## 1 データ構造

## Union-Find

```
struct UnionFind{
        vector < int > dat;
3
        UnionFind(int sz){
4
5
            dat.assign(sz, -1);
        }
6
7
        bool unite(int x, int y){
8
9
            x = root(x), y = root(y);
10
            if(x == y) return(false);
            if(dat[x] > dat[y]) swap(x, y);
11
12
            dat[x] += dat[y];
13
            dat[y] = x;
14
            return(true);
15
        }
16
17
        int root(int k){
            if(dat[k] < 0) return(k);</pre>
18
19
            return(dat[k] = root(dat[k]));
20
21
        int size(int k){
22
23
            return(-dat[root(k)]);
24
        }
25 };
```

# Binary Indexed Tree

```
1 template < class T >
   struct BinaryIndexedTree {
        vector < T > dat;
4
5
       BinaryIndexedTree(int sz) {
            dat.assign(++sz, 0);
7
       }
       T sum(int k){
9
            T ret = 0;
10
11
            for(++k; k > 0; k -= k & -k) ret += data[k];
12
            return ret;
13
       }
14
15
        void add(int k, T x){
16
            for(++k; k < data.size(); k += k & -k) data[k] += x;</pre>
17
        }
18 };
```

#### Segment Tree

```
1 /*
2 !) 0-indexed
3 !) [a, b)に対する演算
4 !) merge, updateNodeを書く
5 */
6 template < typename Monoid >
  struct Segtree{
       int n;
8
9
       vector < Monoid > dat;
       Monoid m0; // データの初期化値
10
       Segtree(int sz, Monoid m0) : m0(m0){
11
           n = 1;
12
13
           while (n < sz) n *= 2;
14
           dat.assign(2*n-1, m0);
15
       }
16
17
       Monoid merge(Monoid a, Monoid b) // 区間をマージする二項演算
       void updateNode(int k, Monoid x) // 区間を操作する二項演算
18
19
20
       void update(int k, Monoid x){
21
           k += n-1;
22
           updateNode(k, x);
23
           while(k > 0) {
24
               k = (k-1)/2;
               dat[k] = merge(dat[k*2+1], dat[k*2+2]);
25
           }
26
27
       }
28
       Monoid query(int a, int b){
29
           Monoid L = m0, R = m0;
30
           int A = a+n-1;
           int B = b+n-1;
31
32
           while(A < B) {
33
               if((A&1) == 0) L = merge(L, dat[A++]);
               if((B\&1) == 0) R = merge(dat[--B], R);
34
35
               A >>= 1:
36
               B >>= 1;
37
           }
38
           return merge(L, R);
39
40
       Monoid operator[](const int &k) const { return dat[k+n-1]; }
41 };
42
43 //######## 例 ########
44 // Range min (AOJ DSL_2_A)
45 Monoid merge(Monoid a, Monoid b){ return min(a,b); }
46 void updateNode(int k, Monoid x){ dat[k] = x; }
47
  Segtree < LL > a(n, (1LL < < 31) - 1);
48
49 // Range add (AOJ DSL_2_B)
50 Monoid merge(Monoid a, Monoid b) { return a + b; }
51 void updateNode(int k, Monoid x){ dat[k] += x; }
52 Segtree < LL > a(n, 0);
```

