An Introduction to Machine Learning

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About the course

1.1 Overview

Machine learning gives computers the ability to learn without being explicitly programmed. It encompasses a broad range of approaches to data analysis with applicability across the biological sciences. Lectures will introduce commonly used algorithms and provide insight into their theoretical underpinnings. In the practical students will apply these algorithms to real biological data-sets using the R language and environment.

During this course you will learn about:

- Some of the core mathematical concepts underpinning machine learning algorithms: matrices and linear algebra; Bayes' theorem.
- Classification (supervised learning): partitioning data into training and test sets; feature selection; logistic regression; support vector machines; artificial neural networks; decision trees; nearest neighbours, cross-validation.
- Exploratory data analysis (unsupervised learning): dimensionality reduction, anomaly detection, clustering.

After this course you should be able to:

- Understand the concepts of machine learning.
- Understand the strengths and limitations of the various machine learning algorithms presented in this course
- Select appropriate machine learning methods for your data.
- Perform machine learning in R.

1.2 Registration

Bioinformatics Training: An Introduction to Machine Learning

1.3 Prerequisites

- Some familiarity with R would be helpful.
- For an introduction to R see An Introduction to Solving Biological Problems with R course.

1.4 Github

bioinformatics-training/intro-machine-learning

1.5 License

GPL-3

1.6 Contact

If you have any **comments**, **questions** or **suggestions** about the material, please contact the authors: Sudhakaran Prabakaran, Matt Wayland and Chris Penfold.

1.7 Colophon

This book was produced using the **bookdown** package (Xie, 2017), which was built on top of R Markdown and **knitr** (Xie, 2015).

Introduction

You can label chapter and section titles using {#label} after them, e.g., we can reference Chapter 2. If you do not manually label them, there will be automatic labels anyway, e.g., Chapter ??.

Figures and tables with captions will be placed in figure and table environments, respectively.

```
par(mar = c(4, 4, .1, .1))
plot(pressure, type = 'b', pch = 19)
```

Reference a figure by its code chunk label with the fig: prefix, e.g., see Figure 2.1. Similarly, you can reference tables generated from knitr::kable(), e.g., see Table 2.1.

```
knitr::kable(
  head(iris, 20), caption = 'Here is a nice table!',
  booktabs = TRUE
)
```



Figure 2.1: Here is a nice figure!

Table 2.1: Here is a nice table!

| Sepal.Length | Sepal.Width | Petal.Length | Petal.Width | Species |
|--------------|-------------|--------------|-------------|---------|
| 5.1 | 3.5 | 1.4 | 0.2 | setosa |
| 4.9 | 3.0 | 1.4 | 0.2 | setosa |
| 4.7 | 3.2 | 1.3 | 0.2 | setosa |
| 4.6 | 3.1 | 1.5 | 0.2 | setosa |
| 5.0 | 3.6 | 1.4 | 0.2 | setosa |
| 5.4 | 3.9 | 1.7 | 0.4 | setosa |
| 4.6 | 3.4 | 1.4 | 0.3 | setosa |
| 5.0 | 3.4 | 1.5 | 0.2 | setosa |
| 4.4 | 2.9 | 1.4 | 0.2 | setosa |
| 4.9 | 3.1 | 1.5 | 0.1 | setosa |
| 5.4 | 3.7 | 1.5 | 0.2 | setosa |
| 4.8 | 3.4 | 1.6 | 0.2 | setosa |
| 4.8 | 3.0 | 1.4 | 0.1 | setosa |
| 4.3 | 3.0 | 1.1 | 0.1 | setosa |
| 5.8 | 4.0 | 1.2 | 0.2 | setosa |
| 5.7 | 4.4 | 1.5 | 0.4 | setosa |
| 5.4 | 3.9 | 1.3 | 0.4 | setosa |
| 5.1 | 3.5 | 1.4 | 0.3 | setosa |
| 5.7 | 3.8 | 1.7 | 0.3 | setosa |
| 5.1 | 3.8 | 1.5 | 0.3 | setosa |

Linear models and matrix algebra

3.1 Exercises

Solutions to exercises can be found in appendix B

Linear and non linear logistic regression

4.1 Exercises

Solutions to exercises can be found in appendix C.

Nearest neighbours

- 5.1 Example one
- 5.2 Example two
- 5.3 Exercises

Solutions to exercises can be found in appendix D.

