 \approx 10^8$$

$n$	$A_1$	$A_2$
1	100	2
100	$10^6$	$2^{100} (2^{10})^{10} \approx 10^{30}$
50	$10^4 \approx 10^6$	$2^{50} \approx 10^{15}$
25	$10^2 \approx 10^6$	$2^{25} \approx 10^7$
15	$10^0 \approx 10^6$	$2^{15} \approx 10^4$
14	$2^{14} \approx 10^6$	$2^{14} \cdot 2^1 \approx 10^6$



$$f(n) = 3n^2 + 2n + 5$$

$$\text{consider } g(n) = n^2$$

for  $n \geq 15$

$$f(n) \geq c * g(n)$$

$$3n^2 + 2n + 5 \geq 1 * n^2$$

$$\text{for } (c=1) \\ n \geq 1$$

$c(n^2)$  is satisfied.

## # Primitive Data Types

↳ int

↳ char

↳ float

↳ double, etc.

## ④ Structures (User-defined data type).

[Syntax] : struct structure\_name {

int roll\_no,

char name[10];

float cgpa;

int sem;

};

## ■ calling / invocation :-

\* Create object

① struct student record

{ int roll\_no;

char name[10];

float cgpa;

int sem;

};

② void main()

{ struct student record s1;

struct student record s2 [60];

for 1 student  
for 60 students

## \* self-referential structures

↳ linked list, Trees, graphs.

Code → struct node

```
int data;
struct * ptr → next;
```

void main()

```
{ struct node N1;
```

```
printf("enter value of node");
scanf("%d", &N1.data);
```

## # Dynamic Memory Allocation (Run-time) [Hence]

## # Static Memory Allocation (compile-time) [STACK]

## # Dynamic Memory Allocation

malloc() → increase size of block

calloc()

realloc  
malloc()

free()

All these fns are declared in <stdlib.h>

① malloc (size of block) ← for 1 block

② calloc (n-blocks, size of each block)  
→ it is a contiguous size allocation. ↑ for more than one block.  
built-in fn in <stdlib.h>.

③ malloc  
→ used to dynamically allocate multiple blocks of memory & each block is of same size.

void \* malloc (4);  
void \* calloc (5, 4);

④ realloc (ptr, size of block);

→ No info. is lost  
→ first block (before) is deleted & new block with new size is created.

void \* realloc (5, 7);

⑤ free(ptr);  
→ frees the memory space  
void \* free (ptr);