#### 遅延伝搬 Segment Tree

```
1 /*
2 !) O-indexed 遅延伝搬セグメント木
3 !) [a, b)に対する演算
4 !) MO, LO, merge, updateNode, propagateを書く
5 */
6 template <typename Monoid>
   struct LazySegtree {
       int n;
9
       vector < Monoid > dat, lazy;
10
       Monoid MO, LO // データと遅延配列の初期化値 queryに合わせて選択する
11
12
13
       LazySegtree(int sz, Monoid dat_init){
14
           n = 1;
15
           while (n < sz) n *= 2;
16
           dat.assign(2*n-1, dat_init);
17
           lazy.assign(2*n-1, L0);
18
       }
19
20
       Monoid merge(Monoid a, Monoid b) // 区間をマージする二項演算
       void updateNode(int k, Monoid x) // 区間を操作する二項演算
21
22
       void propagate(int k, int l, int r) // 遅延配列の伝搬のさせ方
23
24
       void eval(int k, int l, int r) {
           if(lazy[k] == L0) return;
26
           propagate(k, 1, r);
27
           if(r-1 > 1) {
28
               updateNode(2*k+1, lazy[k]);
29
               updateNode(2*k+2, lazy[k]);
30
           }
31
           lazy[k] = L0;
32
       }
33
34
       void update(int a, int b, Monoid x, int k, int l, int r) {
35
           eval(k, 1, r);
36
           if (r <= a || b <= 1) return;
           if (a <= 1 && r <= b) {
37
               updateNode(k, x);
39
               eval(k, 1, r);
40
           }else{
41
               update(a, b, x, k*2+1, 1, (1+r)/2);
42
               update(a, b, x, k*2+2, (1+r)/2, r);
43
               dat[k] = merge(dat[2*k+1], dat[2*k+2]);
44
45
       }
46
47
       void update(int a, int b, Monoid x) {
           update(a, b, x, 0, 0, n);
48
49
50
51
       Monoid query(int a, int b, int k, int l, int r) {
52
           eval(k, 1, r);
53
           if (r <= a || b <= 1) return MO;
54
           if (a <= 1 && r <= b) return dat[k];
55
           Monoid L = query(a, b, k*2+1, 1, (1+r)/2);
```

```
56
           Monoid R = query(a, b, k*2+2, (1+r)/2, r);
57
           return merge(L, R);
58
59
60
       Monoid query(int a, int b){
61
           return query(a, b, 0, 0, n);
62
       }
63 };
64
65 //######## 例 #########
66 // Range update - min (AOJ DSL_2_F)
67 Monoid MO = LLINF, LO = LLINF;
68 Monoid merge(Monoid a, Monoid b) { return min(a, b); }
69 void updateNode(int k, Monoid x){ lazy[k] = x; }
70 void propagate(int k, int l, int r){ dat[k] = lazy[k]; }
71 LazySegtree <LL> seg(n+1, (1LL <<31)-1);
72
73 // Range update - sum (AOJ DSL_2_I)
74 Monoid MO = 0, LO = LLINF;
75 Monoid merge(Monoid a, Monoid b){ return a + b; }
76 void updateNode(int k, Monoid x){ lazy[k] = x; }
77 void propagate(int k, int 1, int r){ dat[k] = lazy[k]*(r-1); }
78 LazySegtree <LL> seg(n+1, 0);
80 // Range add - min (AOJ DSL_2_H)
81 Monoid MO = LLINF, LO = 0;
82 Monoid merge(Monoid a, Monoid b){ return min(a, b); }
83 void updateNode(int k, Monoid x){ lazy[k] += x; }
84 void propagate(int k, int l, int r){ dat[k] += lazy[k]; }
85 LazySegtree < LL > seg(n+1, 0);
86
87 // Range add - sum (AOJ DSL_2_G)
88 Monoid MO = 0, LO = 0;
89 Monoid merge(Monoid a, Monoid b){    return a + b;    }
90 void updateNode(int k, Monoid x){ lazy[k] += x; }
91 void propagate(int k, int l, int r){ dat[k] += lazy[k]*(r-l); }
92 LazySegtree <LL> seg(n+1, 0);
```

## 2 グラフ

#### Grid 上での BFS

```
1 int W, H;
2 vector < vector < char >> s;
   vector < vector < int >> cost;
   int bfs(){
        int dx[] = \{0, 1, 0, -1\}, dy[] = \{1, 0, -1, 0\};
        queue < pair < int , int >> que;
6
7
        que.push(make_pair(0, 0));
8
        cost[0][0] = 0;
9
10
        while(!que.empty()) {
11
            pair<int, int> p = que.front();
12
            que.pop();
            if(p == make_pair(H-1, W-1)){
13
                // ゴールに到達
14
15
                return cost[p.first][p.second];
16
            for(int i = 0; i < 4; i++) {
17
18
                int ny = p.first + dy[i], nx = p.second + dx[i];
                if (nx < 0 \mid | ny < 0 \mid | nx >= W \mid | ny >= H) continue;
19
20
                if(s[ny][nx] == '#') continue;
21
                if(cost[ny][nx] != -1) continue;
22
23
                cost[ny][nx] = cost[p.first][p.second] + 1;
24
                 que.push(make_pair(ny, nx));
25
            }
26
        }
27
        return -1;
28 }
```