Decision trees and random forests

6.1 Exercises

Solutions to exercises can be found in appendix E.

Support vector machines

7.1 Exercises

Solutions to exercises can be found in appendix F

Artificial neural networks

8.1 Exercises

Solutions to exercises can be found in appendix G.

Dimensionality reduction

- 9.1 Linear Dimensionality Reduction
- 9.1.1 Principle Component Analysis
- 9.1.2 Horeshoe effect
- 9.2 Nonlinear Dimensionality Reduction
- 9.2.1 t-SNE
- 9.2.2 Gaussian Process Latent Variable Models
- 9.2.3 GPLVMs with informative priors
- 9.3 Exercises

Solutions to exercises can be found in appendix H.

Clustering

10.1 Introduction

Hierarchic (produce dendrogram) vs partitioning methods

10.2 Distance metrics

dist function cor as.dist(1-cor(x))

Minkowski distance:

$$distance\left(x,y,p\right) = \left(\sum_{i=1}^{n} abs(x_i - y_i)^p\right)^{1/p} \tag{10.1}$$

Graphical explanation of euclidean, manhattan and max (Chebyshev?)

10.2.1 Image segmentation

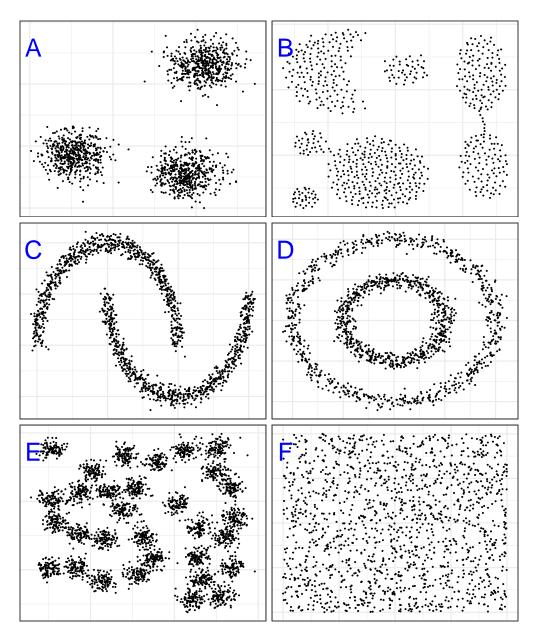
10.3 Hierarchic methods

10.3.1 Linkage algorithms

Make one section panel of three dendrograms one table

Table 10.1: Example distance matrix

| | A | В | С | D |
|--------------|----|----|---|---|
| В | 2 | | | |
| \mathbf{C} | 6 | 5 | | |
| D | 10 | 10 | 5 | |
| \mathbf{E} | 9 | 8 | 3 | 4 |



 $\label{eq:control_problem} \begin{aligned} & \text{Figure 10.1: Example clusters. **A**, *blobs*; **B**, *aggregation* [@Gionis2007]; **C**, *noisy moons*; \\ & \text{**D**, *noisy circles*; **E**, *D31* [@Veenman2002]; **F**, *no structure*.} \end{aligned}$

Table 10.2: Merge distances for objects in the example distance matrix using three different linkage methods.

| Groups | Single | Complete | Average |
|---------------|--------|----------|---------|
| A,B,C,D,E | 0 | 0 | 0 |
| (A,B),C,D,E | 2 | 2 | 2 |
| (A,B),(C,E),D | 3 | 3 | 3 |
| (A,B)(C,D,E) | 4 | 5 | 4.5 |
| (A,B,C,D,E) | 5 | 10 | 8 |

Single linkage - nearest neighbours linkage Complete linkage - furthest neighbours linkage Average linkage - UPGMA (Unweighted Pair Group Method with Arithmetic Mean)

10.3.2 Example: clustering toy data sets

10.3.2.1 Step-by-step instructions

1. Load required packages.

```
library(RColorBrewer)
library(dendextend)
##
## -----
## Welcome to dendextend version 1.5.2
## Type citation('dendextend') for how to cite the package.
## Type browseVignettes(package = 'dendextend') for the package vignette.
## The github page is: https://github.com/talgalili/dendextend/
## Suggestions and bug-reports can be submitted at: https://github.com/talgalili/dendextend/issues
## Or contact: <tal.galili@gmail.com>
##
##
   To suppress this message use: suppressPackageStartupMessages(library(dendextend))
##
## Attaching package: 'dendextend'
## The following object is masked from 'package:ggdendro':
##
##
      theme_dendro
## The following object is masked from 'package:stats':
##
##
       cutree
library(ggplot2)
library(GGally)
```

