

Robustness of Deep Neural Networks to Occlusion

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Occlusion



An occlusion is an event wherein parts of an image are blocked, either partially or completely by another object in the scene.

Types of Occlusion



(a) Uniform

Colour is same in all occluded pixels.



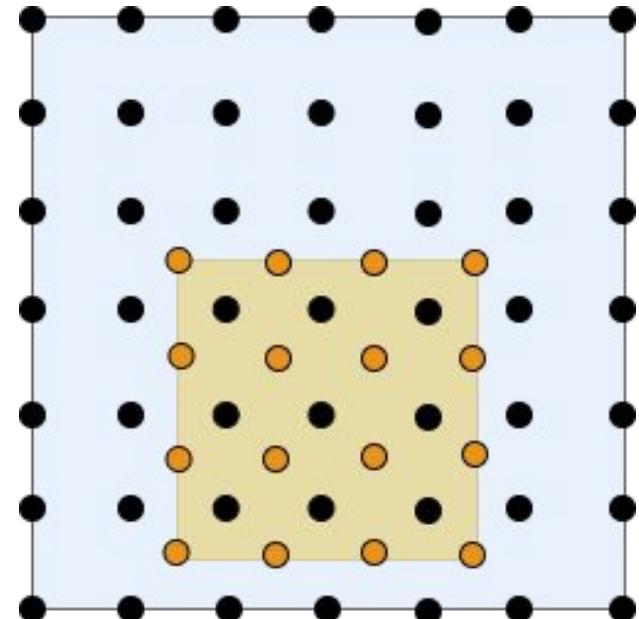
(b) Multiform

Colours vary from $[-\epsilon, \epsilon]$ where ϵ denotes the threshold between original pixel value and occluded pixel value.

Occlusion Position

- L1 distance between image pixel and surrounding occluding pixels is less than 1.
- Contributions from all four surrounding pixels is summed up.

$$s_{ij} = \max(0, \sum_{i' \in \mathbb{I}_n} (|i - i'| + 1) + \sum_{j' \in \mathbb{I}_n} (|j - j'| + 1) - 1)$$



Occlusion Operation

$$x'_{ij} = x_{ij} - s_{ij} \times (x_{ij} - \zeta(x, i, j))$$

$x_{i,j}$: Original pixel value

$x'_{i,j}$: Updated pixel value

$s_{i,j}$: Coefficient of occlusion

$\zeta(x, i, j)$: Colour of occlusion at (i, j)

Uniform occlusion: $\zeta(x, i, j) = \mu$.

Multiform occlusion: $\zeta(x, i, j) = x_{ij} + \Delta_p$ $\Delta_p \in [-\epsilon, \epsilon]$

Objective

To explore various occlusion encodings for benchmark datasets like MNIST, CIFAR-10 and GTSRB and verify the robustness of neural networks to these perturbations.

Random Erasing

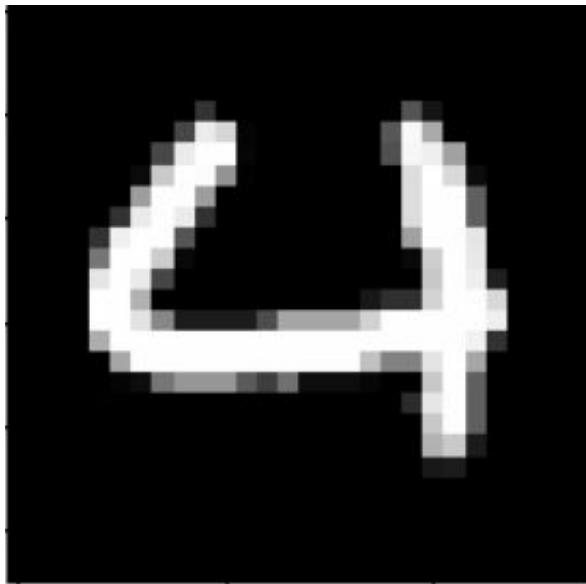
- Randomly picks upper left corner of occlusion rectangle.
- Replaces or “erases” occlusion rectangle with random colour.