## Dijkstra 法 (単一始点最短経路)

```
1 struct edge{
        int to, cost;
3 };
   using WeightedGraph = vector<vector<edge>>;
 6
   vector<int> dijkstra(WeightedGraph &G, int st){
        vector<int> dist(G.size(), INF);
7
8
        using pi = pair<int, int>;
9
        priority_queue < pi, vector < pi >, greater < pi >> que;
        dist[st] = 0;
10
11
        que.push(mp(dist[st], st));
12
        while(!que.empty()){
13
            int cost, idx;
14
            tie(cost, idx) = que.top(); que.pop();
            if(dist[idx] < cost) continue;</pre>
15
16
            for(auto &e: G[idx]){
17
                if(dist[e.to] <= cost+e.cost) continue;</pre>
                dist[e.to] = cost+e.cost;
18
19
                 que.push(mp(dist[e.to], e.to));
20
            }
```

```
21 }
22 return dist;
23 }
```

## Bellman-Ford 法 (負路あり単一始点最短経路)

```
1 struct edge{
       int src, to, cost;
3 };
  using Edges = vector<edge>;
6
   vector<int> bellman_ford(Edges &E, int V, int st){
7
       vector < int > dist(V, INF);
       dist[st] = 0;
8
       rep(i, V-1){
9
10
            for(auto &e: E){
                if(dist[e.src] == INF) continue;
11
12
                dist[e.to] = min(dist[e.to], dist[e.src]+e.cost);
            }
1.3
14
       }
15
       for(auto &e: E){
16
            if(dist[e.src] == INF) continue;
17
            if(dist[e.to] > dist[e.src]+e.cost){
                // 負閉路が存在
18
19
                return vector < int > ();
20
            }
21
       }
22
       return dist;
23 }
```

## Warshall-Floyd 法 (全点対間最短経路)

```
1 using Graph = vector < vector < int >>;
2
3 void warshall_floyd(Graph & G) {
4    int V = G.size();
5    rep(k, V)rep(i, V)rep(j, V) {
6        if(G[i][k] == INF || G[k][j] == INF) continue;
7    G[i][j] = min(G[i][j], G[i][k]+G[k][j]);
8    }
9    // G[i][i] < Oが存在 <=> 負閉路が存在
10 }
```

#### Kruskal 法 (最小全域木)

```
1 // UnionFindが必要
2
3 struct edge{
4    int src, to, cost;
5 };
6 using Edges = vector<edge>;
7
8 int kruskal(Edges &E, int V)
9 {
10    sort(all(E), [](const edge &a, const edge &b)
11 {
```

```
12
            return (a.cost < b.cost);</pre>
13
        });
14
        UnionFind tree(V);
15
        int res = 0;
16
        for(auto &e : E) {
17
            if(tree.unite(e.src, e.to)) res += e.cost;
18
        }
19
        return (res);
20 }
```

### トポロジカルソート

```
1 struct edge{
2
       int to, cost;
3 };
4 using WeightedGraph = vector<vector<edge>>;
  vector<int> tsort(WeightedGraph &G){
7
       vector<int> tsorted;
8
       vector<int> used(G.size(), 0);
9
       bool f = false;
       function < void(int) > dfs = [&](int u){
10
            if(used[u] > 0){
11
                if(used[u] == 1) f = true;
12
13
                return;
14
           }
           used[u] = 1;
15
16
           for(auto &e : G[u]) dfs(e.to);
17
           used[u] = 2;
18
            tsorted.pb(u);
19
       };
20
       rep(i, G.size()) dfs(i);
21
       if(f){}
22
            // 閉路が存在
23
           return vector <int >();
24
       }
25
       reverse(all(tsorted));
26
       return tsorted;
27 }
```