2. Retrieve a palette of eight colours.

```
cluster_colours <- brewer.pal(8,"Dark2")</pre>
```

3. Read in data for **blobs** example.

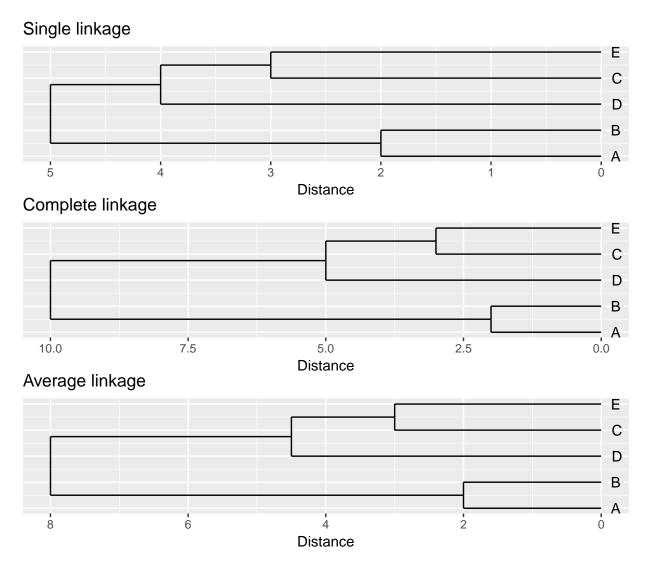


Figure 10.2: Dendrograms for the example distance matrix using three different linkage methods.

```
blobs <- read.csv("data/example_clusters/blobs.csv", header=F)</pre>
```

4. Create distance matrix using Euclidean distance metric.

```
d <- dist(blobs[,1:2])</pre>
```

5. Perform hierarchical clustering using the **average** agglomeration method and convert the result to an object of class **dendrogram**. A **dendrogram** object can be edited using the advanced features of the **dendextend** package.

```
dend <- as.dendrogram(hclust(d, method="average"))</pre>
```

6. Cut the tree into three clusters

```
clusters <- cutree(dend,3,order_clusters_as_data=F)</pre>
```

7. The vector **clusters** contains the cluster membership (in this case 1, 2 or 3) of each observation (data point) in the order they appear on the dendrogram. We can use this vector to colour the branches of the dendrogram by cluster.

```
dend <- color_branches(dend, clusters=clusters, col=cluster_colours[1:3])</pre>
```

8. We can use the **labels** function to annotate the leaves of the dendrogram. However, it is not possible to create legible labels for the 1,500 leaves in our example dendrogram, so we will set the label for each leaf to an empty string.

```
labels(dend) <- rep("", length(blobs[,1]))</pre>
```

9. If we want to plot the dendrogram using **ggplot**, we must convert it to an object of class **ggdend**.

```
ggd <- as.ggdend(dend)
```

10. The **nodes** attribute of **ggd** is a data.frame of parameters related to the plotting of dendogram nodes. The **nodes** data.frame contains some NAs which will generate warning messages when **ggd** is processed by **ggplot**. Since we are not interested in annotating dendrogram nodes, the easiest option here is to delete all of the rows of **nodes**.

```
ggd$nodes <- ggd$nodes[!(1:length(ggd$nodes[,1])),]</pre>
```

11. We can use the cluster membership of each observation contained in the vector **clusters** to assign colours to the data points of a scatterplot. However, first we need to reorder the vector so that the cluster memberships are in the same order that the observations appear in the data frame of observations. Fortunately the names of the elements of the vector are the indices of the observations in the data frame and so reordering can be accomplished in one line.

```
clusters <- clusters[order(as.numeric(names(clusters)))]</pre>
```

12. We are now ready to plot a dendrogram and scatterplot. We will use the **ggmatrix** function from the **GGally** package to place the plots side-by-side.