Limitation: Only picks integer coordinates
We need to consider real-valued
coordinates.

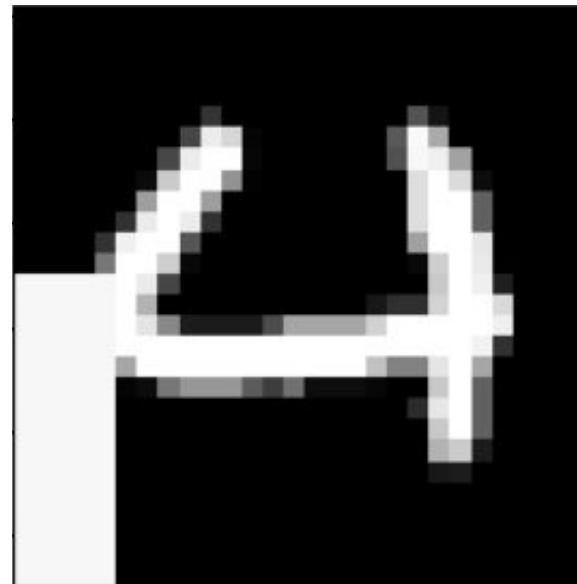
Algorithm 1: Random Erasing Procedure

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Input : Input image  $I$ ; Image size  $W$  and  $H$ ; Area of image  $S$ ; Erasing probability  $p$ ; Erasing area ratio range  $s_l$  and  $s_h$ ; Erasing aspect ratio range  $r_1$  and  $r_2$ .  
Output: Erased image  $I^*$ .  
Initialization:  $p_1 \leftarrow \text{Rand}(0, 1)$ .  
1 if  $p_1 \geq p$  then  
2    $I^* \leftarrow I$ ;  
3   return  $I^*$ .  
4 else  
5   while True do  
6      $S_e \leftarrow \text{Rand}(s_l, s_h) \times S$ ;  
7      $r_e \leftarrow \text{Rand}(r_1, r_2)$ ;  