## Dinic 法 (最大流)

```
1 template < typename flow_t >
2 struct Dinic{
3
       const flow_t INF_flow_t = INF; // WRITE HERE
4
5
       struct edge{
6
           int to;
7
           flow_t cap;
8
            int rev;
9
       };
10
       using WeightedGraph = vector<vector<edge>>;
       int V;
11
12
       WeightedGraph G;
13
       vector<int> itr, level;
14
```

```
15
        Dinic(int V) : V(V) { G.assign(V, vector<edge>()); }
16
17
        void add_edge(int from, int to, int cap) {
            G[from].push_back((edge){to, cap, (int)G[to].size()});
18
19
            G[to].push_back((edge){from, 0, (int)G[from].size()-1});
20
21
22
        void bfs(int s) {
23
            level.assign(V, -1);
24
            queue <int> que;
            level[s] = 0;
25
26
            que.push(s);
27
            while (!que.empty()) {
28
                int v = que.front(); que.pop();
29
                for(auto &&e: G[v]){
30
                     if (e.cap > 0 && level[e.to] < 0) {</pre>
31
                         level[e.to] = level[v] + 1;
32
                         que.push(e.to);
33
                    }
34
                }
35
            }
        }
36
37
38
        flow_t dfs(int v, int t, flow_t f) {
39
            if(v == t) return f;
40
            for(int &i = itr[v]; i < (int)G[v].size(); i++) {</pre>
41
                edge &e = G[v][i];
                if (e.cap > 0 && level[v] < level[e.to]) {</pre>
42
                     flow_t d = dfs(e.to, t, min(f, e.cap));
43
                     if (d > 0) {
44
45
                         e.cap -= d;
46
                         G[e.to][e.rev].cap += d;
47
                         return d;
48
                    }
49
                }
50
            }
51
            return 0;
52
        }
53
54
        flow_t max_flow(int s, int t) {
55
            flow_t res = 0, f;
56
            while(bfs(s), level[t] >= 0) {
57
                itr.assign(V, 0);
                while((f = dfs(s, t, INF_flow_t)) > 0) res += f;
58
59
60
            return res;
61
        }
62
   };
63
   // 最小流量制限付き最大流
  // 各辺に[lb, ub]の容量の辺を張る
   template < typename flow_t >
   struct DinicWithLowerBound{
68
        Dinic < flow_t > flow;
69
        int S, T;
70
        flow_t sum_lb;
71
```

```
72
       DinicWithLowerBound(int V): flow(V+2), S(V), T(V+1), sum_lb(0) {}
73
74
       void add_edge(int from, int to, flow_t lb, flow_t ub) {
75
            flow.add_edge(from, to, ub-lb);
76
            flow.add_edge(S, to, lb);
77
            flow.add_edge(from, T, lb);
78
            sum_lb += lb;
       }
79
80
81
       flow_t max_flow(int s, int t) {
            auto a = flow.max_flow(S, T);
82
            auto b = flow.max_flow(s, T);
83
84
            auto c = flow.max_flow(S, t);
85
            auto d = flow.max_flow(s, t);
86
            return (b == c && a + b == sum_lb) ? b+d : -1;
87
       }
88 };
```

#### 二部マッチング

```
struct BipartiteMatching {
2
        using Graph = vector<vector<int>>;
3
        Graph G;
 4
        vector<int> match, alive, used;
5
        int timestamp;
6
        BipartiteMatching(int n) : G(n), alive(n, 1),
 7
                                     used(n, 0), match(n, -1), timestamp(0) {}
8
9
        void add_edge(int u, int v) {
10
11
            G[u].push_back(v);
12
            G[v].push_back(u);
13
        }
14
15
        int dfs(int idx) {
            used[idx] = timestamp;
16
17
            for(auto &&to : G[idx]) {
18
                int w = match[to];
19
                if(alive[to] == 0) continue;
                if (w < 0 \mid | (used[w] \mid = timestamp && dfs(w)))  {
20
21
                     match[idx] = to;
22
                     match[to] = idx;
23
                     return 1;
24
                }
            }
25
26
            return 0;
27
        }
28
29
        int bipartite_matching() {
30
            int res = 0;
31
            for(int i = 0; i < G.size(); i++) {
32
                if(alive[i] == 0) continue;
33
                if(match[i] == -1) {
34
                     ++timestamp;
35
                     res += dfs(i);
36
                }
37
            }
```

```
38
             return res;
39
        }
40
41
         void output() {
42
             for(int i = 0; i < G.size(); i++) {</pre>
43
                  if(i < match[i]) {</pre>
                      cout << i << "-" << match[i] << endl;</pre>
44
45
                  }
             }
46
47
        }
48 };
```