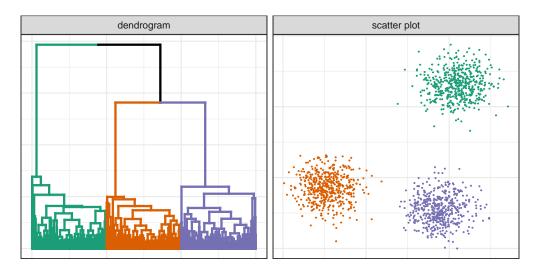


Figure 10.3: Hierarchical clustering of the blobs data set.

10.3.2.2 Clustering of other toy data sets

```
aggregation <- read.table("data/example clusters/aggregation.txt")</pre>
noisy_moons <- read.csv("data/example_clusters/noisy_moons.csv", header=F)</pre>
noisy_circles <- read.csv("data/example_clusters/noisy_circles.csv", header=F)
no_structure <- read.csv("data/example_clusters/no_structure.csv", header=F)
hclust_plots <- function(data_set, n){
  d <- dist(data_set[,1:2])</pre>
  dend <- as.dendrogram(hclust(d, method="average"))</pre>
  clusters <- cutree(dend,n,order_clusters_as_data=F)</pre>
  dend <- color_branches(dend, clusters=clusters, col=cluster_colours[1:n])</pre>
  clusters <- clusters[order(as.numeric(names(clusters)))]</pre>
  labels(dend) <- rep("", length(data_set[,1]))</pre>
  ggd <- as.ggdend(dend)</pre>
  ggd$nodes <- ggd$nodes[!(1:length(ggd$nodes[,1])),]</pre>
  plotPair <- list(ggplot(ggd),</pre>
    ggplot(data_set, aes(V1,V2)) + geom_point(col=cluster_colours[clusters], size=0.2))
  return(plotPair)
}
plotList <- c(</pre>
  hclust_plots(aggregation, 7),
  hclust_plots(noisy_moons, 2),
  hclust_plots(noisy_circles, 2),
  hclust_plots(no_structure, 3)
pm <- ggmatrix(</pre>
  plotList, nrow=4, ncol=2, showXAxisPlotLabels = F, showYAxisPlotLabels = F, xAxisLabels=c("dendrogram"
) + theme_bw()
pm
```

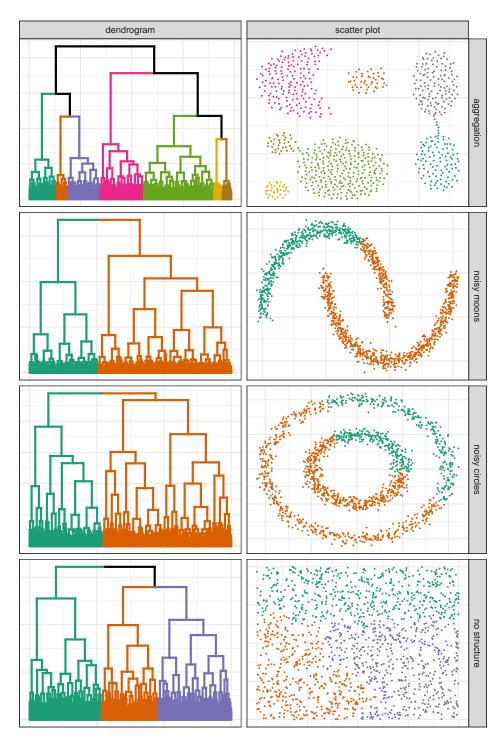


Figure 10.4: Hierarchical clustering of toy data-sets.

Cluster Dendrogram

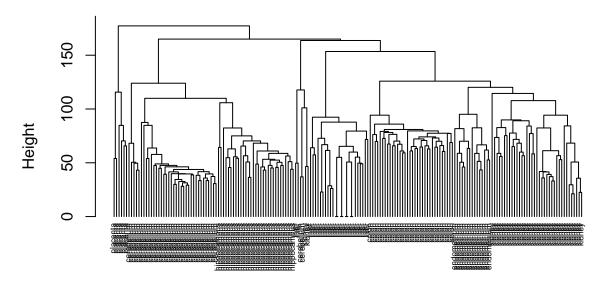


Figure 10.5: Clustering of tissue samples based on gene expression profiles.

