

Reg: FA21-BSE-133

Name: AOUN-HAIDER

Course Title: Discrete Structures (CSC102)

Section: A

Assignment: 03

Submitted to: Mahwish Waqas

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$\therefore \frac{1}{[CLO-4]}$

Q No: - 01

$$a) \sum_{k=1}^5 \sum_{m=6}^9 3(2k+7)$$

$$= \sum_{k=1}^5 3 \times 4 (2k+7)$$

$$= \sum_{k=1}^5 12(2k+7)$$

$$= 12 \left[\sum_{k=1}^5 2k+7 \right]$$

$$= 12((2(1)+7) + (2(2)+7) + (2(3)+7) + (2(4)+7) + (2(5)+7))$$

$$= 12(9 + 11 + 13 + 15 + 17)$$

$$= 12 \times 65$$

$$\Rightarrow 780$$

$$\sum_{i=20}^{110} (2i + i^3)$$

$$= 2 \sum_{i=20}^{110} i + \sum_{i=20}^{110} i^3$$

$$\sum_{i=1}^{110} i = \sum_{i=1}^{19} i + \sum_{i=20}^{110} i$$

$$\sum_{i=20}^{110} i = \sum_{i=1}^{110} i - \sum_{i=1}^{19} i$$

$$\therefore \sum_{i=1}^n i = \frac{n(n+1)}{2}$$

putting above formula to given values:

$$= \frac{110(110+1)}{2} - \frac{19(19+1)}{2}$$

$$= \frac{110 \times 111}{2} - \frac{19 \times 20}{2}$$

$$= \frac{12,210}{2} - \frac{380}{2}$$

$$\therefore \sum_{i=20}^{110} i = \frac{11830}{2}$$

$$\sum_{i=20}^{110} i = 11830$$

$$\sum_{i=20}^{110} i^3 = ?$$

$$\sum_{i=1}^{110} i^3 = \sum_{i=1}^{19} i^3 + \sum_{i=20}^{110} i^3$$

$$\therefore \sum_{i=1}^n i^3 = \frac{n^2(n+1)^2}{4}$$

$$= \frac{(110)^2(110+1)^2}{4} - \frac{(19)^2(19+1)^2}{4}$$

$$= \frac{(110)^2(111)^2}{4} - \frac{(19)^2(20)^2}{4}$$

$$= \frac{12100 \times 12,321}{4} - \frac{361 \times 400}{4}$$

$$= \frac{149,084,100}{4} - \frac{144,400}{4}$$

$$= 37,234,925$$

$$\sum_{i=20}^{110} (2i+i^3) \Rightarrow 11830 + 37234925$$

$$= 37,246,755$$

Q No:- 02

a) Consider Sequence:

$$-2, 1, -1/2, 1/4, \dots$$

$$30^{\text{th}} \text{ term} = ?$$

$$a_1 = -2$$

$$r = -\frac{1}{2}$$

Geometric
(Arithmetic sequence)

$$a_n = a_1 r^{n-1}$$

$$a_{30} = (-2) \left(-\frac{1}{2}\right)^{30-1}$$

$$= (-2) \left(-\frac{1}{2}\right)^{29}$$

$$= (-2) \left(\frac{1}{536,870,912}\right) \Rightarrow \frac{2}{536,870,912}$$

$$a_{30} = \frac{1}{536,870,912}$$

$-\frac{1}{34359738368}$ is which term of sequence? ⁽⁴⁾

Given that

$$a_1 = -2, r = -\frac{1}{2}$$

$$\begin{aligned} a_{37} &= (-2)\left(-\frac{1}{2}\right)^{37-1} \\ &= (-2)\left(-\frac{1}{2}\right)^{36} \end{aligned}$$

$$| a_{37} = -\frac{1}{34359738368}$$

Its 37th term of sequence.

Q No: -03: Find explicit & recursive formula:

a) $-31, -14, 3, 20, 37, 54, \dots$

$a_1 = -31$ (explicit formula)

$d = 17$

$a_n = -31 + (n-1)d$

$= -31 + (n-1)17$

$= -31 + 17n - 17$

$| a_n = 17n - 48$

(Recursive formula)

Basic step:

$a_1 = -31$

Recursive step:

$| a_{n+1} = a_n + 17$

$a_{2+1} = a_2 + 17$

$a_3 = -14 + 17 = 3$

$| a_3 = 3$

$$3) b) \frac{1}{5}, \frac{1}{25}, \frac{1}{125}, \frac{1}{625}, \dots$$

— (Explicit formula) —

$$a_1 = \frac{1}{5}$$

$$r = \frac{1}{5}$$

$$a_n = a_1 r^{n-1}$$

$$a_n = \left(\frac{1}{5}\right) \left(\frac{1}{5}\right)^{n-1}$$

$$a_n = \left(\frac{1}{5}\right)^{n-1+1}$$

$$\boxed{a_n = \left(\frac{1}{5}\right)^n} \leftarrow \text{explicit formula}$$

— (Recursive formula) —

Basic step:

$$a_1 = \frac{1}{5}$$

Recursive step:

$$\boxed{a_{n+1} = \frac{1}{5} \times a_n}$$

$$a_{1+1} = a_1 \times \frac{1}{5}$$

$$a_2 = \frac{1}{5} \times \frac{1}{5}$$

$$\boxed{a_2 = \frac{1}{25}}$$

hence proved!

The End ☺