8      $H_e \leftarrow \sqrt{S_e \times r_e}$ ,  $W_e \leftarrow \sqrt{\frac{S_e}{r_e}}$ ;  
9      $x_e \leftarrow \text{Rand}(0, W)$ ,  $y_e \leftarrow \text{Rand}(0, H)$ ;  
10    if  $x_e + W_e \leq W$  and  $y_e + H_e \leq H$  then  
11       $I_e \leftarrow (x_e, y_e, x_e + W_e, y_e + H_e)$ ;  
12       $I(I_e) \leftarrow \text{Rand}(0, 255)$ ;  
13       $I^* \leftarrow I$ ;  
14      return  $I^*$ .  
15    end  
16  end  
17 end
```

Random Erasing



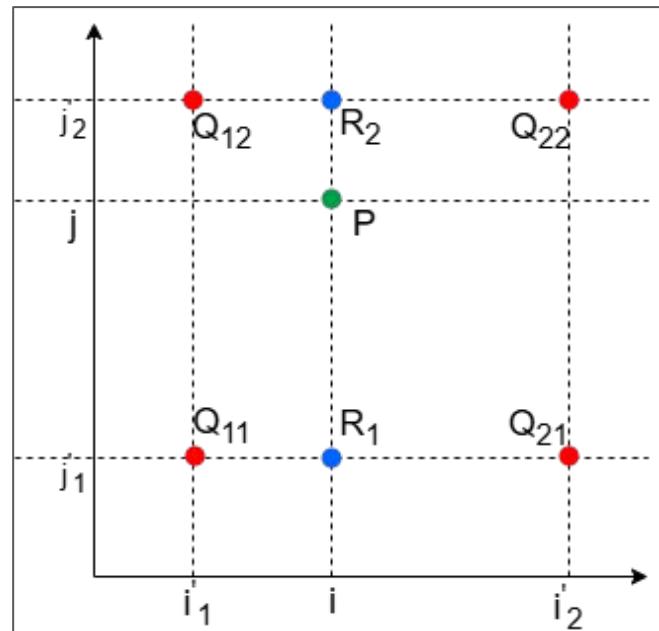
Original Image



Occluded image

Bilinear Interpolation

- Calculates pixel intensities when image is mapped to another geometry.
- Bilinear interpolation considers 4 nearest neighbors of interpolated point.