10.3.3 Example: gene expression profiling of human tissues

10.3.3.1 Basics

```
Load required libraries
```

```
library(RColorBrewer)
library(dendextend)
```

Load data

```
load("data/tissues_gene_expression/tissuesGeneExpression.rda")
```

Inspect data

```
table(tissue)
```

```
## tissue
##
    cerebellum
                      colon endometrium hippocampus
                                                            kidney
                                                                          liver
                         34
                                                                             26
##
             38
                                      15
                                                                39
##
      placenta
##
dim(e)
```

```
## [1] 22215 189
```

Compute distance between each sample

```
d <- dist(t(e))</pre>
```

perform hierarchical clustering

```
hc <- hclust(d, method="average")
plot(hc, labels=tissue, cex=0.5, hang=-1, xlab="", sub="")</pre>
```

10.3.3.2 Colour labels

use dendextend library to plot dendrogram with colour labels

```
tissue_type <- unique(tissue)
dend <- as.dendrogram(hc)
dend_colours <- brewer.pal(length(unique(tissue)), "Dark2")
names(dend_colours) <- tissue_type
labels(dend) <- tissue[order.dendrogram(dend)]
labels_colors(dend) <- dend_colours[tissue][order.dendrogram(dend)]
labels_cex(dend) = 0.5
plot(dend, horiz=T)</pre>
```

10.3.3.3 Defining clusters by cutting tree

Define clusters by cutting tree at a specific height

```
plot(dend, horiz=T)
abline(v=125, lwd=2, lty=2, col="blue")
hclusters <- cutree(dend, h=125)
table(tissue, cluster=hclusters)</pre>
```

```
##
             cluster
            1 2 3 4 5 6
## tissue
##
   cerebellum 0 36 0 0 2 0
##
    colon 0 0 34 0 0 0
##
    endometrium 15 \quad 0 \quad 0 \quad 0 \quad 0
##
    hippocampus 0 31 0 0 0 0
##
    kidney
              37 0 0 0 2 0
##
               0 0 0 24 2 0
    liver
##
               0 0 0 0 0 6
    placenta
```

Select a specific number of clusters.

```
plot(dend, horiz=T)
abline(v = heights_per_k.dendrogram(dend)["8"], lwd = 2, lty = 2, col = "blue")
hclusters <- cutree(dend, k=8)
table(tissue, cluster=hclusters)</pre>
```

```
##
            cluster
## tissue
            1 2 3 4 5 6 7 8
   cerebellum 0 31 0 0 2 0 5 0
##
##
   colon
             0 0 34 0 0 0 0
##
   endometrium 0 0 0 0 0 15 0 0
   hippocampus 0 31 0 0 0 0 0 0
##
         37 0 0 0 2 0 0 0
##
   kidney
##
   liver
             0 0 0 24 2 0 0 0
##
   placenta 0 0 0 0 0 0 6
```

10.3.3.4 Heatmap

Base R provides a **heatmap** function, but we will use the more advanced **heatmap.2** from the **gplots** package.

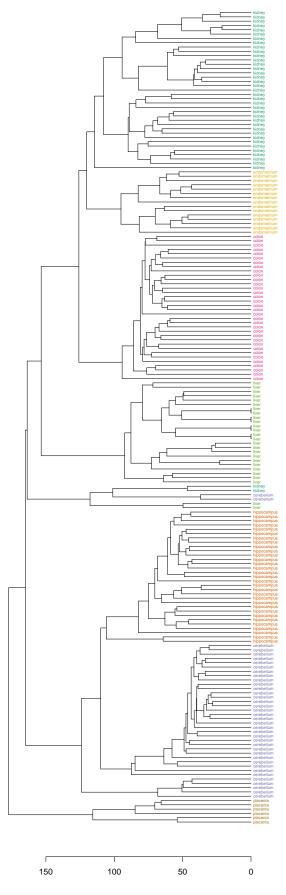


Figure 10.6: Clustering of tissue samples based on gene expression profiles with labels coloured by tissue type.