# 3 木

## 木の直径

```
1 struct edge{
       int to, cost;
3 };
4 using WeightedGraph = vector<vector<edge>>;
5 using pi = pair<int, int>;
7 pi dfs(WeightedGraph &G, int idx, int src){
       pi res(0, idx);
       for(auto &e : G[idx]) {
9
           if(e.to == src) continue;
10
11
           pi cost = dfs(G, e.to, idx);
           cost.first += e.cost;
12
13
           res = max(res, cost);
       }
14
15
       return res;
16 }
17
18 int tree_diameter(WeightedGraph &G)
19 {
20
       auto far = dfs(G, 0, -1);
21
       auto res = dfs(G, far.second, -1);
22
       return (res.first);
23 }
```

## 4 数学

#### GCD · LCM

```
1 LL gcd(LL a, LL b){
2    if(a < b) swap(a, b);
3    if(b == 0) return a;
4    return gcd(b, a%b);
5 }
6
7 LL lcm(LL a, LL b){
8    return a*b/gcd(a,b);
9 }</pre>
```

#### ModInt

```
1 template < int mod >
   struct ModInt {
3
        int x;
4
        ModInt() : x(0) {}
5
6
         ModInt(long long y) : x(y >= 0 ? y \% mod : (mod - (-y) \% mod) \% mod) { }  
7
8
        ModInt &operator+=(const ModInt &p) {
            if((x += p.x) >= mod) x -= mod;
9
            return *this;
10
11
12
        ModInt &operator -= (const ModInt &p) {
13
            if((x += mod - p.x) >= mod) x -= mod;
14
            return *this;
15
16
        ModInt &operator*=(const ModInt &p) {
17
            x = (int)(1LL * x * p.x % mod);
18
            return *this;
19
        }
20
        ModInt &operator/=(const ModInt &p) {
21
            *this *= p.inverse();
22
            return *this;
23
        }
24
25
        ModInt operator-() const { return ModInt(-x); }
26
        ModInt operator+(const ModInt &p) const { return ModInt(*this) += p; }
        ModInt operator-(const ModInt &p) const { return ModInt(*this) -= p; }
27
28
        ModInt operator*(const ModInt &p) const { return ModInt(*this) *= p; }
29
        ModInt operator/(const ModInt &p) const { return ModInt(*this) /= p; }
30
31
        bool operator == (const ModInt &p) const { return x == p.x; }
32
        bool operator!=(const ModInt &p) const { return x != p.x; }
33
34
        ModInt inverse() const{
35
            int a = x, b = mod, u = 1, v = 0, t;
36
            while(b > 0) {
37
                t = a / b;
38
                a -= t * b;
39
                swap(a, b);
```

```
40
                u -= t * v;
41
                swap(u, v);
42
43
            return ModInt(u);
44
        }
45
46
        ModInt pow(int e){
47
            long long a = 1, p = x;
48
            while(e > 0) {
49
                 if(e%2 == 0) {p = (p*p) % mod; e /= 2;}
50
                else \{a = (a*p) \% mod; e--;\}
51
52
            return ModInt(a);
53
54
55
        friend ostream &operator<<(ostream &os, const ModInt<mod> &p) {
56
            return os << p.x;
57
        }
        friend istream &operator>>(istream &is, ModInt<mod> &a) {
59
            long long x;
60
            is >> x;
61
            a = ModInt < mod > (x);
62
            return (is);
63
64 };
65
66 const int mod = 1e9 + 7;
67 using modint = ModInt < mod > ;
```