- Image pixel is affected by occlusion pixel if they are less than $\sqrt{2}$ units apart.

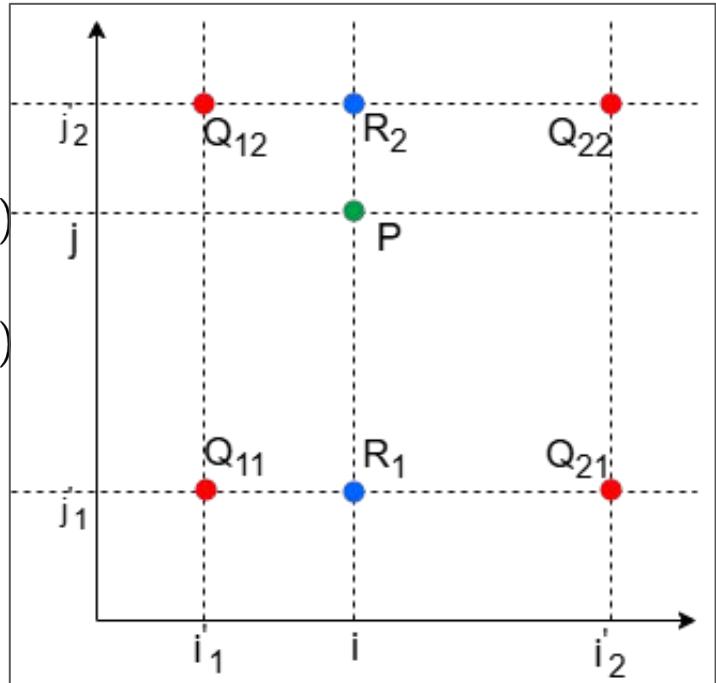


Bilinear Interpolation

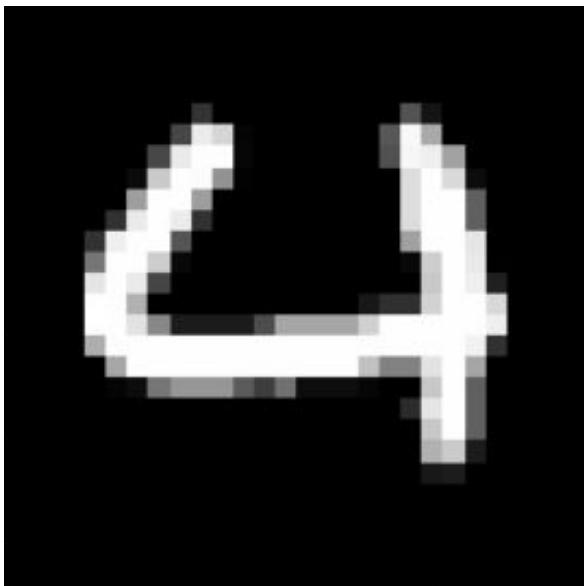
$$R_1(x, y) = Q_{11}(x_2 - x)/(x_2 - x_1) + Q_{21}(x - x_1)/(x_2 - x_1)$$

$$R_2(x, y) = Q_{12}(x_2 - x)/(x_2 - x_1) + Q_{22}(x - x_1)/(x_2 - x_1)$$

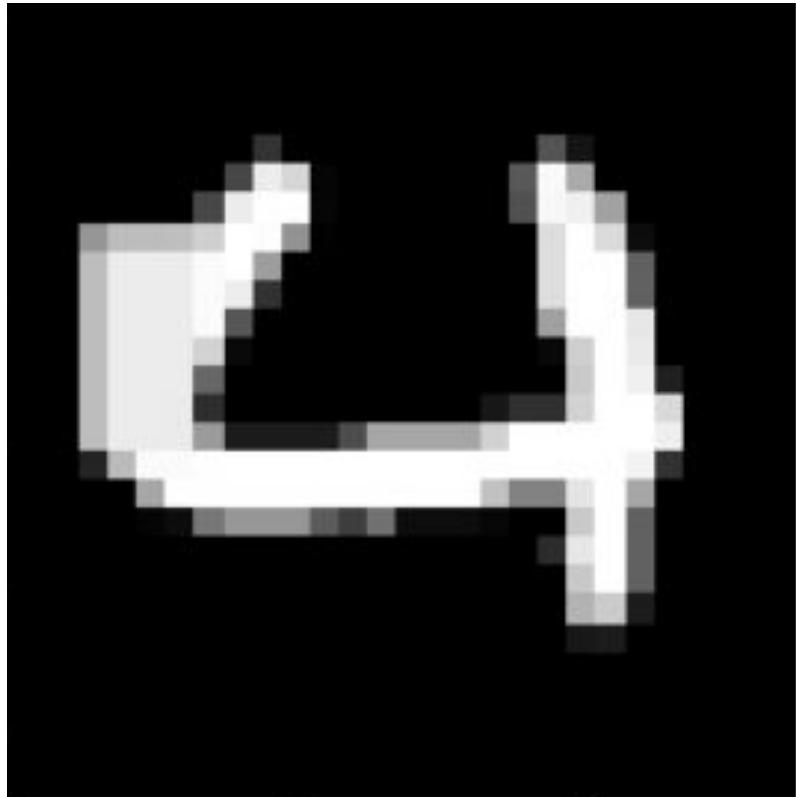
$$P(x, y) = R_1(y_2 - y)/(y_2 - y_1) + R_2(y - y_1)/(y_2 - y_1)$$



Bilinear Interpolation

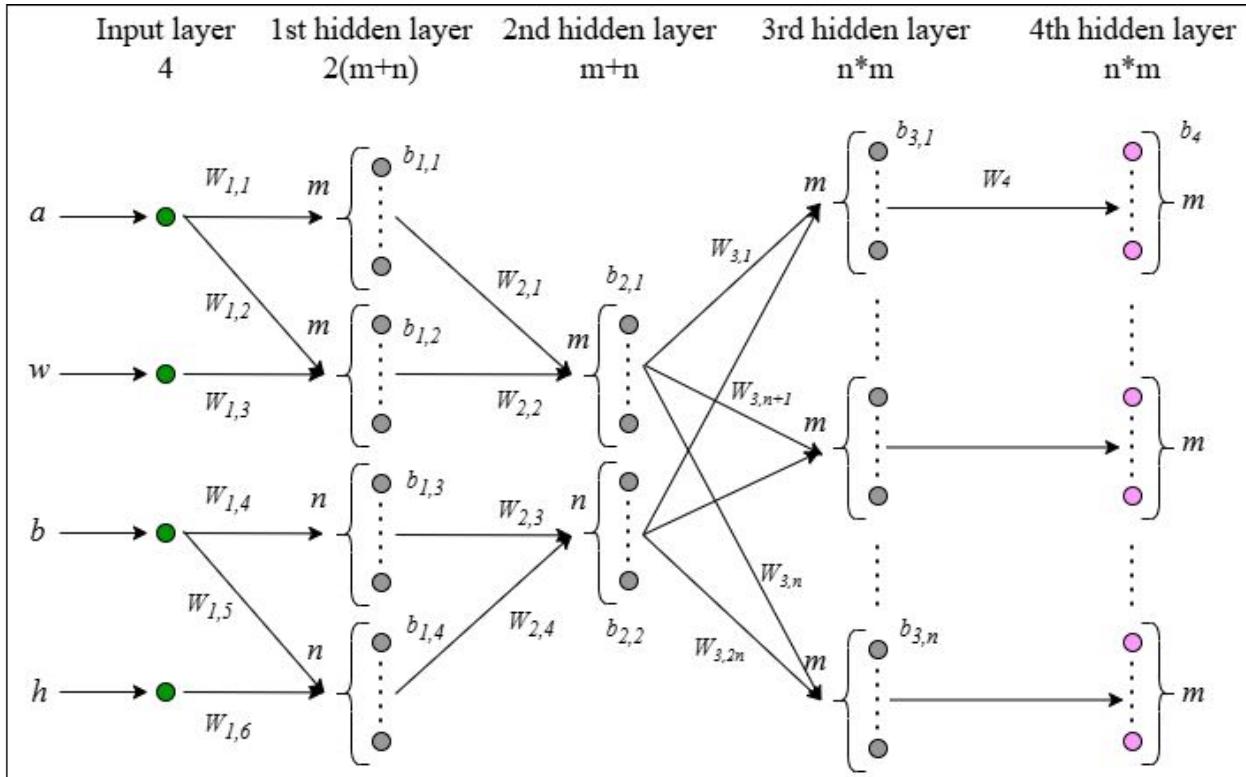


Original Image



Occluded image

Occlusion Encoding with Neural Networks

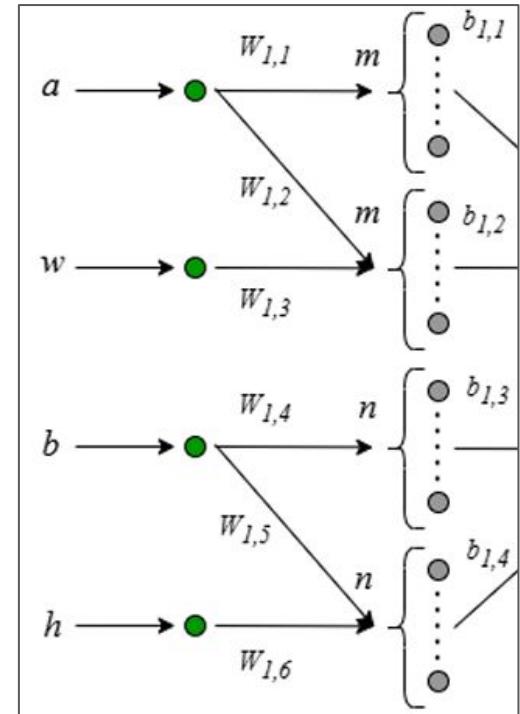


Occlusion Encoding with Neural Networks

First layer encodes the input (a, w, b, h)

