

**Academic Year: 2023-24 (ODD)**

**Test : Internal Examination I**

**Date & Session : 14/08/2023 & FN**

**Course Code & Title : 21MAB201T&Transforms and Boundary Value Problems Duration: 1 Hour**

**Year & Sem : 2<sup>nd</sup> Year & III Sem**

**Max. Marks: 30**

**Part - A**

**Answer all questions**

**(10Q x 1M = 10 Marks)**

Q. No	Question	Marks	BL	CO	PO
1	A complete solution of PDE $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} - z = \frac{\partial z}{\partial x} \frac{\partial z}{\partial y}$ (a) $z=ax+by-ab$ , where a,b are arbitrary constants. (b) $z=x^2+y^2-2ab$ , where ab and b are arbitrary constants. (c) $z=ax^2+by^2+abxy$ , where a and b are arbitrary constants. (d) $z=ax-by+ab$ , where a,b are arbitrary constants.	1	4	1	1
2	Which of the following statement is correct for the given partial differential equation $\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} = \frac{\partial^2 u}{\partial x^2}$ a. It is linear equation of order two. c. It is linear equation of order one. b. It is non-linear equation of order two. d. It is non-linear equation of order one.	1	4	1	2
3	To solve the form of $Pp+Qq=R$ , we form the subsidiary equation of the form: (a) $\frac{dx}{P} = \frac{dy}{Q} = \frac{dz}{R}$ , (b) $\frac{dx}{x} = \frac{dy}{y} = \frac{dz}{z}$ , (c) $\frac{xdx}{P} = \frac{ydy}{Q} = \frac{zdz}{R}$ , (d) $\frac{dx}{P} = \frac{dy}{Q} = \frac{dz}{R}$	1	1	1	2
4	A partial differential equation has (a) one independent variable, (c) two or more independent variables, (b) more than one dependent variable, (d) equal number of dependent and independent variables	1	1	1	1
5	Find the Complementary function of $(D^2 + DD' - 2D'^2)z = 0$ (a) $z = \phi_1(y-2x) + \phi_2(y-x)$ , (c) $z = \phi_1(y-2x) + \phi_2(y+x)$ (b) $z = \phi_1(y+2x) + \phi_2(y+x)$ , (d) $z = \phi_1(y+2x) + \phi_2(y-x)$	1	2	1	2
6	The P.I. of $(D^3 + 7DD'^2 - 6D'^3)z = e^{2x+3y}$ (a) $\frac{-1}{28}e^{2x+3y}$ , (b) $\frac{-1}{12}e^{2x+3y}$ , (c) $\frac{1}{28}e^{2x+3y}$ , (d) $\frac{-1}{28}e^{2x+3y}$	1	4	1	2
7	The two sets of Lagrange's multipliers of $(3z-4y)p+(4x-2z)q=2y-3x$ are (a) x,y,z; 2,3,4 (b) $\frac{1}{x}, \frac{1}{y}, \frac{1}{z}$ ; 2,3,4 (c) x,y,z; 4,2,3 (d) $\frac{1}{x}, \frac{1}{y}, \frac{1}{z}$ ; 4,2,3	1	4	1	2
8	The general solution of $\frac{\partial z}{\partial x} P + \frac{\partial z}{\partial y} Q = z$ is (a) $f\left(\frac{x}{y}, \frac{y}{z}\right)$ (b) $f\left(\frac{x}{x}, \frac{y}{z}\right)$ (c) $f\left(\frac{x}{z}, \frac{y}{y}\right)$ (d) $f\left(\frac{x}{x}, \frac{y}{y}\right)$	1	4	1	2
9	If the given PDE is of the type $F(p,q)=0$ , its complete solution is given by (a) $z=a+bx+c$ (b) $z=ax+by+c$ (c) $z=ax^2+by^2+c$ (d) $z=ax+b+y+cz$	1	1	1	2
10	The complete integral of $p=4qx$ is (a) $z = ax^2 + ay + c$ (b) $z = 2ax^2 + ay + c$ (c) $z = ax^2 + by + c$ (d) $z = ax^2 + by^2 + c$	1	4	1	1

**Part B**  
**Answer any three questions**

**3Q x 4M = 12 Marks**

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|----|--|---|---|---|---|
| 11 | Form the Partial Differential Equation $2z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$  | 4 | 4 | 1 | 2 |
| 12 | Solve $\frac{\partial^2 z}{\partial x^2} + \frac{\partial^2 z}{\partial x \partial y} - 6 \frac{\partial^2 z}{\partial y^2} = x + y$ | 4 | 4 | 1 | 2 |
| 13 | Solve the partial differential equation $\frac{y-z}{yz} p = \frac{z-x}{zx} q = \frac{x-y}{xy} r$                                     | 4 | 4 | 1 | 2 |
| 14 | Solve $p \cot x + q \cot y = \cot z$   | 4 | 4 | 1 | 2 |

**Part C**  
**Answer all questions**

**1Q x 8M = 8 Marks**

- |     |   |   |   |   |   |
|-----|---|---|---|---|---|
| 15. | (A) Solve $(D^2 + DD' - 6D'^2)z = x^2 \sin(x+y)$      | 8 | 4 | 1 | 2 |
|     | (OR)  |   |   |   |   |
|     | (B) Obtain the solution of the following equation:    | 8 | 4 | 1 | 2 |
|     | $(D^2 + DD' - 6D'^2)z = \cos(x-y) + x^2 + xy^2 + y^3$ |   |   |   |   |