#### **FFT**

```
1 // https://ei1333.github.io/luzhiled/snippets/math/fast-fourier-transform.html
   namespace FastFourierTransform {
3
        using real = double;
4
        struct C {
5
            real x, y;
6
7
            C() : x(0), y(0) {}
            C(real x, real y) : x(x), y(y) {}
8
            inline C operator+(const C &c) const { return C(x + c.x, y + c.y); }
9
            inline C operator-(const C &c) const { return C(x - c.x, y - c.y); }
10
11
            inline C operator*(const C &c) const {
12
                return C(x * c.x - y * c.y, x * c.y + y * c.x);
13
            }
14
            inline C conj() const { return C(x, -y); }
15
        };
16
17
        const real PI = acosl(-1);
18
        int base = 1;
19
        vector < C > rts = { {0, 0}, }
20
                             {1, 0} };
        vector< int > rev = {0, 1};
21
22
23
24
        void ensure_base(int nbase) {
25
            if(nbase <= base) return;</pre>
26
            rev.resize(1 << nbase);</pre>
```

```
27
            rts.resize(1 << nbase);
28
            for(int i = 0; i < (1 << nbase); i++) {
29
                rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
30
            }
31
            while(base < nbase) {</pre>
            real angle = PI * 2.0 / (1 << (base + 1));
32
            for(int i = 1 << (base - 1); i < (1 << base); i++) {
33
34
                rts[i << 1] = rts[i];
35
                real angle_i = angle * (2 * i + 1 - (1 << base));
36
                rts[(i << 1) + 1] = C(cos(angle_i), sin(angle_i));
37
            }
38
                ++base;
39
            }
40
        }
41
42
        void fft(vector < C > &a, int n) {
43
            assert((n & (n - 1)) == 0);
44
            int zeros = __builtin_ctz(n);
            ensure_base(zeros);
45
46
            int shift = base - zeros;
47
            for(int i = 0; i < n; i++) {
48
                if(i < (rev[i] >> shift)) {
                     swap(a[i], a[rev[i] >> shift]);
49
50
                }
51
            }
52
            for(int k = 1; k < n; k <<= 1) {
53
                for(int i = 0; i < n; i += 2 * k) {
54
                     for(int j = 0; j < k; j++) {
55
                     C z = a[i + j + k] * rts[j + k];
56
                     a[i + j + k] = a[i + j] - z;
57
                     a[i + j] = a[i + j] + z;
58
59
                }
60
            }
61
        }
62
        vector< int64_t > multiply(const vector< int > &a, const vector< int > &b) {
63
64
            int need = (int) a.size() + (int) b.size() - 1;
65
            int nbase = 1;
            while((1 << nbase) < need) nbase++;</pre>
66
67
            ensure_base(nbase);
68
            int sz = 1 << nbase;</pre>
69
            vector< C > fa(sz);
70
            for(int i = 0; i < sz; i++) {
                int x = (i < (int) a.size() ? a[i] : 0);</pre>
71
                int y = (i < (int) b.size() ? b[i] : 0);</pre>
72
73
                fa[i] = C(x, y);
74
            }
75
            fft(fa, sz);
76
            C r(0, -0.25 / (sz >> 1)), s(0, 1), t(0.5, 0);
77
            for(int i = 0; i \le (sz >> 1); i++) {
78
                int j = (sz - i) & (sz - 1);
79
                C z = (fa[j] * fa[j] - (fa[i] * fa[i]).conj()) * r;
                fa[j] = (fa[i] * fa[i] - (fa[j] * fa[j]).conj()) * r;
80
81
                fa[i] = z;
82
83
            for(int i = 0; i < (sz >> 1); i++) {
```

```
84
                C AO = (fa[i] + fa[i + (sz >> 1)]) * t;
85
                C A1 = (fa[i] - fa[i + (sz >> 1)]) * t * rts[(sz >> 1) + i];
86
                fa[i] = A0 + A1 * s;
            }
87
88
            fft(fa, sz >> 1);
            vector < int64_t > ret(need);
89
            for(int i = 0; i < need; i++) {
90
91
                ret[i] = llround(i & 1 ? fa[i >> 1].y : fa[i >> 1].x);
92
            }
93
            return ret;
        }
94
95 };
96 // auto C = FastFourierTransform::multiply(A, B);
```