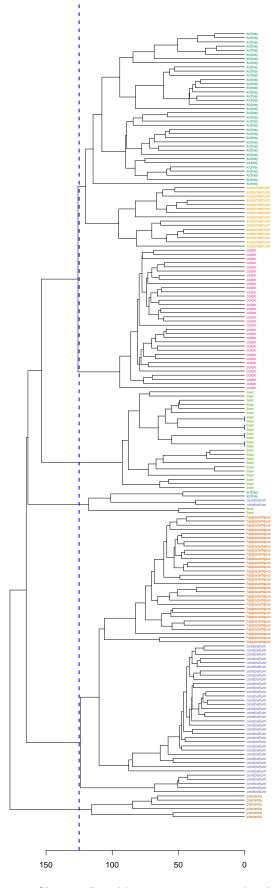


Figure 10.7: Clusters found by cutting tree at a height of 125

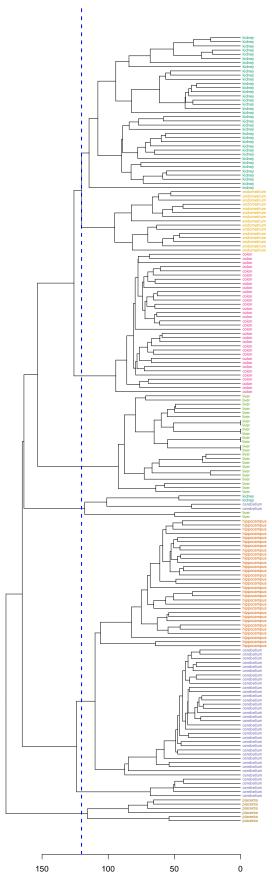


Figure 10.8: Selection of eight clusters from the dendogram $\,$

```
library(gplots)
## Attaching package: 'gplots'
## The following object is masked from 'package:stats':
##
       lowess
Define a colour palette (also known as a lookup table).
heatmap_colours <- colorRampPalette(brewer.pal(9, "PuBuGn"))(100)
Calculate the variance of each gene.
geneVariance <- apply(e,1,var)</pre>
Find the row numbers of the 40 genes with the highest variance.
idxTop40 <- order(-geneVariance)[1:40]</pre>
Define colours for tissues.
tissueColours <- palette(brewer.pal(8, "Dark2"))[as.numeric(as.factor(tissue))]
Plot heatmap.
heatmap.2(e[idxTop40,], labCol=tissue, trace="none",
          ColSideColors=tissueColours, col=heatmap_colours)
```

10.4 Partitioning methods

10.4.1 K-means

10.4.1.1 Algorithm

Pseudocode

to illustrate range of different types of data that can be clustered - image segmentation

The default setting of the **kmeans** function is to perform a maximum of 10 iterations and if the algorithm fails to converge a warning is issued. The maximum number of iterations is set with the argument **iter.max**.

10.4.1.2 Choosing initial cluster centres

```
library(RColorBrewer)
point_shapes <- c(15,17,19)
point_colours <- brewer.pal(3,"Dark2")
point_size = 1.5
center_point_size = 8

blobs <- as.data.frame(read.csv("data/example_clusters/blobs.csv", header=F))
good_centres <- as.data.frame(matrix(c(2,8,7,3,12,7), ncol=2, byrow=T))
bad_centres <- as.data.frame(matrix(c(13,13,8,12,2,2), ncol=2, byrow=T))</pre>
```

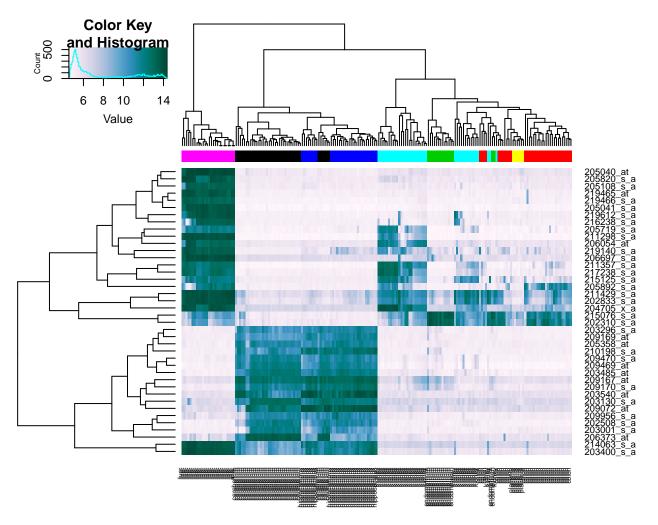


Figure 10.9: Heatmap of the expression of the 40 genes with the highest variance.