$$W_{1,1} = \begin{bmatrix} 1 \\ 1 \\ \cdot \\ \cdot \\ 1 \end{bmatrix}_{m \times 1}, W_{1,2} = \begin{bmatrix} -1 \\ -1 \\ \cdot \\ \cdot \\ -1 \end{bmatrix}_{m \times 1}, W_{1,3} = \begin{bmatrix} -1 \\ -1 \\ \cdot \\ \cdot \\ -1 \end{bmatrix}_{m \times 1},$$

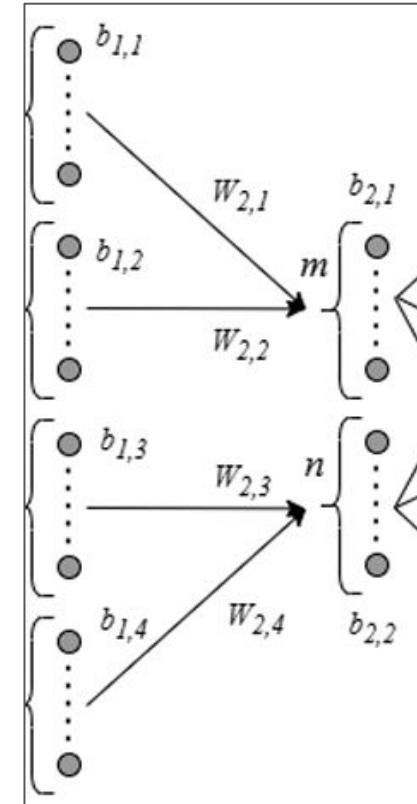
$$b_{1,1} = \begin{bmatrix} -1 \\ -2 \\ \cdot \\ \cdot \\ -m \end{bmatrix}_{m \times 1}, b_{1,2} = \begin{bmatrix} 2 \\ 3 \\ \cdot \\ \cdot \\ m+1 \end{bmatrix}_{m \times 1}$$



Occlusion Encoding with Neural Networks

Second layer: if i^{th} neuron in the first m neurons is 1 and j^{th} neuron in the next n neurons is 1 then (i,j) is occluded.

$$W_{2,i} = \begin{bmatrix} -1 & & & \\ & -1 & & \\ & & \ddots & \\ & & & -1 \end{bmatrix}_{m \times m}$$