#### Lagrange 補間

```
1 template < typename T >
2 T lagrange_polynomial(const vector< T > &y, int64_t t) {
     int N = y.size() - 1;
     Combination < T > comb(N);
     if(t <= N) return y[t];</pre>
5
     T ret(0);
     vector < T > dp(N + 1, 1), pd(N + 1, 1);
7
8
     for(int i = 0; i < N; i++) dp[i + 1] = dp[i] * (t - i);
     for(int i = N; i > 0; i--) pd[i - 1] = pd[i] * (t - i);
     for(int i = 0; i <= N; i++) {
10
       T tmp = y[i] * dp[i] * pd[i] * comb.rfact(i) * comb.rfact(N - i);
12
       if((N - i) & 1) ret -= tmp;
13
       else ret += tmp;
14
15
     return ret;
16 }
17
18 int main() {
    int N, T;
20
     cin >> N;
21
     vector < modint > A(N + 1);
22
     cin >> A;
23
     cin >> T;
     cout << lagrange_polynomial(A, T) << endl;</pre>
25 }
```

# 5 文字列

#### KMP 法

文字列 S[0,i-1] の接頭辞と接尾辞が最大何文字一致しているかを記録した配列を O(|S|) で構築する

```
1 vector<int> A(s.size()+1);
2 A[0] = -1;
3 int j = -1;
4 for (int i = 0; i < s.size(); i++) {
5     while (j >= 0 && s[i] != s[j]) j = A[j];
6     j++;
7     A[i+1] = j;
8 }
```

#### ローリングハッシュ

```
1
   struct RollingHash {
2
       using T = long long;
3
       using hash_type = pair<T, T>;
       const T mod1 = 1000000007, mod2 = 1000000009;
       T base1, base2;
5
       vector <T> hash1, hash2, pow1, pow2;
6
7
       RollingHash(const string &s){
8
9
            int n = s.size();
10
            std::random_device rnd;
            std::mt19937 mt(rnd());
11
            base1 = mt()\%(mod1-2)+2;
12
            base2 = mt()\%(mod2-2)+2;
13
14
            hash1.assign(n+1,0);
15
            hash2.assign(n+1,0);
16
17
            pow1.assign(n+1,1);
18
            pow2.assign(n+1,1);
            for(int i=0; i<n; i++){
19
                hash1[i+1] = (hash1[i]*base1+s[i])%mod1;
วก
21
                hash2[i+1] = (hash2[i]*base2+s[i])%mod2;
22
                pow1[i+1]=pow1[i]*base1%mod1;
23
                pow2[i+1]=pow2[i]*base2%mod2;
24
            }
       }
25
26
27
       // [l, r)
28
       hash_type get(int 1,int r){
29
           T res1 = ((hash1[r] - hash1[l]*pow1[r-l]) % mod1 + mod1) % mod1;
           T res2 = ((hash2[r] - hash2[1]*pow2[r-1]) \% mod2 + mod2) \% mod2;
30
31
            return make_pair(res1, res2);
32
       }
33
34
       hash_type concat(hash_type h1, hash_type h2, int h2len) {
35
            T res1 = (h1.first*pow1[h2len] + h2.first) % mod1;
36
            T res2 = (h1.second*pow2[h2len] + h2.second) % mod2;
37
            return make_pair(res1, res2);
       // LCPは長さで二分探索する
39
40 };
```

### 6 テクニック

#### 座標圧縮

```
1 vector<int> unzip = a;
2 map<int, int> zip;
3 sort(all(unzip));
4 unzip.erase(unique(all(unzip)), unzip.end());
5 for(int i=0; i<unzip.size(); i++) zip[unzip[i]] = i;</pre>
```

## スライド最小値

## [i-k,i] の最小値を格納した vector を返す

```
1 vector<int> slide_min(vector<int> &a, int k){
       deque<int> deq;
2
3
       vector<int> b;
       rep(i, a.size()){
           // maxはここの不等号の向きを変える
5
6
           while(!deq.empty() && a[deq.back()] >= a[i]) deq.pop_back();
7
           deq.push_back(i);
8
           b.push_back(a[deq.front()]);
           if(i-k+1 >= 0 \&\& deq.front() == i-k+1) deq.pop_front();
9
10
       }
11
       return b;
12 }
```