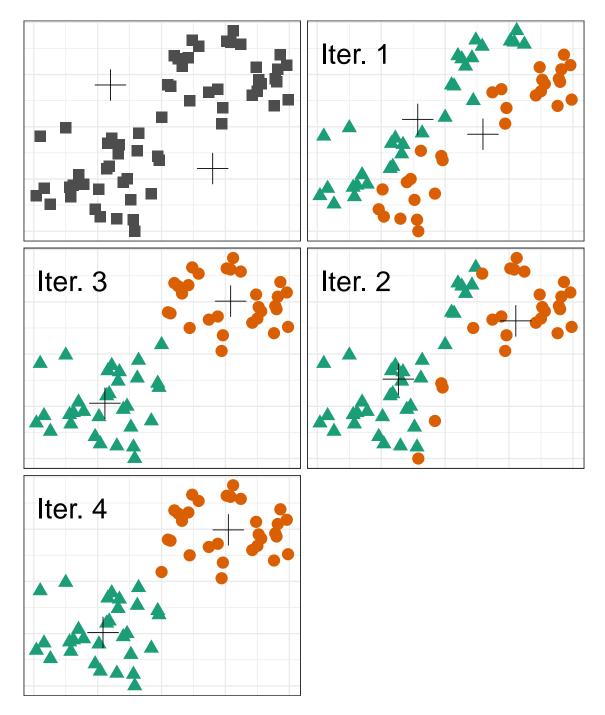


Figure 10.10: Iterations of the k-means algorithm

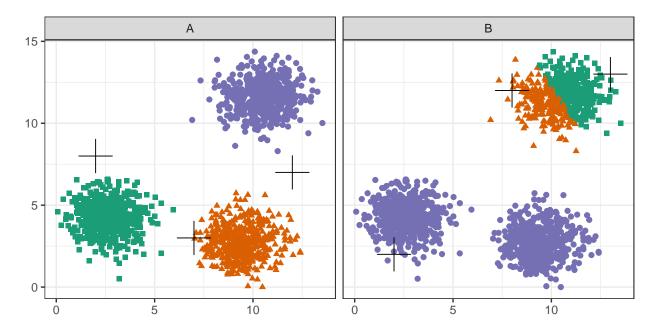


Figure 10.11: Initial centres determine clusters. The starting centres are shown as crosses. **A**, real clusters found; **B**, convergence to a local minimum.

```
good_result <- kmeans(blobs[,1:2], centers=good_centres)
bad_result <- kmeans(blobs[,1:2], centers=bad_centres)

plotList <- list(
ggplot(blobs, aes(V1,V2)) + geom_point(col=point_colours[good_result$cluster], shape=point_shapes[good_ggplot(blobs, aes(V1,V2)) + geom_point(col=point_colours[bad_result$cluster], shape=point_shapes[bad_re])

pm <- ggmatrix(
    plotList, nrow=1, ncol=2, showXAxisPlotLabels = T, showYAxisPlotLabels = T, xAxisLabels=c("A", "B")
) + theme_bw()

pm</pre>
```

Convergence to a local minimum can be avoided by starting the algorithm multiple times, with different random centres. The **nstart** argument to the **k-means** function can be used to specify the number of random sets and optimal solution will be selected automatically.

10.4.1.3 Choosing k

```
cluster_colours <- brewer.pal(9,"Set1")
k <- 1:9
res <- lapply(k, function(i){kmeans(blobs[,1:2], i, nstart=50)})

plotList <- lapply(k, function(i){
    ggplot(blobs, aes(V1, V2)) +
        geom_point(col=cluster_colours[res[[i]]$cluster], size=1) +
        geom_point(data=as.data.frame(res[[i]]$centers), aes(V1,V2), shape=3, col="black", size=5) +
        annotate("text", x=2, y=13, label=paste("k=", i, sep=""), size=8, col="black") +</pre>
```

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```
theme_bw()
}
)

pm <- ggmatrix(
   plotList, nrow=3, ncol=3, showXAxisPlotLabels = T, showYAxisPlotLabels = T
) + theme_bw()

pm

tot_withinss <- sapply(k, function(i){res[[i]]$tot.withinss})

qplot(k, tot_withinss, geom=c("point", "line"), ylab="Total within-cluster sum of squares") + theme_bw(</pre>
```

N.B. we have set nstart=50 so that the algorithm is started 50 times wi

10.4.2 DBSCAN

Density-based spatial clustering of applications with noise

10.4.2.1 Algorithm

Abstract DBSCAN algorithm in pseudocode (Schubert et al., 2017)