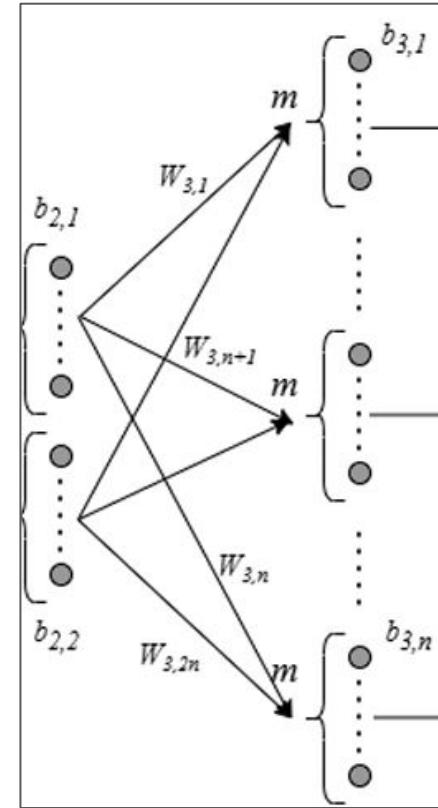


Occlusion Encoding with Neural Networks

Third layer: Outputs $m \times n$ neurons, each neuron has the occlusion factor s_{ij} of each pixel.

$$W_{3,i} = \begin{bmatrix} 1 & 0 & \dots & 0 \\ 1 & 0 & \dots & 0 \\ \vdots & & \ddots & \vdots \\ 1 & 0 & \dots & 0 \end{bmatrix}_{m \times m}, W_{3,n+i} = \begin{bmatrix} 1 & & & \\ & 1 & & \\ & & \ddots & \\ & & & 1 \end{bmatrix}_{m \times n}$$

$$b_{3,i} = \begin{bmatrix} -1 \\ -1 \\ \vdots \\ -1 \end{bmatrix}_{1 \times m}$$



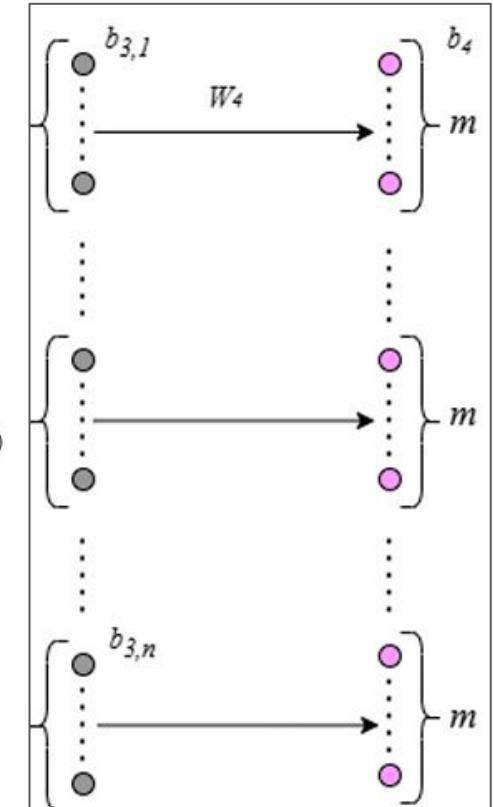
Occlusion Encoding with Neural Networks

Fourth layer: Encodes the pixel values of original image and occlusion colours.

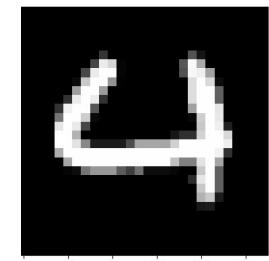
