

## Filters $\sigma_{A=k}$ :

- $l'_A = k$
- $u'_A = k$
- $d'_A = 1, \text{ if } k \in d_A, 0 \text{ otherwise}$
- $f'_A = \frac{f_A}{d_A}, \text{ if } k \in d_A, 0 \text{ otherwise}$

Statics for any other column C for the array that filter has been applied:

- $l'_C = l_C$
- $u'_C = u_C$
- $d'_C = d_C * (1 - (1 - (\frac{f'_A}{f_A})^{\frac{f_C}{d_C}}))$
- $f'_C = f'_A$

## Filters $\sigma_{k1 \leq A \leq k2}$ :

- $l'_A = k1$
- $u'_A = k2$
- $d'_A = \frac{(k2 - k1)}{(u_A - l_A)} * d_A$
- $f'_A = \frac{(k2 - k1)}{(u_A - l_A)} * f_A$

The above equations are applied if for k1, k2:

- $k1 < l_A \text{ then } k1 = l_A$
- $k2 > u_A \text{ then } k2 = u_A$

Statics for any other column C for the array that filter has been applied:

- $l'_C = l_C$
- $u'_C = u_C$
- $d'_C = d_C * (1 - (1 - (\frac{f'_A}{f_A})^{\frac{f_C}{d_C}}))$
- $f'_C = f'_A$

## Filters $\sigma_{A=B}$ :

If filters of the same array is applied (R.A = R.B):

- $l'_A = l'_B = \max(l_A, l_B)$
- $u'_A = u'_B = \min(u_A, u_B)$
- $f'_A = f'_B = \frac{f}{n}$
- $d'_A = d'_B = d_A * (1 - (1 - (\frac{f'_A}{f_A})^{\frac{f_A}{d_A}}))$

, where  $n = u'_A - l'_A + 1$

Statics for any other column C for the array that filter has been applied:

- $l'_C = l_C$
- $u'_C = u_C$
- $d'_C = d_C * (1 - (1 - (\frac{f'_A}{f_A})^{\frac{f_C}{d_C}}))$
- $f'_C = f'_A$

Join of two different arrays:

- $l'_A = l'_B = l_A = l_B$
  - $u'_A = u'_B = u_A = u_B$
  - $f'_A = f'_B = \frac{(f_A * f_B)}{n}$
  - $d'_A = d'_B = \frac{(d_A * d_B)}{n}$
- , where  $n = u_{A,B} - l_{A,B} + 1$

Statics for any other column C for the array that filter has been applied:

- $l'_C = l_C$
- $u'_C = u_C$
- $f'_C = f'_A$
- $d'_C = d_C * (1 - (1 - (\frac{d'_A}{d_A})^{\frac{f_C}{d_C}})) \text{ if } C \in A$
- $d'_C = d_C * (1 - (1 - (\frac{d'_B}{d_B})^{\frac{f_C}{d_C}})) \text{ if } C \in B$

Self Join:

- $l'_A = l_A$
- $u'_A = u_A$
- $d'_A = d_A$
- $f'_A = \frac{(f_A f_A)}{n}$

Statics for any other column C for the array that filter has been applied:

- $l'_C = l_C$
- $u'_C = u_C$
- $d'_C = d_C$
- $f'_C = f'_A$