```
1 Compute neighbours of each point and identify core points // Identify core points
2 Join neighbouring core points into clusters // Assign core points
3 foreach non-core point do
Add to a neighbouring core point if possible // Assign border points
Otherwise, add to noise // Assign noise points
```

10.4.2.2 Choosing parameters

10.4.3 Gene expression

tissue types?

10.5 Summary

- 10.5.1 Applications
- 10.5.2 Strengths
- 10.5.3 Limitations

10.6 Exercises

Exercise solutions: I

Solutions to exercises can be found in appendix I.

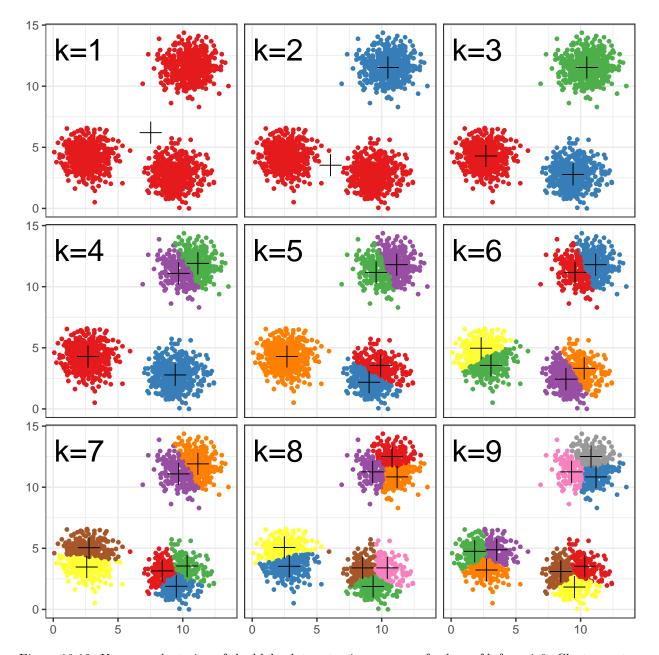


Figure 10.12: K-means clustering of the blobs data set using a range of values of k from 1-9. Cluster centres indicated with a cross.

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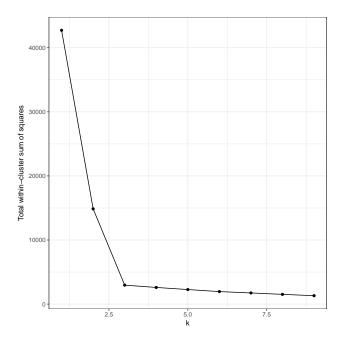


Figure 10.13: Variance within the clusters. Total within-cluster sum of squares plotted against k.

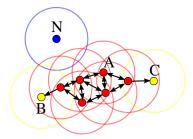


Figure 10.14: Illustration of the DBSCAN algorithm.

Appendix A

Resources

A.1 Python

scikit-learn

A.2 Machine learning data set repository

mldata.org

This repository manages the following types of objects:

- Data Sets Raw data as a collection of similarily structured objects.
- Material and Methods Descriptions of the computational pipeline.
- Learning Tasks Learning tasks defined on raw data.
- Challenges Collections of tasks which have a particular theme.

Appendix B

Solutions ch. 3 - Linear models and matrix algebra

Solutions to exercises of chapter 3.

- B.1 Exercise 1
- B.2 Exercise 2

Appendix C

Solutions ch. 4 - Linear and non-linear logistic regression

Solutions to exercises of chapter 4.

- C.1 Exercise 1
- C.2 Exercise 2

Appendix D

Solutions ch. 5 - Nearest neighbours

Solutions to exercises of chapter 5.

- D.1 Exercise 1
- D.2 Exercise 2

Appendix E

Solutions ch. 6 - Decision trees and random forests

Solutions to exercises of chapter 6.

- E.1 Exercise 1
- E.2 Exercise 2

Appendix F

Solutions ch. 7 - Support vector machines

Solutions to exercises of chapter 7.

- F.1 Exercise 1
- F.2 Exercise 2

Appendix G

Solutions ch. 8 - Artificial neural networks

Solutions to exercises of chapter 8.

- G.1 Exercise 1
- G.2 Exercise 2

Appendix H

Solutions ch. 9 - Dimensionality reduction

Solutions to exercises of chapter 9.

- H.1 Exercise 1
- H.2 Exercise 2

Appendix I

Solutions ch. 10 - Clustering

Solutions to exercises of chapter 10.

- I.1 Exercise 1
- I.2 Exercise 2

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