$$W_4 = \begin{bmatrix} \mu - x_1 & \mu - x_2 & \cdot & \cdot \\ & \cdot & \cdot & \cdot \\ & & \cdot & \cdot \\ & & & \mu - x_{m \times n} \end{bmatrix}_{(mn) \times (mn)}$$

$$b_4 = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_{mn} \end{bmatrix}_{mn \times 1}$$

$$W_4 = \begin{bmatrix} \Delta_1 & \Delta_2 & \cdot & \cdot \\ & \cdot & \cdot & \cdot \\ & & \cdot & \cdot \\ & & & \Delta_{mn} \end{bmatrix}_{(mn) \times (mn)}$$
$$W_4 \cdot O_3 + b_4 = (\zeta(x, i, j) - x_{ij}) \times s_{ij} + x_{ij}$$



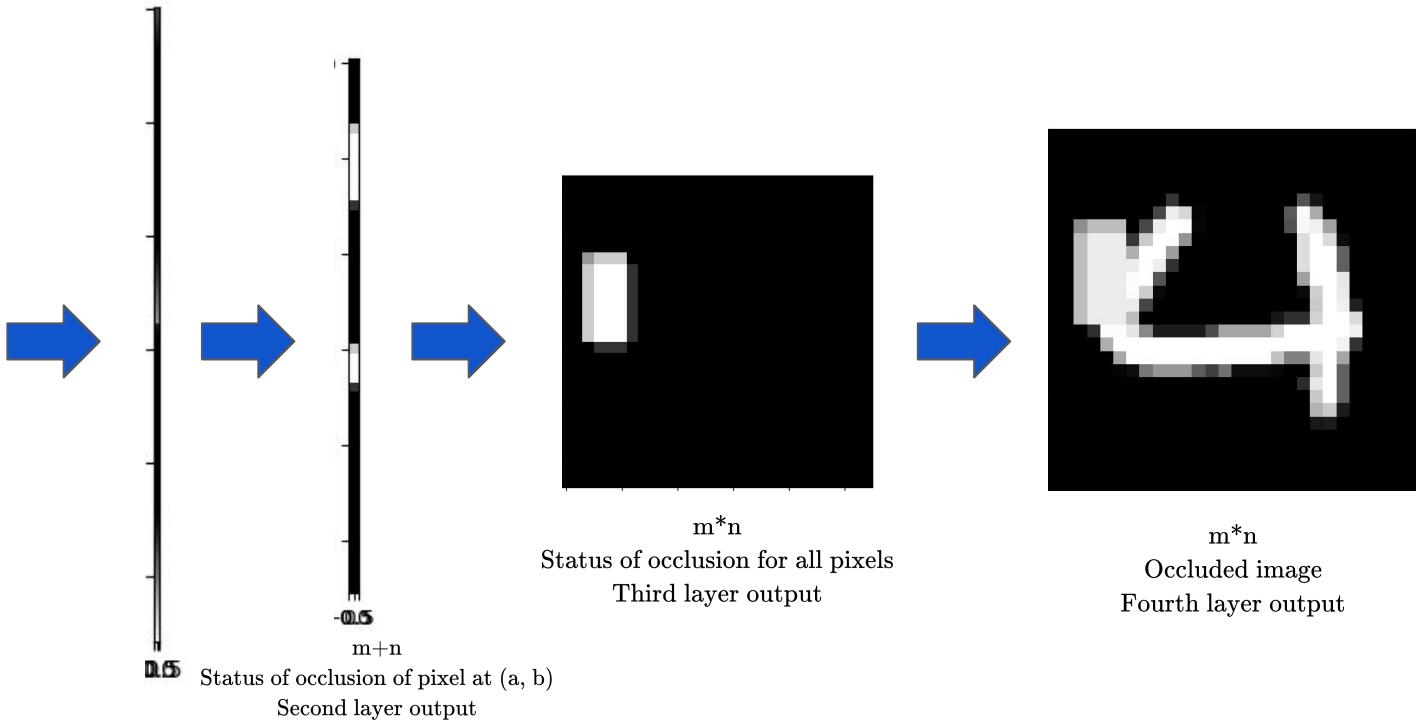
Occlusion Encoding with Neural Networks



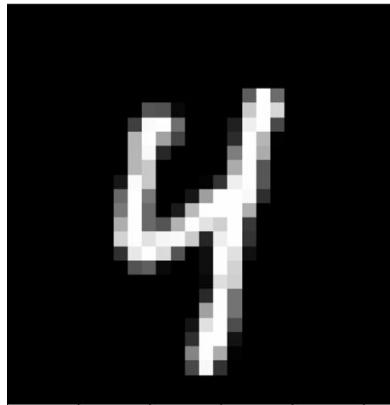
$(a, b) = (8.2, 3.2)$

$(w, h) = (8, 4)$

Occlusion colour : 234

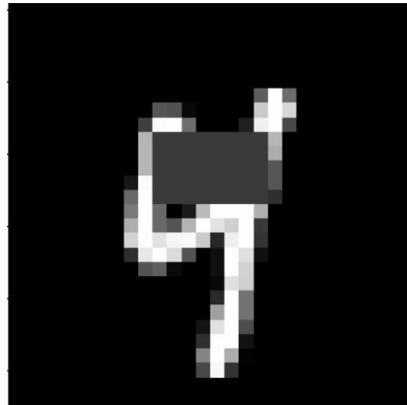


Results

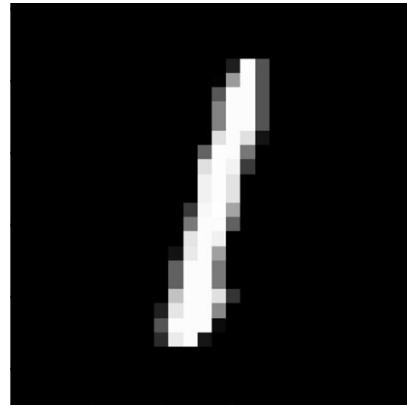


Original image

“4” classified as “9”

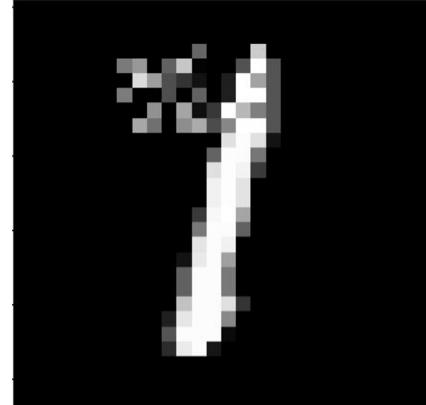


Occluded Image



Original image

“1” classified as “8”



Occluded Image

Results



Original image

“deer” classified as “bird”

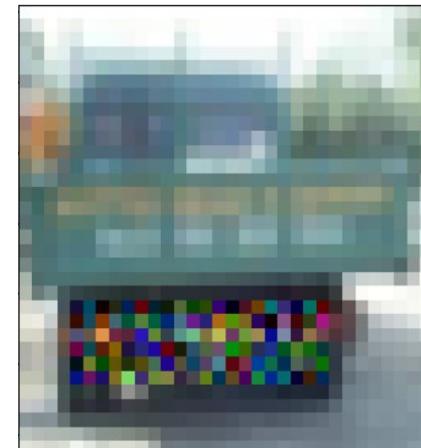


Occluded Image



Original image

“truck” classified as “ship”



Occluded Image

Results



Original image

“50” classified as “80”



Occluded Image



Occluded image

“70” classified as “30”



Original Image

Future Work

- Extend encoding to handle more complex shapes like parallelograms, triangles and circles.
- Estimate a range for the threshold ϵ .

References

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Thank You